

TIME SERIES ANALYSIS

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Background

Time series is a sequence of discrete-time data (Wikimedia Foundation, 2020). Time series is useful to analyze how a given variable changes over time. Now, we will perform time series analysis of temperature and precipitation data of two cities.

Data Source

There are two datasets used in this analysis:

- 1.) Average temperature by month of Welland from January 1985 to December 1994.
- 2.) Total precipitation in Waterloo for the years 1970 to 1995.

This report is divided into two main sections, section 1 and section 2. In section 1 we analyze Welland's temperature data and in section 2 we analyze Waterloo's rainfall data.

Section 1: Welland Temperature

1. Data Transformation and Cleaning (Description)

Dates

The dates column was removed since we only need temperature data to perform time series analysis.

Temperature

The monthly temperature data was converted to time series data using function `ts()`.

	Jan	Feb	Mar	Apr	May	Jun
1985	-6.616129	-4.328571	1.367742	8.926667	14.151613	16.450000

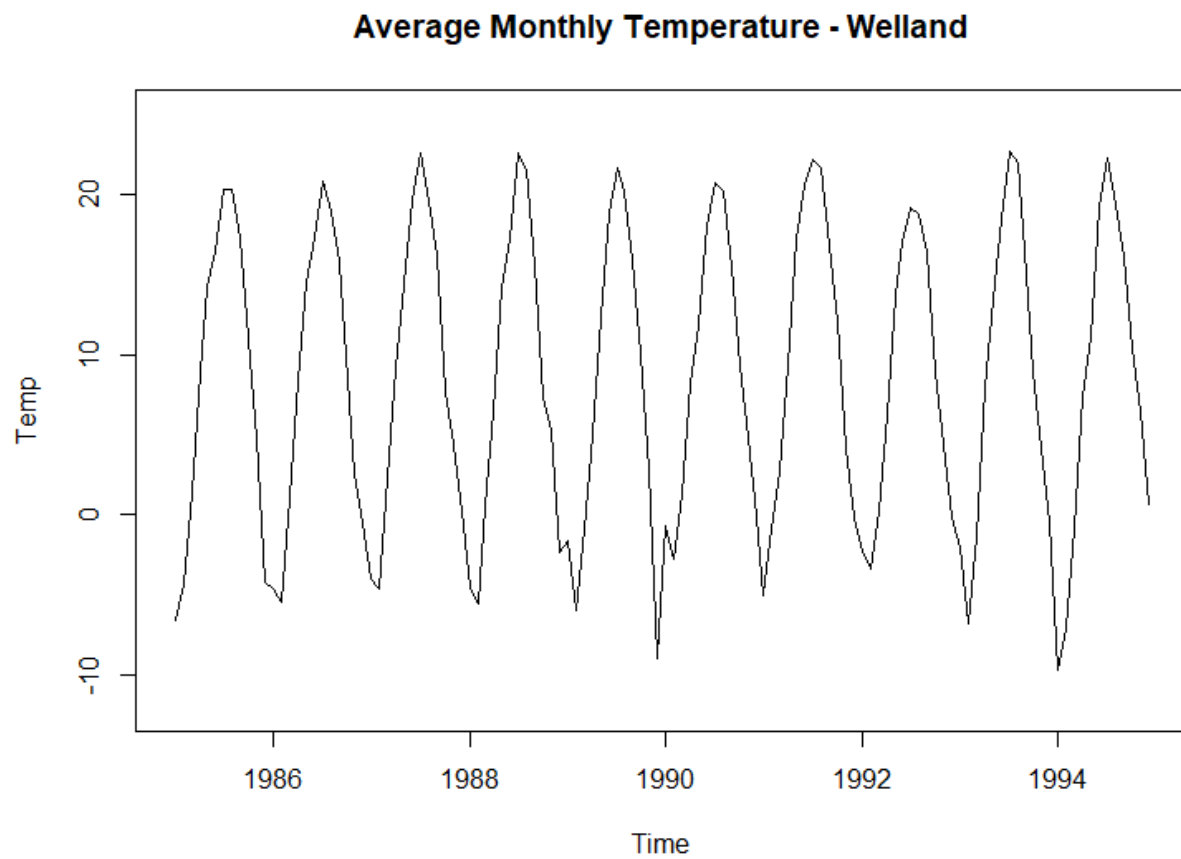
2. Descriptive Data Analysis

2.1 Summary of the temperature information:

	Temp
nbr.val	120.0000000
nbr.null	0.0000000
nbr.na	0.0000000
min	-9.7129032
max	22.6387097
range	32.3516129
sum	1015.5660173
median	8.9326882
mean	8.4630501

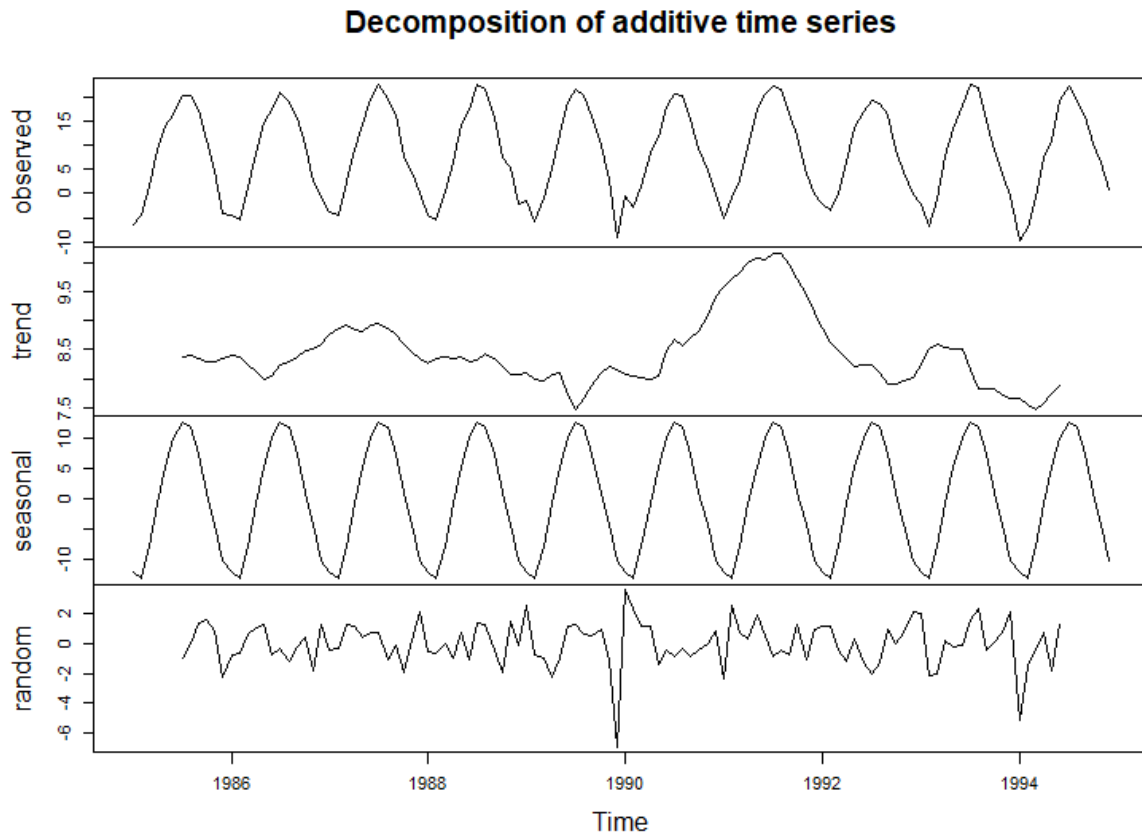
SE.mean	0.850028
CI.mean.0.95	1.6830905
var	86.7005765
std.dev	9.3113144
coef.var	1.1002315

2.2 Plot of time series :



Temperature data shows strong seasonal tendencies although the mean temperature appears to be relatively constant.

