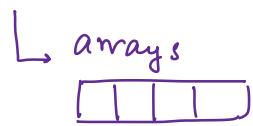


## Today's Content

- Trees Intro
- Naming Convention
- Tree Traversal
- Basic Tree Problems

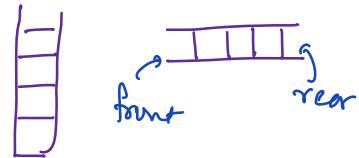
Linear:



LinkedList

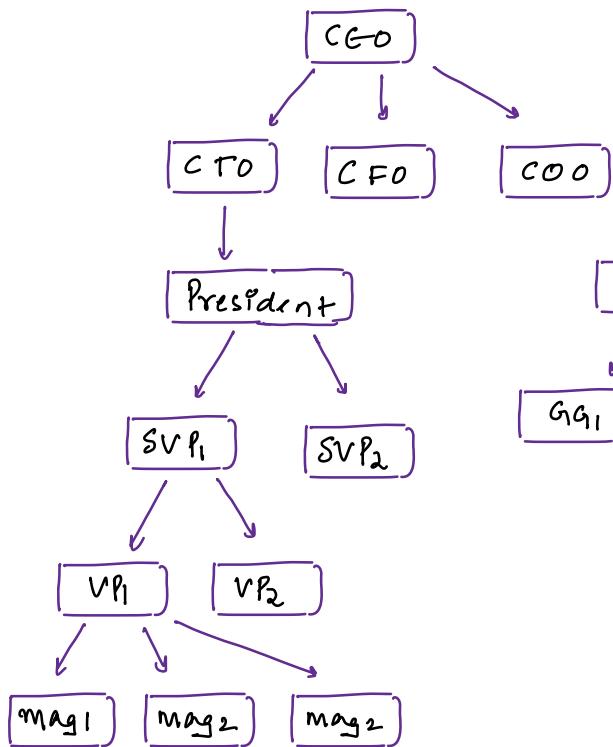


stacks & Queues

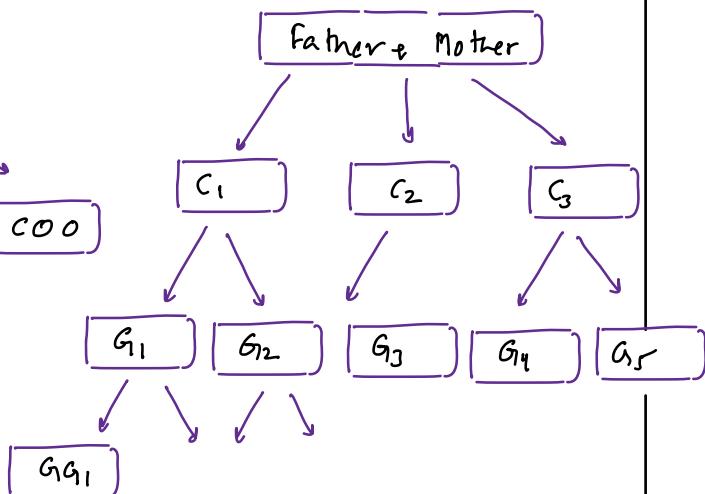


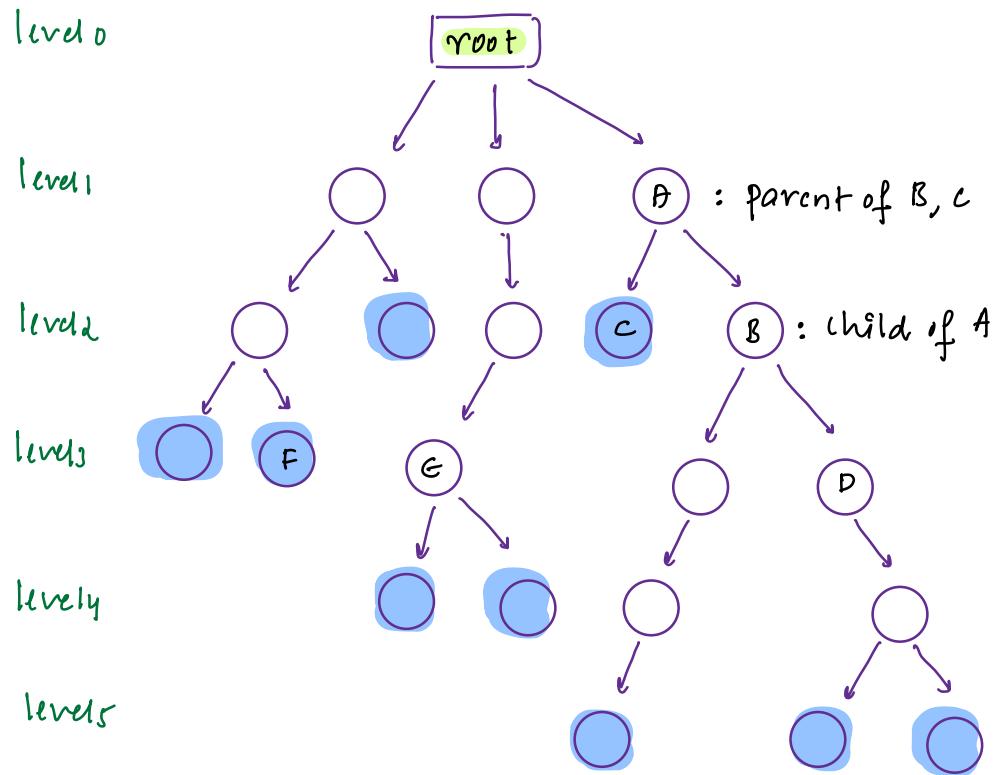
Hierarchical Data

Ex: Company organisation



Ex: Family Tree:





### Naming

$A \rightarrow D$ : A is ancestor of D & D is decendent of A

$B \rightarrow C$ : Sibling node, share same parent

F, E, D: Nodes at same level

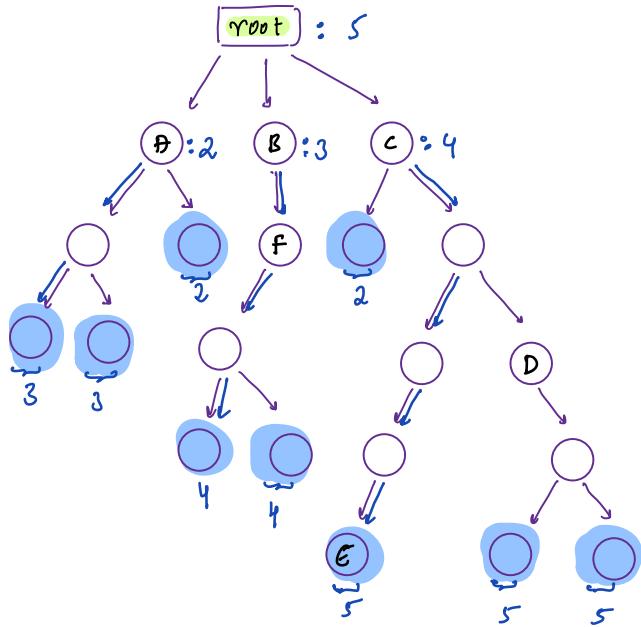
root: Node without a parent

leaf: Nodes without children

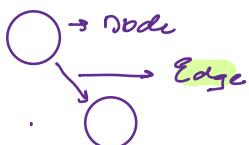
True: [We will have only 1 root node  
for every node only 1 single parent]

height(Node):

length of longest path  
from node, to any of  
its descendant leaf  
nodes



Note: Path is calculated  
Based on no. of edges



$$h(A) = 2 \quad \underline{\text{obs1:}}$$

$$h(B) = 3 \quad h(\text{node}) = 1 + \max(\text{height of its child nodes})$$

$$h(C) = 4 \quad \underline{\text{obs2:}}$$

$$h(D) = 2 \quad h(\text{leaf Node}) = 0$$

$$h(E) = 0$$

$$h(F) = 2$$

**Terminologies**  
 $\text{height(Tree)} = \text{height}(\text{root node})$   
 $\text{depth(Tree)} = \text{max depth of leaf node}$

depth(Node):

