1

Assignment 4

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Download latex-tikz codes from

https://github.com/Bharat437/Matrix_Theory/tree/master/Assignment4

1 Question

(Geometry,1.10) Q. Using cosine formula in an equilateral triangle, show that $\cos 60^{\circ} = \frac{1}{2}$.

2 Explanation

Consider an equilateral $\triangle ABC$ as shown in below figure:

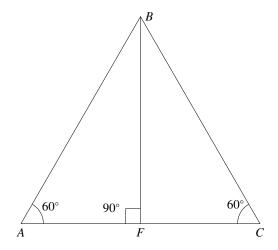


Fig. 1: Equilateral $\triangle ABC$

We know that in an equilateral triangle all sides have equal length.

$$\implies ||AB|| = ||BC|| = ||AC||$$
 (2.0.1)

Since F is midpoint of line AC.

$$\implies ||AF|| = \frac{1}{2} ||AC|| \qquad (2.0.2)$$

From (2.0.1),

$$\implies ||AF|| = \frac{1}{2} ||AB|| \qquad (2.0.3)$$

 $\triangle ABF$ forms a right-angled triangle. Using cosine formula,

$$\implies \cos 60^\circ = \frac{||AF||}{||AB||} \tag{2.0.4}$$

$$=\frac{\frac{1}{2}\,||AB||}{||AB||}\tag{2.0.5}$$

$$\implies \cos 60^\circ = \frac{1}{2} \tag{2.0.6}$$

Hence proved.