

1. The intrinsic carrier density is $1.5 \times 10^{16} \text{ m}^{-3}$. If the mobility of electron and hole are 0.13 and $0.05 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$, calculate the conductivity.

Solution :

Given :

$$n_i = 1.5 \times 10^{16} \text{ m}^{-3}$$

$$\mu_e = 0.13 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$

$$\mu_h = 0.05 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$

$$\text{Conductivity } \sigma = n_i e (\mu_e + \mu_h)$$

$$\sigma = 1.5 \times 10^{16} \times 1.6 \times 10^{-19} (0.13 + 0.05)$$

$$\text{Conductivity } \sigma = 4.32 \times 10^{-4} \Omega^{-1} \text{ m}^{-1}$$

2. The Intrinsic carrier density at room temperature in Ge is $2.37 \times 10^{19} \text{ m}^{-3}$ if the electron and hole mobilities are 0.38 and $0.18 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ respectively, calculate the resistivity.

Given:

$$n_i = 2.37 \times 10^{19} \text{ m}^{-3}$$

$$\mu_e = 0.38 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$

$$\mu_h = 0.18 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$

$$\text{Conductivity } \sigma = n_i e (\mu_e + \mu_h)$$

$$= 2.37 \times 10^{19} \times 1.6 \times 10^{-19} (0.38 + 0.18)$$

$$= 2.1235 \Omega^{-1} \text{ m}^{-1}$$

$$\text{Resistivity } \rho = \frac{1}{\sigma}$$

$$\rho = \frac{1}{2.1235}$$

$$\text{Resistivity } \rho = 0.4709 \Omega \text{ m}$$

3. The Hall coefficient of certain silicon specimen was found to be $-7.35 \times 10^{-5} \text{ m}^3 \text{ C}^{-1}$ from 100 to 400 K. Determine the nature of the semiconductor. If the conductivity was found to be $200 \Omega^{-1} \text{ m}^{-1}$. Calculate the density and mobility of the charge carrier.

Solution:

$$\text{Conductivity } \sigma = 200 \, \Omega^{-1} \text{m}^{-1}$$

$$\text{Hall co-efficient } R_H = -7.35 \times 10^{-5} \text{m}^3 \text{C}^{-1} \quad \dots (1)$$

a) Density of electrons

$$n = \frac{-1}{R_H e} \text{ (from equation (1))}$$

$$n = \frac{1}{(7.35 \times 10^{-5} \times 1.609 \times 10^{-19})}$$

$$\text{(i.e.)} = 8.455 \times 10^{22} \text{m}^{-3}$$

We know Conductivity

$$\sigma = n e \mu_e$$

b) Mobility

$$\mu = \frac{\sigma}{n e} = \frac{200}{8.455 \times 10^{22} \times 1.6 \times 10^{-19}}$$

$$= 0.0147$$

$$\text{Mobility } \mu = 0.0147 \text{m}^2 \text{v}^{-1} \text{s}^{-1}$$

$$\text{Density of electrons (n)} = 8.053 \times 10^{22} \text{m}^{-3}$$

$$\text{Mobility } (\mu) = 0.0147 \text{m}^2 \text{v}^{-1} \text{s}^{-1}$$

4. In a P-type germanium, $n_i = 2.1 \times 10^{19} \text{m}^{-3}$ density of boron $4.5 \times 10^{23} \text{atoms /m}^3$. The electron and hole mobility are 0.4 and $0.2 \text{m}^2 \text{v}^{-1} \text{s}^{-1}$ respectively. What is its conductivity before and after addition of boron atoms.

Solution:

Given:

$$\text{Intrinsic carrier concentration } n_i = 2.1 \times 10^{19} \text{m}^{-3}$$

$$\text{Mobility of electrons } \mu_e = 0.4 \text{m}^2 \text{v}^{-1} \text{s}^{-1}$$

$$\text{Mobility of holes } \mu_h = 0.2 \text{m}^2 \text{v}^{-1} \text{s}^{-1}$$

a) Conductivity before the addition of boron atoms

$$\sigma = n_i e (\mu_e + \mu_h)$$

$$= 2.1 \times 10^{19} \times 1.6 \times 10^{-19} (0.4 + 0.2)$$

$$= 2.016 \, \Omega^{-1} \text{m}^{-1}$$

b) Conductivity after the addition of boron atoms, Boron is a P-type impurity atom

$$\sigma = p e \mu_h$$

$$= 4.5 \times 10^{23} \times 1.6 \times 10^{-19} \times 0.2$$

$$\sigma = 14400 \, \Omega^{-1} \text{m}^{-1}$$

5. An N-type semiconductor has hall coefficient = $4.16 \times 10^{-4} \text{ m}^3 \text{ C}^{-1}$. The conductivity is $108 \text{ } \Omega^{-1} \text{ m}^{-1}$. Calculate its charge carrier density ' n_e ' and electron mobility at room temperature.

