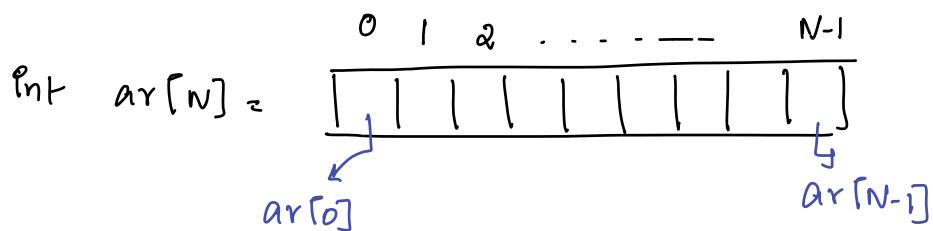
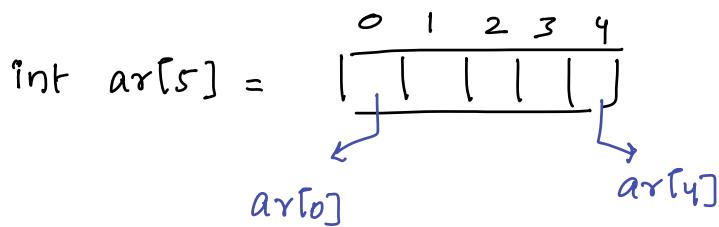


Today's Content

- Arrays
- Doubt → public chat
- Answer → private chat



ar[-1] or ar[N] or ar[N+1] ... Errr

Input Span ↗
void printArr(int ar[]) { ↗ We are passing array as parameter, in function

```
int n = ar.length  
for(int i=0; i < n; i++) {  
    print(ar[i])  
}
```

T_C: O(N)
S_C: O(1)

Q) Given N array elements, count no: of Elements, having all corr
1 element greater than itself

$$ar[7] = \{ -3, -2, 6, 8, 4, 8, 5 \} \# ans = 5$$

$$c = 0 \quad +1 \quad +1 \quad +1 \quad +1 \quad +1$$

$$ar[8] = \{ 2, 3, 10, 7, 3, 2, 10, 8 \} \# ans = 6$$

$$ar[10] = \{ 2, 5, 1, 4, 8, 0, 8, 1, 3, 8 \} \# ans = 7$$

$$ar[5] = \{ 8, 8, 8, 8, 8 \} \# ans = 0$$

Obs1: For man element we cannot have number greater than
itself

Obs2: Iterate & get no: of man elements = C

Final ans : (Total number of Elements) - (C)

Pseudocode:

```
int countgreater(int ar[]){  
    int am = ar[0];  
    int N = ar.length  
    for(int i=1; i< N; i++) {  
        if(am < ar[i]) {am = ar[i]};  
    }  
    int c = 0;  
    for(int i=0; i< N; i++) {  
        if(am == ar[i]) {c = c+1};  
    }  
    return N-c  
}
```

TODO: Try to solve above question by iterating on array

only 1 time

→ Next Session, doubt's session part we will discuss

Q8) Given N array elements, check if there exists a pair (i, j)

such that $\text{arr}[i] + \text{arr}[j] == k$ $\&$ $i \neq j$ boolean

Note: i & j are index value, k is given sum

$\left. \begin{array}{l} \text{Indices cannot} \\ \text{be same but} \\ \text{elements can} \\ \text{be same} \end{array} \right\}$

$\text{arr}[] :$

0	1	2	3	4	5	6
3	-2	1	4	3	6	8

$k = 10 :$

i	j
3	5

 $\Rightarrow \text{arr}[3] + \text{arr}[5] \rightarrow 10$: return True

$\text{arr}[] :$

0	1	2	3
2	4	-3	7

$k = 5$: No pair, return False

$\text{arr}[] :$

0	1	2	3
2	4	-3	7

$k = 8 :$

i	j
1	1

$1 + 1 \rightarrow \text{arr}[1] + \text{arr}[1] = 8$, wrong $i \neq j$

return False

$\text{arr}[] :$

0	1	2	3	4
3	5	2	7	3

$k = 6$

i	j
0	4

 $\rightarrow \text{arr}[0] + \text{arr}[4]$

$0 + 4 \rightarrow \text{arr}[0] + \text{arr}[4] \rightarrow 6 == \text{Return True}$