2.3 Decomposition of the times series data into the constituent components:



As we noted earlier, the trend is relatively constant except for a peak around 1992.

2.4 Stationarity:

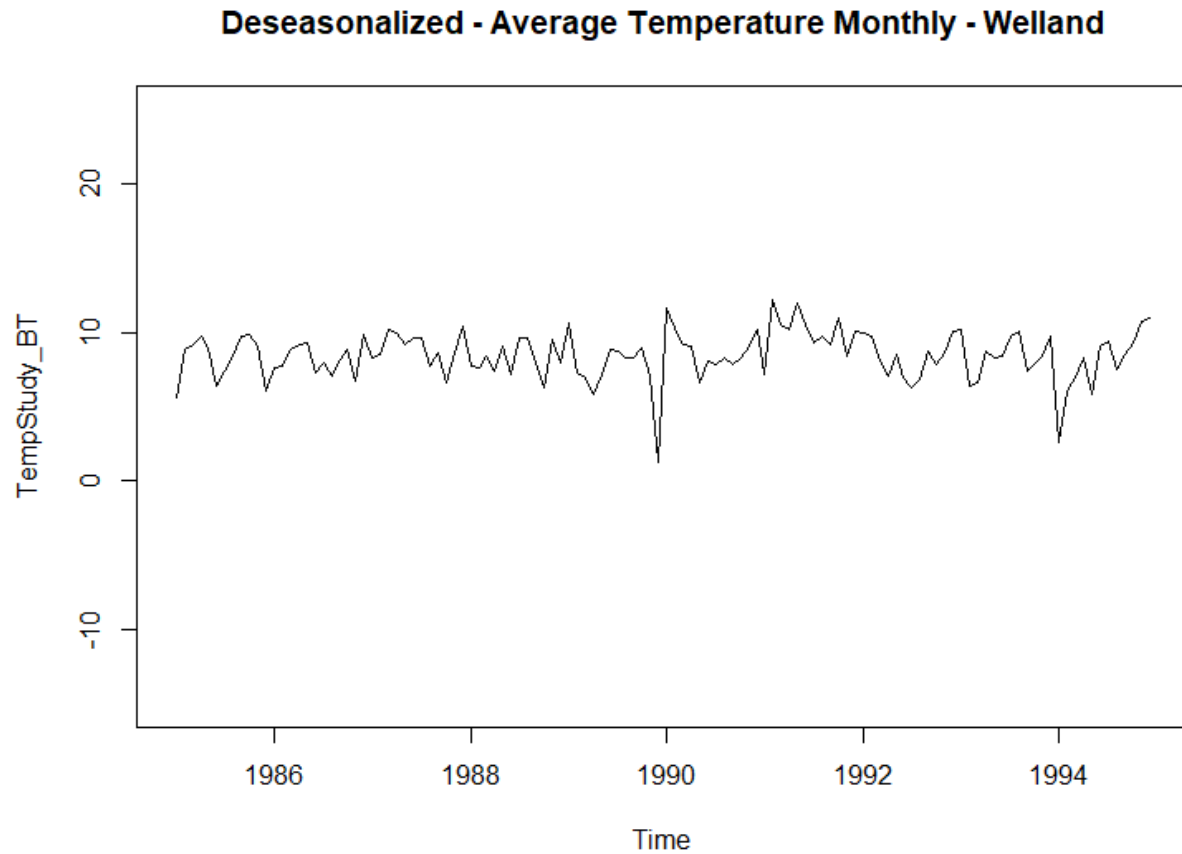
```
Warning in adf.test(TempStudy_BT): p-value smaller than printed p-value
```

Augmented Dickey-Fuller Test

```
data: TempStudy_BT  
Dickey-Fuller = -13.342, Lag order = 4, p-value = 0.01  
alternative hypothesis: stationary
```

Augmented Dickey-Fuller test resulted in a p-value less than .05 indicating that the time series is stationary.

