## Chapter 3: Data Preprocessing

Data Preprocessing: An Overview



- Data Quality
- Major Tasks in Data Preprocessing
- Data Cleaning
- Data Integration
- Data Reduction
- Data Transformation and Data Discretization
- Summary

## Data Quality: Why Preprocess the Data?

- Measures for data quality: A multidimensional view
  - Accuracy: correct or wrong, accurate or not
  - Completeness: not recorded, unavailable, not imp,not relevant
  - Consistency: some modified but some not, dangling, ...
  - Timeliness: timely update?
  - Believability: how trustable the data are correct?
  - Interpretability: how easily the data can be understood?

## Major Tasks in Data Preprocessing

#### Data cleaning

Fill in missing values, smooth noisy data, identify or remove outliers,
 and resolve inconsistencies

#### Data integration

Integration of multiple databases, data cubes, or files

#### Data reduction: data in smaller form

- Dimensionality reduction : compressed data
- Numerosity reduction: replace by smaller parametric model.
- Data compression:

#### Data transformation and data discretization

- Normalization
- Concept hierarchy generation: raw data

## Chapter 3: Data Preprocessing

- Data Preprocessing: An Overview
  - Data Quality
  - Major Tasks in Data Preprocessing
- Data Cleaning



- Data Integration
- Data Reduction
- Data Transformation and Data Discretization
- Summary

# **Data Cleaning**

- Data in the Real World Is Dirty: Lots of potentially incorrect data,
- smooth out noise while identifying outliers, and correct inconsistencies in the data
- e.g., instrument faulty, human or computer error, transmission error
  - <u>incomplete</u>: lacking attribute values, lacking certain attributes of interest, or containing only aggregate data
    - e.g., Occupation="" (missing data)
  - noisy: containing noise, errors, or outliers
    - e.g., Salary="-10" (an error)
  - inconsistent: containing discrepancies in codes or names, e.g.,
    - Age="42", Birthday="03/07/2010"
    - Was rating "1, 2, 3", now rating "A, B, C"
    - discrepancy between duplicate records

# Incomplete (Missing) Data

- Data is not always available
  - E.g., many tuples have no recorded value for several attributes, such as customer income in sales data
- Missing data may be due to
  - equipment malfunction
  - inconsistent with other recorded data and thus deleted
  - data not entered due to misunderstanding
  - certain data may not be considered important at the time of entry
  - not register history or changes of the data
- Missing data may need to be inferred

## How to Handle Missing Data?

- Ignore the tuple: usually done when class label is missing (when doing classification)—not effective when the % of missing values per attribute varies considerably
- Fill in the missing value manually: tedious + infeasible?
- Fill in it automatically with
  - a global constant : e.g., "unknown", a new class?!
  - the attribute mean
  - the attribute mean for all samples belonging to the same class: smarter
  - the most probable value: inference-based such as Bayesian formula or decision tree

## **Noisy Data**

- Noise: random error or variance in a measured variable
- Incorrect attribute values may be due to
  - faulty data collection instruments
  - data entry problems
  - data transmission problems
  - technology limitation
  - inconsistency in naming convention
- Other data problems which require data cleaning
  - duplicate records
  - incomplete data
  - inconsistent data

# How to Handle Noisy Data?

### Binning

- first sort data and partition into (equal-frequency) bins
- then one can smooth by bin means, smooth by bin median, smooth by bin boundaries, etc.

### Regression

- smooth by fitting the data into regression functions
- Outlier Analysis
  - detect and remove outliers.

## Data Cleaning as a Process

- Data discrepancy detection
  - Use metadata (e.g., domain, range, dependency, distribution)
  - Check field overloading
  - Check uniqueness rule, consecutive rule and null rule
  - Use commercial tools
    - Data scrubbing: use simple domain knowledge (e.g., postal code, spell-check) to detect errors and make corrections
    - Data auditing: by analyzing data to discover rules and relationship to detect violators (e.g., correlation and clustering to find outliers)
- Data migration and integration
  - Data migration tools: allow transformations to be specified
  - ETL (Extraction/Transformation/Loading) tools: allow users to specify transformations through a graphical user interface
- Integration of the two processes
  - Iterative and interactive (e.g., Potter's Wheels)