All ideas

1) All pairs $\rightarrow O(N^2)$

2) Optimized all pairs $\rightarrow O(N^2)$

3) Hashmap $\rightarrow O(N)$ future

4) Sorting + BS $\rightarrow O(N \log N)$

5) Sorting + 2 Pointers $\rightarrow O(N \log N)$

Idea1: $\rightarrow TC: O(N^2) \ SC: O(1)$

bool sum(int ar[], int k){

int N = ar.length;

i = 0; i < N; i++) {

j = 0; j < N; j++) {

if ($i \neq j$ &&

$ar[i] + ar[j] == k$) {

return True

} return False

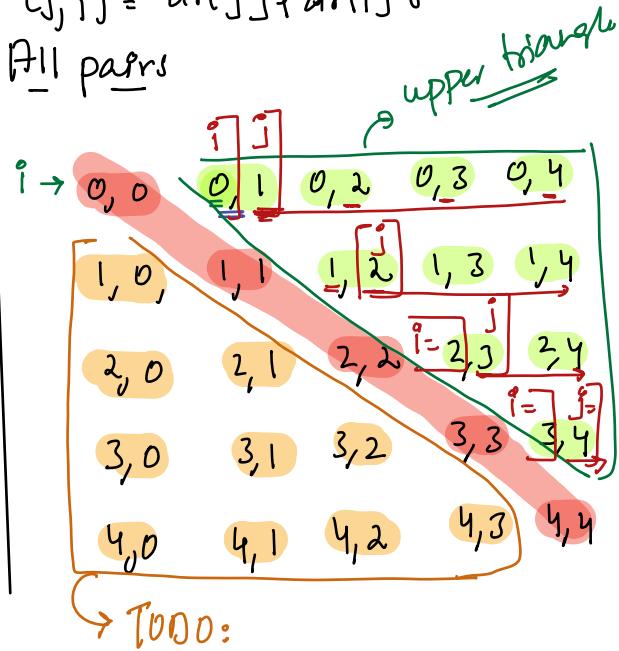
Idea: For every pair get sum == k

N=5 \rightarrow Index: {0, 1, 2, 3, 4}

$(i, j) = ar[i] + ar[j]$

$(j, i) = ar[j] + ar[i]$

All pairs



Idea2: $\rightarrow TC: O(N^2) \ SC: O(1) \rightarrow$ 2nd approach optimized approach

bool checksum(int ar[], k){

int N = ar.length

i = 0; i < N; i++) {

// last i = N-1, j = N, it won't go inside j loop
j = i+1; j < N; j++) {

if ($ar[i] + ar[j] == k$) {

return True

} return False

Calculate iterations

i	j: [i+1, N-1]	Total Iterations
0	[1, N-1]	N-1
1	[2, N-1]	N-2
2	[3, N-1]	N-3
3	[4, N-1]	N-4
:		
N-1	[N, N-1]	0

