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# Image Restoration

Lecture 7, March 23<sup>rd</sup>, 2009

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EE4830 Digital Image Processing  
<http://www.ee.columbia.edu/~lx/ee4830/>

thanks to G&W website, Min Wu and others for slide materials

# Announcements

- Midterm results this week
- HW3 due next Monday
  - question 1.4, plot energy distribution as %energy included vs. #eigen dimensions

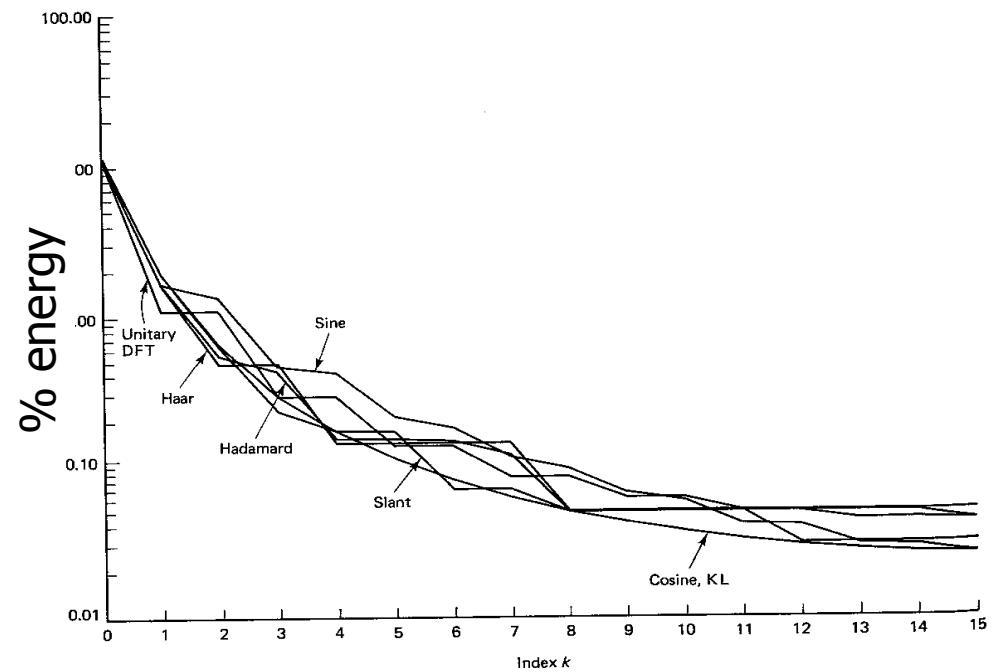
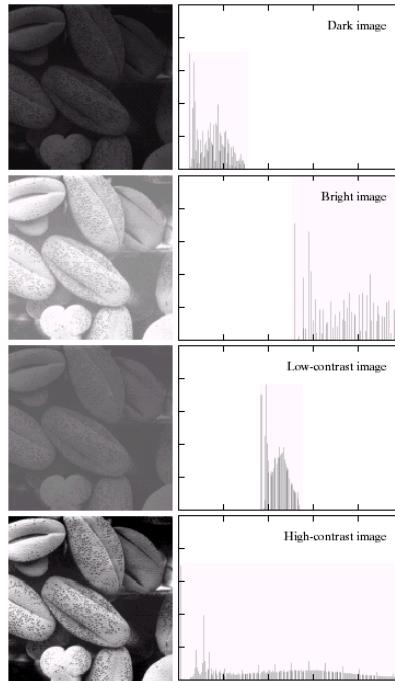


Figure 5.18 Distribution of variances of the transform coefficients (in decreasing order) of a stationary Markov sequence with  $N = 16$ ,  $\rho = 0.95$  (see Example 5.9).

# we have covered ...



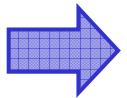
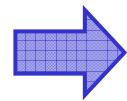
Spatial Domain  
processing

Image Transform  
and Filtering

Image sensing



Image Restoration



# outline

- What is image restoration
  - Scope, history and applications
  - A model for (linear) image degradation
- Restoration from noise
  - Different types of noise
  - Examples of restoration operations
- Restoration from linear degradation
  - Inverse and pseudo-inverse filtering
  - Wiener filters
  - Blind de-convolution
- Geometric distortion and its corrections

# degraded images



ideal image



Blurred image

- What caused the image to blur?
  - Camera: translation, shake, out-of-focus ...
  - Environment: scattered and reflected light
  - Device noise: CCD/CMOS sensor and circuitry
  - Quantization noise
- Can we improve the image, or “undo” the effects?



Original image



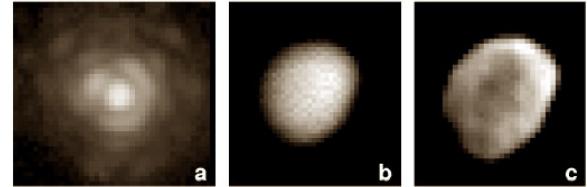
Blurred image

- Image enhancement: “improve” an image subjectively.
- Image restoration: remove distortion from image in order to go back to the “original” → objective process.