length of path from  
root to the node

$$d(A) = 1$$

$$d(F) = 2$$

$$d(E) = 5$$

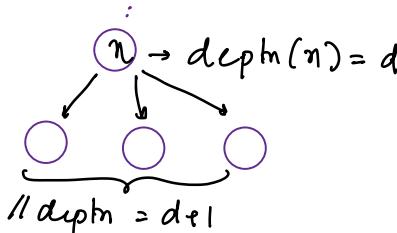
$$d(D) = 3$$

root

obs: if depth of Node = d,  
depth of its child  
nodes = d+1

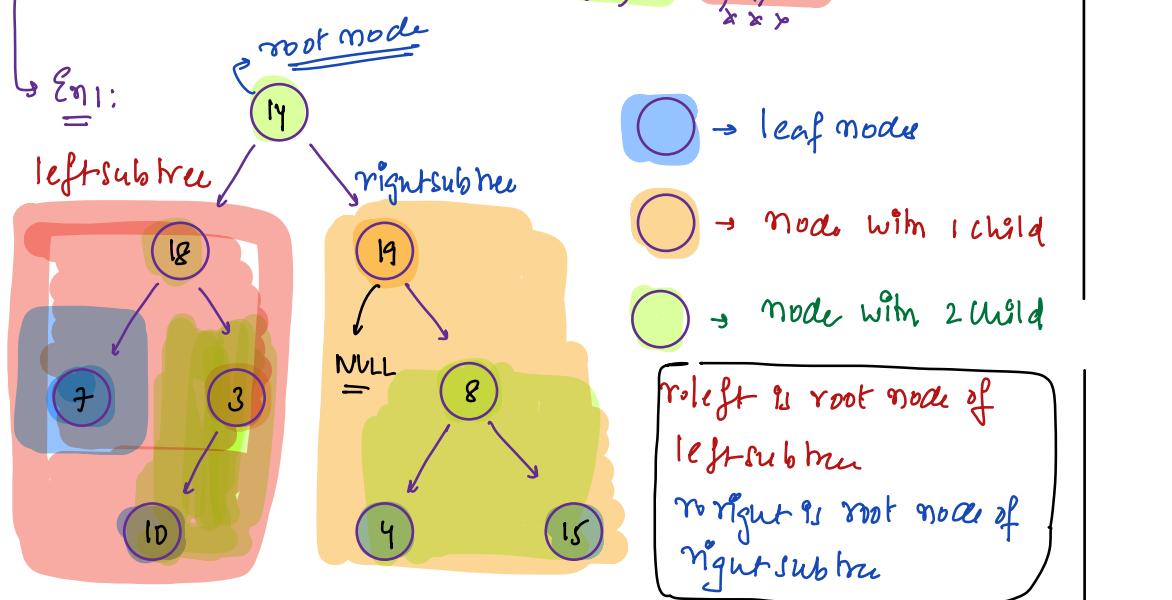
obs2: depth(root) = 0

Note: wrong  
 $\text{height(node)} = \text{depth(node)}$



Binary Tree : Every node can at max have 2 children

0, 1, 2    3, 4, 5  
x x x

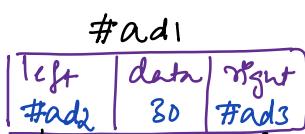


Class node {

```

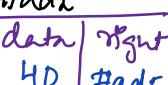
int d;
node left; // obj ref, which can hold address of node object
node right; // obj ref, which can hold address of node object
node(int n) {
    d = n
    left = null
    right = null
}
    
```

Node r = new Node(30)

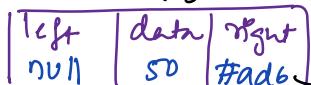


Obs: Given root node we can traverse entire tree

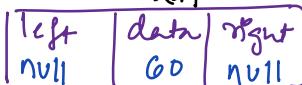
#ad2



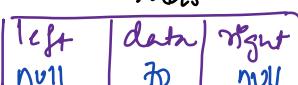
#ad3



#ad4



#ad5



#ad6



II Tree Construction, can be explained by **Serialization & deserialization**  
in adv context

→ Note: For all Tree problems, tree is already constructed we  
are just given root node

### Tree Traversals:

→ preOrder	→ level order
→ InOrder	→ vertical level order
→ postOrder	<hr/> <u>Adv</u>

## Tree Traversals:

→ Preorder:  $\text{data} \rightarrow \text{LST} \rightarrow \text{RST}$

Step1: print( $\text{root} \cdot \text{data}$ )

