

## #Task 1

The U - value of a window:

$$U_{window} = \frac{U_{center}A_{center} + U_{edge}A_{edge} + U_{fram}A_{fram}}{A_{window}}$$

If it is a double - pane window, disregard the thermal resistances of glass layers:

$$\frac{1}{U_{double - pane (center region)}} = \frac{1}{h_i} + \frac{1}{h_{space}} + \frac{1}{h_o}, \quad h_{space} = h_{rad, space} + h_{conv, space}$$

The  $h_{space}$  changes by changing the gas that fills the gap.

From the diagram in the right side, we can see that: When the gap thickness is 13 mm,

**By changing the gas that fills the gap from air to argon, the**

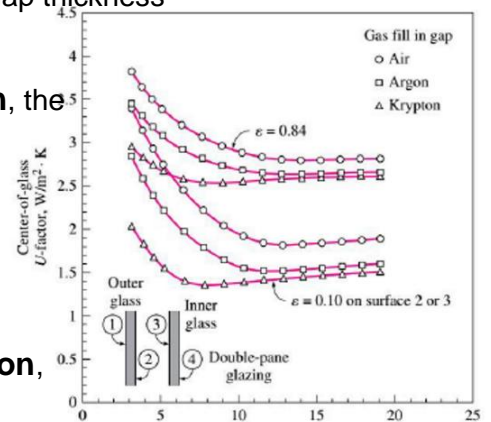
U-value of the center of the glass decreases from  $2.8 \frac{W}{m^2 \cdot K}$  to  $2.65 \frac{W}{m^2 \cdot K}$

, which means the U-value decreases about 6.43%

**By changing the gas that fills the gap from air to krypton,**

the U-value of the center of the glass decrease from  $2.8 \frac{W}{m^2 \cdot K}$  to  $2.6 \frac{W}{m^2 \cdot K}$

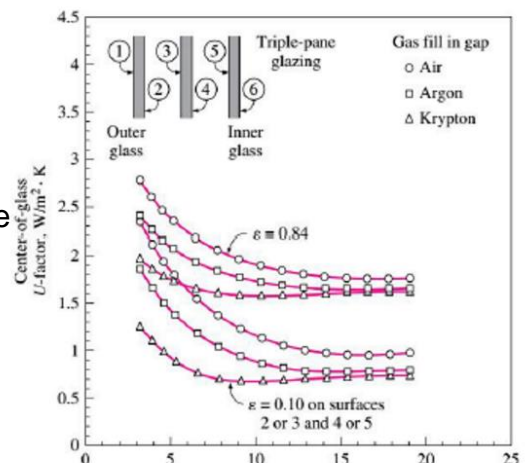
, which means the U-value decreases about 7.14%.



The  $h_{space}$  changes by adding an extra pane.

From the diagram in the right side, we can see that:

When the gap thickness is 13 mm, and the gas that fills the gap is air,



By adding an extra pane,

the U-value of the center of the glass decreases  
from  $2.8 \frac{W}{m^2K}$  to  $1.8 \frac{W}{m^2K}$   
, which means the U-value decreases about 55.6%.

Another way to change the  $U_{center}$ , is to coat the glass surfaces  
with a film that has a low emissivity.

From the diagram in the right we can see that:  
When the gap thickness is 13 mm, and the gas fills the gap is air,

By coating the glass surfaces with a film that has the emissivity of 0.1 to change the  
 $U_{center}$ , the U-value of the center  
of the glass  
decreases from  $2.8 \frac{W}{m^2K}$  to  $1.8 \frac{W}{m^2K}$   
, which means the U-value decreases about 55.6%.