# image restoration

- started from the 1950s
- application domains
  - Scientific explorations
  - Legal investigations
  - Film making and archival
  - Image and video (de-)coding
  - ...
  - Consumer photography
- related problem: image reconstruction in radio astronomy, radar imaging and tomography

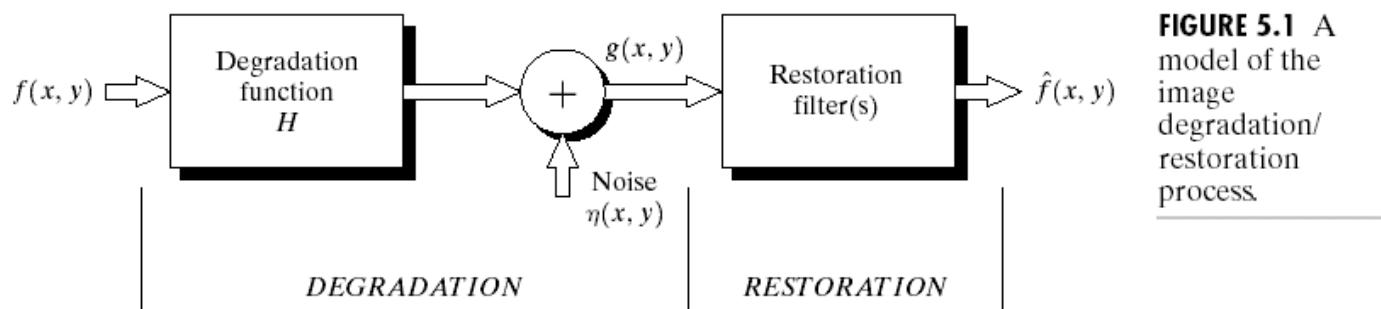
Example of image restoration  
Asteroid Vesta



[Banham and Katsaggelos 97]

# a model for image distortion

- Image enhancement: “improve” an image subjectively.
- Image restoration: remove distortion from image, to go back to the “original” -- objective process



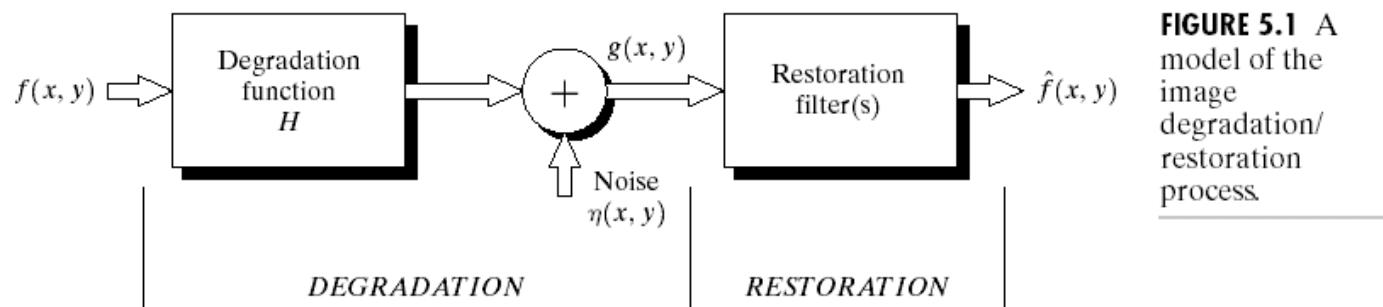
**FIGURE 5.1** A model of the image degradation/restoration process.

$$g(x, y) = H[f(x, y)] + \eta(x, y)$$

# a model for image distortion

- Image restoration

- Use a priori knowledge of the degradation
- Modeling the degradation and apply the inverse process
- Formulate and evaluate objective criteria of goodness



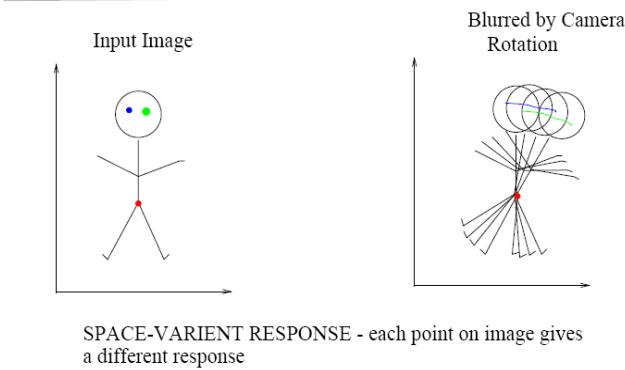
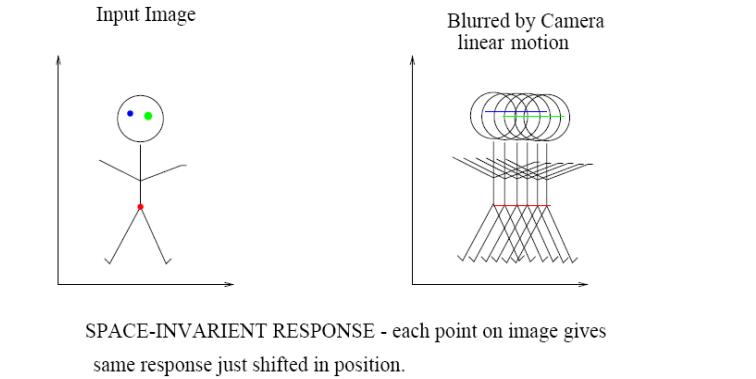
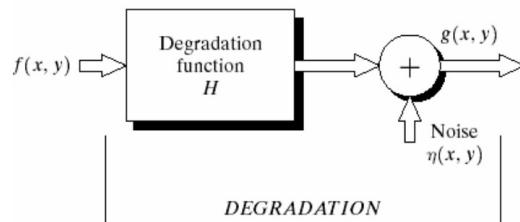
**FIGURE 5.1** A model of the image degradation/restoration process.

$$g(x, y) = H[f(x, y)] + \eta(x, y)$$

→ design restoration filters such that  
 $\hat{f}(x, y)$  is as close to  $f(x, y)$  as possible.

# usual assumptions for the distortion model

- Noise
  - Independent of spatial location
    - Exception: periodic noise ...
  - Uncorrelated with image
- Degradation function H
  - Linear
  - Position-invariant



divide-and-conquer step #1: image degraded only by noise.