## Chapter 3: Data Preprocessing

- Data Preprocessing: An Overview
  - Data Quality
  - Major Tasks in Data Preprocessing
- Data Cleaning
- Data Integration



- Data Reduction
- Data Transformation and Data Discretization
- Summary

## **Data Integration**

#### Data integration:

- Combines data from multiple sources into a coherent store
- Schema integration: e.g., A.cust-id ≡ B.cust-#
  - Integrate metadata from different sources
- Entity identification problem:
  - Identify real world entities from multiple data sources, e.g., Bill Clinton =
     William Clinton
- Detecting and resolving data value conflicts
  - For the same real world entity, attribute values from different sources are different
  - Possible reasons: different representations, different scales, e.g., metric
     vs. British units

## Handling Redundancy in Data Integration

- Redundant data occur often when integration of multiple databases
  - Object identification: The same attribute or object may have different names in different databases
  - Derivable data: One attribute may be a "derived" attribute in another table, e.g., annual revenue
- Redundant attributes may be able to be detected by correlation analysis and covariance analysis
- Careful integration of the data from multiple sources may help reduce/avoid redundancies and inconsistencies and improve mining speed and quality

## **Correlation Analysis (Nominal Data)**

X<sup>2</sup> (chi-square) test

$$\chi^2 = \sum \frac{(Observed - Expected)^2}{Expected}$$

- The larger the X<sup>2</sup> value, the more likely the variables are related
- X<sup>2</sup> checks the hypothesis that A and B are independent. If this hypothesis can be rejected, we can say that A and B are statically correlated and one of the them (either A or B) can be discarded.
- If the correlation constant is 0 then the attributes are independent.
- If it is negative then one attribute discourages the other i.e if the value of one attribute increases then value of other decreases.

## Covariance (Numeric Data)

Covariance is similar to correlation

$$Cov(A,B) = E((A-\bar{A})(B-\bar{B})) = \frac{\sum_{i=1}^{n}(a_i-\bar{A})(b_i-\bar{B})}{n}$$
 Correlation coefficient: 
$$r_{A,B} = \frac{Cov(A,B)}{\sigma_A\sigma_B}$$

where n is the number of tuples,  $\overline{A}$  and  $\overline{B}$  are the respective mean or expected values of A and B,  $\sigma_A$  and  $\sigma_B$  are the respective standard deviation of A and B.

- **Positive covariance**: If  $Cov_{A,B} > 0$ , then A and B both tend to be larger than their expected values.
- Negative covariance: If  $Cov_{A,B} < 0$  then if A is larger than its expected value, B is likely to be smaller than its expected value.
- Independence: Cov<sub>A,B</sub> = 0 but the converse is not true:
  - Some pairs of random variables may have a covariance of 0 but are not independent.
     Only under some additional assumptions (e.g., the data follow multivariate normal distributions) does a covariance of 0 imply independence

# Co-Variance: An Example

$$Cov(A, B) = E((A - \bar{A})(B - \bar{B})) = \frac{\sum_{i=1}^{n} (a_i - \bar{A})(b_i - \bar{B})}{n}$$

It can be simplified in computation as

$$Cov(A, B) = E(A \cdot B) - \bar{A}\bar{B}$$

- Suppose two stocks A and B have the following values in one week: (2, 5), (3, 8), (5, 10), (4, 11), (6, 14).
- Question: If the stocks are affected by the same industry trends, will their prices rise or fall together?

$$- E(A) = (2 + 3 + 5 + 4 + 6)/5 = 20/5 = 4$$

$$- E(B) = (5 + 8 + 10 + 11 + 14) / 5 = 48 / 5 = 9.6$$

$$- \text{Cov}(A,B) = (2 \times 5 + 3 \times 8 + 5 \times 10 + 4 \times 11 + 6 \times 14)/5 - 4 \times 9.6 = 4$$

Thus, A and B rise together since Cov(A, B) > 0.

