# Operations Research (Paper III) MSc. (Computer Science) Semester III 2022-23

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# **Practical 1**

**Aim:** Use graphical method to solve the following LPP:

Max 
$$Z = 3x + 5y$$
  
w.r.t.  
 $x + 2y \le 2000$ ,  
 $x + y \le 1500$ ,  
 $y \le 600$ ,  $x, y \ge 0$ 

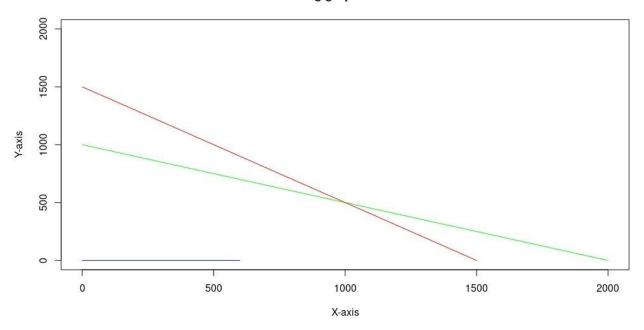
#### **Source Code:**

```
require(lpSolv
e) C < -c(3, 5)
A \leftarrow matrix(c(1, 2,
              0, 1), nrow = 3, byrow =
T) B < c(2000, 1500, 600)
constraint direction <- c("<=", "<=",
"<=")
plot.new()
plot.window(xlim = c(0, 2000), ylim = c(0, 2000))
2000)) axis(1) axis(2)
title (main = "LPP using graphical method", xlab = "X-axis",
ylab = "Yaxis") box()
segments (x0 = 2000, y0 = 0, x1 = 0, y1 = 1000, col =
"green") segments (x0 = 1500, y0 = 0, x1 = 0, y1 = 1500,
col = "red") segments (x0 = 0, y0 = 0, x1 = 600, y1 = 0,
col = "blue") z <- lp(direction = "max",</pre>
        objective.in = C,
const.mat = A,
                        const.dir =
constraint direction,
const.rhs = B_{r}
                      all.int = T
) print(z$status)
best sol <- z$solution names(best sol) <-
c("x1", "x2") print(paste("Total cost: ",
z$objval, sep = ""))
```

```
# Use graphical method to solve the following LPP:
# Max z = 3x + 5y
  B \leftarrow c(2000, 1500, 600)
[1] 0
```

```
> best_sol ← z$solution
> names(best_sol) ← c("x1", "x2")
> print(paste("Total cost: ", z$objval, sep = ""))
[1] "Total cost: 5500"
> |
```

#### LPP using graphical method



**Aim:** Use simplex method to solve the following LPP:

# **Practical 2**

```
Max Z = 3x + 2y
w.r.t.
x + y \le 4,
x - y \le 2,
x, y \ge 0
```

### **Source Code:**

```
In [1]:
          1 from scipy.optimize import linprog
          3 \text{ obj} = [-3, -2]
             lhs_ineq = [[1, 1],
                          [1, -1]]
          7 rhs_ineq = [4,
          8
          10 bound = [(0, float("inf")),
          11
                       (0, float("inf"))]
          z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
bounds = bound, method = "revised simplex")
In [2]:
           3
Out[2]:
              con: array([], dtype=float64)
              fun: -11.0
          message: 'Optimization terminated successfully.'
              nit: 2
            slack: array([0., 0.])
           status: 0
          success: True
                x: array([3., 1.])
          1 print(z.fun)
In [3]:
           print(z.success)
          3 print(z.x)
         -11.0
         True
         [3. 1.]
```

## **Practical 3**

Min 
$$Z = x_1 - 3x_2 + 2x_3$$
  
w.r.t  
 $3x_1 - x_2 + 3x_3 \le 7$ ,  
 $-2x_1 + 4x_2 \le 12$ ,  $-4x_1$   
 $+ 3x_2 + 8x_3 \le 10$ ,  $x_1$ ,  
 $x_2, x_3 \ge 0$ 

