

QMM Assignment 1

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Question 1

a.

Decision variables

The choice variables in this problem are two distinct bag models. They are Mini and Collegiate. We'll refer to them as follows.

$$\text{Collegiatebag} = X_a$$

$$\text{Minibag} = X_b$$

b.

objective function

A profit of 32dollar is made from each Collegiate bag, and a profit of 24dollar from each Mini backpack.

$$\text{Maximize(Profit)} Z = 32X_a + 24X_b$$

c.

Constraints

In this problem, we have two different kinds of constraints. They're

Labor constraints:

$$45X_a + 40X_b \leq (35)(40)(60)$$

It takes 45 minutes to labor each Collegiate and 40 minutes to labor each Mini.

Material constraint:

$$3X_a + 2X_b \leq 5000$$

Three square feet are used by each Collegiate and two square feet by each Mini.

Non negativity :

$$X_a, X_b \geq 0$$

$$X_a \leq 1000$$

$$X_b \leq 1200$$

d.

Full mathematical formulation

$$\begin{aligned} \text{Max } Z &= 32X_a + 24X_b \\ 45X_a + 40X_b &\leq (35)(40)(60) \end{aligned}$$

$$3X_a + 2X_b \leq 5000$$

$$X_a, X_b \geq 0$$

$$X_a \leq 1000$$

$$X_b \leq 1200$$

Question 2:

a. Decision variables

L_n = number of large shirts produced in nth plant

M_n = number of medium shirts produced in nth plant

S_n = number of small shirts produced in nth plant

where $n=1,2,3$.

b. LP Model

objective function :

$$\text{Maximize } Z = 420(L_1 + L_2 + L_3) + 360(M_1 + M_2 + M_3) + 300(S_1 + S_2 + S_3)$$

Constraints

capacity constraint:

$$L_1 + M_1 + S_1 \leq 750$$

$$l_2 + M_2 + S_2 \leq 900$$

$$L_3 + M_3 + S_3 \leq 450$$

storage constraints:

$$20L_1 + 15M_1 + 12S_1 \leq 13000$$

$$20L_2 + 15M_2 + 12S_2 \leq 12000$$

$$20L_3 + 15M_3 + 12S_3 \leq 5000$$

sales constraint:

$$L_1 + L_2 + L_3 \leq 900$$

$$M_1 + M_2 + M_3 \leq 1200$$

$$S_1 + S_2 + S_3 \leq 750$$

constraints to avoid lay off's

$$(L_1 + M_1 + S_1) * (100/750) = (L_2 + M_2 + S_2) * (100/900) = (L_3 + M_3 + S_3) * (100/450)$$

Non negativity :

$$L_1, L_2, L_3 \geq 0$$

$$M_1, M_2, M_3 \geq 0$$

$$S_1, S_2, S_3 \geq 0$$