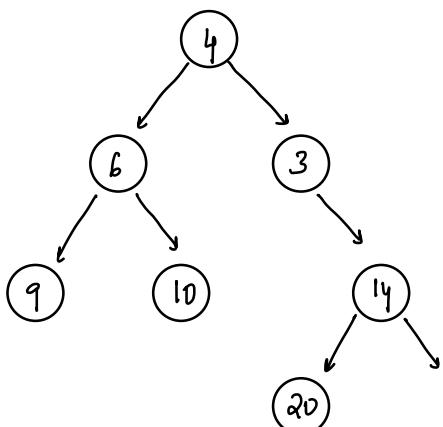
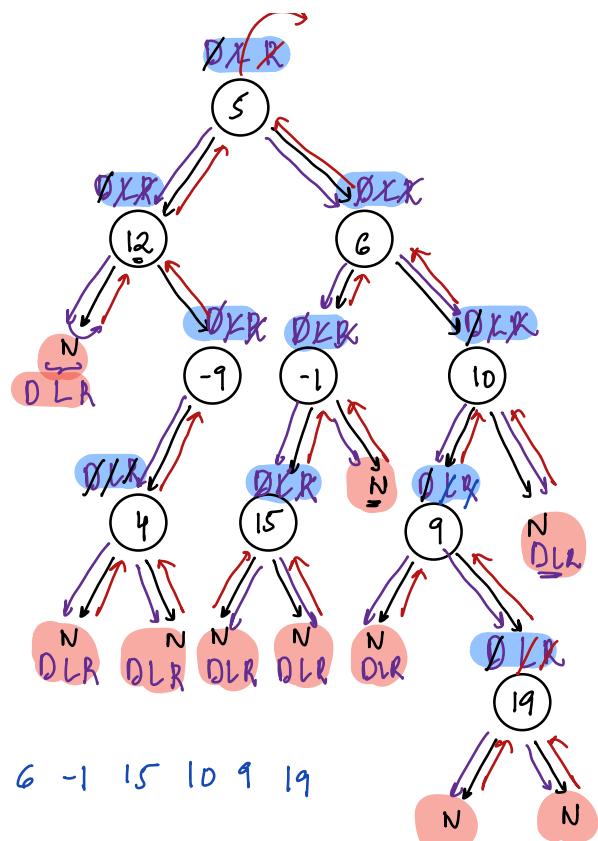
Step2: goto leftsubtree

& print entire leftsubtree  
in preorder

Step3: goto rightsubtree

& print entire rightsubtree  
in preorder

→ output: 5, 12 -9 4 6 -1 15 10 9 19



Preorder: DLR : 4 6 9 10 3 14 20

Inorder: LDR : 9 6 10 4 3 20 14

Postorder: LRD : 9 10 6 20 14 3 4

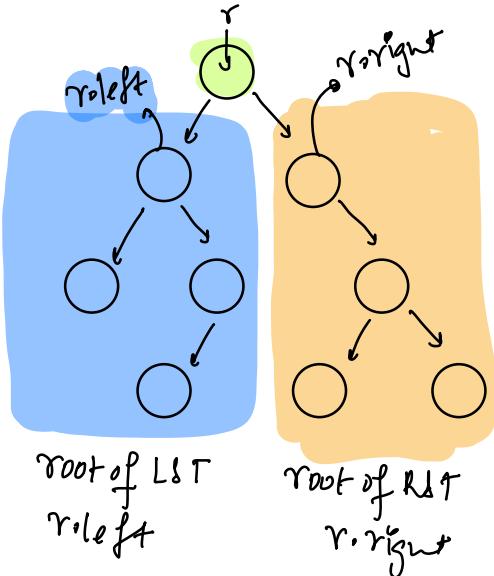
## Pseudo Code:

Ass: Given root node, print entire in pre-order

```
void preOrder(Node r) {
    1 If(r==null) {return}
    2 print(r.data)
    3 preOrder(r.left)
    4 preOrder(r.right)
}
```

Tc: O(N)    Sc: O(h)