## **Chapter 3: Data Preprocessing**

- Data Preprocessing: An Overview
  - Data Quality
  - Major Tasks in Data Preprocessing
- Data Cleaning
- Data Integration
- Data Reduction



- Data Transformation and Data Discretization
- Summary

### **Data Reduction Strategies**

- Data reduction: Obtain a reduced representation of the data set that is much smaller in volume but yet produces the same (or almost the same) analytical results
- Why data reduction? A database/data warehouse may store terabytes of data. Complex data analysis may take a very long time to run on the complete data set.
- Data reduction strategies
  - Dimensionality reduction, e.g., remove unimportant attributes
    - Wavelet transforms
    - Principal Components Analysis (PCA)
    - Feature subset selection, feature creation
  - Numerosity reduction (some simply call it: Data Reduction)
    - Regression and Log-Linear Models
    - Histograms, clustering, sampling
    - Data cube aggregation
  - Data compression

# Data Reduction 1: Dimensionality Reduction

#### Curse of dimensionality

- When dimensionality increases, data becomes increasingly sparse
- Density and distance between points, which is critical to clustering, outlier analysis, becomes less meaningful
- The possible combinations of subspaces will grow exponentially

#### Dimensionality reduction

- Avoid the curse of dimensionality
- Help eliminate irrelevant features and reduce noise
- Reduce time and space required in data mining
- Allow easier visualization

#### Dimensionality reduction techniques

- Wavelet transforms
- Principal Component Analysis
- Supervised and nonlinear techniques (e.g., feature selection)

## **Attribute Subset Selection**

- Another way to reduce dimensionality of data
- Redundant attributes
  - Duplicate much or all of the information contained in one or more other attributes
  - E.g., purchase price of a product and the amount of sales tax paid
- Irrelevant attributes
  - Contain no information that is useful for the data mining task at hand
  - E.g., students' ID is often irrelevant to the task of predicting students' GPA

### Heuristic Search in Attribute Selection

- There are  $2^d$  possible attribute combinations of d attributes
- Typical heuristic attribute selection methods:
  - Best single attribute under the attribute independence assumption: choose by significance tests
  - Best step-wise feature selection:
    - The best single-attribute is picked first
    - Then next best attribute condition to the first, ...
  - Step-wise attribute elimination:
    - Repeatedly eliminate the worst attribute
  - Best combined attribute selection and elimination
  - Optimal branch and bound:
    - Use attribute elimination and backtracking

# Attribute Creation (Feature Generation)

- Create new attributes (features) that can capture the important information in a data set more effectively than the original ones
- Three general methodologies
  - Attribute extraction
    - Domain-specific
  - Mapping data to new space
  - E.g., Fourier transformation, wavelet transformation, manifold approaches (not covered)
  - Attribute construction
    - Combining features
    - Data discretization

# Data Reduction 2: Numerosity Reduction

- Reduce data volume by choosing alternative, smaller forms of data representation
- Parametric methods (e.g., regression)
  - Assume the data fits some model, estimate model parameters, store only the parameters, and discard the data (except possible outliers)
  - Ex.: Log-linear models—obtain value at a point in m-D space as the product on appropriate marginal subspaces
- Non-parametric methods
  - Do not assume models
  - Major families: histograms, clustering, sampling, ...

# Parametric Data Reduction: Regression and Log-Linear Models

### Linear regression

- Data modeled to fit a straight line
- Often uses the least-square method to fit the line

### Multiple regression

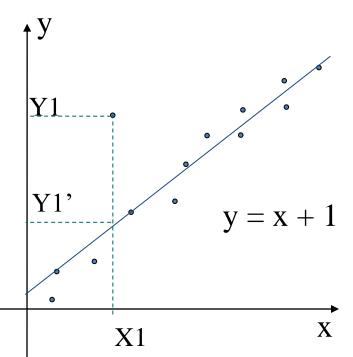
 Allows a response variable Y to be modeled as a linear function of multidimensional feature vector

#### Log-linear model

Approximates discrete multidimensional probability distributions

# Regression Analysis

- Regression analysis: A collective name for techniques for the modeling and analysis of numerical data consisting of values of a dependent variable (also called response variable or measurement) and of one or more independent variables (aka. explanatory variables or predictors)
- The parameters are estimated so as to give a "best fit" of the data
- Most commonly the best fit is evaluated by using the *least squares method*, but other criteria have also been used



