

1.) Minimizing the Risk \sim Maximizing the posterior probability
 (Classification problem)

1.) Modelled using Gaussian

① An accepted low risk customer \rightarrow increases profit

A rejected high risk customer \rightarrow decreases loss

② Loss for high risk customer erroneously accepted is different from the gain for an erroneously rejected low risk customer.

③ $x_1 \rightarrow \text{income}$ & $x_2 \rightarrow \text{saving}$
 Let decide outcome

$c = 1$ high risk & $c = 0$ low risk

④ For any new data $x_1 = x_1$ and $x_2 = x_2$ knowing $P(c|x_1, x_2)$ we can choose

a) $c = 1$, if $P(c=1|x_1, x_2) > 0.5$ and $c = 0$ otherwise

b) $c = 1$, if $P(c=1|x_1, x_2) > P(c=0|x_1, x_2)$ and $c = 0$ otherwise

⑤ Probability of error = $1 - \max \left(P(c=1|x_1, x_2), P(c=0|x_1, x_2) \right)$

Therefore, we

are minimizing the risk by maximizing the posterior probability.

maximizing the posterior probability

(UI9CS012)

(Q2)

(RAHAGYA RANA)

Sport Video summarization

(Feature Based)

Object

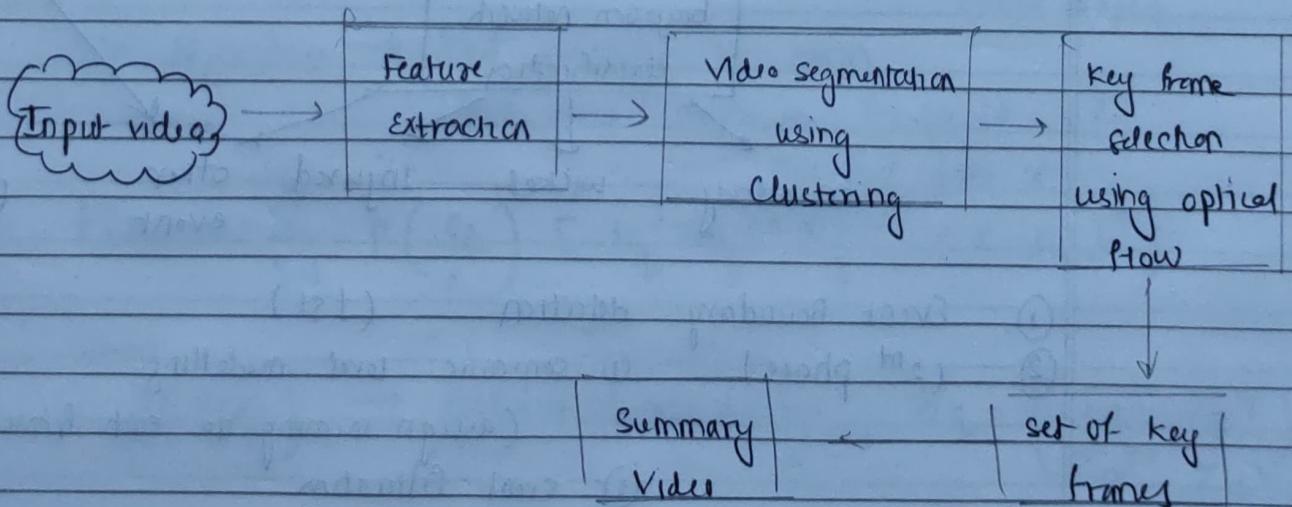
- ① Target objects can be ball, player, umpire, field, audience,
- ② Object segmentation is computationally expensive
 - (Need to separate object from environment)

* Aim: Efficient video summary generation using dominant feature for cricket.