↳ Height of Tree  
↳ Recursion Stack



## Pseudo Code:

Preorder: 1 2 3 4      1 → base

2 → print

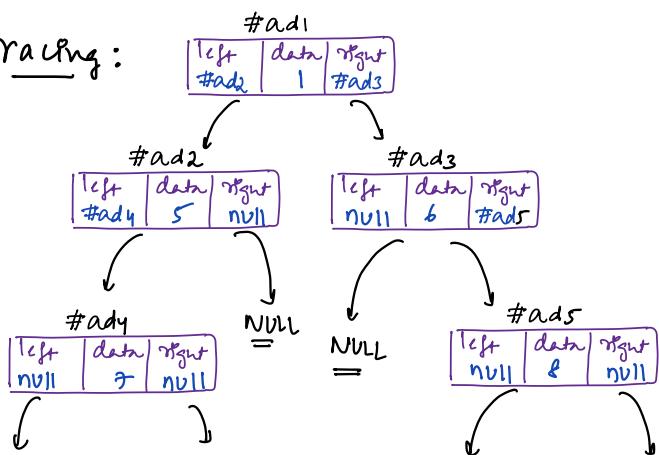
3 → goto left

4 → goto right

TODO

Assignments: Use Recursion

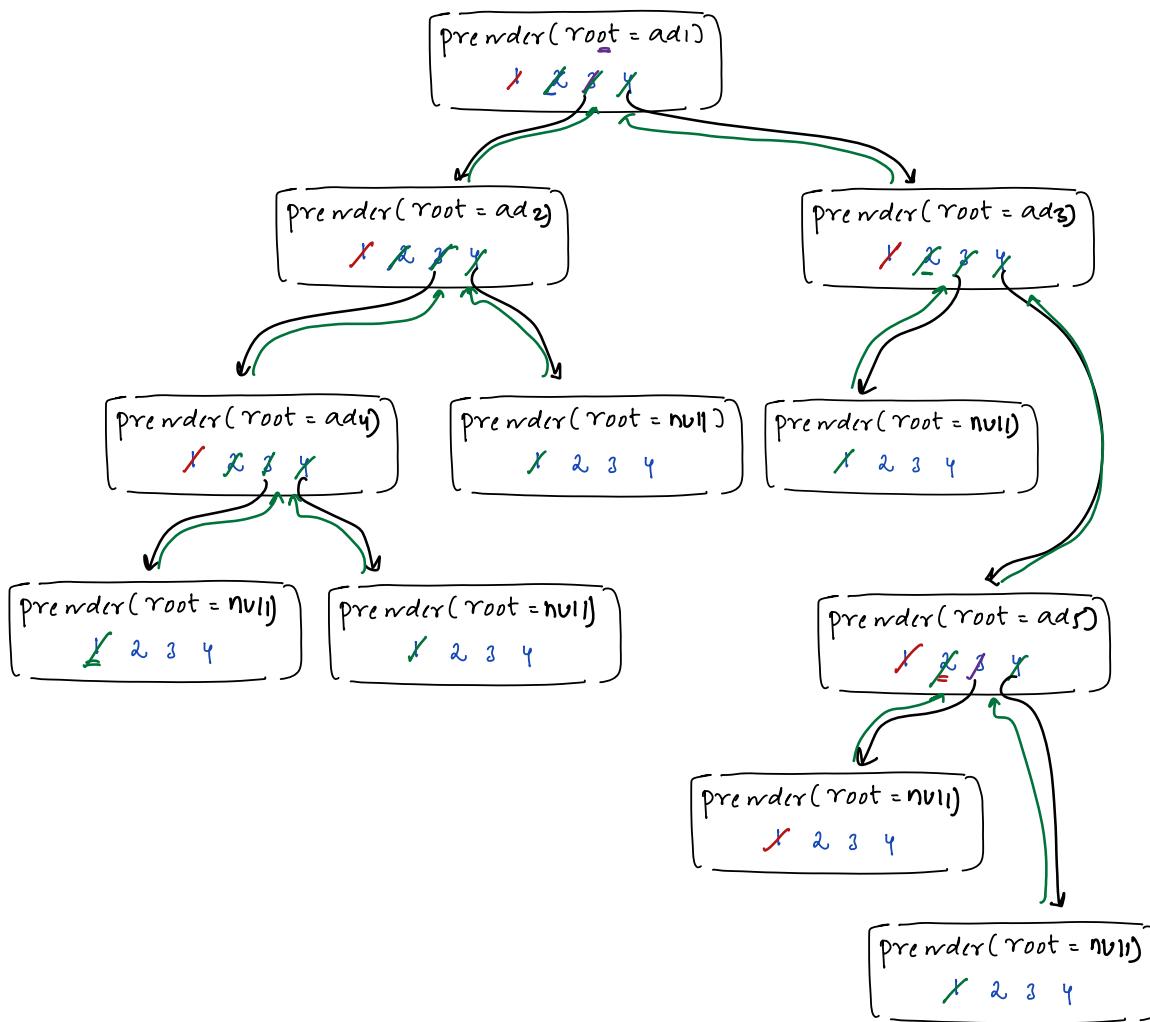
Tracing:



```

void preOrder(Node r) {
    1 if(r == null) {return}
    2 print(r.data)
    3 preOrder(r.left)
    4 preOrder(r.right)
}
    
```