# common noise models

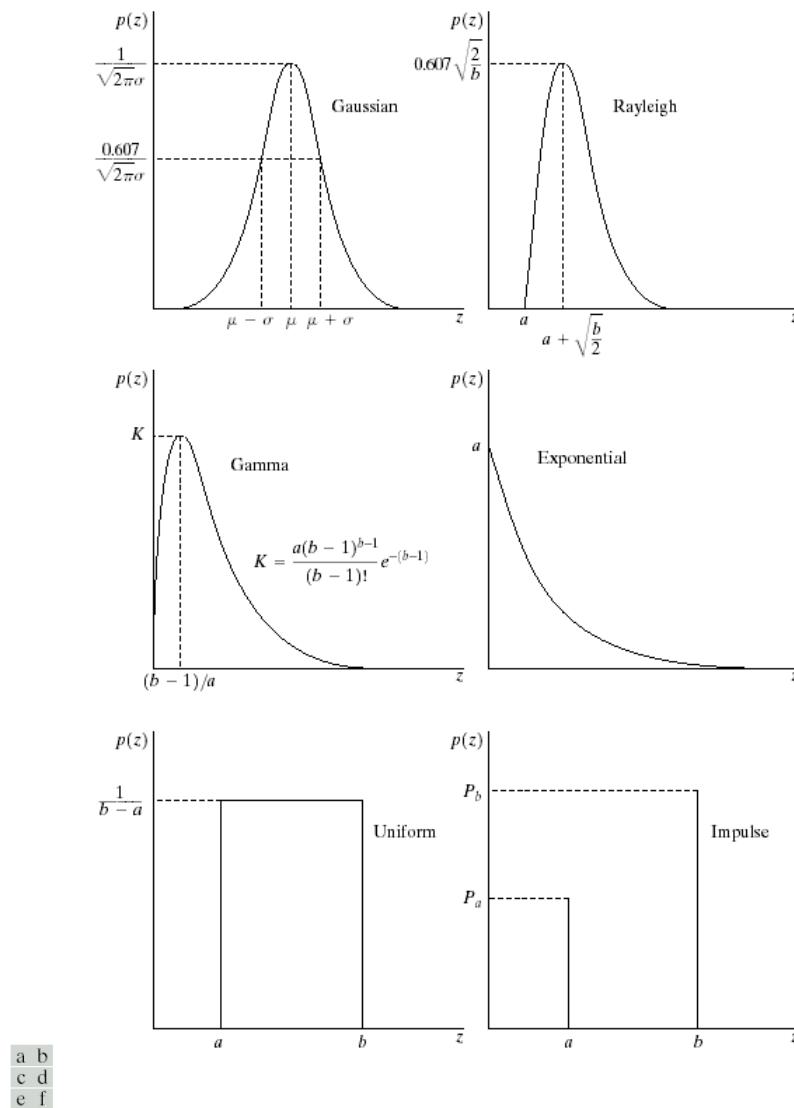


FIGURE 5.2 Some important probability density functions.

*Gaussian*

$$p(z) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(z-\mu)^2/2\sigma^2}$$

*Rayleigh*

$$p(z) = \frac{2}{b} (z-a) e^{-(z-a)^2/b}, \text{ for } z \geq a$$

*Erlang, Gamma(a,b)*

$$p(z) = \frac{a^b z^{b-1}}{(b-a)!} e^{-az}, \text{ for } z \geq 0$$

*Exponential*

$$p(z) = a e^{-az}, \text{ for } z \geq 0$$

→ additive noise

Salt-and-Pepper:

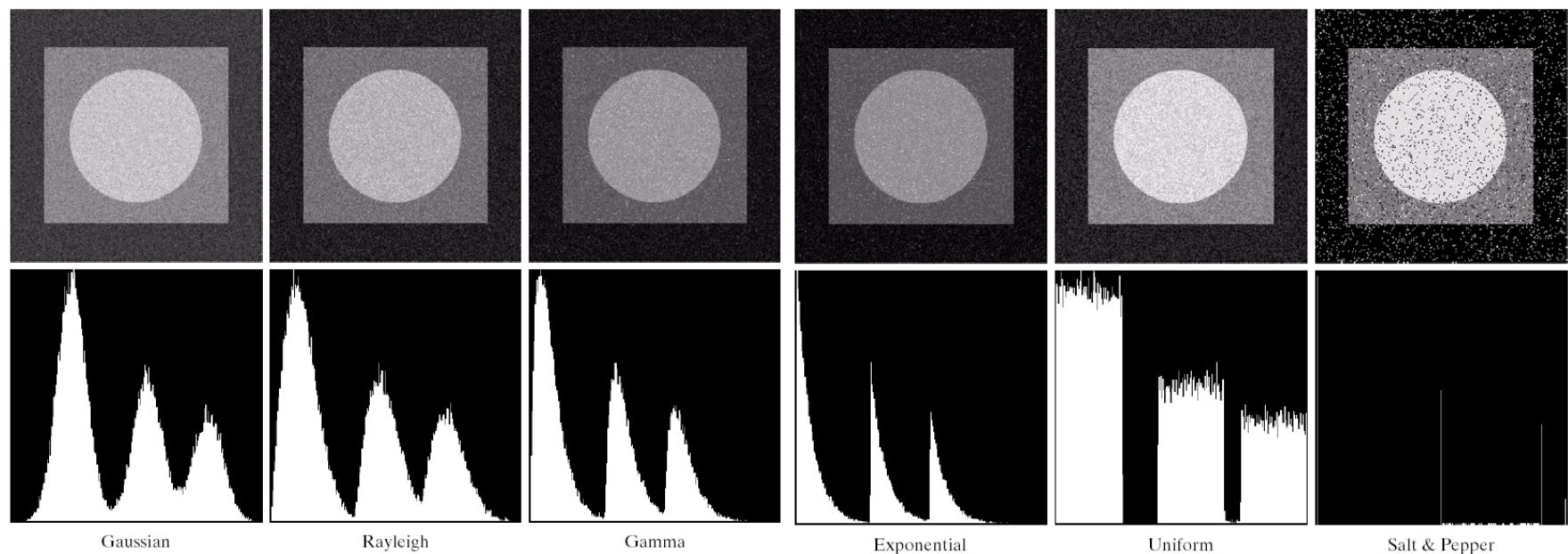
$$p(z) = P_a \delta(z-a) + P_b \delta(z-b)$$