A) Color & Change in Motion

- (i) partition video into shots using dominant color feature
- (ii) select key frames from each shot using change in motion

& Dominant color = Green field in cricket

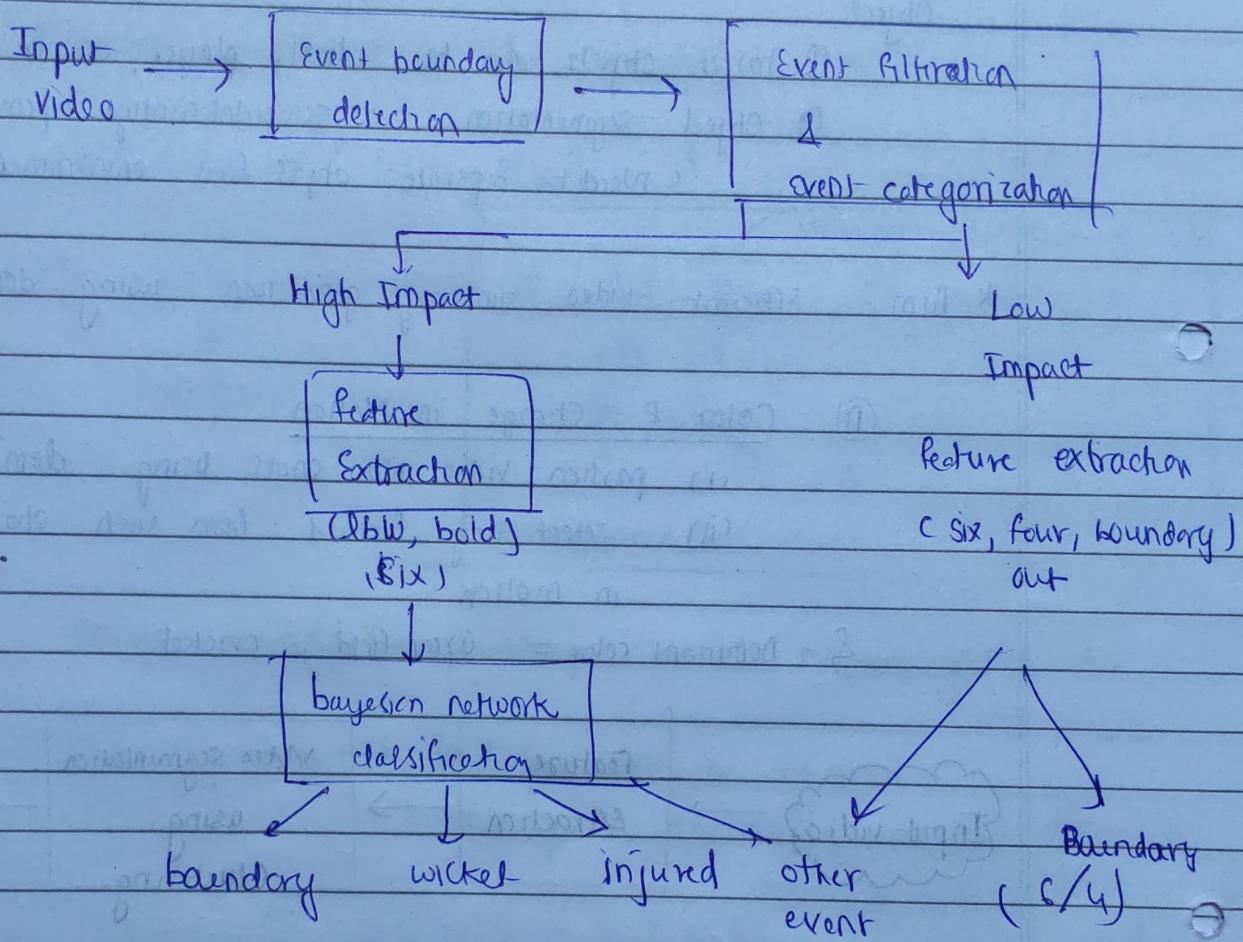


B) Event identification & state based event modelling
Solt:

→ Semantic Based analysis for cricket match video summarization

Hybrid Model
 Supervised Training + Unsupervised
 (Train it using old season of cricket match)

(Event =
 set of
 frames)



