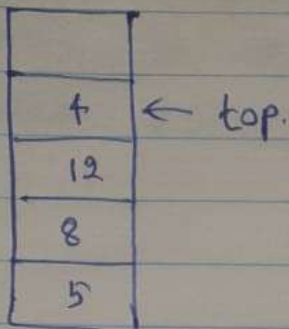
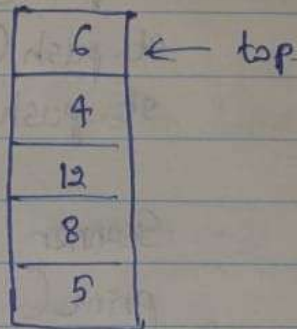


# DSA - 2022 Regular.

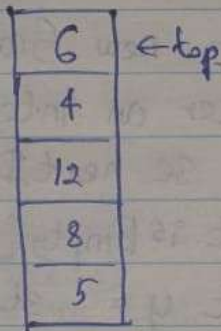
## Question 1



i) myStack.push(6)

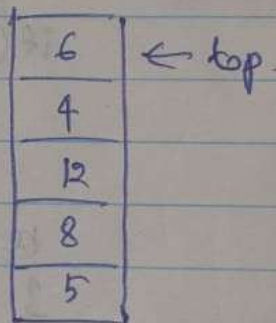


ii) myStack.peek()  
returns 6

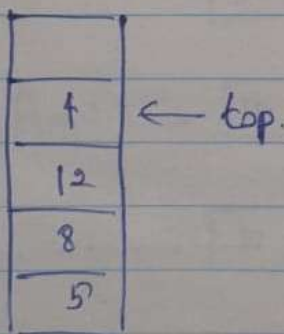


iii) myStack.push(2).

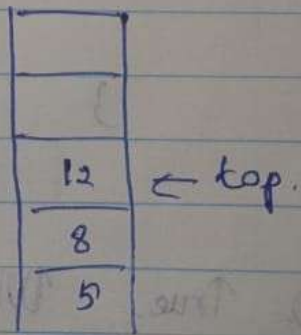
error → stack is full  
Cannot push element to the  
stack.



iv) myStack.pop();



v) myStack.pop.



b. class StackApp {  
public static void main (String c[] args) {

StackX st = new StackX(7);

st.push(20);

st.push(43);

st.push(12);

st.push(37);

Scanner sc = new Scanner (System.in);

print ("Enter an Integer: " + ~~sc.nextInt()~~);

int i = sc.nextInt();

while (!st.isEmpty()) {

int y = st.pop();

if (y == i) {

System.out.println ("The number is  
exists in the array;")

return true; break;

}

else {

return false;

}

}

}

}

c. d. True. When it comes to stack, we can do the insert and remove from the top only, and it has stack ~~class~~ has stackArray size when we creating a stack. We cannot insert any value when the stack is full. Queue is also fixed sized. We cannot insert any element to the QueueArray when the no of items at the queueArray equal to its maxSize.



And It leads to wasted space. In some cases array implementation may result in wasted space. If the capacity of the array is significantly larger than the no of items stored in the array.

(ii). false

Circular queue allow to insert items from the rear and remove done from the front.

After an element is removed front is incremented by one.  
After remove an element rear is increment by one.

(d).

	Linear Queue.	Circular Queue
boolean isEmpty()	if (nItems == 0) return true; else return false;	if (nItems == 0) return true; else return false;
boolean isFull()	if (rear == maxSize - 1) return true; else return false;	if (nItems == maxSize) return true; else return false.

## Question 2

(a) first → [100] ← (insertFirst(100));

(ii) first → [50] → [100]

(iii) first → [10] → [50] → [100]

(iv) first → [10] → [50] → [100] → [200]

(v) first → [10] → [50] → [100] → [200]  
first → [50] → [100] → [200]

```

b. public int countVacantBeds() {
    int count = 0;
    * Link current = first;
    while (current != null) {

```

```

6) 9 public int countVacantBeds() {
    int count = 0;
    PatientBed current = first;

    while (current != null) {
        if (current.vacant == 1) {
            count++;
        }
        else {
            current = current.next;
        }
    }

    return count;
}

```

9) find Vacant ()  $\rightarrow$  first vacant PatientBed.  
no vacant beds  $\rightarrow$  return NULL.

```

class Main {
    public static void main (String [] args) {
        PatientBed vacantBed = new LinkList();
        LinkList list = new LinkList();
        PatientBed vacantBed = list.findVacant();
        if (vacantBed != null) {
            vacantBed.assignBed();
            System.out.println("Assigned Bed No: " + vacantBed.bedNo);
        }
    }
}

```



else {

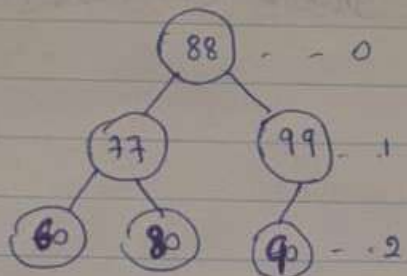
System.out.println("Patient beds are not available");

}

}

}

88, 99, 77, 80, 90, 60.



left to right

71.

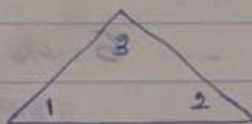
~~log no of nodes~~

no of depths = height

h = 2

911.

Post Order

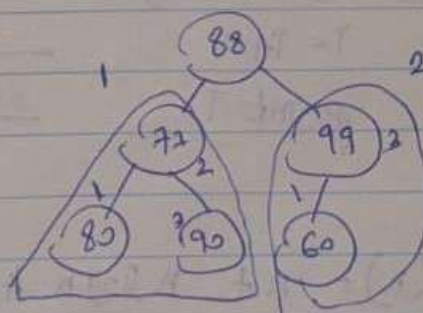


left, right, Root

```

private void postOrder(Node localNode) {
    postOrder(localNode.leftChild);
    local postOrder(localNode.rightChild);
    localNode.displayNode();
}
  
```

80 90 77 60 99 88

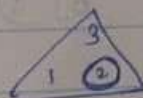


90.

public class display Greater Than Root {

display Greater Than Root(root);

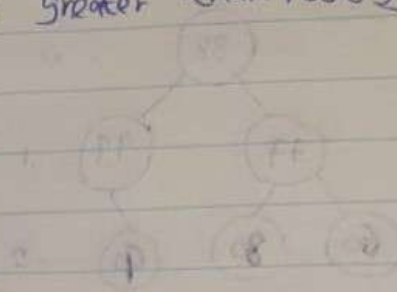
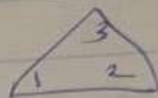
}



```

    public
    private void display Greater Than Root (Node local Node) {
        if (root == null) {
            System.out.println ("Tree is empty");
            return;
        }
        else {
            System.out.println ("Node greater than root");
            InOrder (root);
        }
    }
}

```



### Question 3

a) i)  $\int_1^5 x dx = \frac{x^2}{2} \Big|_1^5 = \frac{25}{2} - \frac{1}{2} = 12$

\* print i —  $1 \times 5$  —  $5$   
 while ( $j \leq 5$ ) —  $5 + 4 = 9$   
 $j = j + 1$  —  $2 \times 5 = 10$   
 print j —  $1 \times 5 = 5$   
 Sum —  $5 + 9 + 10 = 24$

$i = 2$   
 $i = 3$   
 $i = 4$   
 $i = 5$

ii)  $\int_1^0 x dx = -\frac{x^2}{2} \Big|_1^0 = -\frac{0}{2} + \frac{1}{2} = \frac{1}{2}$

b) i)  $T(n) = n + n \log n + n^2 + 5$   
 $O(n^2)$

ii)  $T(n) = 2n + 15$   
 $O(n)$

iii)  $T(n) = 3^n + n! + 4n^2 + n^n - 8$   
 $= O(n^n)$



⑧ T(n) = 2T(n/2) + O(n)

⑨ In Merge Sort Algorithm partition is always balanced.

