

Todays Content:

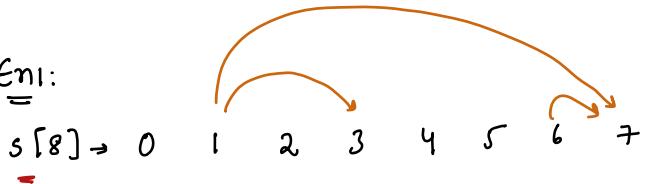
- Count pairs
- leaders in array
- Subarray basics → {concept}
- Smallest Subarray with Both min & max : {Asked in Interviews}

18) Count Pairs 'ag'

Given a char[], calculate no of pairs i, j such that

$i < j$ & $s[i] = 'a'$ & $s[j] = 'g'$ All characters are lowercase
 $\underline{a - g}$

Ex1:

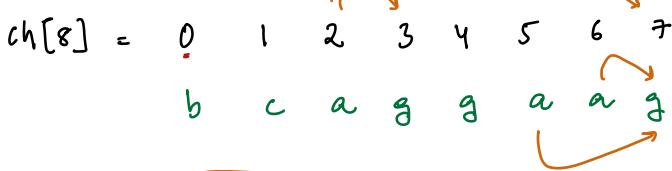


pairs: $\rightarrow 5$ pairs

$\langle 1,3 \rangle \ \langle 1,7 \rangle$

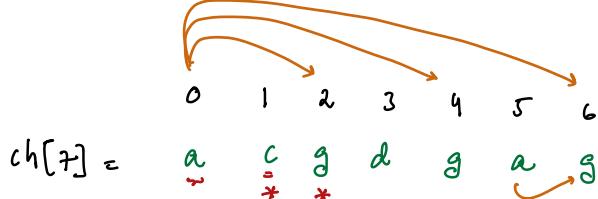
$\langle 2,3 \rangle \ \langle 2,7 \rangle \ \langle 6,7 \rangle$

$\boxed{\langle 3,6 \rangle : i > j \rightarrow \text{Not valid}}$



Pairs:

$\langle 2,3 \rangle \ \langle 2,4 \rangle \ \langle 2,7 \rangle$
 $\langle 5,7 \rangle \ \langle 6,7 \rangle$



Pairs: $\langle 0,2 \rangle \ \langle 0,4 \rangle \ \langle 0,6 \rangle$
 $\langle 5,6 \rangle$

Ideal: Check all pairs

$\xrightarrow{\text{optimization}}$

int pairs(char s[]){

int n = s.length, c = 0

i=0; $i < n$; $i = i + 1$ {

$j = i + 1$; $j < n$; $j = j + 1$ {

if ($s[i] == 'a'$

 && $s[j] == 'g'$) {

 c = c + 1

} return c; $TC \rightarrow O(N^2) \ SC \rightarrow O(1)$

int pairs(char s[]){

int n = s.length, c = 0

i=0; $i < n$; $i = i + 1$ {

if ($s[i] == 'a'$) {

$j = i + 1$; $j < n$; $j = j + 1$ {

if ($s[j] == 'g'$) {

 c = c + 1

} return c;

$TC: O(N^2) \ SC: O(1)$

Tracing

If $s[i] == 'a'$, q iterate in right side to get no. of g's

Ex2:

	0	1	2	3	4	5	6	7	8
$ch[9]$	a	d	g	a	g	a	g	f	g
$c=0$	✓								
		✓							
	*	*	✓						

$\Rightarrow C = C + 4$.

$\Rightarrow C = C + 3$.

$\Rightarrow C = C + 2$.

$\Rightarrow C = 9$

Iterate once from Rght - Left+1
get no. of g's for every a

Tracing

Ex3:

$ch[9]$:	0	1	2	3	4	5	6	7	8
	a	d	g	a	g	a	g	f	g
	$ans = ans + c$	$c = c + 1$	$ans = ans + c$	$c = c + 1$	$ans = ans + c$	$c = c + 1, c = 2$			
	$ans = 1$	$c = 4$	$ans = 5$	$c = 3$	$ans = 2$				
	$final ans$								