output: 1 5 7 6 8



## Tree Problems:

// All below problems solve with recursion & no global variables

a)  $\text{Size}(\text{Node root})$  ✓

b)  $\text{Sum}(\text{Node root})$  ✓

c)  $\text{Height}(\text{Node root})$  ✓

d)  $\text{Fill depth}()$  TODO

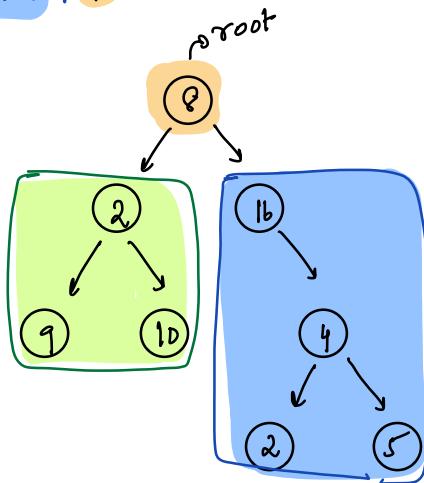
Ass: Given root node, return size of Tree

$$\text{Size}(\text{root}) = \underline{\text{Size of LST}} + \underline{\text{Size of RST}} + 1$$

```
int Size (Node root)
{
    if (root == null) { return 0 }

    int l = Size (root.left)
    int r = Size (root.right)

    return l + r + 1
}
```



Ass: Given root node, it will return sum of all nodes

$$\text{Sum}(\text{root}) = \underline{\text{sum of node LST}} + \underline{\text{sum of node RST}} + \underline{\text{root.data}}$$

```
int sum (Node root) {
    if (root == null) { return 0 }

    int ls = sum (root.left)
    int rs = sum (root.right)

    return ls + rs + root.data
}
```

$\xrightarrow{\leftarrow \rightarrow}$   
↳ value of root node

Ass: Given root node, it will height of tree

$$\text{height}(\text{root}) = 1 + \max(\underline{\text{height of LST}}, \underline{\text{height of RST}})$$

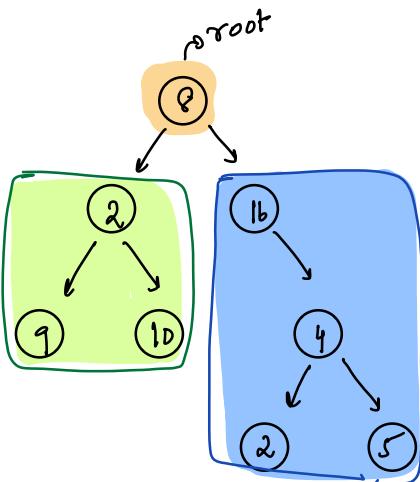
```
int height(root){
```

```
    if (root == null) { return -1; }
```

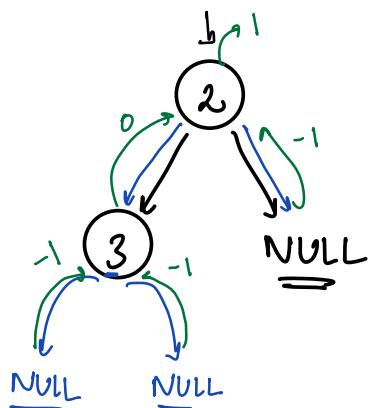
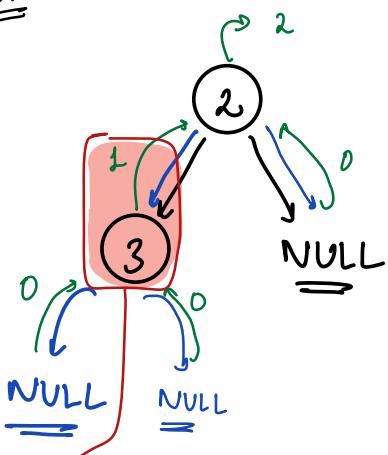
```
    int hl = height(root.left);
```

```
    int hr = height(root.right);
```

```
    return max(hl, hr) + 1;
```



Trace



Issue: Leaf node height = 0,  
it is returning 1

Note: In your assignment, length of path calculate based  
on no. of nodes