⑩ A = {8, 2, 10, 3, 5}

MERGESORT (A, p, r)

1. If  $p < r$

2.  $q = \lfloor (p+r)/2 \rfloor = \lfloor (1+8)/2 \rfloor = 4$

3. MERGESORT (A, p, q)

⑪ A = {8, 2, 10, 3, 5}

PARTITION (A, p, r)

1.  $x = A[r]$   
 $x = A[8] = 5$

2.  $i = p-1$   
 $i = 1-1 = 0$

3. for  $j = p$  to  $r-1$   
 for  $j = 1$  to  $(5-1) 4$

$j = 1$

4. if  $A[j] \leq x$   
 $A[i] \leq 5$

$8 \leq 5$

(i)

$j=2$

if  $A[2] \leq 5$   
 $2 \leq 5 \checkmark$

5

$i = i+1$   
 $i = 0+1 = 1$

6.

exchange  $A[i]$  with  $A[j]$   
 $A[1] \leftrightarrow A[2]$   
 $8 \leftrightarrow 2$

2	8	10	3	5
---	---	----	---	---

~~$j=4$~~

7. exchange  $A[i+1]$  with  $A[r]$   
 $A[3]$  with  $A[5]$   
 $10 \leftrightarrow 5$

2	3	5	8	10
---	---	---	---	----

8. return  $i+1$

$2+1 = 3$

return  $3$

Question 4

(a) for  $i = \lfloor A.length/2 \rfloor$  down to 1

In this BUILD\_MAX\_HEAP function only calling for the parent nodes (non-leaf nodes)

$j=3$

if  $A[3] \leq 5$   
 $10 \leq 5 \times$

$j=4$

if  $A[4] \leq 5$   
 $3 \leq 5 \checkmark$

5.  $i = i+1$   
 $i = 1+1 = 2$

exchange  $A[i]$  with  $A[j]$   
 $A[2] \leftrightarrow A[4]$   
 $8 \leftrightarrow 3$

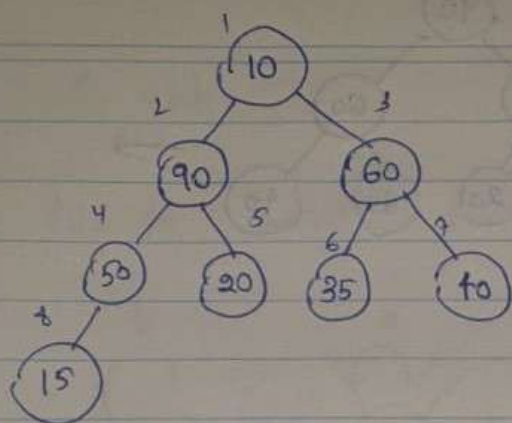
2	3	10	8	5
---	---	----	---	---



(11)

A

10	90	60	50	20	35	40	15
----	----	----	----	----	----	----	----

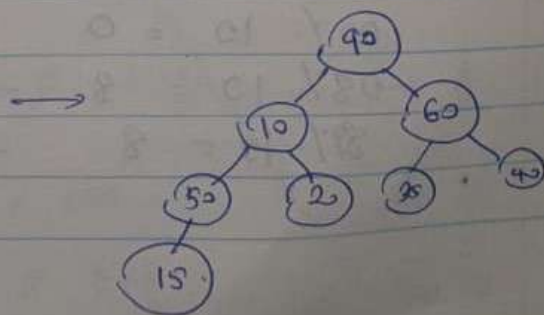
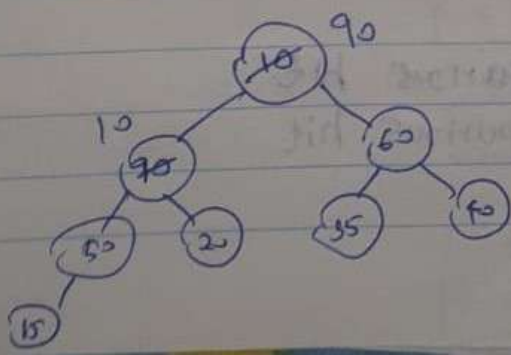


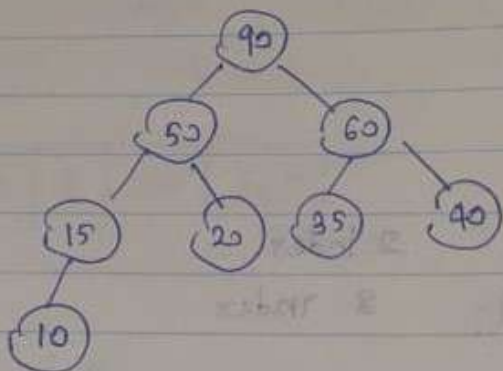
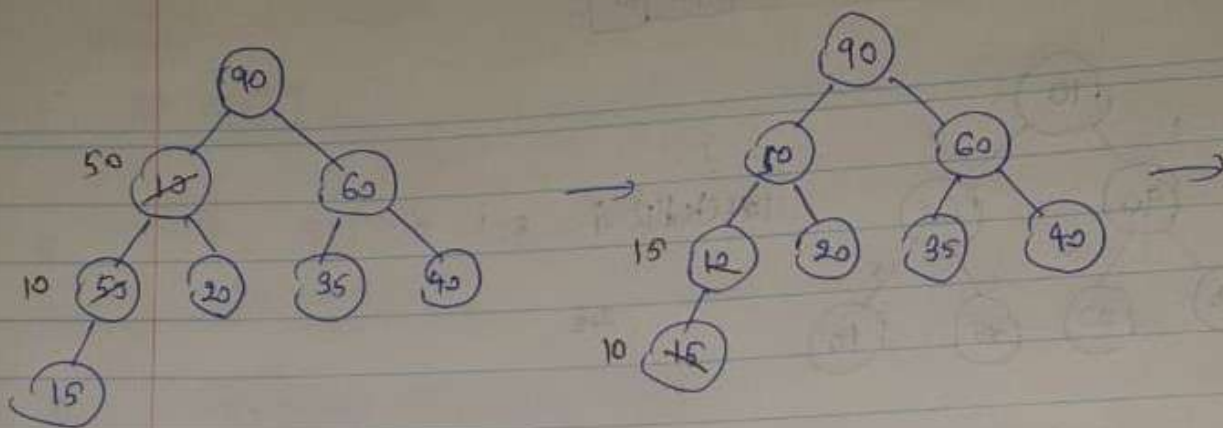
$$\text{leftChild}(i) = 2i, \quad 2 \times 1 = 2$$

2x2

8, 1  
MAX\_HEAPIFY(A, i)

1.  $l = \text{LEFT\_CHILD}(i);$  2 index.
2.  $r = \text{RIGHT\_CHILD}(i);$  3 index
3. if  $l \leq \text{heap\_size}[A]$  and  $A[l] > A[i]$   
 $2 \leq 8$  &&  $90 > 60$  ✓
4. largest = l  
 largest = 2
5. else largest = i; X
6. if  $r \leq \text{heap\_size}[A]$  and  $A[r] > A[\text{largest}]$   
 $3 \leq 8$  &&  $60 > 90$  X
7. largest = r; X
8. if largest  $\neq i$   
 $2 \neq 1$  ✓
9. exchange  $A[i] \leftrightarrow A[\text{largest}]$   
 $10 \leftrightarrow 90$
10. MAX\_HEAPIFY(A, largest)  
 MAX\_HEAPIFY(B, 2)





(b)

modulo  $q = 10$ .