Speckle noise:  $a = a_R + j a_I$

$$|g(x,y)|^2 \simeq |f(x,y)|^2 |a(x,y)|^2 + \eta(x,y)$$

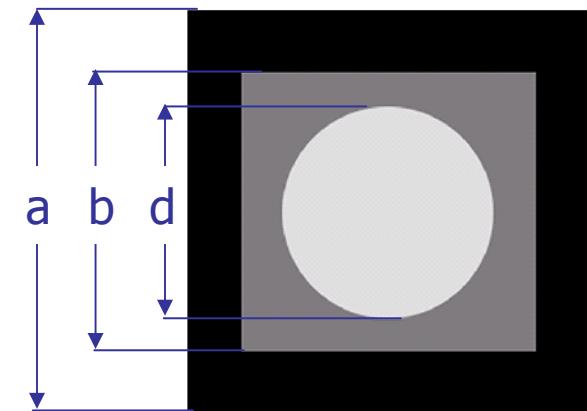
$a_R, a_I$  zero mean, independent Gaussian  
→ multiplicative noise on signal magnitude

# the visual effects of noise



**FIGURE 5.4** Images and histograms resulting from adding Gaussian, Rayleigh, and gamma noise to the image in Fig. 5.3.

**FIGURE 5.4 (Continued)** Images and histograms resulting from adding exponential, uniform, and impulse noise to the image in Fig. 5.3.



# recovering from noise

- overall process

Observe and estimate noise type and parameters → apply optimal (spatial) filtering (if known) → observe result, adjust filter type/parameters ...

- Example noise-reduction filters [G&W 5.3]

- Mean/median filter family
- Adaptive filter family
- Other filter family
  - e.g. Homomorphic filtering for multiplicative noise [G&W 4.9.6, Jain 8.13]

