TUTORIAL - 3

Q1. Write linear search Pseudo code to search an element in a sorted array with minimum Comparisons.

Ans

```
for (i=0 to n)
  {
    if (arr[i] == value)
      // element found
  }
```

Q2. Write Pseudo Code for iterative & recursive insertion sort. Insertion sort is called Online sorting. Why? What about other sorting algorithms that has been discussed?

Ans. Iterative

```
void insertion_sort (int arr[], int n)
 {
   for (int i=1 ; i<n ; i++)
     {
       j = i-1 ;
       x = arr[i] ;
     while (j>-1 && arr[j] > x)
       {
         arr[j+1] = arr[j] ;
         j-- ;
       }
     arr[j+1] = x ;
   }
}
```

Recursive

```
void insertion_sort (int arr[], int n)
{
    if (n <= 1)
        return;
    insertion_sort (arr, n-1);
    int last = arr[n-1];
    int j = n-2;
    while (j >= 0 && arr[j] > last)
    {
        arr[j+1] = arr[j];
        j--;
    }
    arr[j+1] = last;
}
```

Insertion sort is called 'Online Sort' because it does not need to know anything about what values it will sort and information is requested while algorithm is running.

Other Sorting Algorithms :-

- Bubble Sort
- Quick Sort
- Merge Sort
- Selection Sort
- Heap Sort

3. Complexity of all sorting algorithm that has been discussed in lectures.

Ans.

Sorting Algorithm	Best	Worst	Average
Selection Sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Bubble Sort	$O(n)$	$O(n^2)$	$O(n^2)$
Insertion Sort	$O(n)$	$O(n^2)$	$O(n^2)$
Heap Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$
Quick Sort	$O(n \log n)$	$O(n^2)$	$O(n \log n)$
Merge Sort	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$

Q4. Divide all sorting algorithms into inplace / stable / Online sorting

Ans.

INPLACE SORTING	STABLE SORTING	ONLINE SORTING
Bubble Sort Selection Sort Insertion Sort Quick Sort Heap Sort	Merge Sort Bubble Sort Insertion Sort Count Sort	Insertion Sort

Q5. Write recursive / iterative pseudocode for binary search. What is the Time & Space Complexity of Linear & Binary Search.

Ans. (1)

Iterative ⇒

```
int le_search ( int arr[], int l, int r, int key)
  {
     while (l <= r)    {
      int  m = ((l+r)/2) ;
      if (arr[m] == key)
          return m;
     else if  (key < arr[m])
          r = m-1;
      else
          l = m+1;
      }
       return -1;
  }
```

Recursive ⇒

```
int le_search(int arr[], int l, int r, int key)
    {
       while (l <= r)  {
      int m = ((l+r)/2);
      if (key == arr[m])
            return m;
     else if (key < arr[m])
          return b_search(arr, l, mid-1, key);
      else
        return b_search(arr, mid+1, r, key);
     }
     return -1;
  }
```

Time Complexity :-

a) Linear Search - O(n)
b) Binary Search - O(log n)

6. Write recurrence relation for binary recursive search.

Ans.

$$T(n) = T(n/2) + 1 \quad \text{— (1)}$$
$$T(n/2) = T(n/4) + 1 \quad \text{— (2)}$$
$$T(n/4) = T(n/8) + 1 \quad \text{— (3)}$$

$$T(n) = T(n/2) + 1$$
$$= T(n/4) + 1 + 1$$
$$= T(n/8) + 1 + 1 + 1$$
$$\vdots$$
$$T(n/2^k) + 1 \text{ (k Times)}$$

Let $g^k = n$

$k = \log n$.

$T(n) = T(n/n) + \log n$

$T(n) = T(1) + \log n$

$T(n) = O(\log n)$ → Answer.

Q7. Find two indexes such that $A[i] + A[j] = k$ in minimum time Complexity.

→
```
for (i=0; i<n; i++)
    {
      for (int j=0; j<n; j++)
        {
          if (a[i] + a[j] == k)
            printf("%d %d", i, j);
        }
    }
```

Q8. Which sorting is best for practical uses ? Explain.

→ Quick sort is fastest general-purpose sort. In most practical situations quicksort is the method of choice as stability is important and space is available, mergesort might be best.

Q9. What do you mean by inversions in an array? Count the number of inversions in Array arr[] = {7, 21, 31, 8, 10, 1, 20, 6, 4, 5} using merge sort.

Ans. A Pair (A[i], A[j]) is said to be inversion if
- A[i] > A[j]
- i < j
- Total no. of inversions in given array are 31 using merge sort.

Q10. In which cases Quick Sort will give best & worst case time complexity.

Ans. Worst Case $O(n^2)$ → The worst case occurs when the pivot element is an extreme (smallest / largest) element. This happens when input array is sorted or reverse sorted and either first or last element is selected as pivot.

Best Case $O(n \log n)$ → The best case occurs when we will select pivot element as a mean element.

Q11. Write Recurrence Relation of Merge / Quick Sort in best & worst case. What are the similarities & differences between complexities of two algorithm & why?

Ans. Merge Sort →

Best Case → $T(n) = 2T(n/2) + O(n)$
Worst Case → $T(n) = 2T(n/2) + O(n)$ } $O(n \log n)$

Quick Sort →

Best Case → $T(n) = 2T(n/2) + O(n) \rightarrow O(n \log n)$
Worst Case → $T(n) = T(n-1) + O(n) \rightarrow O(n^2)$

In quick sort, array of element is divided into 2 parts repeatedly until it is not possible to divide it further.

In merge sort the elements are split into 2 subarray $(n/2)$ again & again until only one element is left.

Q. Selection sort is not stable by default but can you write a version of stable selection sort?

Ans

```
for(int i=0; i<n-1; i++)
  {
     int min = i;
  for(int j = i+1; j<n; j++)
    {
       if (a[min]>a[j])
          min=j;
    }
  int key = a[min];
   while (min>i)
     {
       a[min]=a[min-j];
        min--;
     }
     a[i]= key;
}
```

Q13. Bubble sort scans array even when array is sorted. Can you modify the bubble sort so that it does not scan the whole array once it is sorted.

Ans.

A better version of bubble sort, known as modified bubble sort, includes a flag that is set of a exchange is made after an entire pass over. If no exchange is made then it should be called the array is already order because no two elements need to be switched.