$T = 902883280088$

$p = 28$

$p \% q = 28 \% 10 = 8$

~~$90 \% 10 = 0$~~

~~$02 \% 10 = 2$~~

~~valid~~

$90 \% 10 = 0$

$02 \% 10 = 2$

$28 \% 10 = 8$

→ valid

$88 \% 10 = 8$

→ Spurious hit.

$83 \% 10 = 3$

$32 \% 10 = 2$

$28 \% 10 = 8$

→ valid

$80 \% 10 = 0$

$00 \% 10 = 0$

$08 \% 10 = 8$

→ spurious hit.

$88 \% 10 = 8$

→ Spurious hit



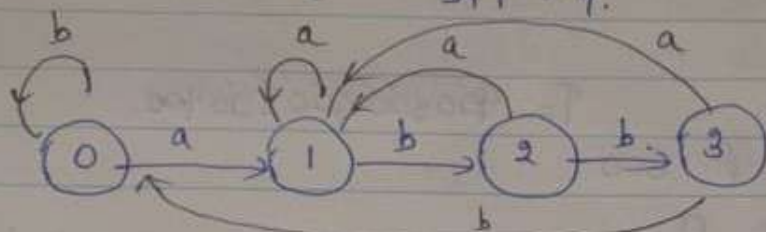
Valid hits = 2

Spurious hits = 3

(c).  $P = abb$

No of states = characters inside pattern + 1

$$= 3 + 1 = 4.$$



$\{a, b\}$

$T = a \checkmark$      $T = a \underline{b} a \times$      $T = a b a \times$      $T = a b b a$   
 $T = b \times$      $T = a b \checkmark$      $T = a b \underline{b} \checkmark$      $T = a \underline{b} \underline{b} \underline{b}$

(d). Native - String-Matcher ( $T, P$ )

$abb = P$

1.  $n = \text{length}(T)$     10

2.  $m = \text{length}(P)$     3

3. for  $s = 0$  to  $n - m$

if  $P[1..m] = T[s+1..s+m]$

$s = 0$

~~abb~~  $abb \neq aAb$      $\rightarrow 2$

$s = 1$

~~abb~~  $abb \neq Abb$      $\rightarrow 1$

$s = 2$

~~abb~~  $abb \neq bbb$      $\rightarrow 1$

$s = 3$

~~abb~~  $abb \neq bba$      $\rightarrow 1$

$s = 4$

$abb \neq baq$      $\rightarrow 1$

$s = 5$

$abb \neq aaa$      $\rightarrow 2$

$s = 6$

$abb \neq aab$      $\rightarrow 2$

$s = 7$

$abb \neq aba$      $\rightarrow 2$

$$\text{Comparisons} = 2 + 1 + 1 + 1 + 2 + 2 + 2 = 12 //$$

2002 - June

Question 4

① moduls  $q = 100$ .

$T = 900800600300900$

$P = 600$

$$600 \% 100 = \underline{0}$$

$$900 \% 100 = 0 \rightarrow \text{Spurious hit}$$

$$008 \% 100 = 8$$

$$080 \% 100 = 80 \rightarrow \text{Spurious hit}$$

$$800 \% 100 = 0 \rightarrow \text{Spurious hit}$$

$$006 \% 100 = 6$$

$$060 \% 100 = 60 \rightarrow \text{Spurious hit}$$

$$600 \% 100 = 0 \rightarrow \text{Valid}$$

$$003 \% 100 = 3$$

$$030 \% 100 = 30 \rightarrow \text{Spurious hit}$$

$$300 \% 100 = 0 \rightarrow \text{Spurious hit}$$

$$009 \% 100 = 9$$

$$090 \% 100 = 90 \rightarrow \text{Spurious hit}$$

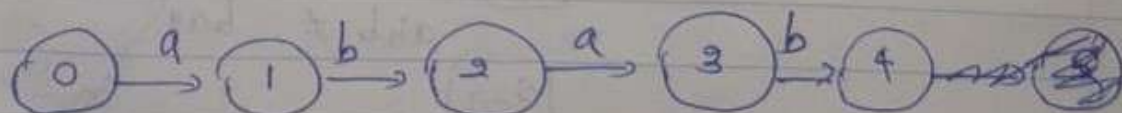
$$900 \% 100 = 0 \rightarrow \text{Spurious hit}$$

$$\text{Valid} = 1$$

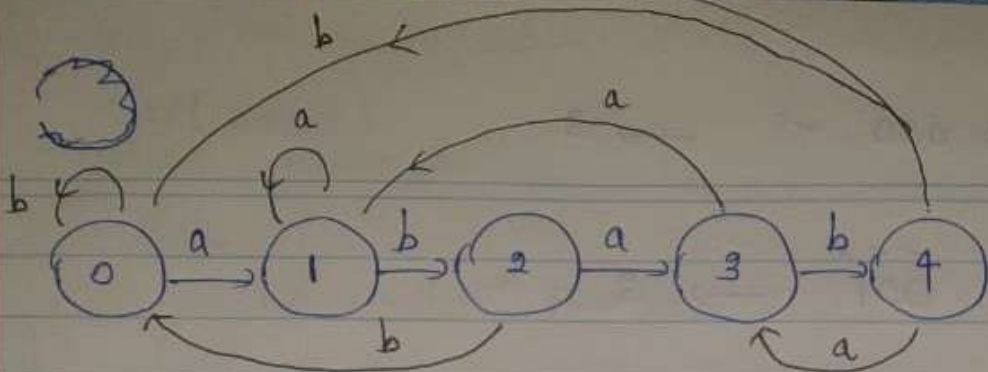
$$\text{Spurious} = \underline{\underline{11}}$$

$P = abab$

② No of states  $\rightarrow$  Characters inside pattern + 1  
 $= 4 + 1 = \underline{\underline{5}}$







$T = a \checkmark$   
 $T = b \times$

$T = abax \checkmark$   
 $T = ab \checkmark$

$T = abax \checkmark$   
 $T = abb \checkmark$

$T = abax \checkmark$   
 $T = abab \checkmark$

$T = abab/a$   
 $T = ababb$

$ab \checkmark$

$abab \checkmark$

$T = abab/a$   
 $T = ababb$   
 $\uparrow$   
 $T = abab \checkmark$

$T = abab \checkmark$

### 3. Native-String-Matcher ( $T, P$ )

1.  $n \leftarrow \text{length}(T) = 9$

2.  $m \leftarrow \text{length}(P) = 3$

3. for  $s \leftarrow 0$  to  $n-m$   
 $s \leftarrow 0$  to  $9-3=6$

do if  $[1..m] = T[s+1..s+m]$

$s=0$

$[1..3] = T[1..3]$

000 = 100  $\times \rightarrow 1$

$s=1$

000 = 000  $\checkmark \rightarrow 3$

$s=2$

000 = 001  $\times \rightarrow 3$

$s=3$

000 = 010  $\times \rightarrow 2$

$s=4$

000 = 100  $\times \rightarrow 1$

$$S=5$$

$$000 = 000 \checkmark \rightarrow 3$$

$$S=6$$

$$000 = 001 \rightarrow 3$$

(a)

$$3+3+3+3+2+1+1$$

$$12+4 = \underline{\underline{16}}$$

(b)

$$\text{Text size} = n$$

$$\text{Pattern size} = m.$$

In best case there is no any spurious hits or valid hits.

