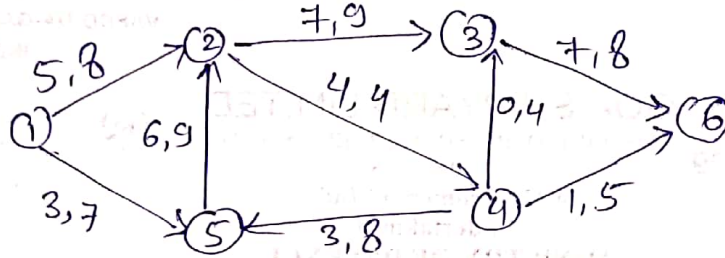


## Assignment.

- ① P.T. If  $f: (G_1, *) \rightarrow (G_2, \circ)$ , is homomorphism from  $G_1$  to  $G_2$ , then  $f(e_1) = e_2$ ,  $f(a^{-1}) = (f(a))^\dagger$ ,  $\forall a \in G_1$ . Also,  $\ker f$  is normal subgroup of  $G_1$ .
- ② Define Digraphs. What is the minimum no. of edges in a strongly connected digraph having  $n$  vertices? What shape does such digraph have? Why?
- ③ Draw a graph having the given properties or explain why no such graph exists.
- (i) Graph with four vertices of degree 1, 1, 2 & 3.
  - (ii) " " " " " " 1, 1, 3 & 3.
  - (iii) Simple graph with four vertices of degree 1, 1, 3 & 3.
  - (iv) Graph with five vertices of degree 0, 1, 2, 2, 3.
- ④ P.T. edge connectivity of graph  $G$  cannot exceed the smallest degree in  $G$ , & vertex connectivity of  $G$  can never exceed the edge connectivity of  $G$ .
- ⑤ Define planar graph, region. Are  $K_5$  &  $K_{3,3}$  planar graphs? Why?
- ⑥ Define Euler graph & S.T. a graph  $G$  is Euler graph iff every vertex in  $G$  has even degree. What happens if there are exactly two odd vertices?
- ⑦ What is  $k$ -chromatic graph? Explain with example. Also find chromatic number of complete graph  $K_n$ .

8. What is feasible flow? Find out in the capacitated flow given below & hence verify  $f(G) = f(S, T) - f(T, S)$ , for  $(S, T)$  is cut.



9. Explain in brief: Hoare's logic for programme verification.
10. Explain in brief: Linear recurrence relation, inclusion & exclusion for counting.
11. Explain in brief: first counting principle, second counting principle, circular permutations.