## #Task 2

Cooling design temperature  **$T_{cooling} = 24^\circ C$** ,  
,and heating design temperature  **$T_{heating} = 20^\circ C$** , therefore,

$$\Delta T_{cooling} = 31.9^\circ C - 24^\circ C = 7.9^\circ C = 7.9K$$

$$\Delta T_{heating} = 20^\circ C - (-4.8^\circ C) = 24.8^\circ C = 24.8K$$

From the table above,  $DR = 11.9^\circ C = 11.9K$

### The cooling load of the fixed window on the west is:

$q_{windowwest} = A \times CF_{windowwest}$   
 $A = 14.4m^2$ ,

$CF_{windowwest}(\text{Heat Transfer Part}) = U_{windowwest} (\Delta T_{cooling} - 0.46 DR)$   
,The window has a fixed heat absorbing double layer glass with a wooden frame,  
And so,  $U_{windowwest} = 2.84 \frac{W}{m^2K}$

$$CF_{windowwest}(\text{Heat Transfer Part}) = 2.84 \frac{W}{m^2K} \times (7.9 K - 0.46 \times 11.9 K) = 6.89 \frac{W}{m^2K}$$

$$P_{XI windowwest} = ED + Ed = 559 + 188 = 747$$

$$\text{SHGC} = 0.54$$

No internal shading, so IAC = 1 FFs = 0.56

$$\text{CF windowwest}(\text{Irradiation Part}) = \text{PXi} \times \text{SHGC} \times \text{IAC} \times \text{FFs}$$

$$\begin{aligned} q_{\text{windowwest}} &= A \times \text{CF windowwest} = A \times (\text{CF windowwest}(\text{Heat Transfer Part}) + \\ &\text{CF windowwest}(\text{Irradiation Part})) \\ &= 14.4 \text{ m}^2 \times (6.89 + 747 \times 0.54 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} = 3352.07 \text{ W} \end{aligned}$$

### The heating load of the fixed window on the west is:

$$\begin{aligned} q_{\text{windowwest}} &= A \times \text{HF windowwest} = A \times U_{\text{windowwest}} \cdot \Delta T_{\text{heating}} \\ &= 14.4 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 1014.22 \text{ W} \end{aligned}$$

When the frame were to be aluminium,

$$U_{\text{windowwest}} = 3.61 \frac{\text{W}}{\text{m}^2\text{K}}, \text{ HSGC} = 0.56$$

$$\text{CF}'_{\text{windowwest}} (\text{heat transfer part}) = U'_{\text{windowwest}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$= 3.61 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{windowwest}} = A \times \text{CF}'_{\text{windowwest}}$$

$$\begin{aligned} &= A \times (\text{CF}'_{\text{windowwest}}(\text{Heat Transfer Part}) + \text{CF}'_{\text{windowwest}}(\text{Irradiation Part})) \\ &= 14.4 \text{ m}^2 \times (8.76 + 747 \times 0.56 \times 1 \times 0.56) \frac{\text{W}}{\text{m}^2} = 3499.48 \text{ W} \end{aligned}$$

$$\text{Heating load } q'_{\text{windowwest}} = A \times \text{HF}'_{\text{windowwest}} = A \times U'_{\text{windowwest}} \cdot \Delta T_{\text{heating}}$$

$$= 14.4 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 1289.20 \text{ W}$$

### The cooling load of the fixed window on the south is:

$$q_{\text{windowssouth}} = A \times \text{CF windowssouth}$$

$$A = 3.6 \text{ m}^2,$$

$$\text{CF windowssouth}(\text{Heat Transfer Part}) = U_{\text{windowssouth}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

The window has a fixed heat absorbing double layer glass with a wooden frame,

$$\text{So, } U_{\text{windowssouth}} = 2.842.84 \frac{\text{W}}{\text{m}^2\text{K}}$$

$$, \text{ CF windowssouth}(\text{Heat Transfer Part}) = 2.842.84 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 6.89 \frac{\text{W}}{\text{m}^2}$$

$$\text{PXi windowssouth} = \text{ED} + \text{Ed} = 348 + 209 = 557$$

$$\text{SHGC} = 0.55$$

No internal shading, so IAC =1

$$\text{FFs} = 0.47$$

$$\text{CF windowsouth(Irradiation Part)} = \text{PFI} \times \text{SHGC} \times \text{IAC} \times \text{FFs}$$

$$q_{\text{windowsouth}} = A \times \text{CF windowsouth} = A \times (\text{CF windowsouth(Heat Transfer Part)} + \text{CF windowsouth(Irradiation Part)})$$

$$= 3.6 \text{ m}^2 \times (6.89 + 557 \times 0.54 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} = 553.72 \text{ W}$$