In best case Shifter should be 2.

Total number of best Shifter = 2

Total number of Comparisons = ~~30~~ = total number of Shifter

$$= n - m + 1$$

$$\text{The complexity} = \underline{\underline{O(n-m+1)}}$$

## Question 2

(1)

$$\text{Pow}(x, n) = x^n$$

$$x^n = x \times x^{n-1}$$

$$\text{Pow}(x, n-1) = x^{(n-1)}$$

$$\text{Pow}(x, n) = x \times x^{n-1}$$

$$\text{Pow}(x, n) = x \times \text{Pow}(x, n-1)$$



b.  $\text{int pow}(\text{int } x, \text{int } n) \{$   
      $\text{if}(n == 0)$   
          $\text{return } 1$   
      $\text{else}$   
          $\text{return } (x * \text{pow}(x, (n-1)));$   
 $\}$

c.  $\text{int pow}(\text{int } x, \text{int } n) \{ \rightarrow T(n)$   
      $\text{if}(n == 0) \rightarrow c_1$   
          $\text{return } 1 \rightarrow c_2$   
      $\text{else}$   
          $\text{return } (\underbrace{x}_{c_3} * \underbrace{\text{pow}(x, (n-1))}_{T(n-1)});$   
 $\}$

$n > 0$   
     recurrence equation  $T(n) = c_1 + c_3 + T(n-1)$   
      $= c + T(n-1)$   
      $= \underline{\underline{O(n)}}$

2.  $\text{sum} \leftarrow 0$   
     for  $i \leftarrow n$  down to 0  
          $\text{sum} = \text{sum} + 1$   
      $\rightarrow 1$   
      $\rightarrow (n+1)$   
      $\rightarrow (n+2)$   
      $\rightarrow (n+2)$   
      $\rightarrow 2(n+1)$   
      $\rightarrow 1$   
      $\rightarrow 3n+5$   
      $\rightarrow 2n+2$   
      $\rightarrow 5n+8$

3. 

1	2	3	4	5	6
28	15	1	20	0	8

Procedure  $\text{QUICKSORT}(A, p, r)$

1.  $\text{if } p < r$   $1 < 6$  ✓
2. then  $q \leftarrow \text{PARTITION}(A, p, r)$   
      $1, 6$   
      $1 \rightarrow A[1]$
3.  $\text{QUICKSORT}(A, p, q-1)$
4.  $\text{QUICKSORT}(A, q+1, r)$

# Procedure PARTITION ( $A, p, r$ )

1.  $x \leftarrow A[r]$

$x \leftarrow A[6]$

$x \leftarrow 8$

$x = 8$

2.  $i \leftarrow p - 1$

$i = 1 - 1 = 0$

3. for  $j \leftarrow p$  to  $r - 1$

for  $j = 1$  to 5

$j = 1$

do if  $A[j] \leq x$

$A[1] \leq 8$

$28 \leq 8 \times$

$j = 2$

do if  $A[j] \leq x$

$A[2] \leq 8$

$15 \leq 8 \times$

$j = 3$

do if  $A[j] \leq x$

$A[3] \leq 8$

$1 \leq 8$

5. then  $i \leftarrow i + 1$

$i = 0 + 1 = 1$

6

exchange  $A[i] \leftrightarrow A[j]$

$A[1] \leftrightarrow A[3]$

$28 \leftrightarrow 1$



1	16	28	30	0	8
---	----	----	----	---	---

7. ~~exchange~~  $A[i+1] \leftrightarrow A[r]$

~~$A[2] \leftrightarrow A[6]$~~

~~$15 \leftrightarrow 8$~~

1	8	28	30	0	15
---	---	----	----	---	----

8. ~~return~~  $i+1$

return 2

4. ~~exchange~~ A for  $j=4$

do if  $A[i] \leq x$

$A[4] \leq 8$

$30 \leq 8 \times$

4.  $j=5$

do if  $A[i] \leq x$

$A[5] \leq 8$

$0 \leq 8 \checkmark$

5. then  $i = i+1$

$i = 1+1 = 2$

6. exchange  $A[i] \leftrightarrow A[j]$

$A[2] \leftrightarrow A[5]$

$15 \leftrightarrow 0$

1	0	28	30	15	8
---	---	----	----	----	---

7. exchange  $A[i+1] \leftrightarrow A[r]$

$A[3] \leftrightarrow A[6]$

$28 \leftrightarrow 8$

1	0	8	28	0	
---	---	---	----	---	--

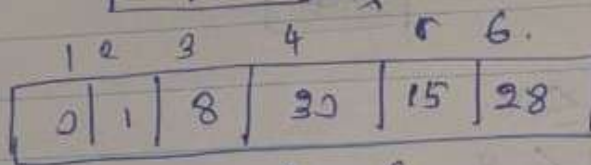
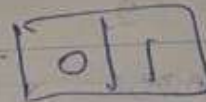
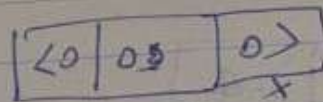
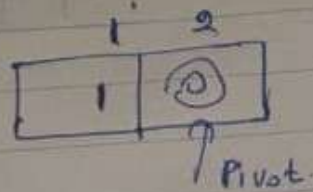
8. return  $i+1$

return 3

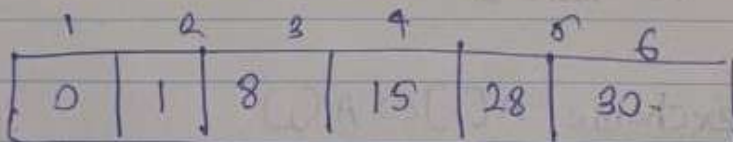
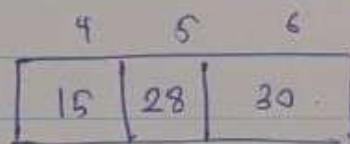
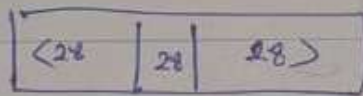
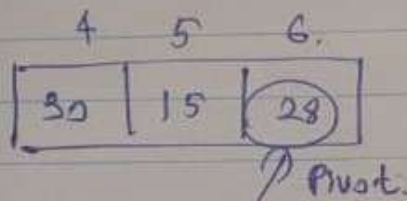
1	0	8	30	15	28
---	---	---	----	----	----

diagrammatic way.