Total Iter = Sum of N-1 Natural numbers

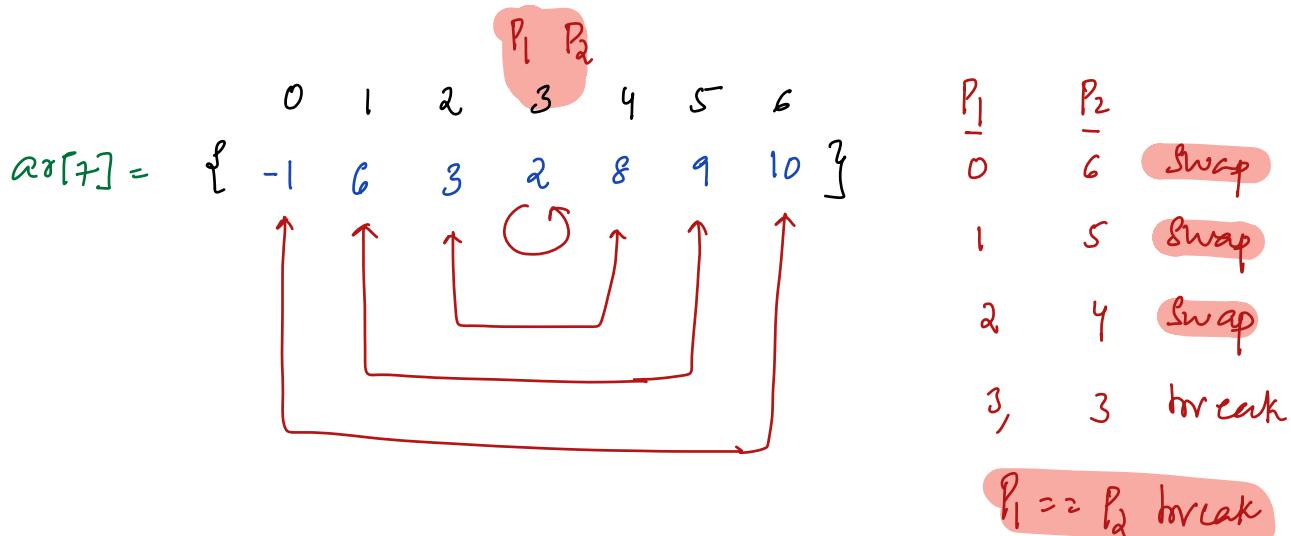
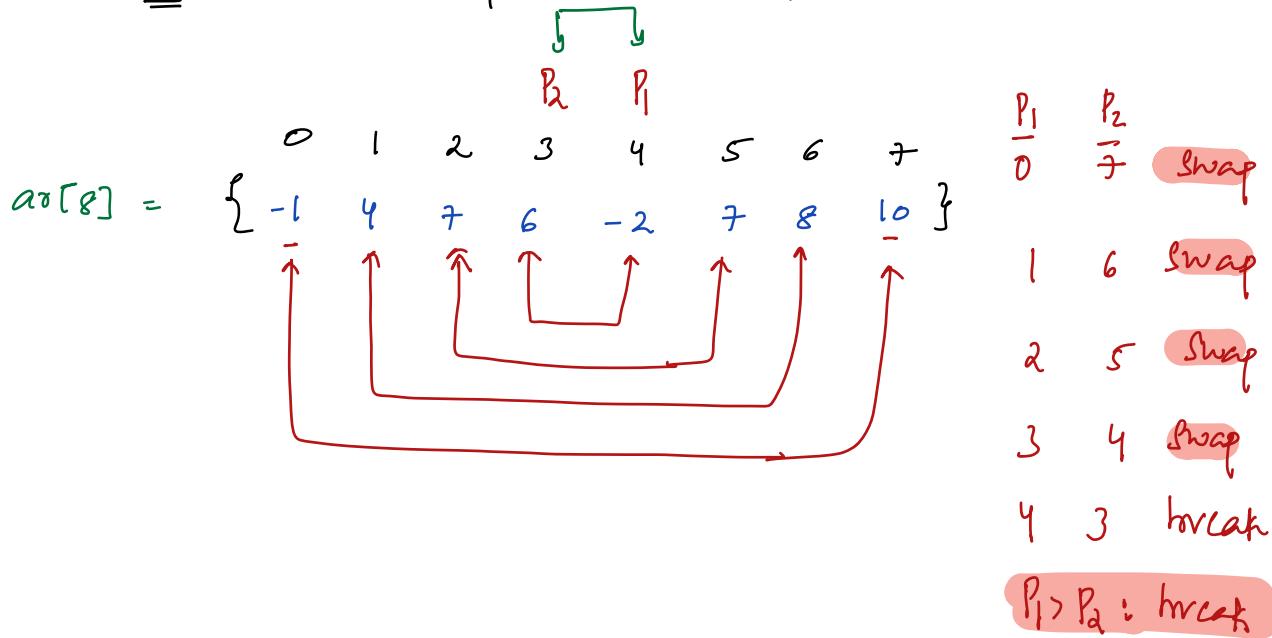
$$(N-1) + (N-2) + (N-3) + \dots + 2 + 1$$

$$S_N = \frac{(N)(N+1)}{2}$$

$$S_{N-1} = \frac{(N-1)(N)}{2}$$

Q8) Given an array, Reverse entire arr[]] Expected SC: O(1)

Note: arr[] itself should change



Breaking Condition

- $P_1 > P_2$ break]
 - $P_1 == P_2$ break]
- $\underline{P_1 >= P_2}$ break \leftrightarrow $P_1 \leq P_2$ continues the swapping process

void reverse (int ar[]){ Iterations: $N/2 \rightarrow O(N) \Rightarrow TC$

int $P_1 = 0, P_2 = ar.length - 1$

while ($P_1 < P_2$) {

 Swap $ar[P_1], ar[P_2]$

$P_1++ ; P_2--$

SC: $\rightarrow O(1)$ Independent of input size

↳ Constant Space

$\left[\begin{array}{l} \text{int temp} = ar[P_1] \\ ar[P_1] = ar[P_2] \\ ar[P_2] = temp \end{array} \right]$

