

Classical Mechanics : Center of Mass

Assignment-3

Assignment- 2 : Please search some good problems of Newton's Laws of motion (Body moving in curved path) and solve them by plane polar coordinate

1. Find the center of mass of the 2-dimensional region bounded by the x-axis, y-axis and the curve  $y = 4 - x^2$  in the first quadrant, if the surface density is uniform. [ Ans:  $(x,y)=(3/4, 8/5)$  ]
2. Find the center of mass of the triangle with vertices  $(x,y) = (0,0)$ ,  $(-4,2)$  and  $(0,6)$ , if the area has a uniform surface density. [Ans:  $(x,y) = (-3/4, 8/3)$  ]
3. Find the center of mass of a hollow hemisphere with uniform surface density, with radius  $S$ , total mass  $M$  and the center of the base lying at the origin of coordinates. [Ans:  $z=S/2$  ]
4. A uniform plate has the shape of the region bounded by the parabola  $y = ax^2$  and the line  $y=H$  in the x-y plane . Find the center of mass in terms of  $H$  only [Ans:  $3/5 H J$  ]