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        "import pandas as pd\n",
        "import matplotlib.pyplot as plt\n",
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        "# roc curve and auc score\n",
        "from sklearn.datasets import make_classification"
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  "from sklearn.ensemble import RandomForestClassifier\n",
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  "rf_model.fit(X_train, y_train)\n",
  "ytrain_pred = rf_model.predict_proba(X_train)\n",
  "print('RF train roc-auc: {}'.format(roc_auc_score(y_train,
ytrain_pred[:,1])))\n",
  "ytest_pred = rf_model.predict_proba(X_test)\n",
  "print('RF test roc-auc: {}'.format(roc_auc_score(y_test,
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    "ytrain_pred = log_classifier.predict_proba(X_train)\n",
    "print('Logistic train roc-auc: {}'.format(roc_auc_score(y_train,\n",
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    "ytest_pred = log_classifier.predict_proba(X_test)\n",
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        "print('Adaboost train roc-auc: {}'.format(roc_auc_score(y_train,\n",
ytrain_pred[:,1])))\n",
        "ytest_pred = ada_classifier.predict_proba(X_test)\n",
        "print('Adaboost test roc-auc: {}'.format(roc_auc_score(y_test,\n",
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        "ytrain_pred = knn_classifier.predict_proba(X_train)\n",
        "print('Adaboost train roc-auc: {}'.format(roc_auc_score(y_train,\n",
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        "ytest_pred = knn_classifier.predict_proba(X_test)\n",
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"    pred.append(pd.Series(model.predict_proba(X_test)[: ,1]))\n",
"    final_prediction=pd.concat(pred,axis=1).mean(axis=1)\n",
"    print('Ensemble test roc-auc:
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    "    accuracy_ls.append(accuracy_score(y_test, y_pred,\nnormalize=True))\n",
    "    \n",
    "accuracy_ls = pd.concat([pd.Series(thresholds),\npd.Series(accuracy_ls)],\n",
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    "accuracy_ls.columns = ['thresholds', 'accuracy']\n",
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