2.5 Deseasonalized Temperature Data :



2.6 Comments :

1. Overall trend component is not varying much, except for a peak around 1992.
2. As one would expect seasonal component has a strong cyclic nature.
3. The random component seems to have constant variance.

Section 2: Waterloo Precipitation

1. Data Transformation and Cleaning (Description)

Dates

The dates column was removed since we only need precipitation data to perform time series analysis.

Precipitation

The total precipitation data was converted to time series data using function `ts()`.

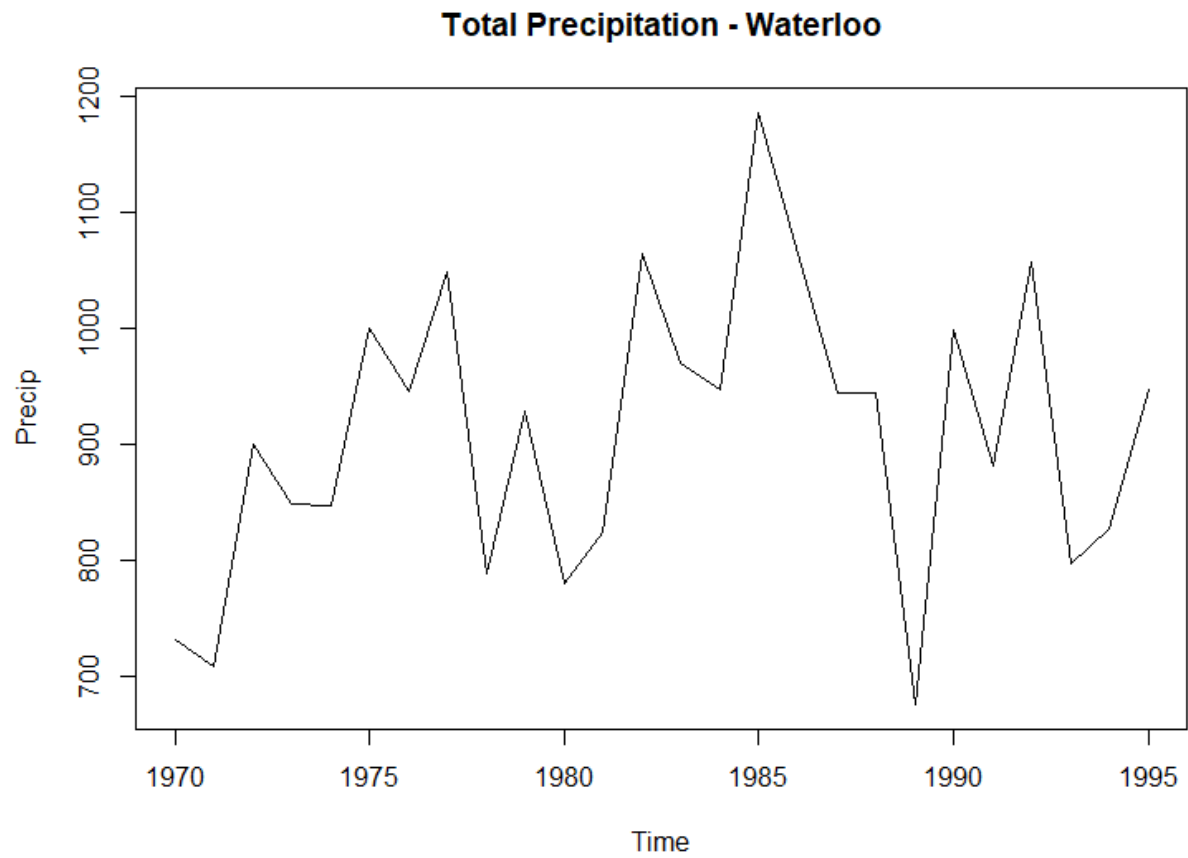
```
Time Series:
Start = 1970
End = 1975
Frequency = 1
      Precip
[1,]  731.3
[2,]  707.7
[3,]  899.5
[4,]  847.9
[5,]  846.4
[6,]  999.8
```