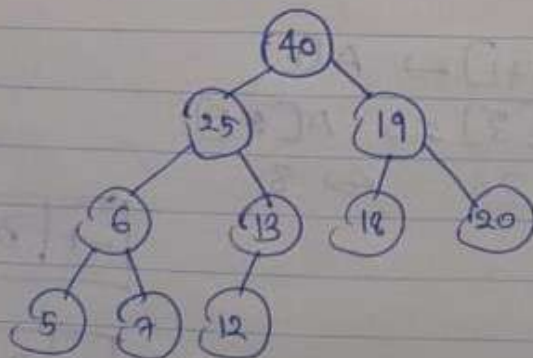
③ QUICKSORT ( $A, p, q-1$ )



④ QUICKSORT ( $A, q+1, p$ )



⑤  $\langle 40, 25, 19, 6, 13, 18, 20, 5, 7, 12 \rangle$



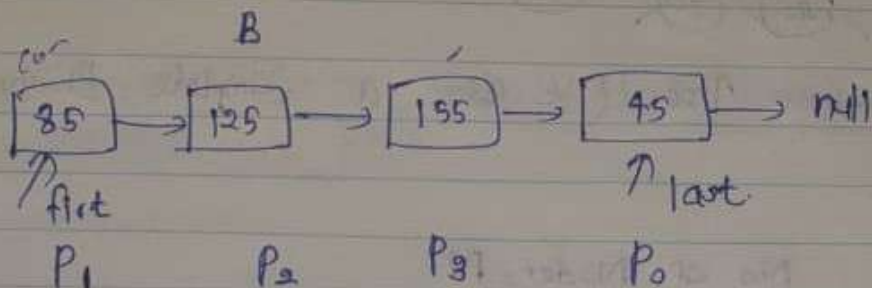
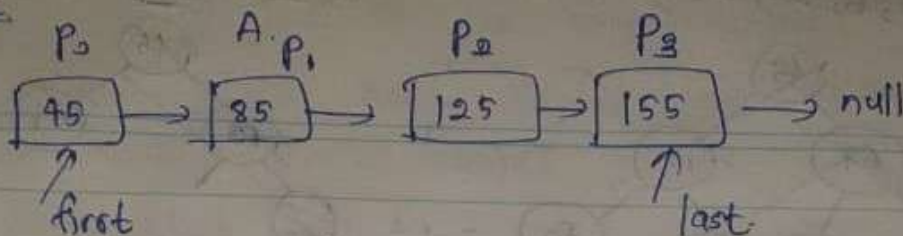
No

Because the root 6 and 19 are not the maximum values when it compares with ~~it~~ <sup>their</sup> right and left child nodes.



# Question 3

1.



A ~~from~~ LinkedList

LinkedList P3 = null last;

LinkedList P0 = first;

LinkedList P1 = P0.next;

LinkedList P2 = P1.next;

LinkedList P3 = P2.next;

P3.next = null

B LinkedList

first = P1

P1.next = P2

P2.next = P3

P3.next = P0

~~last = null~~

~~P0.next = null~~

P0 = last

P0.next = null

2. public deleteLast(int key) {

Link cur = first;

2. public boolean deleteLast() {

Link cur = first;

~~while (cur != null)~~

~~while (cur != null)~~

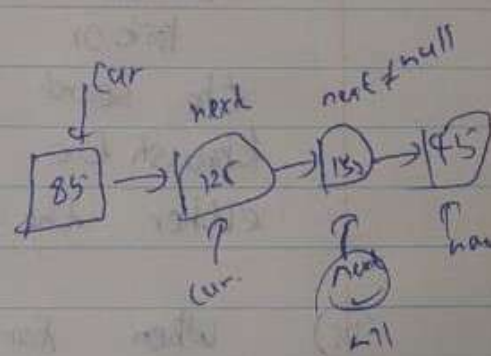
while (current.next.next != null) {

current = current.next;

}

current.next = null;

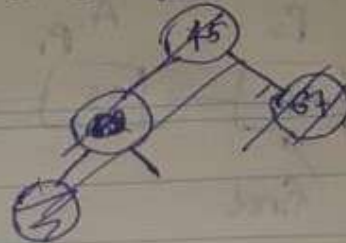
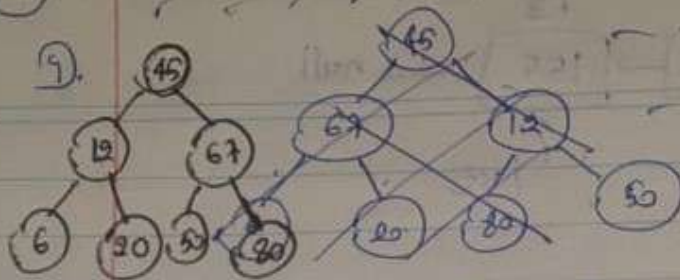
}



3.

45, 67, 12, 6, 20, 80, 50.

6, 12, 20, 45, 50, 67, 80



9i.

Full Binary Tree (it also a Complete Binary Tree.)

9ii.

2

9v.

No of Nodes =  $N$

Searches is depend on the No of Nodes inside the binary tree.

$$T(N) = O(\log N)$$

9vi.

This is a balanced case then it's  $T(N) = O(\log N)$ .  $\rightarrow$  best case  
(worst case  $\rightarrow O(N)$ )

9vii.

edges =  $N$

$O(N)$

best case  $\rightarrow$  target value at the head  
 $O(1)$

worst case

(In this case target value is located somewhere within the linked list or not present at all, so, the search operation would need to traverse through the linked list, examining each link until either the target value is found or not).

9viii.

When for a binary search tree, the average and worst case time complexity for searching is  $O(\log N)$  in a balanced tree. This means that as the number of Nodes increases, running time also increase. This logarithmic growth allows binary search tree to efficiently search for values even with large  $N$  values.



In Linked List, the worst-case time complexity for searching is  $O(N)$ . Number of Link  $\uparrow$  then running times grows linearly.  
The linear growth makes Linked List less efficient for search when dealing with large  $N$  values compared to binary search trees.

$\therefore$  Binary Search tree is faster than linked list when we searching a value

#### Question 4

(1.)

Stack.

Follows LIFO principle  
Array size is fixed  
and linear data  
structure.

Queue.

Follows FIFO principle.  
Size is fixed and linear  
data structure.

(2.)

```
public void deleteMiddle() {  
    int count = 0;
```

```
    while (!s1.isEmpty()) {  
        s1.push(s1.pop());  
        count = count + 1;
```

```
    }
```

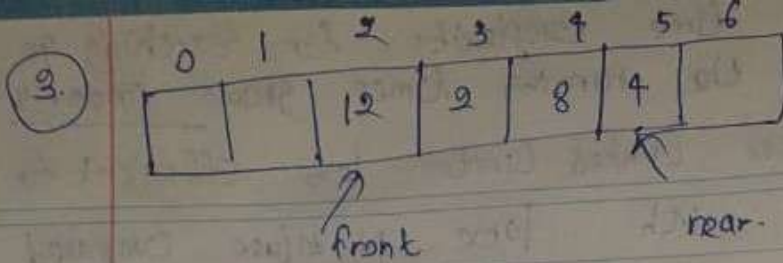
```
    int middle = count / 2;
```

```
    for (int i = 0; i < middle; i++) {  
        s1.push(s1.pop());
```

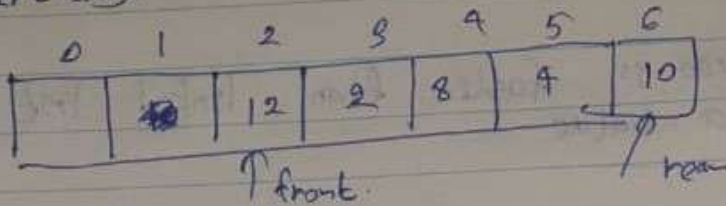
```
    }
```

```
    s1.push(s1.pop());
```

```
}
```