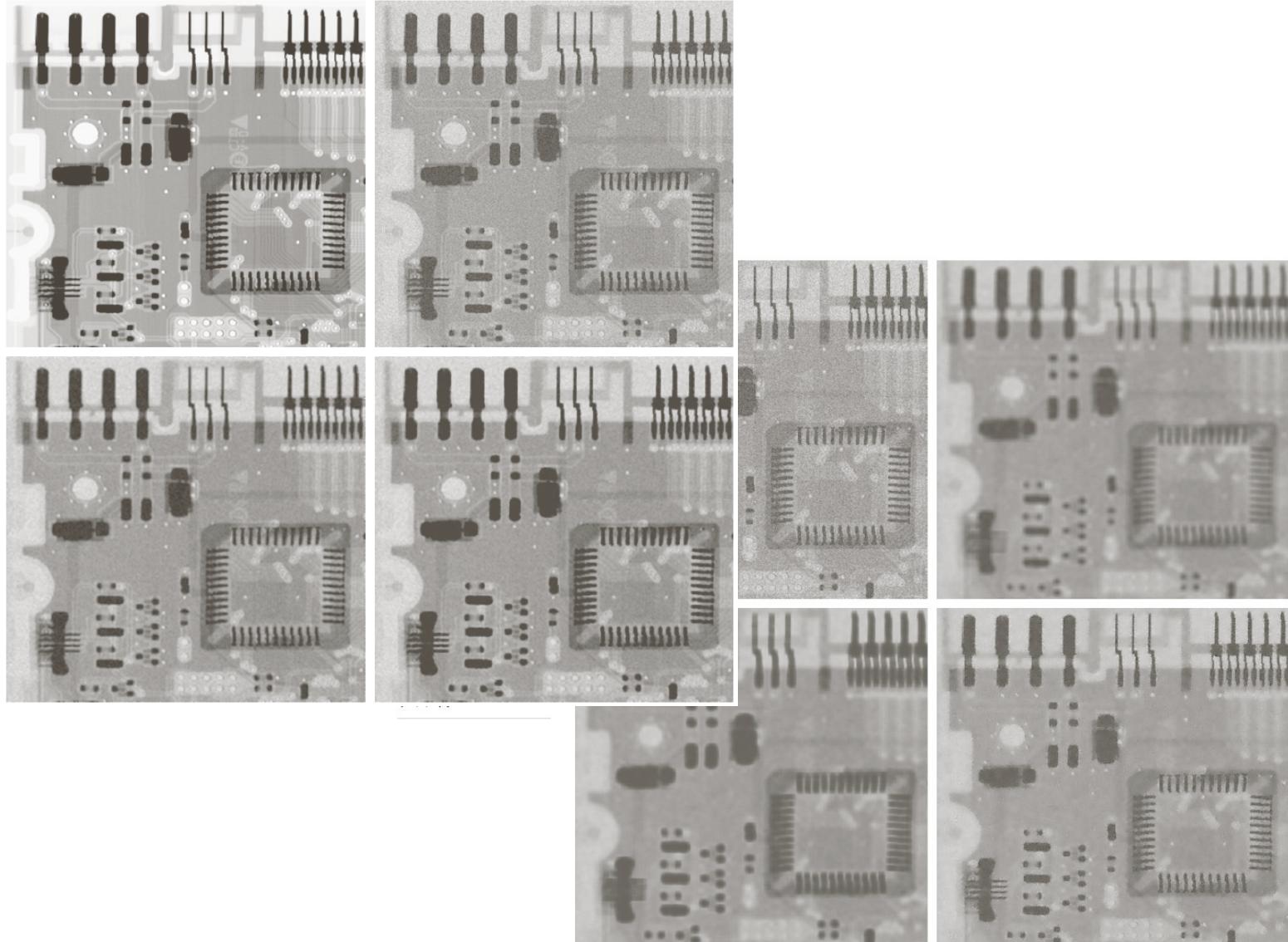
# example: Gaussian noise

a b  
c d

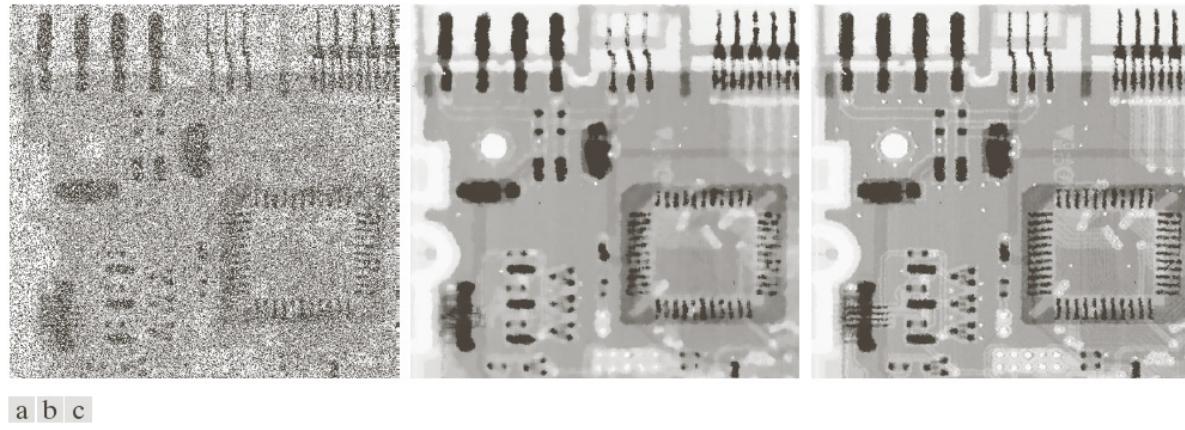
**FIGURE 5.7**

(a) X-ray image.  
(b) Image corrupted by additive Gaussian noise. (c) Result of filtering with an arithmetic mean filter of size  $3 \times 3$ . (d) Result of filtering with a geometric mean filter of the same size.

(Original image courtesy of Mr. Joseph E. Pascente, Lixi, Inc.)



## example: salt-and-pepper noise

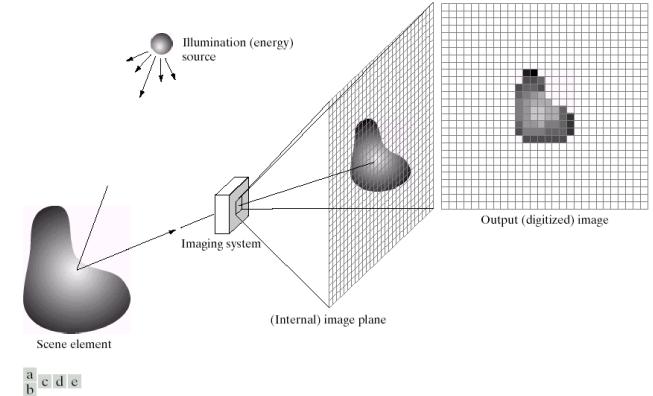
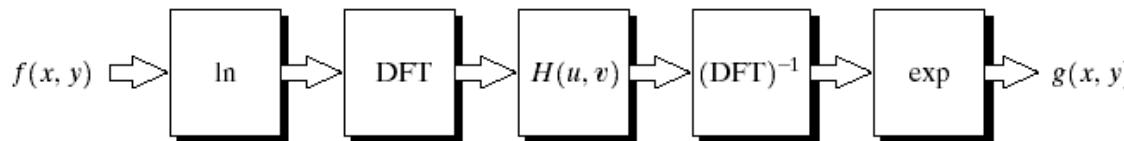


**FIGURE 5.14** (a) Image corrupted by salt-and-pepper noise with probabilities  $P_a = P_b = 0.25$ . (b) Result of filtering with a  $7 \times 7$  median filter. (c) Result of adaptive median filtering with  $S_{\max} = 7$ .

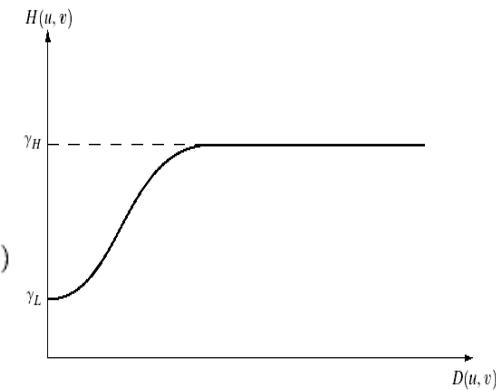
# Homomorphic Filtering

- Recall image formation model in Chapter 2:
  - Slow-changing illumination  $i(x,y)$  and fast-changing reflectance  $r(x,y)$
$$f(x,y) = i(x,y)r(x,y)$$

$$z(x,y) = \ln f(x,y) = \ln i(x,y) + \ln r(x,y)$$
- Used to remove multiplicative noise, or illumination variations
- Also used in to separate excitation and filtering effects in speech, e.g. hearing aids



**FIGURE 2.15** An example of the digital image acquisition process. (a) Energy (“illumination”) source. (b) An element of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.