TODD

}

Q8) Given N array element a_i $[S_i \ a_i \ e_i]$ $\xrightarrow{\text{start index}}$ $\xrightarrow{\text{end index}}$
 reverse array from $[S_i \ e_i]$ Note $S_i \leq e_i$ $\&$ index will range

$$ar[] = \{ -3 \ 4 \ 2 \ 8 \ 7 \ 9 \ 6 \ 2 \ 10 \}$$

$S_i \ e_i$

$[S_i \ e_i]$

$$ar[] = \{ -3 \ 4 \ 2 \ 2 \ 6 \ 9 \ 7 \ 8 \ 10 \}$$

void reverse part (int ar[], int $s = S_i$, int $e = e_i$) { $\xrightarrow{\text{start index}}$ $\xrightarrow{\text{end index}}$

int $P_1 = s$, $P_2 = e$ \longrightarrow $Tc: O(N)$

while ($P_1 < P_2$) { $\xrightarrow{\text{Sc: } O(1)}$

swap ($ar[P_1]$, $ar[P_2]$)

P_1++ , P_2--

}

TODO: Using for loop —

{ How to do it using for loop, stay back & discuss with my

SQ8) Given N array elements, Rotate array from last to first

by k times SC: O(1), $k \geq 0 \Rightarrow$ {good/avg/m}

$k=3$ 0 1 2 3 4 5 6
ar[7] = [3 -2 1 4 6 9 8]
 $k=1$: 8 3 -2 1 4 6 9
 $k=2$: 9 8 3 -2 1 4 6
→ $k=3$: 6 9 8 3 -2 1 4

$k=4$ 0 1 2 3 4 5 6 7 8
ar[9] = [4 1 6 9 2 14 7 8 3]
 $k=1$: 3 4 1 6 9 2 14 7 8
 $k=2$: 8 3 4 1 6 9 2 14 7
 $k=3$: 7 8 3 4 1 6 9 2 14
→ $k=4$: 14 7 8 3 4 1 6 9 2

Q2)

$k=3$ 0 1 2 3 4 5 6 7 8 9

$arr[10] = \boxed{-2 \quad 3 \quad 1 \quad 4 \quad 6 \quad 2 \quad 8 \quad 7 \quad 9 \quad 3}$

$k=1$ 3 -2 3 1 4 6 2 8 7 9

$k=2$ 9 3 -2 3 1 4 6 2 8 7

$\rightarrow k=3$ 7 9 3 $\boxed{-2 \quad 3 \quad 1 \quad 4 \quad 6 \quad 2 \quad 8}$

$k=5$

$arr[13] : \boxed{a_0 \quad a_1 \quad a_2 \quad a_3 \quad a_4 \quad a_5 \quad a_6 \quad a_7 \quad a_8 \quad a_9 \quad a_{10} \quad a_{11} \quad a_{12}}$



reverse : $\underbrace{a_{12} \quad a_{11} \quad a_{10} \quad a_9 \quad a_8}_{\text{reverse first 5 Elements}} \quad \underbrace{a_7 \quad a_6 \quad a_5 \quad a_4 \quad a_3 \quad a_2 \quad a_1 \quad a_0}_{\text{reverse last 8 elements}}$



$\boxed{a_8 \quad a_9 \quad a_{10} \quad a_{11} \quad a_{12}}$

$\boxed{a_0 \quad a_1 \quad a_2 \quad a_3 \quad a_4 \quad a_5 \quad a_6 \quad a_7}$

After rotate : $\boxed{a_8 \quad a_9 \quad a_{10} \quad a_{11} \quad a_{12}}$ $\boxed{a_0 \quad a_1 \quad a_2 \quad a_3 \quad a_4 \quad a_5 \quad a_6 \quad a_7}$

Idea :

Step1 : Reverse entire array $\rightarrow \text{reverse part}(arr, 0, N-1)$

Step2 : Reverse first k elements $\rightarrow \text{reverse part}(arr, 0, k-1)$

Step3 : Reverse last $N-k$ Elements $\rightarrow \text{reverse part}(arr, k, N-1)$

