

BTech II (CSE) Semester IV - Mid Semester Examination March 2021

Subject: MA 212 Linear Algebra and Statistical Analysis, Time: 9:00 - 9:45 am

* Required

Attempt All Questions

Which of the following are used for modeling times series and sequences? *

- ☐ Decision graphs
- ☐ Parameter tuning
- ☐ Value of information
- ☒ Dynamic Bayesian networks

The nodes and links of the Bayesian network form *

- ☒ structural specification
- ☐ none of these
- ☐ multi-variable nodes
- ☐ conditional linear Gaussian distributions



A dice is tossed. If X is a random variable denoting the outcome on the dice, the expected value of X is _____ *

- ☐ 7/6
- ☐ 6/6
- ☒ 7/2
- ☐ 1/6

*

The density function of X is $f(x) = \begin{cases} 2x, & \text{if } 0 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases}$, then $E[X^2] =$ _____

- ☐ 1/18
- ☐ 2
- ☒ 1/2
- ☐ 2/3

*

In \mathbb{R}^3 , $\alpha = (4, 3, 5)$, $\beta = (0, 1, 3)$, $\gamma = (2, 1, 1)$, $\delta = (4, 2, 2)$.
Which of the following is true?

α is not a linear combination of β and γ

β is a linear combination of γ and δ

☐ Option 1

☐ Option 2

α is a linear combination of β and γ

☐ None

☒ Option 3

*

The integer solution of the system of equation

$$x + 2y + z = 1$$

$$3x + y + 2z = 3$$

$$x + 7y + 2z = 1 \quad \text{is}$$

$$(1-3k, -k, 5k)$$

☒ Option 1

$$(-3k, -3k, 5k)$$

☐ Option 2

$$(1+3k, -k, 5k)$$

☐ None

☐ Option 3



If X and Y are independent discrete random variables with variances 9 and 3 respectively, then Variance of $[4X-2Y+6]=$ ____ *

- ☐ 150
- ☐ 160
- ☒ 156
- ☐ 144
- ☐ None

*

An eigen vector corresponding to eigen value i of the matrix $A = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ is

$$\begin{pmatrix} i \\ -i \end{pmatrix}$$

☐ Option 1

$$\begin{pmatrix} 1 \\ i \end{pmatrix}$$

☐ Option 2

$$\begin{pmatrix} i \\ 1 \end{pmatrix}$$

☐ None

☒ Option 3

What is a clique? *

- ☐ the set of all nodes of a graph
- ☒ a set of mutually-neighboring nodes on a graph
- ☐ a particular case of Markov chain
- ☐ the set of all neighboring nodes

*

. The rank of $\begin{pmatrix} 1 & 0 & 3 \\ 4 & -1 & 5 \\ 2 & 0 & 6 \end{pmatrix}$ is

- ☐ 4
- ☐ 3
- ☒ 2
- ☐ 1

For a continuous probability density function f which of the following holds true?

*

- ☒ $f(0.1) = c, 1 \geq c \geq 0$
- ☒ Total area under the curve $f(x) = 1$
- ☒ $f(x)$ is bounded function
- ☐ $f(0.1) = 0$
- ☐ Total area under the curve $f(x) \geq 1$

The Bayesian network graph does not contain any cyclic graph. Hence, it is known as a *

- ☒ DAG
- ☐ DCG
- ☐ SAG
- ☐ CAG

Bayesian networks are a factorized representation of the full joint. *

- ☐ False
- ☐ can be true or false
- ☐ none of these
- ☒ True



*

The condition for which the system of equations

$$x + y + z = 1$$

$$x + 2y - z = b$$

$$5x + 7y + az = b^2$$

admits a unique solution is

$$a=1$$

☒ Option 1

$$a \neq -1$$

☐ Option 2

$$a \neq 1$$

☐ None

☐ Option 3



*

Let the subset $S = \{(x, y, z) \in \mathbb{R}^3: x^2 + y^2 = z^2\}$ and subset $T = \{(x, y, z) \in \mathbb{R}^3: x = z = 0\}$. Which of the following is true?

- ☐ S is a subspace but T is not a subspace
- ☒ S is not a subspace but T is a subspace
- ☐ Both S and T are subspaces
- ☐ Both S and T are not subspaces

In a Bayesian network variable is? *

- ☒ both continuous and discrete
- ☐ continuous
- ☐ none of these
- ☐ discrete



*

In the ring of 2×2 matrices over the field of real numbers, the zero element of the ring is

$$\begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

☐ Option 1

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

☐ Option 2

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

☐ Option 3

$$\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

☒ Option 4



*

A linear mapping $T: \mathbb{R}^3 \rightarrow \mathbb{R}^4$ is defined by

$$T(x_1, x_2, x_3) = (x_2 + x_3, x_3 + x_1, x_1 + x_2, x_1 + x_2 + x_3), \quad (x_1, x_2, x_3) \in \mathbb{R}^3.$$

Find Ker T?

$$\text{Ker } T = \{1\}$$

☐ Option 1

$$\text{Ker } T = \{0\}$$

☒ Option 2

$$\text{Ker } T = \{2\}$$

☐ Option 3

☐ None

The Markov property for random field states that the conditional distribution of a pixel given all other pixels: *

- ☒ depends only on neighboring pixels
- ☐ is a multivariate Gaussian distribution
- ☐ depends only on previous pixels
- ☐ none of these



Where does the bayes rule can be used? *

- ☒ answering the query more accurately
- ☐ solving queries
- ☐ reducing complexity
- ☐ all of the above

*

The exponential distribution $f(x)$ is defined by $f(x) = ae^{-2x}, 0 < x < \infty$, then $a =$ _____

- ☐ 1
- ☒ 2
- ☐ 1/2
- ☐ 0

What does the Bayesian network provides? *

- ☐ partical description of the domain
- ☒ complete description of the problem
- ☐ none of these
- ☐ complete description of the domain



*

The singleton $\{0\}$ is a ring with respect to

- ☐ Addition
- ☐ Multiplication
- ☒ Both Option 1 and Option 2
- ☐ None

If $E[X]$ denotes the expected value of random variable X , then following statements are always true. *

- ☒ $E[X]$ is theoretical average value.
- ☒ $E[X]$ is a non-negative number.
- ☐ $E[X]$ is expressed in units of original data.
- ☐ $E[X]$ is a location parameter.



*

If $A = \begin{pmatrix} i & 0 \\ 0 & i/2 \end{pmatrix}$, ($i = \sqrt{-1}$), then $A^{-1} = ?$

$$\begin{pmatrix} i & 0 \\ 0 & i/2 \end{pmatrix}$$

☐ Option 1

$$\begin{pmatrix} -i & 0 \\ 0 & -2i \end{pmatrix}$$

☒ Option 2

$$\begin{pmatrix} i & 0 \\ 0 & 2i \end{pmatrix}$$

☐ Option 3

$$\begin{pmatrix} 0 & i \\ 2i & 0 \end{pmatrix}$$

☐ Option 4

What is a Markov Random Field ? *

- ☒ a random process on undirected graphs
- ☐ a Bayesian model
- ☐ a particular case of Markov chain
- ☐ all options correct

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