**FIGURE 4.32**  
Cross section of a circularly symmetric filter function.  $D(u,v)$  is the distance from the origin of the centered transform.

developed in the 1960s by [Thomas Stockham](#), [Alan V. Oppenheim](#), and [Ronald W. Schafer](#) at [MIT](#)

# Recovering from Periodic Noise

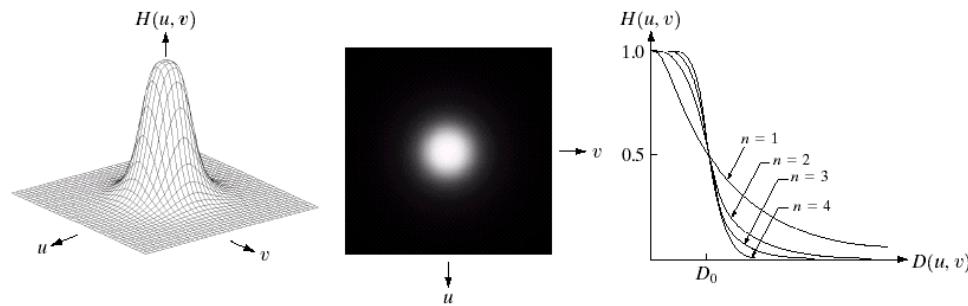
[G&W 5.4]

Recall: Butterworth LPF

$$H(u, v) = \frac{1}{1 + [D(u, v)/D_0]^{2n}}$$

Butterworth bandreject filter

$$H(u, v) = \frac{1}{1 + [\frac{D(u, v)W}{D^2(u, v) - D_0^2}]^{2n}}$$



a b c

**FIGURE 4.14** (a) Perspective plot of a Butterworth lowpass filter transfer function. (b) Filter displayed as an image. (c) Filter radial cross sections of orders 1 through 4.



a b c

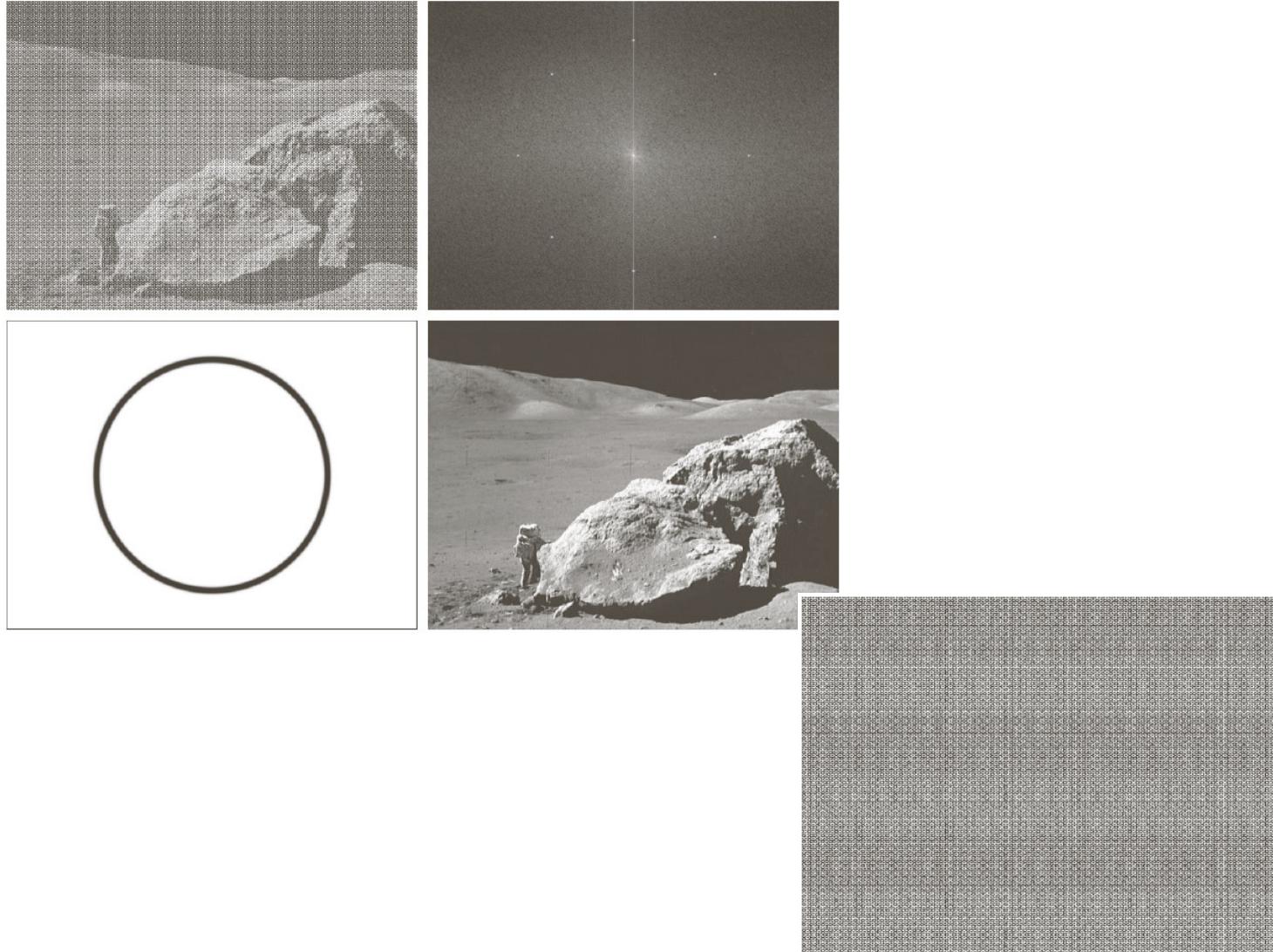
**FIGURE 5.15** From left to right, perspective plots of ideal, Butterworth (of order 1), and Gaussian bandreject filters.