#### **Source Code:**

**Aim:** Use simplex method to solve the following LPP: from scipy.optimize import linprog

```
In [1]:
         1 from scipy.optimize import linprog
            obj = [1, -3, 2]
            lhs_ineq = [[3, -1, 3],
                         [-2, 4, 0],
          7
                         [-4, 3, 8]]
          9 rhs_ineq = [7,
         10
         11
                         10]
         12
         13 bound = [(0, float("inf")),
         14
                      (0, float("inf")),
         15
                      (0, float("inf"))]
In [2]:
         1 z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
                         bounds = bound, method = "revised simplex")
          2
          3
          4
             con: array([], dtype=float64)
Out[2]:
             fun: -11.0
         message: 'Optimization terminated successfully.'
             nit: 2
           slack: array([ 0., 0., 11.])
          status: 0
         success: True
               x: array([4., 5., 0.])
```

## **Practical 4**

Max 
$$Z = x + 2y$$
  
w.r.t.  
 $2x + y \le 20$ ,  
 $-4x + 5y \le 10$ ,  
 $-x + 2y \ge -2$ ,  $-x$   
 $+5y = 15$ ,  $x, y \ge 0$ 

#### **Source code:**

**Aim:** Use simplex method to solve the following LPP: from scipy.optimize import linprog

```
obj = [-1, -2]
        lhs_ineq = [[2, 1],
                [-4, 5],
        [1, -2]]
        rhs_ineq = [20,
In [1]:
                10,
                2]
        lhs_eq = [[-1, 5]]
        rhs_eq = [15]
        bound = [(0, float("inf")),
              (0, float("inf"))]
        z = linprog(c = obj, A_ub = lhs_ineq, b_ub =
        rhs_ineq,
                A_eq = lhs_eq, b_eq = rhs_eq,
In [2]:
                bounds = bound, method = "revised simplex")
        \mathbf{Z}
```

```
In [1]:
          1 from scipy.optimize import linprog
          3 \text{ obj} = [-1, -2]
          5 lhs_ineq = [[2, 1],
                        [-4, 5],
[1, -2]]
          7
          8
          9 rhs_ineq = [20,
         10
         11
                         2]
         12
         13 lhs_eq = [[-1, 5]]
         14 rhs_eq = [15]
         15
         16 bound = [(0, float("inf")),
                     (0, float("inf"))]
          z = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq,
A_eq = lhs_eq, b_eq = rhs_eq,
In [2]:
                         bounds = bound, method = "revised simplex")
          3
          4
          5 z
Out[2]:
           con: array([0.])
             fun: -16.818181818181817
         message: 'Optimization terminated successfully.'
             nit: 3
           slack: array([ 0. , 18.18181818, 3.36363636])
          status: 0
         success: True
           __ x: array([7.72727273, 4.54545455])
```

# **Practical 5**

Use Big M method to solve the following LPP:

Min 
$$Z = 4x_1 + x_2$$
  
w.r.t.  
 $3x_1 + 4x_2 \ge 12$ ,  
 $x_1 + 5x_2 \ge 15$ ,  
 $x_1, x_2 \ge 0$ 

#### **Source code:**

from scipy.optimize import linprog

opt = linprog(c=obj,A\_ub=lhs\_ineq,b\_ub=rhs\_ineq,
bounds=bound,method="interior-point") In [2]:

opt

```
In [1]:
            from scipy.optimize import linprog
          3
            obj = [4, 1]
            lhs_ineq = [[-3, -4],
                         [-1, -5]]
          6
          7
             rhs_ineq = [-20]
          8
                         -15]
          9
             bound = [(0, float("inf")),
         10
         11
                      (0, float("inf"))]
             opt =linprog(c=obj,A_ub=lhs_ineq,b_ub=rhs_ineq,
In [2]:
                            bounds=bound, method="interior-point")
          3
            opt
Out[2]:
             con: array([], dtype=float64)
             fun: 5.0000000002364455
         message: 'Optimization terminated successfully.'
             nit: 5
           slack: array([1.64270375e-10, 1.00000000e+01])
          status: 0
         success: True
                x: array([6.01160437e-11, 5.00000000e+00])
```