2. Descriptive Data Analysis

2.1 Summary of the precipitation information:

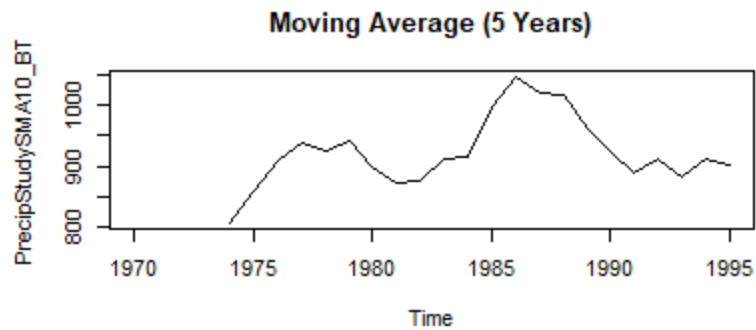
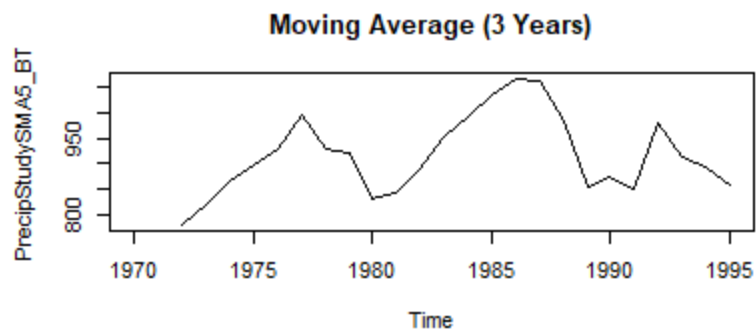
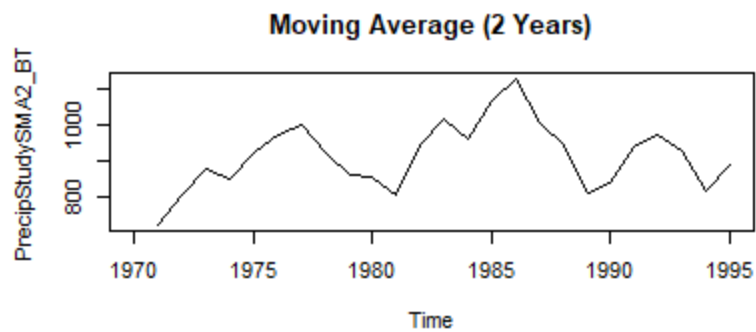
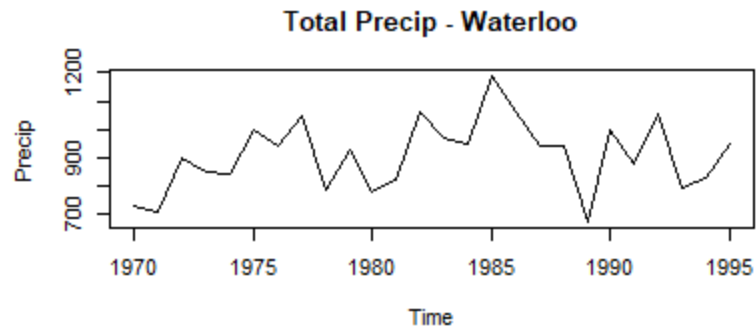
	Precip
nbr.val	26.00000
nbr.null	0.00000
nbr.na	0.00000
min	674.80000
max	1186.40000
range	511.60000
sum	23648.20000
median	936.10000
mean	909.54615
SE.mean	24.39122
CI.mean.0.95	50.23467
var	15468.22738
std.dev	124.37133
coef.var	0.13674

2.2 Plot of time series :



Precipitation significantly varies year-to-year with maxima around 1985 and minima around 1989.

2.3 Decomposition of the times series data into the constituent components:



In my opinion, moving average using 3 years window best conveys the trend since the window size of 2 years still retains the noise whereas 5 years appears to over smoothen the data (leading to loss of details).