$c = 0$

$ans = 0$

Pseudocode: $\rightarrow T(n): O(n)$ $S(n): O(1)$

int Pairs (char s[]) {

int n = s.length;
int c = 0, ans = 0
i = n-1; i >= 0; i-- {

for every 'a'
calculate no. of
'g' on right side

if ($s[i] == 'g'$) { $c = c + 1$ }
else if ($s[i] == 'a'$) {
 ans = ans + c
}

}

return ans;

for every 'g' calculate no: of 'a' on left side

Iterate from left \rightarrow right \rightarrow TODO

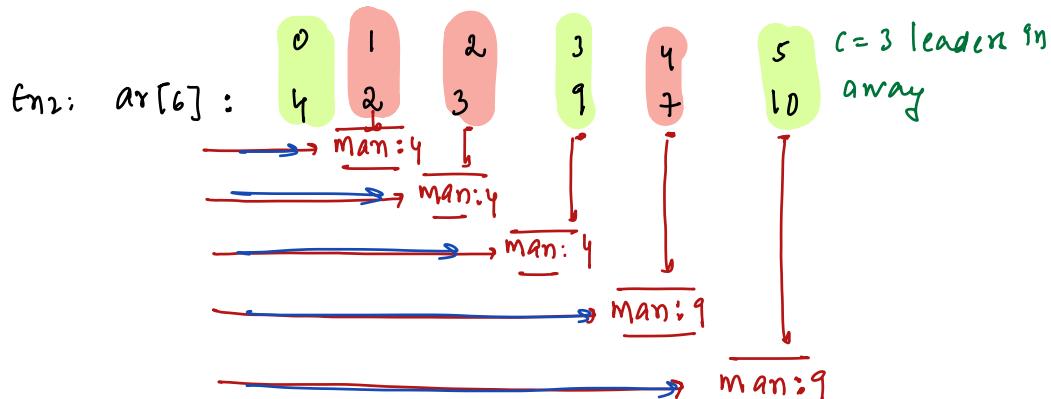
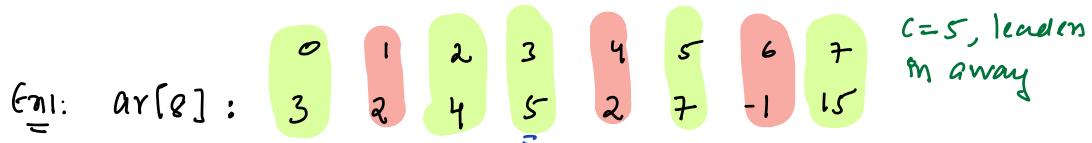
<u>En3:</u>	✓	*	✓	✓	✓	✓	✓	x	e
ch[1]:	0	1	2	3	4	5	6	7	8
c = 0	a	d	g	a	g	a	g	f	g
ans = 0	c = c + 1	ans = ans + c	c = c + 1	ans = ans + c	c = c + 1	ans = ans + c	c = c + 1	ans = ans + c	ans = ans + c
	c = 1	ans = 1	c = 2	ans = 2	c = 3	ans = 3	c = 4	ans = 4	ans = 5

2.8) Leaders in an Array

Given an $ar[N]$, you have to find leaders in $ar[]$

An ele is leader:

- if it is strictly greater than max of all elements in left side
- Note: $ar[0]$ is already considered as leader



Idea:

for every element $ar[i]$,
get max from of array
 $[0, i-1]$ & compare with $< ar[i]$

int leaders (int ar[]) {

```
int n = ar.length;
int c = 1;
for (int i = 1; i < N; i++) {
    // check  $ar[i]$  leader
    // iterate from  $[0, i-1]$ 
    // get max
    if (max < ar[i]) {
        c = c + 1
    }
}
return c;
```

TC: $O(N^2)$ SC: $O(1)$

$\underline{\text{Ex1: ar[8]:}}$	$\begin{array}{c cc} 0 & 1 & 2 \\ \hline 3 & 2 & 4 \end{array}$	$\begin{array}{c cc} 3 & 4 & 5 \\ \hline 2 & \text{man} \times \text{ar}[2] \end{array}$	$\begin{array}{c cc} 4 & 5 & 6 \\ \hline 2 & \text{man} \times \text{ar}[3] \end{array}$	$\begin{array}{c cc} 5 & 6 & 7 \\ \hline 2 & \text{man} \times \text{ar}[4] \end{array}$	$\begin{array}{c cc} 6 & 7 & -1 \\ \hline 2 & \text{man} \times \text{ar}[5] \end{array}$	$\begin{array}{c cc} 7 & -1 & 15 \\ \hline 2 & \text{man} \times \text{ar}[6] \end{array}$
	$C=1$ $\text{man} = 3$	$C=C+1 : 2$ $\text{man} = 4$	$C=C+1 : 3$ $\text{man} = 5$	$C=C+1 : 4$ $\text{man} = 7$	$C=C+1 : 5$ $\text{man} = 15$	