Solution:

Given:

Given:

$$\text{Hall Co-efficient } R_H = 4.16 \times 10^{-4} \text{ m}^3 \text{ C}^{-1}$$

$$\text{Conductivity } \sigma = 108 \text{ } \Omega \text{ m}^{-1}$$

1. For 'n' type the charge carriers density $n_e = \frac{-1}{R_H e}$ Here the negative sign indicates the field direction alone.

$$n_e = \frac{3\pi}{8} \frac{-1}{R_H e}$$

$$n_e = \left[\frac{3 \times 3.14}{8} \right] \left[\frac{1}{1.6 \times 10^{-19} \times 4.6 \times 10^{-4}} \right]$$

$$n_e = 1.7690 \times 10^{22} \text{ m}^{-3}$$

2. Electron mobility $\mu_e = \frac{\sigma_e}{n_e e}$

$$= \frac{108}{(1.7690 \times 10^{22} \times 1.6 \times 10^{-19})}$$

$$\mu_e = 0.0381 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$$

6. In an N-type semiconductor, the concentration of electron is $2 \times 10^{22} \text{ m}^{-3}$. Its electrical conductivity is $112 \text{ } \Omega^{-1} \text{ m}^{-1}$. Calculate the mobility of electrons.

Solution:

Given:

Conductivity $\sigma = 112 \Omega^{-1} \text{ m}^{-1}$

Carrier concentration of electron

$$n_i = 2 \times 10^{22} \text{ m}^{-3}$$

$$\begin{aligned} \text{Hall coefficient } R_H &= \frac{1}{ne} \\ &= \frac{1}{2 \times 10^{22} \times 1.6 \times 10^{-19}} \\ &= 3.125 \times 10^{-4} \text{ m}^3 \text{ C}^{-1} \end{aligned}$$

$$\begin{aligned} \text{Mobility } \mu &= \sigma R_H = 112 \times 3.125 \times 10^{-4} \\ &= 0.035 \text{ m}^2 \text{ v}^{-1} \text{ s}^{-1} \end{aligned}$$

7. A semiconducting crystal with 12 mm long, 5 mm wide and 1 mm thick has a magnetic density of 0.5 Wbm^{-2} applied from front to back perpendicular to largest faces. When a current of 20 mA flows length wise through the specimen, the voltage measured across its width is found to be $37\mu\text{V}$. What is the Hall coefficient of this semiconductor?

Solution:

Given:

$$\text{Hall voltage } V_H = 37 \mu\text{V} = 37 \times 10^{-6} \text{ V}$$

$$\text{Breath of the material } t = 1 \text{ mm} = 1 \times 10^{-3} \text{ m}$$

$$\text{Current } I_H = 20 \text{ mA} = 20 \times 10^{-3} \text{ A}$$

Magnetic flow density

$$B = 0.5 \text{ Wbm}^{-2}$$

$$\begin{aligned} \text{Hall coefficient } R_H &= \frac{V_H t}{I_H B} \\ &= \frac{37 \times 10^{-6} \times 1 \times 10^{-3}}{20 \times 10^{-3} \times 0.5} \\ R_H &= 3.7 \times 10^{-6} \text{ C}^{-1} \text{ m}^3 \end{aligned}$$

$$\therefore \text{Hall coefficient } R_H = 3.7 \times 10^{-6} \text{ C}^{-1} \text{ m}^3$$

8. Find the resistance of an intrinsic Ge rod 1 mm long, 1 mm wide and 1 mm thick at 300 K. the intrinsic carrier density $2.5 \times 10^{19} \text{ m}^{-3}$ is at 300 K and the mobility of electron and hole are 0.39 and $0.19 \text{ m}^2 \text{ v}^{-1} \text{ s}^{-1}$.

Solution:

Given:

Length of Ge rod $l = 1\text{ mm} = 1 \times 10^{-3}\text{ m}$

Breadth $b = 1\text{ mm} = 1 \times 10^{-3}\text{ m}$

Thickness $t = 1\text{ mm} = 1 \times 10^{-3}\text{ m}$

Intrinsic carrier concentration $n_i = 2.5 \times 10^{19}\text{ m}^{-3}$

Mobility of electron $\mu_e = 0.39\text{ m}^2\text{ V}^{-1}\text{ s}^{-1}$

Mobility of hole $\mu_h = 0.19\text{ m}^2\text{ V}^{-1}\text{ s}^{-1}$

a) Conductivity

$$\begin{aligned}\sigma &= n_i e (\mu_e + \mu_h) \\ &= 2.5 \times 10^{19} \times 1.6 \times 10^{-19} (0.39 + 0.19) \\ \sigma &= 2.32\text{ }\Omega^{-1}\text{ m}^{-1}\end{aligned}$$

b) Resistance

$$\begin{aligned}R &= \frac{l}{\sigma A} \\ &= \frac{1 \times 10^{-3}}{2.32 \times (1 \times 10^{-3} \times 1 \times 10^{-3})} \quad \therefore (A = b \times t) \\ R &= 431\text{ }\Omega\end{aligned}$$

9. Hall coefficient of a specimen of doped silicon found to be $3.66 \times 10^{-4}\text{ m}^3\text{ C}^{-1}$. The resistivity of the specimen is $8.93 \times 10^{-3}\text{ }\Omega\text{ m}$. Find the mobility and density of the charge carriers.

