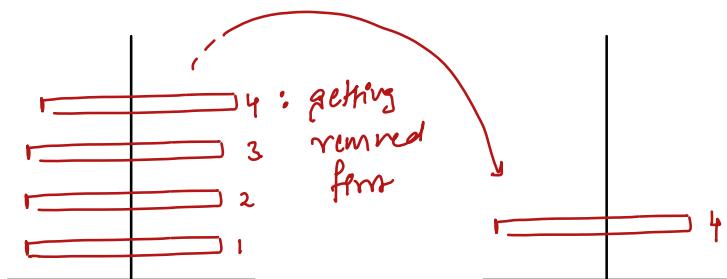


Todays Content

- Stacks Intro & Implementation
- Queues Intro & Implementation

Stacks: Properly followed FILO / LIFO → last in first out
 ↳ first in last out



Stacks : (Real World Use Cases)

- Storing function calls
- Expression Evaluation
 $\text{Infix} \longrightarrow \text{Postfix} \rightarrow \text{Evaluate Postfix Expressions}$
- Undo/Redo
- $[\leftarrow, \rightarrow]$ previous in browser

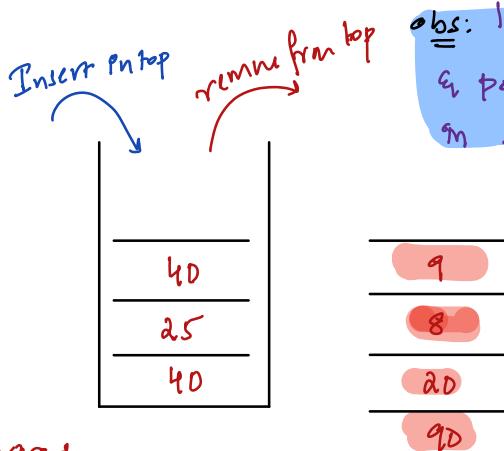
Operations allowed by Stack

TC for each operation in a Stack takes $O(1)$

- push(x):
- pop(): // we delete element at top
- top() / peek(): // Return top element
- size(): // Elements present in stack
- isEmpty(): // Check if stack empty or not

Ex: Operations

- ✓ push(40)
- ✓ push(20)
- ✓ push(8)
- ✓ push(9)
- ✓ pop(): 9 is removed
- ✓ top(): return 8
- ✓ pop(): 8 is removed
- ✓ pop(): 20 is removed
- ✓ top(): 40
- ✓ push(25)
- ✓ push(10)
- ✓ push(90)
- ✓ pop(): 90 is removed
- ✓ top(): return 40



obs: In stack push & pop are performed in same space

obs: When stack is empty &, if we perform pop() / top() we should get error.

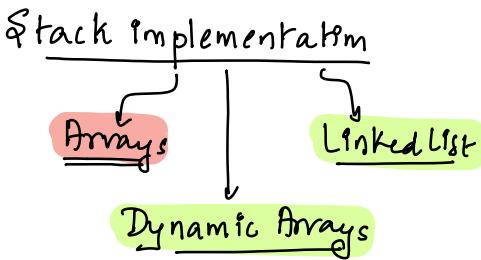
If it is known as underflow

Let stack using array []

ar[5]: [30 | 40 | 50 | 60 | 70 |]

push(30) ✓
push(40) ✓
push(50) ✓
push(60) ✓
push(70) ✓
push(80) ✓

Overflow in stack
Since we don't have any space to insert new element



Using Dynamic Arrays:

	0	1	2	3
list[int > l]	30	40	50	60

operations: push(30) push(40) push(50) push(60) top() pop(): pop()

```

void push(n) {
    l.insert(n)
}

int top() {
    if (l.size() == 0) {
        // underflow
        raise error/exception
    }
    last element in list
    int n = l.size()
    return l[n-1]
}

```

```
void pop() {
    if (lsize == 0) {
        // underflow
        raise error/Enqueue
    }
}
```

If we need to remove last index element in list
to remove (list.pop(-1))

```
int sqzcc()  
|  
| return 1-sqzcc()  
3
```

```
bool IsEmpty() {  
    return l.size == 0; }
```