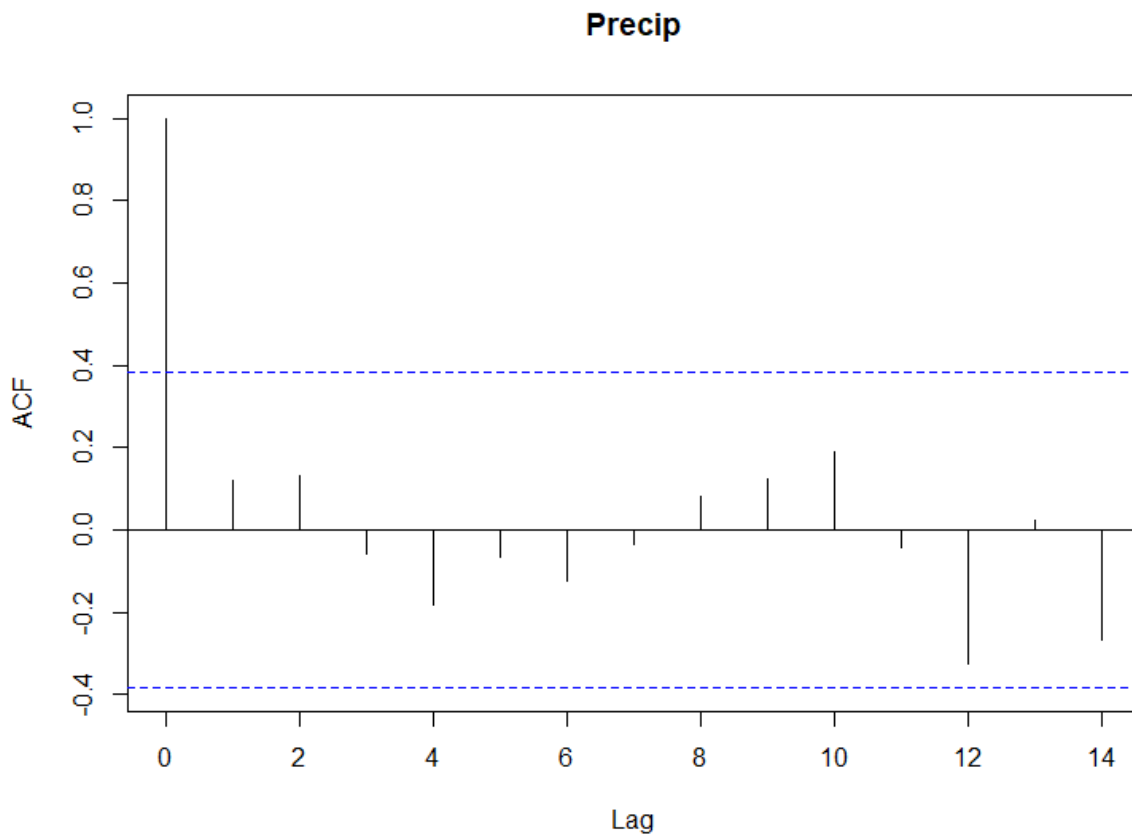
2.4 Stationarity:

Augmented Dickey-Fuller Test

```
data: PrecipStudy_BT  
Dickey-Fuller = -2.5257, Lag order = 2, p-value = 0.3721  
alternative hypothesis: stationary
```

Augmented Dickey-Fuller test resulted in a p-value greater than .05 indicating that time series is non-stationary.

2.5 Autocorrelation chart:



All the lags, except lag 0 (i.e., the correlation of a time series with itself), are not significant as they fall within horizontal blue lines which are the approximate 95% confidence intervals. This means that previous values do not seem to be influencing the current values.