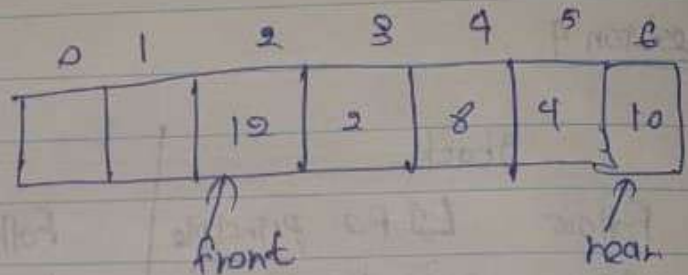


i) Insert (10)



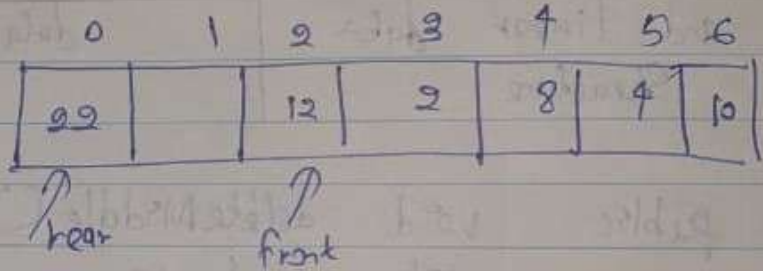
ii) peek Front()

return 12

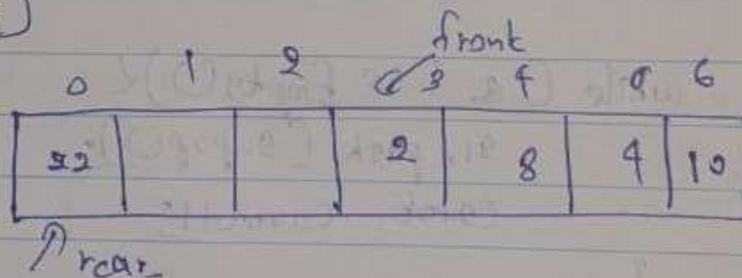


iii) Insert (22)

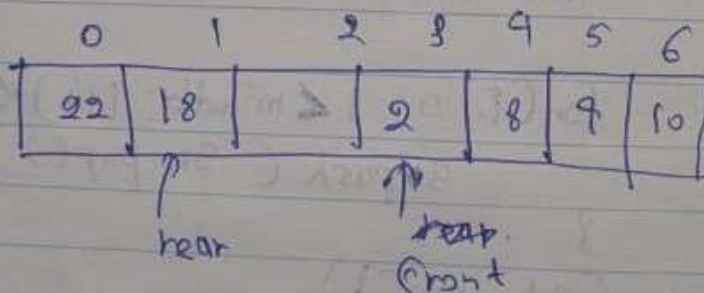
~~Insert (22)~~



iv) remove()



v) insert (18)





```

5. public void calmean() {
    if (nItems == 0) {
        System.out.println("Queue is empty");
    }
    else {

```

```

6. public void calculate Mean And Insert() {

```

```

    Queue tempQueue = new Queue();
    double sum = 0.0;
    int count = 0;

```

```

    while (!queue.isEmpty()) {

```

```

5. public void cal Mean And Insert (Queue <Double> q) {

```

```

    Queue <Double> tempQueue = new LinkedList<>();
    double sum = 0.0;
    int count = 0;

```

```

    while (!q.isEmpty()) {

```

```

        double value = q.remove();
        sum += value;
        count++;
        tempQueue.insert(value);
    }

```

```

    double mean = sum / count;

```

```

    q.insert(mean);

```

```

    while (!tempQueue.isEmpty()) {

```

```

        q.insert(tempQueue.remove());
    }

```

```

}

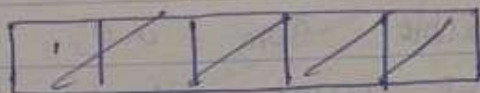
```

## Q. ~~Calculate~~ Cal Mean And Insert (2)

2019-20 October

### Question 01

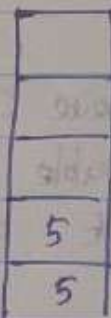
(a) i) s. push(5);



ii) s. push(s. peek());

s. peek() → returns 5

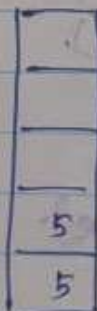
s. push(5)



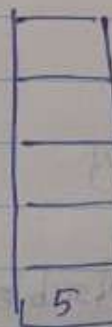
iii) s. push(s. pop());

s. pop() → 5

s. push(5);



iv) s. pop();



ii) public void push(int j) {

if (top == maxSize - 1) — ①

System.out.println("stack is full");

else {

stack[top++] = j; — ②

}

}

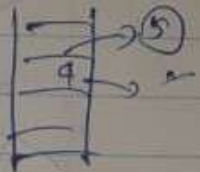
① and ② are edited.



```

iii) public StackMain {
    public static void main (String[] args) {
        Stack s1 = new Stack(5);
        Stack s2 = new Stack(5);
        while (!s1.isEmpty()) {
            int value = s1.pop();
            if (value % 2 != 0)
                if (value % 2 == 0)
                    s2.push(value);
            }
        }
    }
}

```



```

iii) public StackMain {
    public static void main (String[] args) {
        Stack s1 = new Stack(5);
        Stack s2 = new Stack(5);
        while (!s2.isEmpty()) {
            if (true)
                int value = s2.pop();
                if (value % 2 == 2)
                    s2.push(value);
            }
        }
        while (!s2.isEmpty())
            s1.push(s2.pop());
    }
}

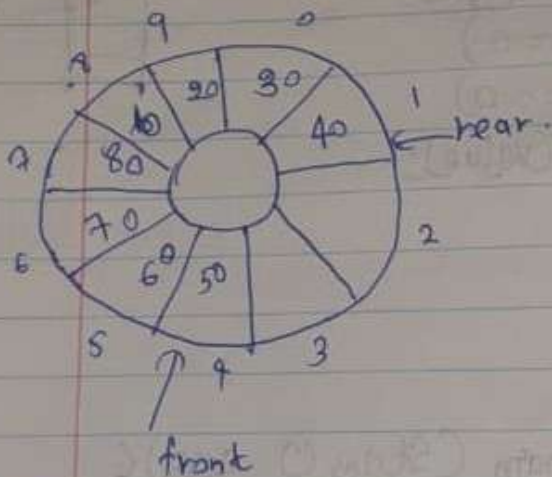
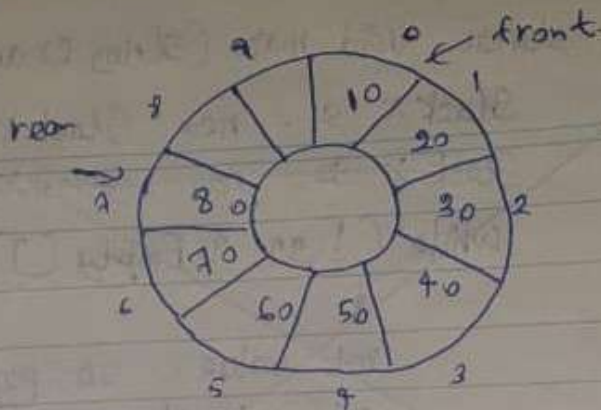
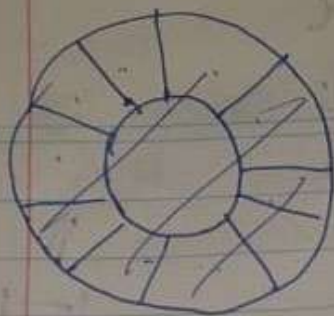
```

```

}

```

(b)