- ① Event Boundary detection (1st)
- ② (2nd phase) ① semantic level modelling
 (assign meaning to each frame)
- ② event filtration
- ③ event categorization
- ④ Event Classification → Hidden Markov model
- ⑤ Out / ~~Injured~~ Injured

(Q3)

(GMM based modelling)

$$P(x|\theta) = \sum_{k=1}^K \pi_k N(x|\mu_k, \Sigma_k)$$

(Gaussian mixture Model) - Density Based model

Ⓐ Different parameters to be estimated =

distribution $N(z|\mu_k, \Sigma_k)$

\rightarrow parameters \rightarrow
of
GMM

θ : ① π_k , (k means μ_k)
 ② μ_k
 ③ Σ_k : $k = 1, \dots, K$
 (covariance)

Ⓑ Design strategy for deciding no. of mixture models for facial images

EM Algorithm \rightarrow find parameter in GMM
that gives maximum likelihood of

$$F(x) = \sum_{q=1}^n P\left(\frac{c_q}{x}\right) \left[\mu_q^T \sum_q^{yx} \sum_q^{xx} (x - \mu_q)^T \right]$$

when

$$P(c_q|x) \rightarrow \text{conditional probability} \quad \Sigma_q = \begin{bmatrix} \Sigma_q^{xx} & \Sigma_q^{xy} \\ \Sigma_q^{yx} & \Sigma_q^{yy} \end{bmatrix}$$

 $m \rightarrow$ GMM mixture in facial conversion

$$\mu_q = \begin{bmatrix} \mu_q^x \\ \mu_q^y \end{bmatrix}$$

★ GMM \rightarrow Joint density model is baseline for mapping

source & target faces

(Cepstrum based GMM) ✓

(Q4)

Incomplete data problem

① \Rightarrow Here ML estimation is made difficult by the absence of some part of data in more familiar and simple data structure

② Solⁿ = Expectation Maximization

1 iteration of EM algorithm

① Expectation Step (E-step)

② Maximization step (M-step)

③ Closely related to ad hoc approach to estimation with missing data

\rightarrow where the parameters are estimated by filling in initial values for the missing data.

\rightarrow the latter are then updated by their predicted values using these initial parameters

\rightarrow the parameters are then re-estimated and so on, proceeding iteratively until convergence.

④ Main idea of EM

Algorithm

Associate with given incomplete-data, a complete data problem for which ML estimation is computationally more tractable

(reformulating the problem in terms of easily solvable data problem)

Algorithm \rightarrow

(Q4)(P2)

(EM Algorithm)

- ① E-step = manufacturing data for the complete data problem using observed data set of incomplete data problem & current value of parameters, so that
- ② the simpler M-step computation can be applied to "completed" data set
- ③ \rightarrow Log likelihood of the complete-data problem that is "manufactured" in E-step
- ④ as it is based on unobservable data, it is replaced by conditional expectation given the observed data, E-step is affected using the current fit for the unknown parameters.

$$\left[\frac{\partial \log L(\psi)}{\partial \psi} = 0 \right]$$

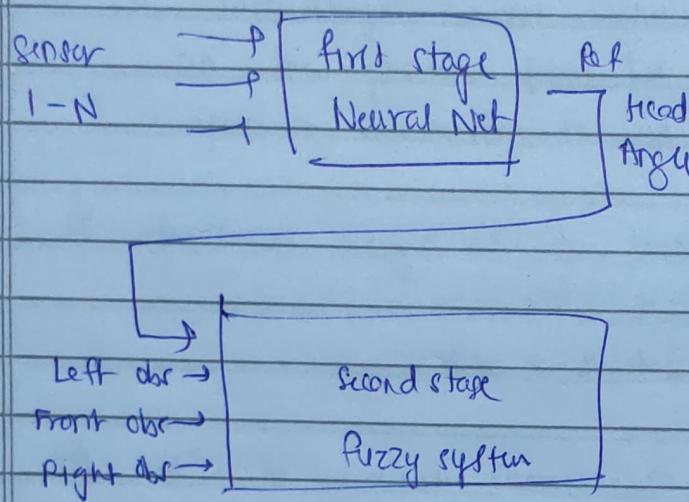
* EM Algorithm \Rightarrow problem of solving the incomplete data approach indirectly by proceeding in terms of complete data log likelihood function $\log L_c(\psi)$