# example of bandreject filter

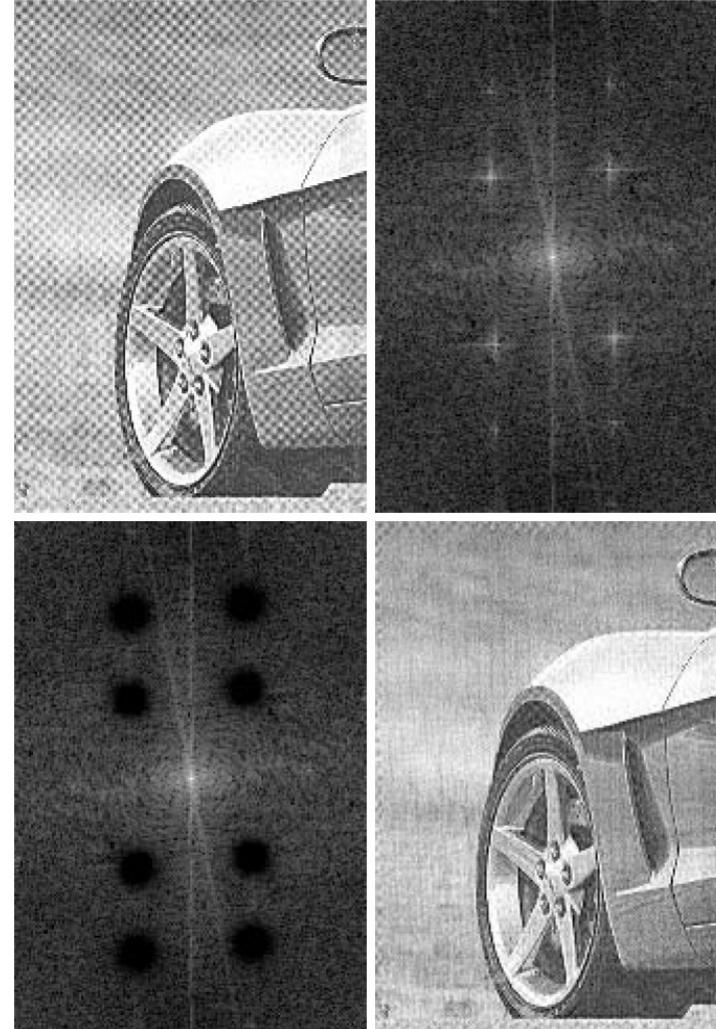
a  
b  
c  
d

**FIGURE 5.16**

(a) Image corrupted by sinusoidal noise.  
(b) Spectrum of (a).  
(c) Butterworth bandreject filter (white represents 1).  
(d) Result of filtering.  
(Original image courtesy of NASA.)



# notch filter



a b  
c d

**FIGURE 4.64**

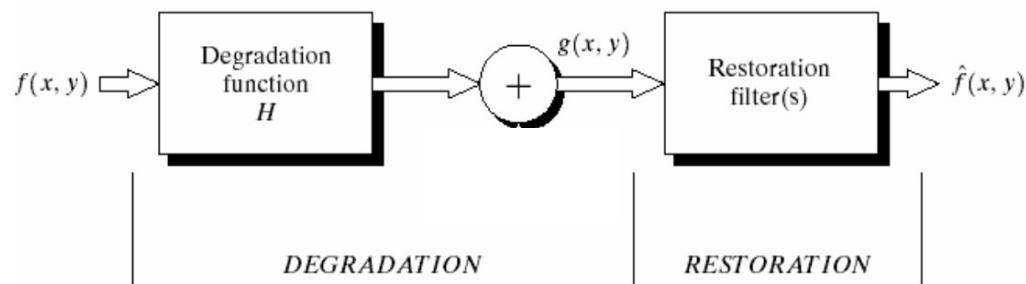
- (a) Sampled newspaper image showing a moiré pattern.
- (b) Spectrum.
- (c) Butterworth notch reject filter multiplied by the Fourier transform.
- (d) Filtered image.

# outline

- Scope, history and applications
- A model for (linear) image degradation
- Restoration from noise
  - Different types of noise
  - Examples of restoration operations
- Restoration from linear degradation
  - Inverse and pseudo-inverse filtering
  - Wiener filters
  - Blind de-convolution
- Geometric distortion and example corrections

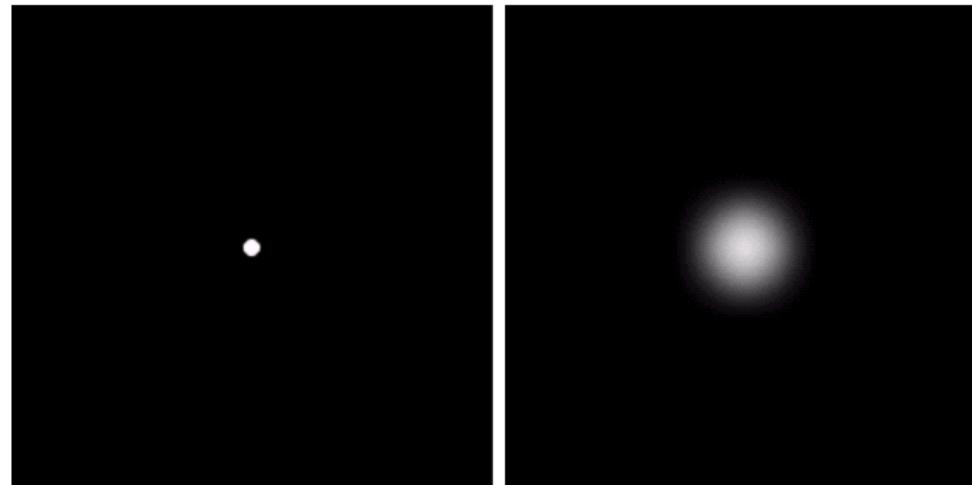
# recover from linear degradation

- Degradation function
    - Linear (eq 5.5-3, 5.5-4)
      - Homogeneity
      - Additivity
    - Position-invariant (in cartesian coordinates, eq 5.5-5)
- linear filtering with  $H(u,v)$   
 convolution with  $h(x,y)$  – point spread function



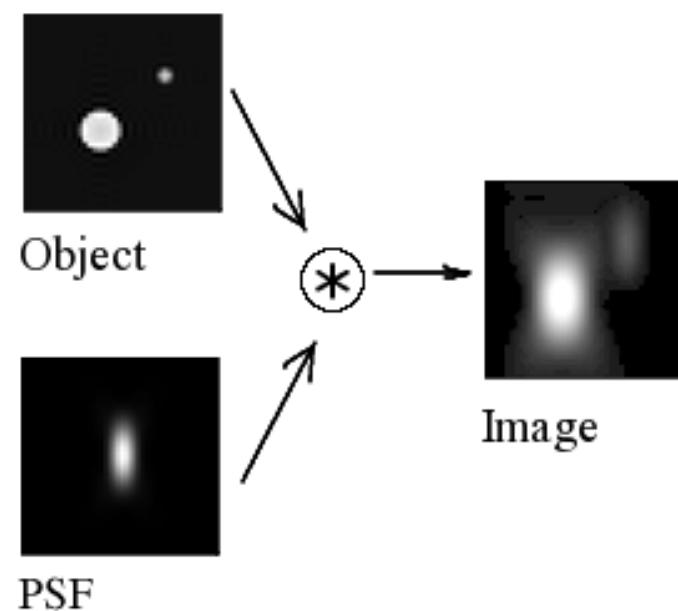
Divide-and-conquer step #2: linear degradation, noise negligible.