(i) queue is empty and front assign to 0 and rear value assign to -1  
no of Items also 0

```

public int getSize() {
    int nItems = 0;
    if (is Empty()) {
        System.out.println("No of Items empty");
    }
    else {
        while (!is Empty()) {
            int nItems =

```

```

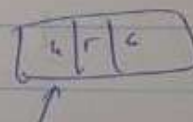
}
public int getSize() {
    return nItems;
}

```

```

c. public Main {
    public static void main(String[] args) {
        Stack myStack = new Stack(5);
        Queue myQueue = new Queue(5);

```





(C) while (!myQueue.isEmpty()) {  
 myStack.push(myQueue.remove());

}

while (!myStack.isEmpty()) {  
 myQueue.push(myStack.pop());  
 myQueue.insert(myStack.pop());

}

}

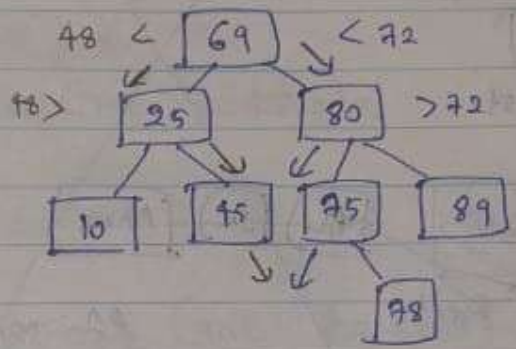
}

### Question 2

(a) 9

75

75



(ii) 45

45

(iii)

non leaf -> parent

25, 80, 75, 69

(iv)

45

(v)

9

(vi)

No

(b) i. Student Lmark = studentMarks.  
 maximum();  
 Lmark.displayDetails();

ii. Student Lmark = studentMarks.  
 minimum();  
 Lmark.displayDetails();

iii. ~~Student~~ allmark = studentMarks.  
 descendingOrder();  
~~allmark.display~~  
 System.out.println(allmark);

~~DD~~ pub/sc

10

while (! cur

9fC

return

~~else L~~

~~has been before~~

3

return false

91

pub/sc

book

②

6.5.5

while

if (

return

3

else

car =

3

3

return

3.

98

Last Page.



```
91) public void lending (int bookNo) {  
    Book book = isAvailable (bookNo)
```

```
    if (book != null) {
```

```
        book.numOfCopies--;
```

```
        System.out.println ("Borrowed");
```

```
    }
```

```
    else {
```

```
        System.out.println ("bookNo is not available");
```

```
    }
```

```
}
```

### Question 3

a)  $O(1)$  In this case 'add' method is a loop it is running 100 times. The loop always executes fixed number of iterations. It has a constant time.  $\therefore O(1) = T(n)$

b) i) QUICKSORT (Arr, low, high)

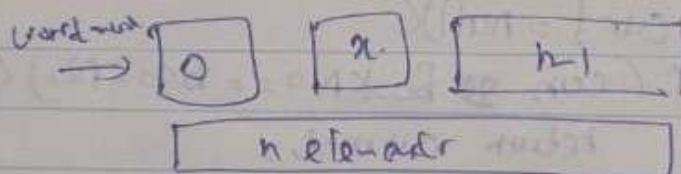
1. If ~~low < high~~ low < high.
2.  $P = \text{PARTITION}(\text{Arr}, \text{low}, \text{high})$
3.  $\text{QUICKSORT}(\text{Arr}, \text{low}, P-1)$
4.  $\text{QUICKSORT}(\text{Arr}, P+1, \text{high})$

1, 3 and 4 lines are incorrect, a correct algorithm

ii)

QUICKSORT (Arr, low, high)  $\rightarrow T(n)$

1. If ~~if~~ ~~low~~ < ~~low~~ high  $\rightarrow C_1$
2.  $P = \text{PARTITION}(\text{Arr}, \text{low}, \text{high}) \rightarrow C_2 \cdot n$
3.  $\text{QUICKSORT}(\text{Arr}, \text{low}, P-1) \rightarrow T(n)$
4.  $\text{QUICKSORT}(\text{Arr}, P+1, \text{high}) \rightarrow T(n-1)$



$$T(n) = T(0) + T(n-1) + C_2 \cdot n + C_1$$

$$T(n) = C_2 n + T(n-1)$$

iii)  $T(n) = T(n-1) + C_2 \cdot n$

$$T(n-1) = T(n-2) + C_2 (n-1)$$

$$T(n-2) = T(n-3) + C_2 (n-2)$$

⋮

⋮

⋮

$$T(2) = T(1) + C_2 \cdot 2$$

$$T(1) = T(0) + C_2 \cdot 1$$

$$T(0) = 0$$



$$T(n) = C_2 \cdot 1 + C_2 \cdot 2 + \dots + C_2(n-2) + C_2(n-1) + C_2 \cdot n$$

$$T(n) = C_2 (1 + 2 + \dots + (n-2) + (n-1) + n)$$

$$S_n = \frac{n}{2} (a + l)$$

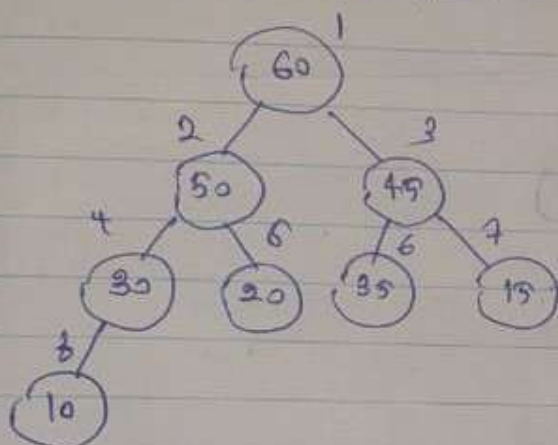
$$S_n = \frac{n}{2} (1 + n)$$

$$T(n) = C_2 \left( \frac{n}{2} + \frac{n^2}{2} \right)$$

$$T(n) = O(n^2)$$

Q. i) Parent node should be greater than ~~the~~ or equal to their child nodes.

(91)



Yes. All the parent nodes are greater than their child nodes values.

d. MIN\_HEAPIFY(A, i)

l = LEFT(i)

r = RIGHT(i)

if  $l \leq A.heap\_size$  and  $A[l] < A[i]$

Smallest = l;

else

Smallest = i;

if  $r \leq A.heap\_size$  and  $A[r] < A[Smallest]$

Smallest = r;

if Smallest  $\neq$  i

exchange A[i] with A[Smallest]

MIN\_HEAPIFY(A, Smallest)

HEAP\_EXTRACT\_MIN(A[1..n])

if  $A.heap\_size \geq 1$

min = A[1]

A[1] = A[A.heap\_size]

A.heap\_size = A.heap\_size - 1

MIN\_HEAPIFY(A, 1)

return min

91) public void lending (int bookNo) <  
 Book book = isAvailable (bookNo)

if (book != null) <

book. num of Copies --;

System.out.println ("Borrowed");

}

else <

System.out.println ("bookNo is not available");

}

}

#### Question 4

a) Native String - Matcher (T, P)

1.  $n = T.length \rightarrow 9$

2.  $m = P.length \rightarrow 3$

3. for  $s=0$  to  $n-m$   
 $s=0$  to  $9-3=6$

f. if  $P[1..h] = T[s+1..s+m]$

•  $\bar{a}bb = \bar{a}aa \times \rightarrow 2$

•  $bba = \bar{a}aa \rightarrow 1$

•  $bac = \bar{a}aa \rightarrow 1$

•  $\bar{a}cd = \bar{a}aa \rightarrow 2$

•  $cda = \bar{a}aa \rightarrow 1$

•  $daa = \bar{a}aa \rightarrow 1$

•  $\bar{a}ab = \bar{a}aa \rightarrow 3$

5. then print "Pattern occurs with shift" s 7

9

$$2 + 2 + 3 + 1 + 1 + 1 + 1 = 11$$

91)