3. Forecast

3.1 Simple Moving Average Forecast

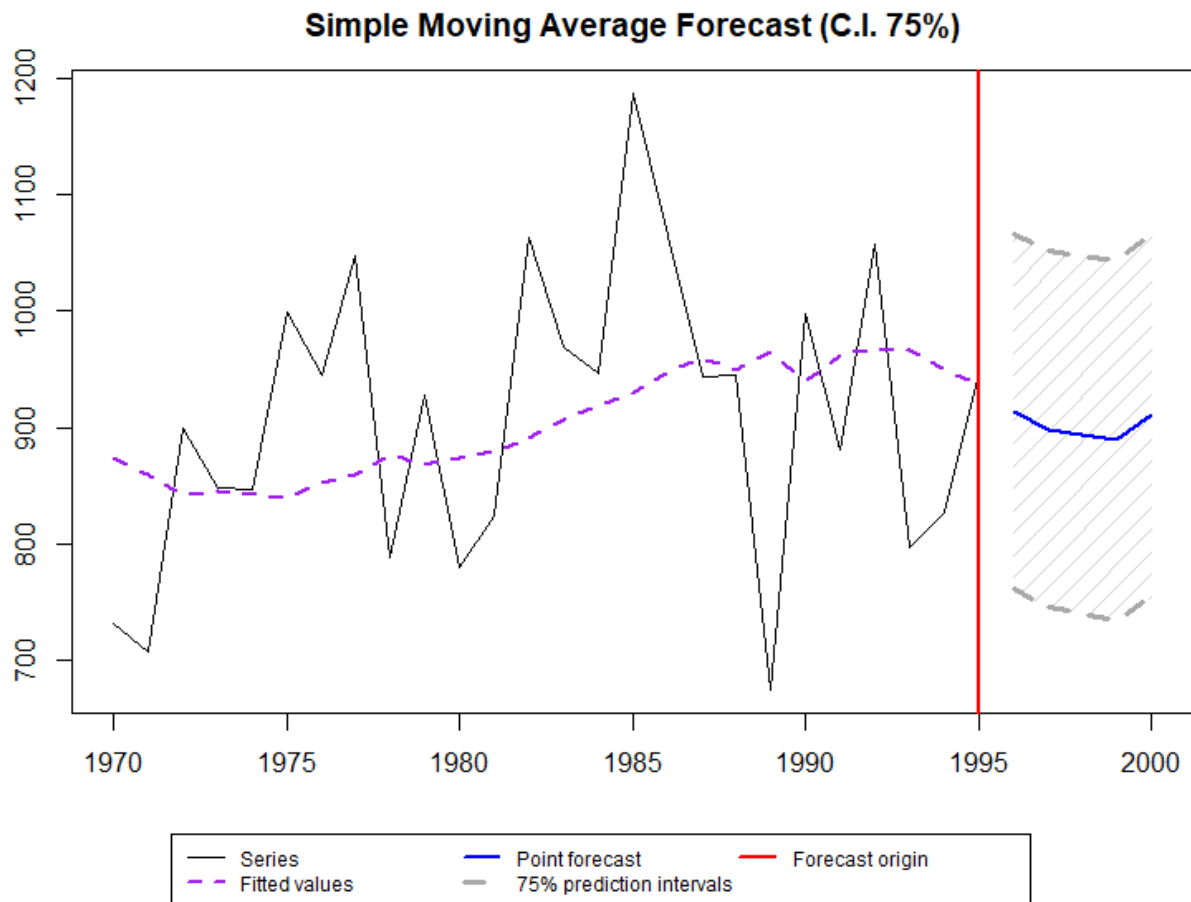
Time Series:

Start = 1996

End = 2000

Frequency = 1

	Point forecast	Lower bound (12.5%)	Upper bound (87.5%)
1996	913.6000	761.3417	1065.858
1997	898.5000	745.4823	1051.518
1998	893.9700	740.0385	1047.902
1999	888.8970	733.8669	1043.927
2000	910.3067	753.9577	1066.656