(BHAGYARANA)
(class 12)

(Q5) Robot Navigation

Q5.7

Two stage Neuro-Fuzzy system



① Input from sensor

↓
Neural network

② output by ^{cnt} experim

③ Neural network is
trained accordingly

(MSE) mean square
error

④ make adjustment
in Neural Network

(Q6)

(Explain hyper plane classification using maximal margin)
(Illustrated & derive)

① if $w \rightarrow$ weight vector realising a functional margin of 1 on the positive point x^+ and the negative point x^- , compute its geometric margin.

② functional margin of 1 implies

$$\langle w \cdot x^+ \rangle + b = +1$$

$$\langle w \cdot x^- \rangle + b = -1$$

③ while to compute Geometric margin, Normalize w , geometric margin $\gamma \rightarrow$ functional margin of resulting classifier

$$\begin{aligned} \gamma &= \frac{1}{2} \left(\left\langle \frac{w}{\|w\|_2} \cdot x^+ \right\rangle - \left\langle \frac{w}{\|w\|_2} \cdot x^- \right\rangle \right) \\ &= \frac{1}{2\|w\|_2} (\langle w \cdot x^+ \rangle - \langle w \cdot x^- \rangle) = \frac{1}{\|w\|_2} \end{aligned}$$

④ Resulting margin = $\frac{1}{\|w\|_2}$

⑤ Given linearly separable training sample

$$S = ((x_1, y_1); (x_2, y_2); \dots; (x_l, y_l))$$

⑥ Hyperplane $[w, b]$ that solves optimization problem

$$\underset{w, b}{\text{minimize}} \quad \langle w, w \rangle$$

$$\text{subject to } y_i (\langle w \cdot x_i \rangle + b) \geq 1, \quad i=1 \dots l,$$

\rightarrow realises the maximum margin

hyperplane with geometric margin = $\left[\gamma = \frac{1}{\|w\|_2} \right]$
(transform it to dual problem)

(Q7)

(COVID Disease)

System parameters

→ Four positive
 True negative
 False positive
 False negative

Forecasting
 the
 time
 based on

(Density function
 for time of covid)

past epidemic
 using
 machine learning

other (distribution)

$$M = S(t) + I(t) + R(t)$$

$$\frac{dS(t)}{dt} = -\beta I(t) S(t)$$

$$\frac{dR(t)}{dt} = \gamma I(t)$$

$$\frac{dI(t)}{dt} = \beta I(t) S(t) - \gamma I(t)$$

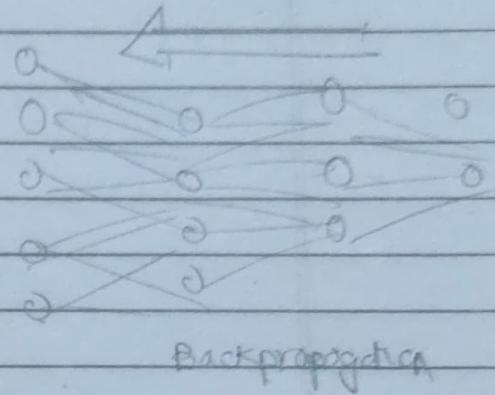
(curve fitting) $\rightarrow (\beta \& \gamma)$ ✓

minimizing (for least square) $I(t) = \frac{N}{(1 - K e^{-\beta t})}$

(Q8)

Back propagation Neural Network

① Backpropagation = process of fine tuning the weights of a neural net base on the error rate (i.e. loss) obtained in previous epoch (i.e. iteration)



Proper tuning of weight ensures ① lower error rate

② making model reliable by increasing its generalization.

③ We need activation function \rightarrow determining activation value at every node

& hypothesis function

& loss function

& calculate delta's in back propagation

④ We do delta calculation, step of every unit, back-propagating the loss into the neural net & finding out what loss every node/unit is responsible for.

⑤ Update the weights