Vorlesung

rotate times (int ar[], int k) {

Code Worst Case

int N = ar.length;

// Reverse entire array

reverse part (ar, 0, N-1)

// Reverse first k Elements

reverse part (ar, 0, k-1)

// Reverse last N-k Elements

reverse part (ar, k, N-1)

Iterations

Total Iterations

$$\frac{N}{2} + \frac{k}{2} + \frac{N-k}{2}$$

$$\Rightarrow \frac{N}{2} + \frac{k}{2} + \frac{N-k}{2}$$

N Iterations

TC $\Rightarrow \Theta(N)$

SC $\Rightarrow \Theta(1)$

}

Idea: $\underbrace{\text{rotate end}}_{N=6} \rightarrow \text{rotate end to start by 8 times}$
 $\underbrace{k=8}$

reverse part (ar, 0, N-1) : reverse part (ar, 0, 5)

reverse part (ar, 0, k-1) : reverse part (ar, 0, 7)

reverse part (ar, k, N-1)

Err: index out of bounds

$ar[6] = a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5$							
$k=0 \Rightarrow a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5$	0	$\Rightarrow 6 \Rightarrow 12$	18				
$k=1 \Rightarrow a_5 \ a_0 \ a_1 \ a_2 \ a_3 \ a_4$	1	$\Rightarrow 7 \Rightarrow 13$	19				
$k=2 \Rightarrow a_4 \ a_5 \ a_0 \ a_1 \ a_2 \ a_3$	2	$\Rightarrow 8 \Rightarrow 14$	20				
$k=3 \Rightarrow a_3 \ a_4 \ a_5 \ a_0 \ a_1 \ a_2$	3	$\Rightarrow 9 \Rightarrow 15$	21				
$k=4 \Rightarrow a_2 \ a_3 \ a_4 \ a_5 \ a_0 \ a_1$	4	$\Rightarrow 10 \Rightarrow 16$					34
$k=5 \Rightarrow a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_0$	5	$\Rightarrow 11 \Rightarrow 17$					
$k=6 \Rightarrow a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5$							

Rotate k times
k rotating factor = $k \% N$ length of array
In general $\Rightarrow k \% N$

void rotateTimes (int ar[], int k) { Correct code

int N = ar.length;

$k = k \% N$ —————>

$\% \Rightarrow$ remainder

reversePart(ar, 0, N-1)

$/ \Rightarrow$ Quotient

reversePart(ar, 0, k-1)

$2 / 6 \Rightarrow 0, 2 \% 6 \Rightarrow 2$

reversePart(ar, k, N-1)

$4 \% 6 \Rightarrow 4$

$4 \% 10 \Rightarrow 4$

Doubts:

```
void reverse1(int arr[]) {  
    int P1 = 0, P2 = arr.length - 1  
    while (P1 < P2) {  
        Swap arr[P1], arr[P2]  
        P1++; P2--  
    }  
}
```

```
void reverse2(int arr[]) {  
    int P1 = 0, P2 = arr.length - 1  
    for ( ; P1 < P2; P1++, P2--) {  
        Swap arr[P1], arr[P2]  
    }  
}
```

```
void reverse3(int arr[]) {  
    int N = arr.length  
    i = 0; i < N; i++) {  
        j = N; j > 0; j-- {  
              
        }  
    }  
}
```

$$a\sigma[6] = a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5 \quad k = k \% N$$