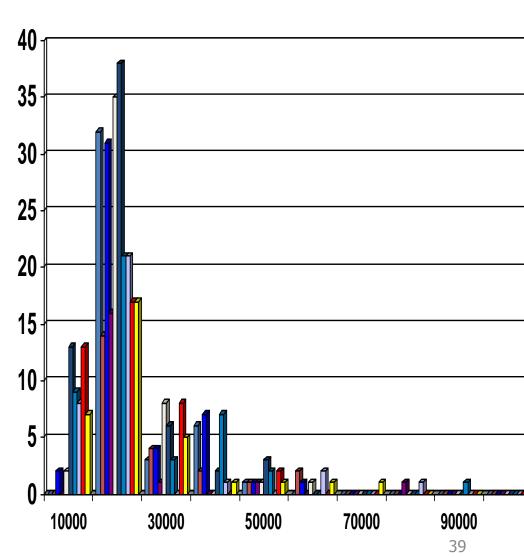
 Used for prediction (including forecasting of time-series data) inference, hypothesis testing, and modeling of causal relationships

# Regress Analysis and Log-Linear Models

- <u>Linear regression</u>: Y = w X + b
  - Two regression coefficients, w and b, specify the line and are to be estimated by using the data at hand
  - Using the least squares criterion to the known values of  $Y_1$ ,  $Y_2$ , ...,  $X_1$ ,  $X_2$ , ....
- Multiple regression:  $Y = b_0 + b_1 X_1 + b_2 X_2$ 
  - Many nonlinear functions can be transformed into the above
- Log-linear models:
  - Approximate discrete multidimensional probability distributions
  - Estimate the probability of each point (tuple) in a multi-dimensional space for a set of discretized attributes, based on a smaller subset of dimensional combinations
  - Useful for dimensionality reduction and data smoothing

# Histogram Analysis

- Divide data into buckets and store average (sum) for each bucket
- Partitioning rules:
  - Equal-width: equal bucket range
  - Equal-frequency (or equaldepth)



# Clustering

- Partition data set into clusters based on similarity, and store cluster representation (e.g., centroid and diameter) only
- Can be very effective if data is clustered but not if data is "smeared"
- Can have hierarchical clustering and be stored in multidimensional index tree structures
- There are many choices of clustering definitions and clustering algorithms
- Cluster analysis will be studied in depth in Chapter 10

# Sampling

- Sampling: obtaining a small sample s to represent the whole data set N
- Allow a mining algorithm to run in complexity that is potentially sub-linear to the size of the data
- Key principle: Choose a representative subset of the data
  - Simple random sampling may have very poor performance in the presence of skew
  - Develop adaptive sampling methods, e.g., stratified sampling:
- Note: Sampling may not reduce database I/Os (page at a time)

# Types of Sampling

### Simple random sampling

There is an equal probability of selecting any particular item

### Sampling without replacement

Once an object is selected, it is removed from the population

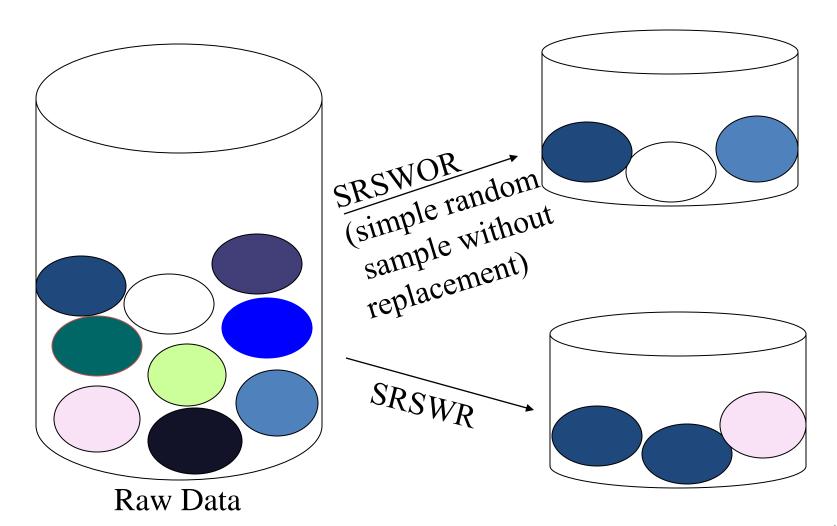
### Sampling with replacement

A selected object is not removed from the population

### Stratified sampling:

- Partition the data set, and draw samples from each partition (proportionally, i.e., approximately the same percentage of the data)
- Used in conjunction with skewed data

