91)
$$T(n) = 3T (n/2) + n^2$$
 $T(n) = aT(n/6) + f(n^2)$
 $a > 1, b > 1$

On campaining

 $a = 3, b = 2, f(n) = n^2$

Now, $c = lag_a = lag_a = 1.584$
 $n^2 = n^{1.524} \le n^2$
 $f(n) > n^2$
 $T(n) = o(n^2)$

92)
$$T(n) = 4T(n/2) + n^2$$

 $\rightarrow a/1, b/1$
 $a = 4, b = 2, f(n) = n^2$
 $c = \log_2 4 = 2$
 $n^2 = n^2 = f(n) = n^2$
 $\therefore T(n) = \theta(n^2 \log_2 n)$

93)
$$T(n)_{2}T(n/2)+2^{n}$$
 $A=1$
 $b=2$
 $f(n)_{2}2^{n}$
 $c \cdot laga \cdot lagc = 0$
 $h^{c} = h^{c} = 1$
 $f(n)_{2}n^{c}$
 $T(n)_{2}o(2^{n})$

35)
$$T(n) = 16 T(n/4) + n$$
 $\rightarrow a = 16, b = 4$
 $f(n) = n$
 $c = \log_{16} = \log_{4}(4)^2 = 2\log_{4} 4$
 $= 2^{4} = \log_{4}(4)^2 = 2\log_{4} 4$
 $n^c \ni n^2$
 $f(n) < f(n) = 0 (n^2)$

30)
$$T(n)=2T(n/2)+n \log n$$

 $\rightarrow a=2, b=2$
 $f(n)=n \log n$
 $c=\log 2=1$
 $n^c=n^l=n$
 $n \log n > n$
 $f(n)>n^c$
 $T(n)=0 (n \log n)$

g7) T(n)= 2T(n/2) + n/lagn > a=2, b=2, f(n)= n/legn C= lag 2 = 1 nc=n1=n · lag n < n · . f(n) < nc · . T(n) = 0 (n) 98) T(n) = 2T(n/4) + n0.51 → a = 2, b = 4, f(n)= n° 51 C= lega = leg 2 = 0.5 n° = n° 5 n° 5 < n° . 51 \$(n)>nc · . T(n) = 0 (n°.51) gg) T(n) = 0.5 T(n/2)+1/n \rightarrow a=0.5, b=2 a 1/1 but here a is 0.5 so we cannot apply Master's Theorem. 910) T(n)= 16T(n/4)+n! -> a=16, b=4, f(n)=n! .. C = lag a = lag 16 2 2 $n^{c} = n^{2}$

As n/ >n2

· . T(n) = 0(n!)

911) 4T(n/2) + lag n -, a=4, b=e, f(n)=lagn C = laga . laga = 2 ne = n2 [(n) · lagn : lagn < n= 2(n)(n° T(n) = 0 (nc) " 0 (n2) Q12) T(n) = squt(n) T(n/2) + logn _, a=\n, b=2 C= lago a - lagon = 1 lagon · · - Lagen < lag(n) · . f(n)>nc T(n) = 0 (f(n)) = 0 (leg (n)) (13) T(n)=3T(n/2)+n \rightarrow a=3; b=2; f(n)=nC = lag a = lag 3 = 1.5849 nc = n 1.5489 n < n1.5849 > f(n) < nc T(n)=0(n1.5841) Q14) T(n)= 3T(n/3) + sgrt (n) $\rightarrow a=3, b=3$ C = leg a = leg 3 = 1 $n^{c} = n^{1} = n$ As sgut (n) < n f(n) (no T(n) = 0 (n)

$$g(5) T(n) = 4T(n/2) + n$$
 $\rightarrow 0 = 4, b = 2$
 $C = lag_b a = lag_b 4 = 2$
 $h^c = n^2$
 $n < n^2$ (for any constant)

 $f(n) < n^c$
 $f(n) = 0 (n^2)$

$$g_{16}$$
) $T(n) = 3T(n/4) + n \log n$
 $\rightarrow a = 3, b = 4, f(n) = n \log n$
 $C = \log_{6} a = \log_{4} 3 = 0.792$
 $n^{c} = n^{0.792}$
 $n^{0.792} < n \log n$
 $T(n) = \theta(n \log n)$

$$g_{17}$$
) $T(n)=3T(n/3)+n/2$
 $\rightarrow a=3;b=3$
 $c=laga-lag_3=1$
 $f(n)=n/2$
 $n^c=n'=n$
 $As n/2 < n$
 $f(n) < n^c$

.. T(n)=0(n)

$$g_{18}$$
) $T(n)=GT(n/3)+n^{2}lagn$
 $\rightarrow a=G;b=3$
 $C=lag_{b}a=lag_{3}G=1.6309$
 $n^{c}=n^{1.6502}$

As n16309 (n2 legn
:. T(n) 20 (n2 legn)

$$g_{19}$$
) $T(n)=4T(nb)$ $\frac{1}{100}$ + $\frac{1}{100}$ + $\frac{1}{100}$ + $\frac{1}{100}$ $\frac{1}{100}$

g20) $T(n) = 64T(n/8) - n^2 lagn$ A = 64 b - 8 $C = lag a = lag 64 = lag (8)^2$ C = 2 $C = n^2$ $\therefore n^2 lagn > n^2$ $T(n) = 0 (n^2 lagn)$

$$\begin{array}{c} (321) \ T(n) = 7T(n/3) + n^2 \\ \rightarrow a = 7; b = 3; f(n) = n^2 \\ C = \log_{3} a = \log_{3} 7 = 1.7712 \\ in^{c} = n^{1.7712} \\ n^{1.7712} < n^{2} \\ T(n) = 0 (n^2) \end{array}$$

$$g^{22}$$
) $T(n) = T(n/2) + n(2-(esn))$
 $\rightarrow a = 1, b = 2$
 $C = leg_b a = leg_1 = 0$
 $n^c = n^c = 1$
 $n(2-(esn)) n^c$
 $T(n) = 0(n(2-(esn))$