TODD \rightarrow TC: $O(N)$ SC: $O(1)$

8:33 pm

Put leaders (Pnt ar[]) {

```

int n = ar.length;
int c = 1;
Pnt m = ar[0];
i = 1; i < N; i++) {
    // ar[i] is leader
    if (ar[i] > m) {
        c = c + 1;
        m = ar[i];
    }
}
return c;
    
```

TC: $O(N)$ SC: $O(1)$

Subarray: Continuous part of an array is called Subarray

- Complete array is also Subarray
- Single element is also Subarray
- [] is not considered as Subarray

0 1 2 3 4 5 6 7 8 9

Ex: arr[10]: 2 4 3 7 9 6 8 7 9 2
 $[2-4] + [6-7] + [9-9]$

Is Subarray?

$[2-5]$: Yes

$[1-4], [6-8]$: No

$[7-9]$: Yes

$[1-1]$: Yes

$[6-9]$: Yes

$[2-4] + [6-7] + [9-9]$: No

length of Subarray: How many elements in Subarray

$$[\underline{\overset{i}{3} \underset{j}{7}}] \Rightarrow \underline{3 \ 4 \ 5 \ 6 \ 7} \Rightarrow 5 = 7-3+1 = 5$$

$$[\underline{\overset{i}{2} \underset{j}{4}}] \Rightarrow \underline{2 \ 3 \ 4} \Rightarrow 3 = 4-2+1 = 3$$

$$[\underline{\overset{i}{5} \underset{j}{8}}] \Rightarrow \underline{5 \ 6 \ 7 \ 8 \ 9} \Rightarrow 4 = 8-5+1 = 4$$

$$[\overset{i}{\underline{1}} \underset{j}{\underline{2}}] \Rightarrow [\underline{j-i+1}]$$

Start index
of subarray
and index
of subarray

3Q) Closest Min Max

Given N array elements, find length of Smallest Subarray which contains Both Min & Max of array

$$\text{Ex1: } \text{arr}[10] : \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 \end{matrix} \left. \begin{matrix} \min = 1 \\ \max = 9 \end{matrix} \right\}$$

1 3 4 6

Subarray: len } ans=4

$$\left. \begin{matrix} [s \ e] : e-s+1 \\ [3 \ 6] : 6-3+1 = 4 \end{matrix} \right\}$$

$$\text{Ex2: } \text{arr}[10] : \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \end{matrix} \left. \begin{matrix} \min = 1 \\ \max = 10 \end{matrix} \right\}$$

6 4 1

Subarray: len } ans=3

$$\left. \begin{matrix} [s \ e] : e-s+1 \\ [5 \ 8] : 8-5+1 = 4 \\ [8 \ 10] : 10-8+1 = 3 \end{matrix} \right\}$$

$$\text{Ex3: } \text{arr}[5] : \begin{matrix} 0 & 1 & 2 & 3 & 4 \end{matrix} \left. \begin{matrix} \min = 0 \\ \max = 4 \end{matrix} \right\}$$

8 8 8 8

[s e] : e-s+1 } ans=1

$$\left. \begin{matrix} 0-0 : 0-0+1 = 1 \\ 2-2 : 2-2+1 = 1 \end{matrix} \right\}$$

observations:

→ Min & Man should be present in corners in final ans subarray

Min ... Man

... Man ... Min ...

↳ Case-I: Min Man : if ar[i] == Min:
get nearest man ind m
right side

Case-II: Man Min : if ar[i] == Man:
get nearest min ind
m right side

Ex:

ary[13] ans = N = 13 min = 1 man = 6

0	1	2	3	4	5	6	7	8	9	10	11	12
2	2	6	4	5	1	5	2	6	4	1	3	4
*	*	*	*	*	↑↑	*	*	↑↑	*	↑↑	*	*

$$\text{len} = [2, 5] = 4 \quad \text{len} = [5, 8] = 4 \quad \text{len} = [8, 10] = 3 \Rightarrow \underline{\underline{\text{ans} = 3}}$$

```
int smallLength(int ar[]){  $\rightarrow$  TC:  $O(N + N^2)$  SC:  $O(1)$ 
```

```
    int man = (man of arr[])  $\Rightarrow$  O(N)  $\rightarrow$  TC:  $O(N^2)$  O(1)  
    int min = (min of arr[])
```

```
    if (man == min) { return 1 }
```

```
    int n = ar.length;
```

```
    int ans = n
```

```
    for (int i = 0; i < N; i++) {  $\rightarrow$  O(N)
```

```
        if (ar[i] == man) {
```

```
            // Search for nearest man and m right
```

```
            for (j = i+1; j < N; j++) {  $\rightarrow$  O(N)
```

```
                if (ar[j] == man) {
```

```
                    // [i, j] len = j - i + 1
```

```
                    if (len < ans) { ans = len }
```

```
                } break;
```

```
}
```

```
        else if (ar[i] == min) {
```

```
            // Search for nearest min and m right
```

```
            for (j = i+1; j < N; j++) {  $\rightarrow$  O(N)
```

```
                if (ar[j] == min) {
```

```
                    // [i, j] len = j - i + 1
```

```
                    if (len < ans) { ans = len }
```

```
                } break;
```

```
}
```

```
    return ans;
```