3.2 Exponentially Smoothed Forecast

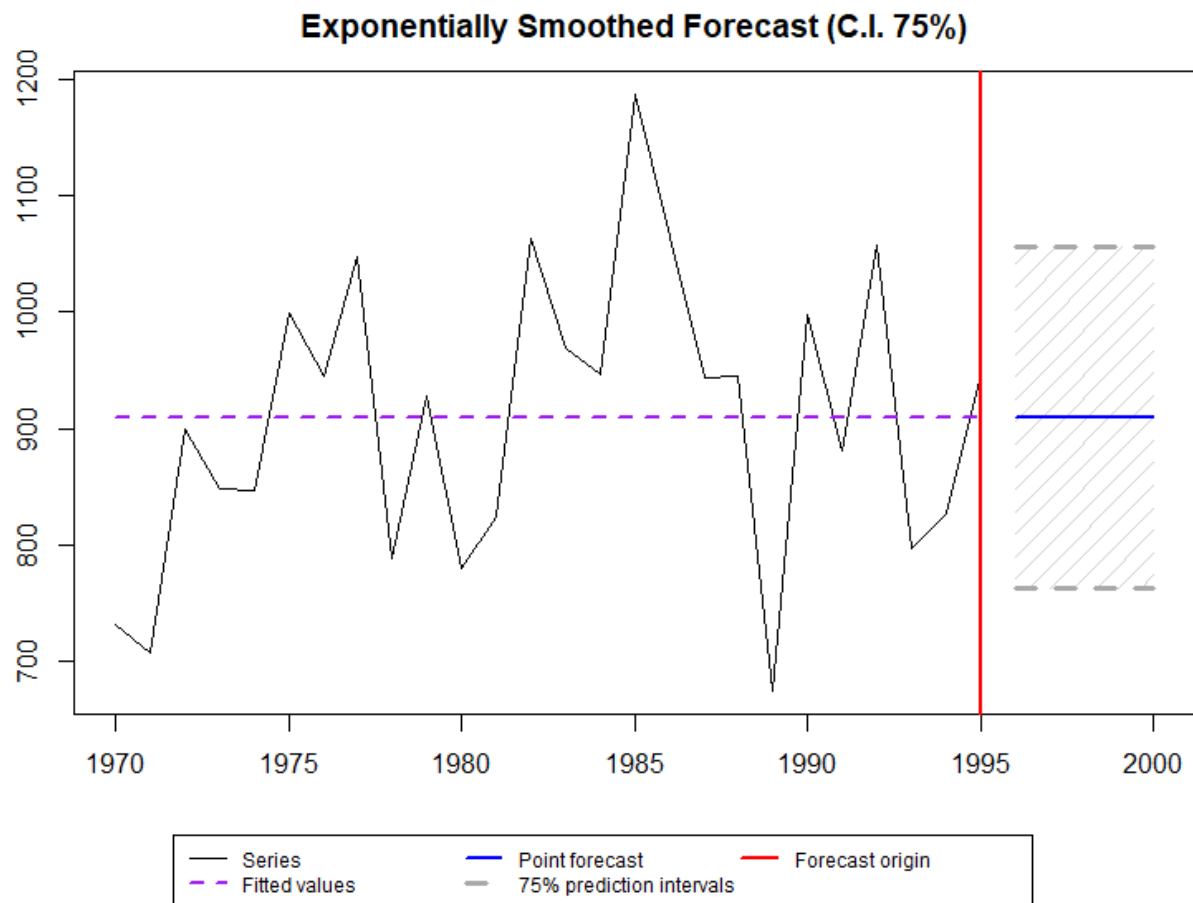
Time Series:

Start = 1996

End = 2000

Frequency = 1

	Point forecast	Lower bound (12.5%)	Upper bound (87.5%)
1996	909.5462	763.072	1056.02
1997	909.5462	763.072	1056.02
1998	909.5462	763.072	1056.02
1999	909.5462	763.072	1056.02
2000	909.5462	763.072	1056.02



3.3 Conclusion

In general, recent years are better for predicting future years. So, in this case, exponential smoothing forecast seems to stand better for forecasting temperature in Waterloo. It appears that the overall trend is relatively constant. It is not going upward or downward. In the case of moving average, we can observe that the trend appears to go first downwards and then upwards, for which we have no reasoning.