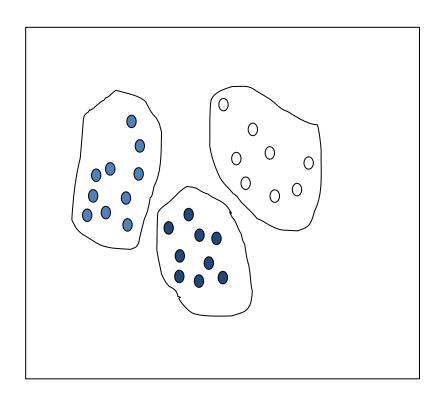
## Sampling: With or without Replacement

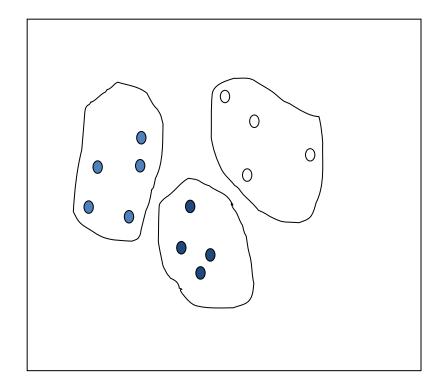


# Sampling: Cluster or Stratified Sampling

Raw Data

Cluster/Stratified Sample





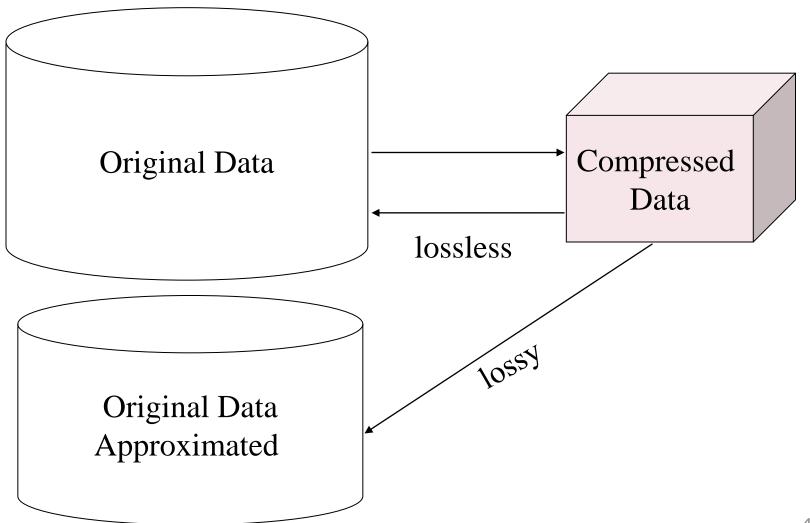
## Data Cube Aggregation

- The lowest level of a data cube (base cuboid)
  - The aggregated data for an individual entity of interest
  - E.g., a customer in a phone calling data warehouse
- Multiple levels of aggregation in data cubes
  - Further reduce the size of data to deal with
- Reference appropriate levels
  - Use the smallest representation which is enough to solve the task
- Queries regarding aggregated information should be answered using data cube, when possible

# Data Reduction 3: Data Compression

- String compression
  - There are extensive theories and well-tuned algorithms
  - Typically lossless, but only limited manipulation is possible without expansion
- Audio/video compression
  - Typically lossy compression, with progressive refinement
  - Sometimes small fragments of signal can be reconstructed without reconstructing the whole
- Time sequence is not audio
  - Typically short and vary slowly with time
- Dimensionality and numerosity reduction may also be considered as forms of data compression

