

(Q3)

(GMM based modelling)

$$P(X/\theta) = \sum_{k=1}^K \pi_k N(x/\mu_k, \Sigma_k)$$

(Gaussian mixture Model) - Density Based model

(A) Different parameters to be estimated =

distribution  $N(x/\mu_k, \Sigma_k)$ 

parameters of  
GMM

$\theta$ : ①  $\pi_k$  (mixture weights  $\pi_k$ )  
 ②  $\mu_k$  ( $k$  means  $\mu_k$ )  
 ③  $\Sigma_k$  (covariances)  
 $k = 1, \dots, K$

(B) Design strategy for deciding no. of mixture models for facial images

EM Algorithm  $\rightarrow$  find parameter in GMM that gives maximum likelihood of

$$F(x) = \sum_{q=1}^m P\left(\frac{c_q}{x}\right) \left[ \mu_q^y \sum_q y^x \Sigma_q^{xy} (x - \mu_q)^x \right]$$

Observed data  $x$

where

$P(c_q/x) \rightarrow$  conditional probability

$$\Sigma_q = \begin{bmatrix} \Sigma_q^{xx} & \Sigma_q^{xy} \\ \Sigma_q^{yx} & \Sigma_q^{yy} \end{bmatrix}$$

$m \rightarrow$  GMM mixture in facial conversion

$$\mu_q = \begin{bmatrix} \mu_q^x \\ \mu_q^y \end{bmatrix}$$

(★) GMM  $\rightarrow$  Joint density model is baseline for mapping source & target faces

(Cepstrum based GMM) ✓