idea2: Iterate from Right to left & get nearest min_index
nearest man_index

// To indicate, yet to found ↪ ←
 $\underline{\text{ary[4]}}: \min = 1, \text{man} = 6, \underline{\text{ans}} = 4, \min_i = -1, \text{man}_i = -1$

0	1	2	3	4	5	6	7	8	9	10	11	12	13
1	6	4	6	5	1	5	2	6	4	4	2	1	5
$\min_i = 0$	$\text{man}_i = 1$	$\min_i = 3$	$\min_i = 5$	$\min_i = 5$	$\text{man}_i = 8$	$\text{man}_i = 8$	$\text{man}_i = 12$	$\text{man}_i = -1$					
$\text{man}_i = 1$	$\min_i = 5$	$\min_i = 5$	$\text{man}_i = 8$	$\text{man}_i = 8$	$\text{man}_i = 12$	$\text{len} = 5$	$\text{len} = 5$	$\text{len} = 5$					
$\text{len} = 2$	$\text{len} = 5$	$\text{len} = 3$	$\text{len} = 4$	$\text{len} = 4$	$\text{len} = 5$	$\text{ans} = 4$	$\text{ans} = 5$	$\text{ans} = 5$					
$\underline{\text{ans}} = 2$	$\text{ans} = 3$	$\text{ans} = 3$											

final ans

no nearest man in right, no update

```
int minLength( int arr[] ) { TC: O(N+N+N) = O(3N)
```

int n = arr.length
int ans = n
int man = {man of arr} int min = {min of arr}

$O(N) \xrightarrow{O(N)} [we can calculate min]$
 $\xleftarrow{man in same loop}$

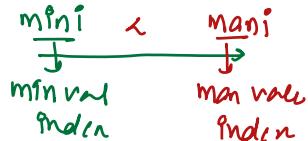
```
if (min == man) { return 1 }
```

```
int minP = -1; int manP = -1
```

```
for (i = N-1; i >= 0; i--) {
```

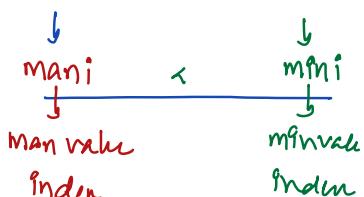
```
if (arr[i] == min) { // nearest min index on right
```

mini = i
if (manP != -1) {
 len = manP - mini + 1
}
if (len < ans) { ans = len }



```
} else if (arr[i] == man) { // nearest man index on right
```

manP = i
if (minP != -1) {
 len = minP - manP + 1
}
if (len < ans) { ans = len }



```
return ans;
```

TC: O(N) SC: O(1)

versim \Rightarrow II \Rightarrow TODO \Rightarrow left \Rightarrow right TC: $O(N)$ SC: $O(1)$

Case-I: Min Man : If $\underline{ar[i]} == \underline{\text{Man}}$:

get nearest min ind m
left side

Case-II: Man Min : If $\underline{ar[i]} == \underline{\text{Min}}$

get nearest man ind
m left side

Doubts :

$ar[]$:	0	1	2	3	4	5	6	7	8	9	10	11	12
$min = 2$	2	3	7		2	6		2	-1	2	3	4	5
$min_i = 0$	0	2	2	0	0	2	0	0	-1	2	3	4	5
$man = 2$	2	3	7	3	7	7	7	7	7	7	7	7	7
$mani = 0$	0	1	2	2	2	2	2	2	2	2	2	2	2

* If we get new man/min we update min & man by their index

0	1	2	3	4	5	6	7	8	9	10	11	12
2	2	6	4	5	1	5	2	6	4	1	3	4
*	*	*	*	*	↑↑	*	*	↑↑	*	↑↑	*	*

$\text{len} = [2, 5] = 4$ $\text{len} = [5, 8] = 4$ $\text{len} = [8, 10] = 3 \Rightarrow \underline{\text{ans}} = 3$