# **Data Compression**



## **Chapter 3: Data Preprocessing**

- Data Preprocessing: An Overview
  - Data Quality
  - Major Tasks in Data Preprocessing
- Data Cleaning
- Data Integration
- Data Reduction
- Data Transformation and Data Discretization



Summary

# **Data Transformation**

- A function that maps the entire set of values of a given attribute to a new set of replacement values s.t. each old value can be identified with one of the new values
- Methods
  - Smoothing: Remove noise from data
  - Attribute/feature construction
    - New attributes constructed from the given ones
  - Aggregation: Summarization, data cube construction
  - Normalization: Scaled to fall within a smaller, specified range
    - min-max normalization
    - z-score normalization
    - normalization by decimal scaling
  - Discretization: Concept hierarchy climbing

# Normalization

Min-max normalization: to [new\_min<sub>A</sub>, new\_max<sub>A</sub>]

$$v' = \frac{v - min_A}{max_A - min_A} (new \_max_A - new \_min_A) + new \_min_A$$

- Ex. Let income range \$12,000 to \$98,000 normalized to [0.0, 1.0]. Then \$73,000 is mapped to  $\frac{73,600-12,000}{98,000-12,000}(1.0-0)+0=0.716$
- **Z-score normalization** (μ: mean, σ: standard deviation):

$$v' = \frac{v - \mu_A}{\sigma_A}$$

- Ex. Let μ = 54,000,  $\sigma$  = 16,000. Then

$$\frac{73,600 - 54,000}{16,000} = 1.225$$

Normalization by decimal scaling

$$v' = \frac{v}{10^{j}}$$
 Where j is the smallest integer such that Max(|v'|) < 1

# Discretization

- Three types of attributes
  - Nominal—values from an unordered set, e.g., color, profession
  - Ordinal—values from an ordered set, e.g., military or academic rank
  - Numeric—real numbers, e.g., integer or real numbers
- Discretization: Divide the range of a continuous attribute into intervals
  - Interval labels can then be used to replace actual data values
  - Reduce data size by discretization
  - Supervised vs. unsupervised
  - Split (top-down) vs. merge (bottom-up)
  - Discretization can be performed recursively on an attribute
  - Prepare for further analysis, e.g., classification

# Data Discretization Methods

- Typical methods: All the methods can be applied recursively
  - Binning
    - Top-down split, unsupervised
  - Histogram analysis
    - Top-down split, unsupervised
  - Clustering analysis (unsupervised, top-down split or bottomup merge)
  - Decision-tree analysis (supervised, top-down split)
  - Correlation (e.g.,  $\chi^2$ ) analysis (unsupervised, bottom-up merge)

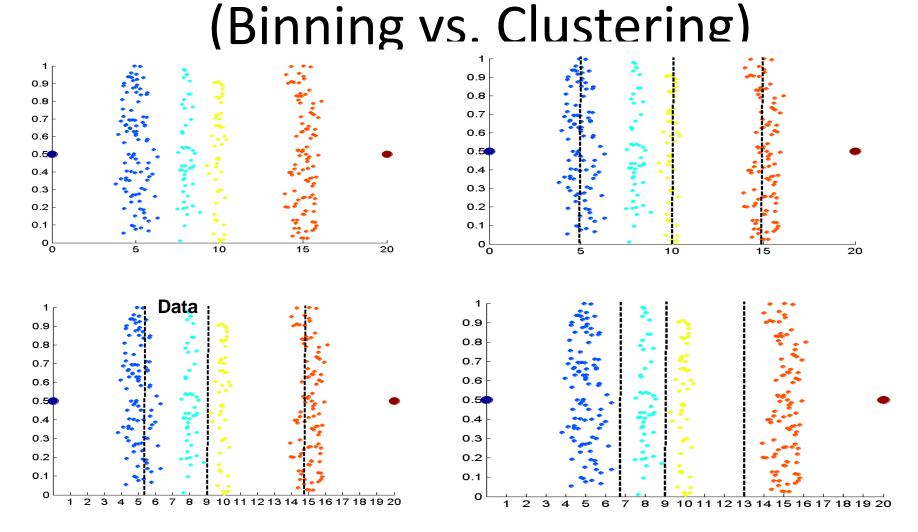
### Simple Discretization: Binning

- Equal-width (distance) partitioning
  - Divides the range into N intervals of equal size: uniform grid
  - if A and B are the lowest and highest values of the attribute, the width of intervals will be: W = (B A)/N.
  - The most straightforward, but outliers may dominate presentation
  - Skewed data is not handled well
- Equal-depth (frequency) partitioning
  - Divides the range into N intervals, each containing approximately same number of samples
  - Good data scaling
  - Managing categorical attributes can be tricky