### **The heating load of the fixed window on the south is:**

$$q_{\text{windowsouth}} = A \times \text{HF windowsouth} = A \times U_{\text{windowsouth}} \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 253.56 \text{ W}$$

When the frame were to be aluminium,

$$U_{\text{windowsouth}} = 3.61 \frac{\text{W}}{\text{m}^2\text{K}}, \text{ HSGC} = 0.56$$

$$\text{CF' windowsouth(Heat Trasnfer Part)} = U'(\text{winidow south})(\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$= 3.61 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{windowsouth}} = A \times \text{CF' windowsouth}$$

$$= A \times (\text{CF' windowsouth(Heat Trasnfer Part)} + \text{CF' windowsouth(Irradiation Part)})$$

$$= 3.6 \text{ m}^2 \times (8.76 + 557 \times 0.56 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} = 559.30 \text{ W}$$

$$\text{Heating load } q'_{\text{windowsouth}} = A \times \text{HF' windowsouth}$$

$$= A \times U'_{\text{windowsouth}} \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 322.30 \text{ W}$$

### **The cooling load of the operable window on the south is:**

$$q_{\text{windowsouth}} = A \times \text{CF windowsouth}$$

$$A = 3.6 \text{ m}^2,$$

$$\text{CF windowsouth(Heat Trasnfer Part)} = U_{\text{windowsouth}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

,The window has an operable heat absorbing double layer glass with a wooden frame,

$$\text{So, } U_{\text{window}} = 2.87 \frac{\text{W}}{\text{m}^2\text{K}}$$

$$\text{, CF}_{\text{window}}(\text{Heat Transfer Part}) = 2.87 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 6.96 \frac{\text{W}}{\text{m}^2}$$

$$\text{P}_{\text{X}} = \text{ED} + \text{Ed} = 348 + 209 = 557$$

$$\text{SHGC} = 0.46$$

No internal shading, so IAC = 1

$$\text{FFs} = 0.47$$

$$\text{CF}_{\text{window}}(\text{Irradiation Part}) = \text{P}_{\text{X}} \times \text{SHGC} \times \text{IAC} \times \text{FFs}$$

$$q_{\text{window}} = A \times \text{CF}_{\text{window}} = A \times (\text{CF}_{\text{window}}(\text{Heat Transfer Part}) + \text{CF}_{\text{window}}(\text{Irradiation Part}))$$

$$= 3.6 \text{ m}^2 \times (6.96 + 557 \times 0.46 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} = 553.98 \text{ W}$$

**The heating load of the fixed window on the south is:**

$$q_{\text{window}} = A \times \text{HF}_{\text{window}} = A \times U_{\text{window}} \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 2.87 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 256.23 \text{ W}$$

$$\text{When the frame were to be aluminium, } U_{\text{window}} = 4.62 \frac{\text{W}}{\text{m}^2\text{K}}, \text{ SHGC} = 0.55$$

$$\text{CF}'_{\text{window}}(\text{Heat Transfer Part}) = U'_{\text{window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR}) \\ = 4.62 \frac{\text{W}}{\text{m}^2\text{K}} \times (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 11.21 \frac{\text{W}}{\text{m}^2}$$

$$\text{Cooling load } q'_{\text{window}} = A \times \text{CF}'_{\text{window}}$$

$$= A \times (\text{CF}'_{\text{window}}(\text{Heat Transfer Part}) + \text{CF}'_{\text{window}}(\text{Irradiation Part}))$$

$$= 3.6 \text{ m}^2 \times (11.21 + 557 \times 0.55 \times 1 \times 0.47) \frac{\text{W}}{\text{m}^2} = 558.70 \text{ W}$$

$$\text{Heating load } q'_{\text{window}} = A \times \text{HF}'_{\text{window}} = A \times U'_{\text{window}} \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 4.62 \frac{\text{W}}{\text{m}^2\text{K}} \times 24.8 \text{ K} = 412.47 \text{ W}$$