3 valid shifters and 4 invalid shifters

2 valid shifters and 6 invalid shifters

b) 9

7



(b) 9  $q = 100$

$p = 100$

1.  $p \cdot q = 100 \cdot 100 = 0$

Text  $T = 203410052006$

$203 \cdot 100 = 3$

$034 \cdot 100 = 34$

$341 \cdot 100 = 41$

$410 \cdot 100 = 10$

$100 \cdot 100 = 0 \rightarrow \text{valid}$

$005 \cdot 100 = 5$

$052 \cdot 100 = 52$

$200 \cdot 100 = 0 \rightarrow \text{spurious}$

valid  $\rightarrow 1$

$006 \cdot 100 = 6$

spurious hit  $\rightarrow 1$

(ii) Increasing the modulus value

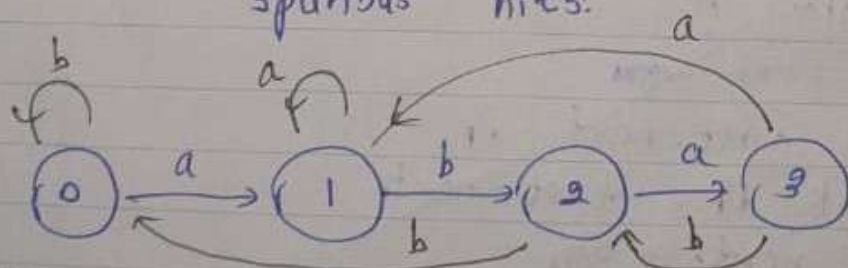
(iii) Worst-case scenario occurs when the Rabin-Karp algorithm has

All the hits valid

All the hits spurious

All hits are combination of valid & spurious hits.

(c)



$T = a$

$T = b$

$T = a b a x$

$T = a b$

$T = a b a$

$T = a b b$

$x =$

$T = a b a a$

$T = a b a b$



## Diagram A

Link first = Anne.

Link P1 = John

Link P2 = ~~Jenny~~ Toby.

first.next = P1

P1.next = P2 first.next.next

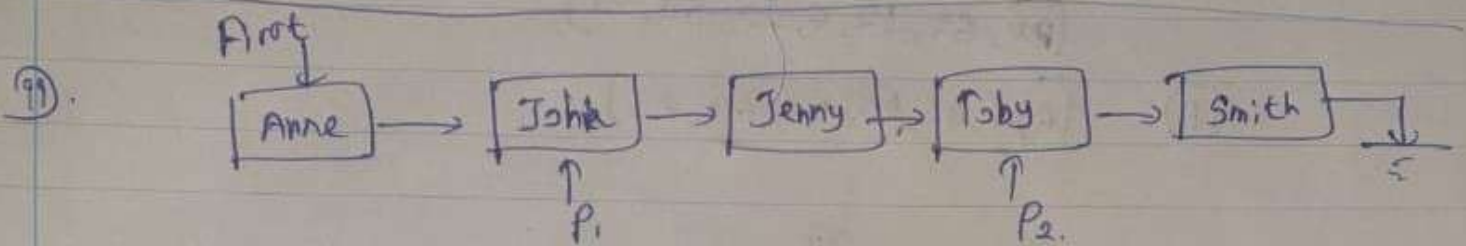
## Diagram B

first = Anne.

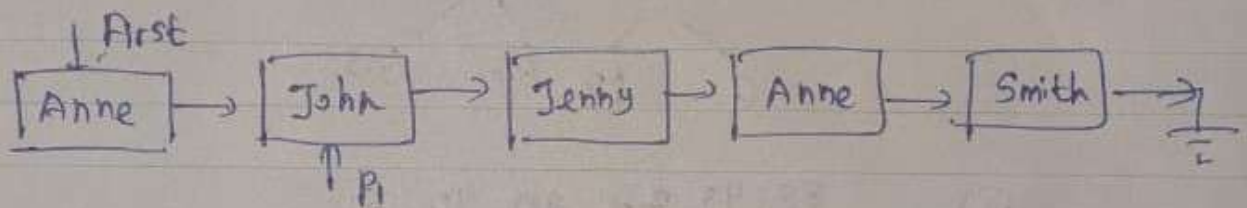
first.next = Jenny;

P1.next = P2

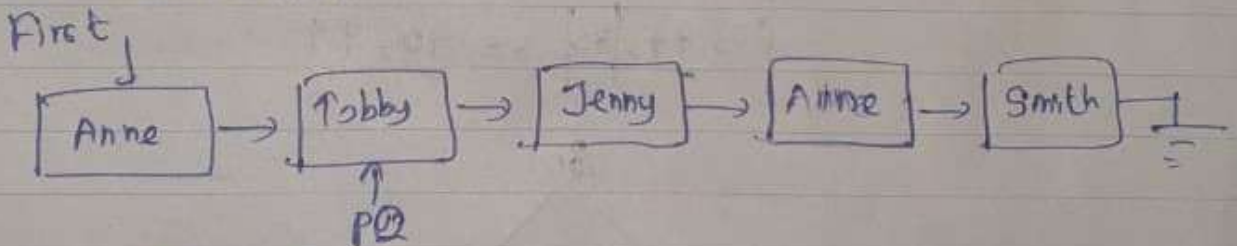
P2.next = Smith.



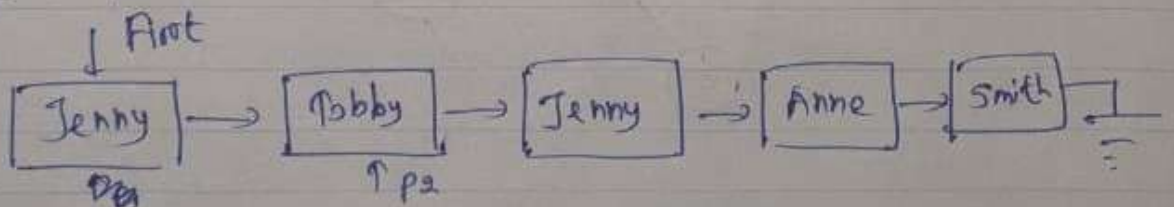
① P1.next.next = first.



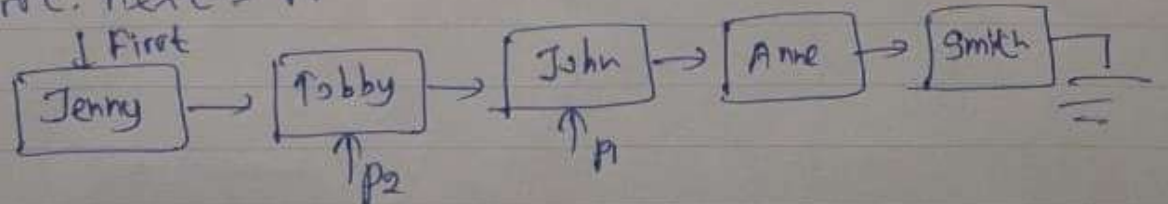
② first.next = P2.



③ first = P2.next.



④ first.next = P1





P2. next = NULL.