## **Practical 6**

Use any method to solve the following resource allocation problem:

```
Max Z = 20x_1 + 12x_2 + 50x_3 + 25x_4 .................(profit) w.r.t. x_1 + x_2 + x_3 + x_4 \le 50 ......................(manpower) 3x_1 + 2x_2 + x_3 \le 100 .......................(material A) x_2 + 2x_3 \le 90, .................................(material B) x_1, x_2, x_3 \ge 0
```

## **Source code:**

from scipy.optimize import linprog

opt = linprog(c = obj, A\_ub = lhs\_ineq, b\_ub =
rhs\_ineq, In [2]: method="revised simplex") opt

```
In [1]: 1 from scipy.optimize import linprog
          3 \text{ obj} = [-20, -12, -40, -25]
          5 lhs_ineq = [[1, 1, 1, 1],
6 [3, 2, 1, 0],
7 [0, 1, 2, 3]]
          9 rhs_ineq = [50,
         10
                       100,
         11
                       90]
In [2]:
         opt = linprog(c = obj, A_ub = lhs_ineq, b_ub = rhs_ineq, method="revised simplex")
          3 opt
Out[2]:
          con: array([], dtype=float64)
             fun: -1900.0
          message: 'Optimization terminated successfully.'
             nit: 2
            slack: array([ 0., 40., 0.])
           status: 0
          success: True
               x: array([ 5., 0., 45., 0.])
```

# **Practical 7**

Use simplex method to solve the following LPP:

```
Max Z = 200x + 300y
w.r.t.
2x + 3y \ge 1200,
x + y \le 400, 2x
+ 1.5y \ge 900, x,
y \ge 0
```

### **Source code:**

```
from scipy.optimize import linprog
```

# **Practical 8**

Use dual simplex method to solve the following LPP:

```
Max Z = 40x_1 + 50x_2
w.r.t.
2x_1 + 3x_2 \le 3,
8x_1 + 4x_2 \le 5,
x_1, x_2 \ge 0
```

#### **Source code:**

```
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals
[1] 15.00 1.25 0.00 0.00
> lp("max", f.obj, f.con, f.dir, f.rhs, compute.sens = T)$duals.to
[1] 3.75e+00 1.20e+01 1.00e+30 1.00e+30
>
```

## **Practical 9**

Solve following transportation problem in which each cell represents unit costs:

	Customers				
	1	2	3	4	Supply
	10	2	20	11	15
Suppliers	12	7	9	20	25
	4	14	16	18	10
Demand	5	15	15	15	

#### **Source code:**

library(lpSolve)

```
> ##SOLVE FOLLOWING TRANSPORTATION PROBLEM IN WHICH CELL ENTRIES REPRESENT UNIT COSTS USING R PROGRAMMIN G.

> # "Customer 1", "Customer 2", "Customer 3", "Customer 4" SUPPLY

> #SUPPLIER 1 10 2 20 11 15

> #SUPPLIER 2 12 7 9 20 25

> #SUPPLIER 3 4 14 16 18 10

> #DEMAND 5 15 15 15

> library(lpSolve)

> cost ← matrix(c(10, 2, 20, 11, 12, 7, 9, 20, 4, 14, 16, 18), nrow = 3, byrow = T)

> colnames(cost) ← c("Customer 1", "Customer 2", "Customer 3", "Customer 4")

> rownames(cost) ← c("Supplier 1", "Supplier 2", "Supplier 3")

> row.signs ← rep("≤", 3)

> row.rhs ← c(15, 25, 10)

> col.signs ← rep("≥", 4)

> col.rhs ← c(5, 15, 15, 15)
```

```
> total.cost ← lp.transport(cost, "min", row.signs, row.rhs, col.signs, col.rhs)
> total.cost$solution
        [,1] [,2] [,3] [,4]
[1,] 0 5 0 10
[2,] 0 10 15 0
[3,] 5 0 0 5
> print(total.cost)
Success: the objective function is 435
```

# **Practical 10**

Solve following assignment problem represented in this matrix:

		Jobs			
		1	2	3	
	1	15	10	9	
Workers	2	9	15	10	
	3	10	12	8	

## **Source Code:**

```
> answer ← lp.assign(cost)
> answer$solution
       [,1] [,2] [,3]
[1,] 0 1 0
[2,] 1 0 0
[3,] 0 0 1
> |
```