Solution:

Hall coefficient $R_H = 3.66 \times 10^{-4}\text{ m}^3\text{ C}^{-1}$

Resistivity $\rho = 8.93 \times 10^{-3}\text{ }\Omega\text{ m}$

i) Density of holes

$$\begin{aligned}n_h &= \frac{1}{R_H e} \\ &= \frac{1}{3.66 \times 10^{-4} \times 1.6 \times 10^{-19}} \\ n_h &= 1.7076 \times 10^{22}\text{ m}^{-3}\end{aligned}$$

ii) Mobility of holes $\mu_n = \frac{1}{\rho n e}$

$$\begin{aligned}\mu_n &= \frac{1}{8.93 \times 10^{-3} \times 1.7076 \times 10^{22} \times 1.6 \times 10^{-19}} \\ \mu_n &= 0.041\text{ m}^2\text{ V}^{-1}\text{ s}^{-1}\end{aligned}$$

10. The intrinsic carrier density of a semiconductor is $2.1 \times 10^{19}\text{ m}^{-3}$. The electron and hole mobilities are 0.4 and $0.2\text{ m}^2\text{ V}^{-1}\text{ s}^{-1}$ respectively. Calculate the conductivity.

Solution:

Solution:

Given data:

Intrinsic carrier concentration $n_i = 2.1 \times 10^{19} \text{ m}^{-3}$

Mobility of electron $\mu_e = 0.4 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$

Mobility of hole $\mu_h = 0.2 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$

Conductivity $\sigma = n_i e (\mu_e + \mu_h)$
 $= 2.1 \times 10^{19} \times 1.6 \times 10^{-19} \times (0.4 + 0.2)$

Conductivity $\sigma = 2.016 \text{ } \Omega^{-1} \text{ m}^{-1}$

11. The electron mobility and hole mobility in Si are $0.135 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ and $0.048 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$ respectively at room temperature. If the carrier concentration is $1.5 \times 10^{16} \text{ m}^{-3}$. Calculate the resistivity of Si at room temperature.

Solution:

Given data:

Carrier concentration $n_i = 1.5 \times 10^{16} \text{ m}^{-3}$

Mobility of electron $\mu_e = 0.135 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$

Mobility of hole $\mu_h = 0.048 \text{ m}^2 \text{ V}^{-1} \text{ s}^{-1}$

i) Electrical Conductivity σ

$$\begin{aligned}\sigma &= n_i e (\mu_e + \mu_h) \\ &= 1.5 \times 10^{16} \times 1.6 \times 10^{-19} \times (0.135 + 0.048) \\ \sigma &= 0.4392 \times 10^{-3} \text{ } \Omega^{-1} \text{ m}^{-1}\end{aligned}$$

ii) Resistivity of silicon

$$\begin{aligned}\rho &= \frac{1}{\sigma} \\ &= \frac{1}{0.4392 \times 10^{-3}} \\ \rho &= 2.2768 \text{ } \Omega \text{ m}\end{aligned}$$

ASSIGNMENT PROBLEMS

1. Find the resistance of an intrinsic germanium rod 1 cm long, 1mm wide and 1mm thick at 300 K. the intrinsic carrier density is $2.5 \times 10^{19} / \text{m}^{-3}$ at 300 K and the mobility of electron and hole are 0.39 and $0.19 \text{ m}^2 \text{ V}^{-1} \text{ S}^{-1}$. **(Ans: 4.31×10^3)**

2. In a Hall experiment a current of 25 A is passed through a long foil of silver which is 0.1mm thick and 3cm wide. If the magnetic field of flux density 0.14 Wb/m^2 is applied perpendicular to the foil, calculate the Hall voltage development and estimate the mobility of electrons in silver. The conductivity the Hall coefficient is $(-8.4 \times 10^{-11}) \text{ m}^3 / \text{coulomb}$. **(Ans : 29.4 V and $57.7 \times 10^{-4} \text{ m}^2 \text{ V}^{-1}$)**

3. The intrinsic carrier density at room temperature in Ge is $2.37 \times 10^{19} \text{ m}^{-3}$. If the electron and hole motilities are 0.38 and $0.18 \text{ m}^2 \text{ V}^{-1} \text{ S}^{-1}$ respectively, calculate the resistivity.
(Ans : 0471 m)

4. A silicon plate of thickness 1mm, breadth 10mm, and length 100mm is placed magnetic field of 0.5 wb/m^2 acting perpendicular to its thickness. If A 10^{-2} current flows along its length, calculate the Hall voltage developed if the Hall coefficient is $3.66 \times 10^{-4} \text{ m}^3 / \text{coulomb}$. **(Ans : $3.7 \times 10^6 \text{ C}^{-1} \text{ m}^3$)**

5. A N-type semiconductor has Hall coefficient = $4.16 \times 10^{-4} \text{ C}^{-1} \text{ m}^3$. The conductivity is $108 \text{ ohm}^{-1} \text{ m}^{-1}$. Calculate its charge carrier density and electron mobility at room temperature. **(Ans : $0.038 \text{ m}^2 \text{ V}^{-1} \text{ S}^{-1}$)**