Stacks Using Linked list

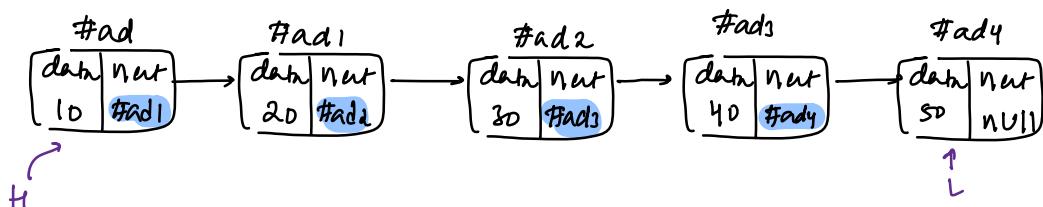
```

class Node{
    int data;
    Node next; // object reference, can hold address of Node object
    Node(int n){ // Constructor, used to initialize attributes at
        data=n;                                time of creating object itself
        next=NULL;
    }
}

```

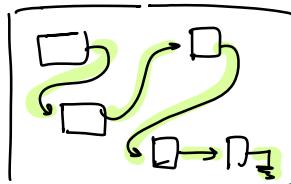
Operations:

push(10), push(20), push(30), push(40), push(50), pop(), pop()



Issue: After deleting last node, we cannot update
L, ref to prev node,

Operations in linked list



Insert at back : $O(1)$

Insert at start : $O(1)$

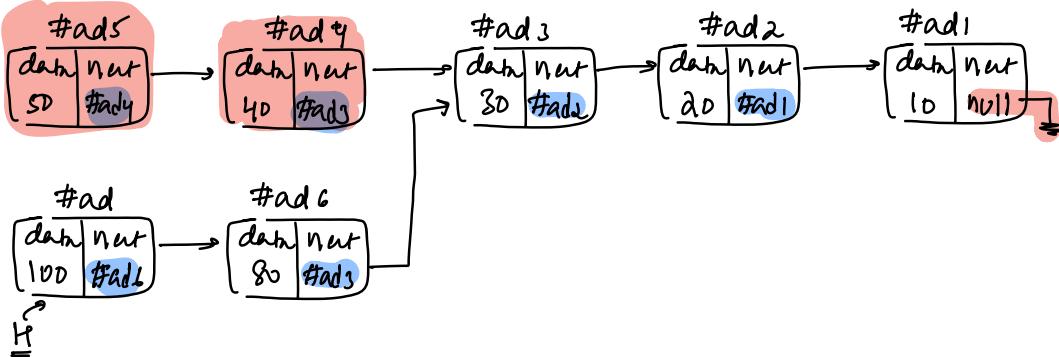
Delete at back : $O(N)$

Delete at start : $O(1)$

} follow these two, & perform
stack operations

operations:

push(10) push(20) push(30) push(40) push(50) **pop()** **pop()** **push(80)** push(100)
 ↓ ↓ ↓ ↓ ↓ **50** **40** ↓



```

class Node {
    int data;
    Node next;
    Node(int n) {
        data = n;
        next = NULL;
    }
}
  
```

```

Node *h = NULL // global variable
int s = 0

void Push(int a){ Tc: O(1) }
{
    Node n = new Node(a);
    n.next = h;
    h = n;
    s = s + 1 // size increased by 1
}
  
```

```

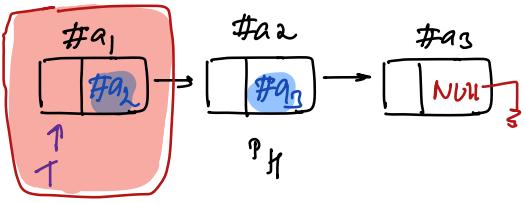
int top(){
    if(h == NULL){
        // underflow
        raise err/Exception
    }
    return h.data
}
  
```

```

bool isEmpty(){
    return h == NULL
}
  
```

```

int size(){
    return s
}
  
```



Void pop()

```
if ( t == NULL) {
    // underflow
    raise err/exception
}
```

Node t = h

h = t.next

[deallocate(t) / destructor(t) / free(t)]

(Check this in your language
of choice, function n
is it done automatically)

↳ // delete node object referred by object reference t

s = s - 1; // reducing size by 1

Predefined Stack Library // Check this library in your language
of choice //

Pseudo Code:

Stack < int> st // stack, each each is int

st.push(n)

st.pop()

st.top()

st.size()

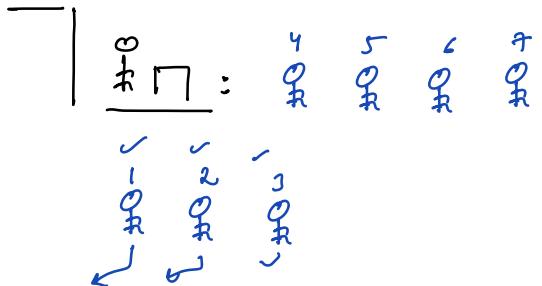
st.isEmpty()

Tc of each operation is O(1)

Quesn: Follow FIFO property or LIFO property

↓

→ first in first out → last in last out



Properties:

enque(n): We insert at rear end

`dequeue()`: We delete front element

`front()`: // first element

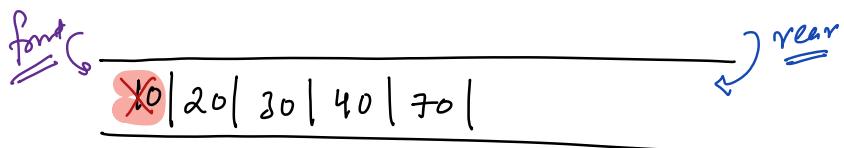
`rear() : // Element just entered queue`

SigCC:

IsEmpty():

Ex 1:

en(10) en(20) en(30) en(40) dec₁₀ for(10) en(70) rec₇₀ for(20)



Implementation of Queue:

Arrays

Linked List

Dynamic arrays

TODO

insert back(): O(1)

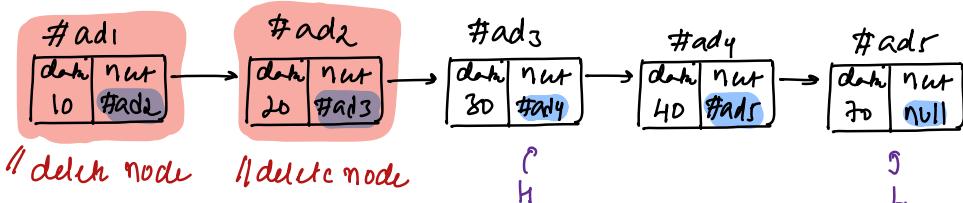
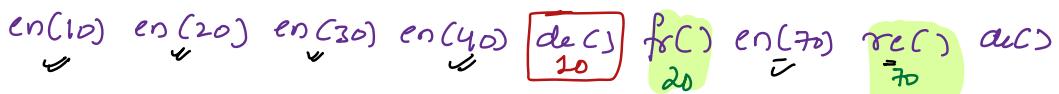
delete front(): O(1)

{ insert at back(): O(1)

delete at start(): O(N)

Note: deleting takes a lot of time

linkedlist:



```
class Node{
    int data;
    Node next;
    Node(int n){
        data = n;
        next = NULL;
    }
}
Node t = null;
Node L = null;
Pnt s = 0;
```

```
void enqueue(int a){
    Node n = new Node(a);
    if(t == NULL){ // 1st node
        t = n, L = n;
    } else {
        L.next = n; // insert at back
        L = n; // update L reference
    }
    s = s + 1; // increase size
}
```

```

int front() {
    // first element
    if (h == NULL) {
        // underflow
        raise err/Exception
    }
    return h->data
}

```

```

int rear() {
    // first element
    if (h == NULL) {
        // underflow
        raise err/Exception
    }
    return l->data
}

```

```

bool isEmpty() {
    return h == NULL
}

```

```

void deque() {
    if (h == NULL) {
        // underflow
        raise err/Exception
    }
    Node t = h
    h = h->next
    free(t)
    s = s - 1; // reducing size by 1
}

int size() {
    return s;
}

```

Inbuilt Library Queue // Please check in your language

Pseudocode :

→ each element is of int

```

queue<int> q;
q.enqueue() // Insert at rear end
q.dequeue() // delete at front end
q.front() // Element at front
q.rear() // Element recently inserted
q.size() // Elements in queue

```