$$k=0 \Rightarrow a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5$$

$$k=1 \Rightarrow a_5 \ a_0 \ a_1 \ a_2 \ a_3 \ a_4$$

$$k=2 \Rightarrow a_4 \ a_5 \ a_0 \ a_1 \ a_2 \ a_3$$

$$k=3 \Rightarrow a_3 \ a_4 \ a_5 \ a_0 \ a_1 \ a_2$$

$$k=4 \Rightarrow a_2 \ a_3 \ a_4 \ a_5 \ a_0 \ a_1$$

$$k=5 \Rightarrow a_1 \ a_2 \ a_3 \ a_4 \ a_5 \ a_0$$

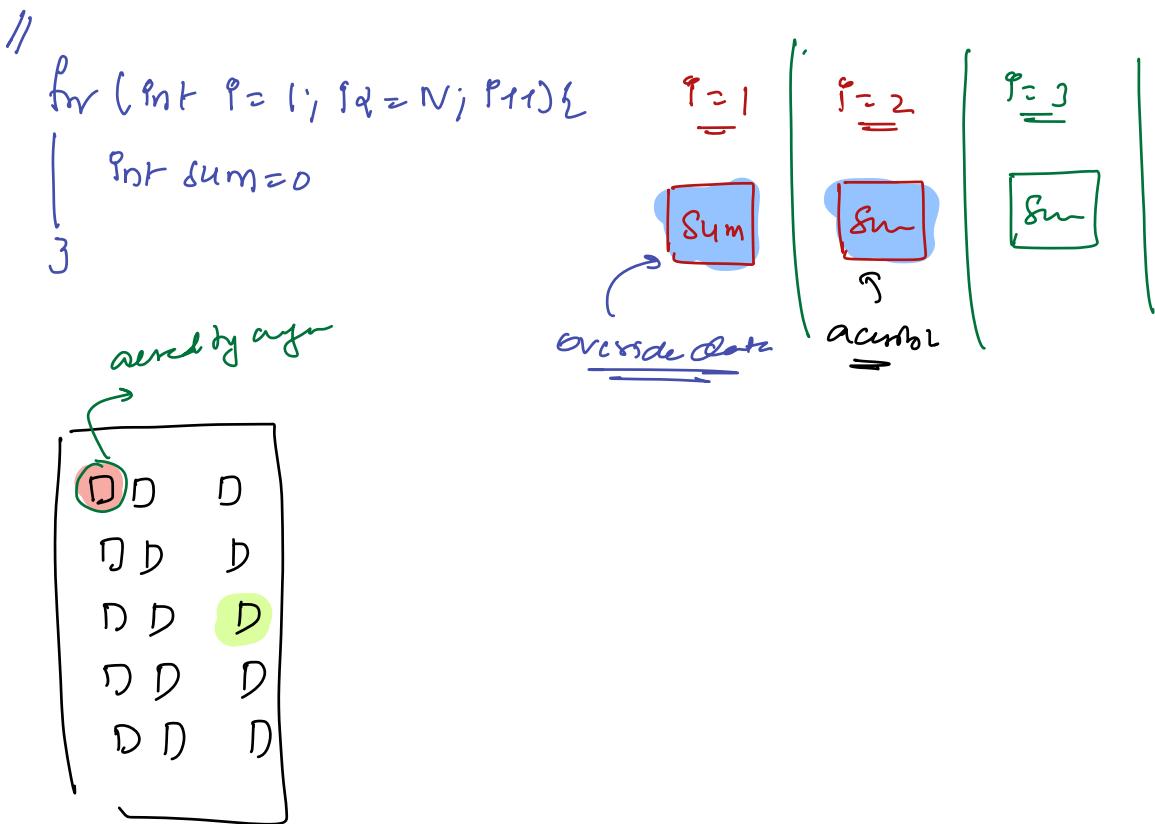
$$k=6 \Rightarrow a_0 \ a_1 \ a_2 \ a_3 \ a_4 \ a_5$$

0	6 = 0	12 = 0	18 = 0
1	7 = 1	13 = 1	19 = 1
2	8 = 2	14 = 2	20 = 2
3	9 = 3	15 = 3	21 = 3
4	10 = 4	16 = 4	22 = 4
5	11 = 5	17 = 5	23 = 5

Before solving

- 1) Read Nodes
- 2) Get all conceptual doubts clear
- 3) Solve assignments
- 4) Solve homework \rightarrow 40

$\left. \begin{array}{l} \rightarrow TA \rightarrow \text{Parking for Henry} \\ \rightarrow ask batch mates \rightarrow \text{f tiny} \\ \rightarrow f in Doubts Session tiny \end{array} \right\}$



$$i=3; i_{\leq} = N; i = p_{t3} \rightarrow N/3$$

$$i=1; i_{\leq} = N; i = p_{t3} \rightarrow N/3$$

$$i=2; i_{\leq} = N; i = p_{t2} \rightarrow N/2$$

$$i=N; i_{>} = 1; i = i_{\frac{N}{2}} \rightarrow \log_2^N$$

$$i=N; i_{>} = 1; i = i_{\frac{N}{3}} \rightarrow \log_3^N$$