# Binning Methods for Data Smoothing

- ☐ Sorted data for price (in dollars): 4, 8, 9, 15, 21, 21, 24, 25, 26, 28, 29, 34
- \* Partition into equal-frequency (equi-depth) bins:
  - Bin 1: 4, 8, 9, 15
  - Bin 2: 21, 21, 24, 25
  - Bin 3: 26, 28, 29, 34
- \* Smoothing by **bin means**:
  - Bin 1: 9, 9, 9, 9
  - Bin 2: 23, 23, 23, 23
  - Bin 3: 29, 29, 29, 29
- \* Smoothing by **bin boundaries**:
  - Bin 1: 4, 4, 4, 15
  - Bin 2: 21, 21, 25, 25
  - Bin 3: 26, 26, 26, 34

# Labels



**Equal frequency (binning)** 

K-means clustering leads to better results

# Discretization by Classification & Correlation Analysis

- Classification (e.g., decision tree analysis)
  - Supervised: Given class labels, e.g., cancerous vs. benign
  - Using entropy to determine split point (discretization point)
  - Top-down, recursive split
  - Details to be covered in Chapter 7
- Correlation analysis (e.g., Chi-merge: χ²-based discretization)
  - Supervised: use class information
  - Bottom-up merge: find the best neighboring intervals (those having similar distributions of classes, i.e., low  $\chi^2$  values) to merge
  - Merge performed recursively, until a predefined stopping condition

# Concept Hierarchy Generation

- **Concept hierarchy** organizes concepts (i.e., attribute values) hierarchically and is usually associated with each dimension in a data warehouse
- Concept hierarchies facilitate <u>drilling and rolling</u> in data warehouses to view data in multiple granularity
- Concept hierarchy formation: Recursively reduce the data by collecting and replacing low level concepts (such as numeric values for age) by higher level concepts (such as youth, adult, or senior)
- Concept hierarchies can be explicitly specified by domain experts and/or data warehouse designers
- Concept hierarchy can be automatically formed for both numeric and nominal data. For numeric data, use discretization methods shown.

# Concept Hierarchy Generation for Nominal Data

- Specification of a partial/total ordering of attributes explicitly at the schema level by users or experts
  - street < city < state < country</p>
- Specification of a hierarchy for a set of values by explicit data grouping
  - {Urbana, Champaign, Chicago} < Illinois</p>
- Specification of only a partial set of attributes
  - E.g., only street < city, not others</li>
- Automatic generation of hierarchies (or attribute levels) by the analysis of the number of distinct values
  - E.g., for a set of attributes: {street, city, state, country}

### Automatic Concept Hierarchy Generation

- Some hierarchies can be automatically generated based on the analysis of the number of distinct values per attribute in the data set
  - The attribute with the most distinct values is placed at the lowest level of the hierarchy
  - Exceptions, e.g., weekday, month, quarter, year



### **Chapter 3: Data Preprocessing**

- Data Preprocessing: An Overview
  - Data Quality
  - Major Tasks in Data Preprocessing
- Data Cleaning
- Data Integration
- Data Reduction
- Data Transformation and Data Discretization
- Summary



# Summary

- Data quality: accuracy, completeness, consistency, timeliness, believability, interpretability
- **Data cleaning**: e.g. missing/noisy values, outliers
- **Data integration** from multiple sources:
  - Entity identification problem
  - Remove redundancies
  - Detect inconsistencies

#### Data reduction

- Dimensionality reduction
- Numerosity reduction
- Data compression

#### Data transformation and data discretization

- Normalization
- Concept hierarchy generation