# point-spread function



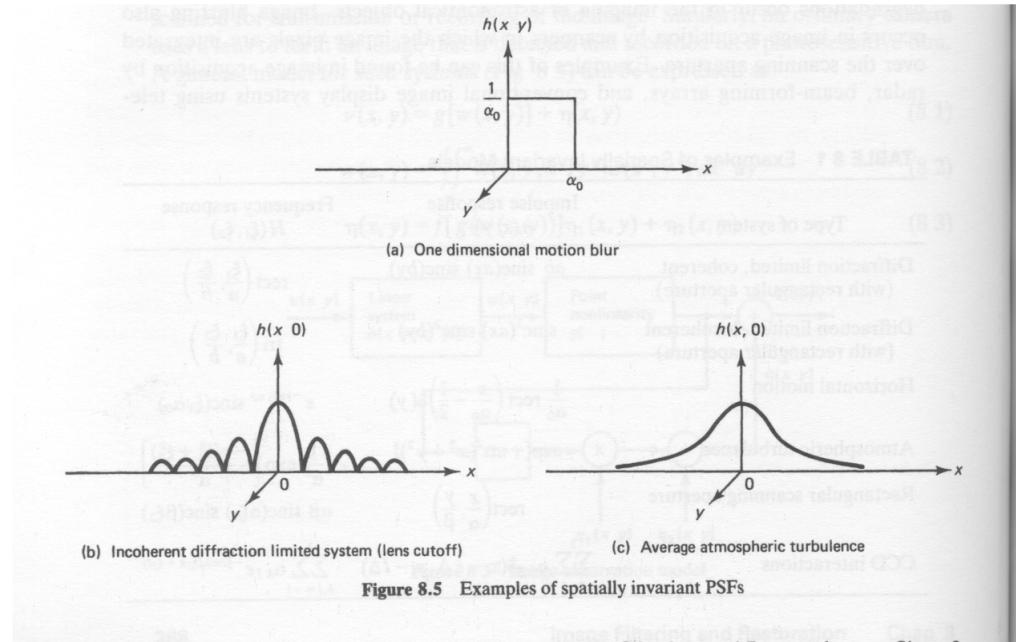
a b

**FIGURE 5.24**  
Degradation  
estimation by  
impulse  
characterization.  
(a) An impulse of  
light (shown  
magnified).  
(b) Imaged  
(degraded)  
impulse.

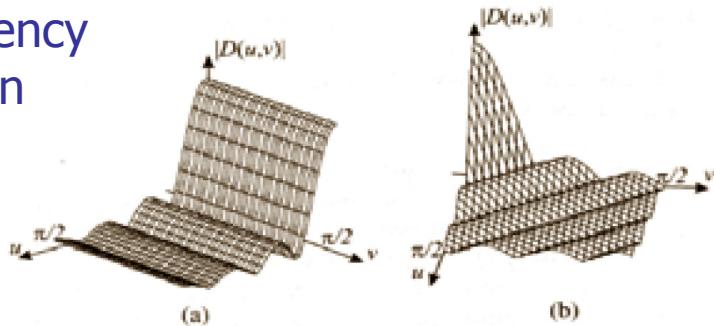


# point-spread functions

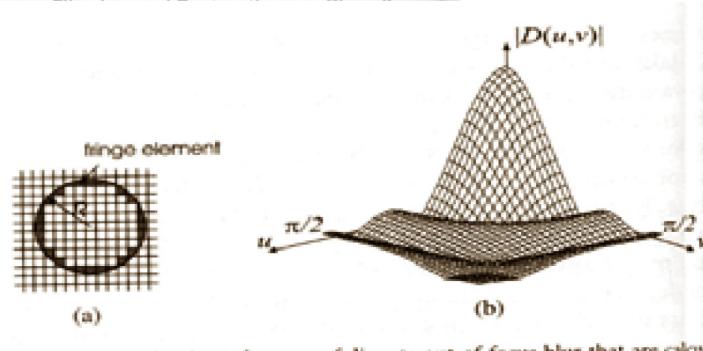
## Spatial domain



## Frequency domain



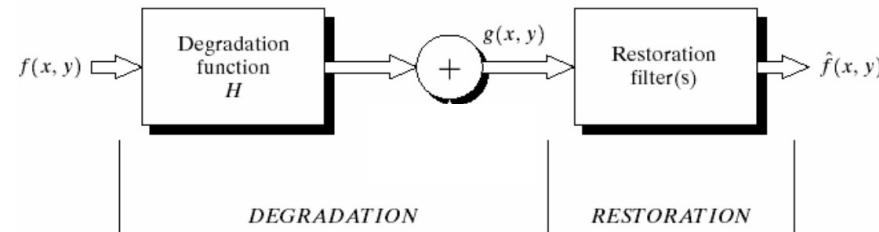
**FIGURE 2** PSF of motion blur in the Fourier domain, showing  $|D(u, v)|$ , for (a)  $L = 7.5$  and  $\Phi = 0$ ; (b)  $L = 7.5$  and  $\Phi = \pi/4$



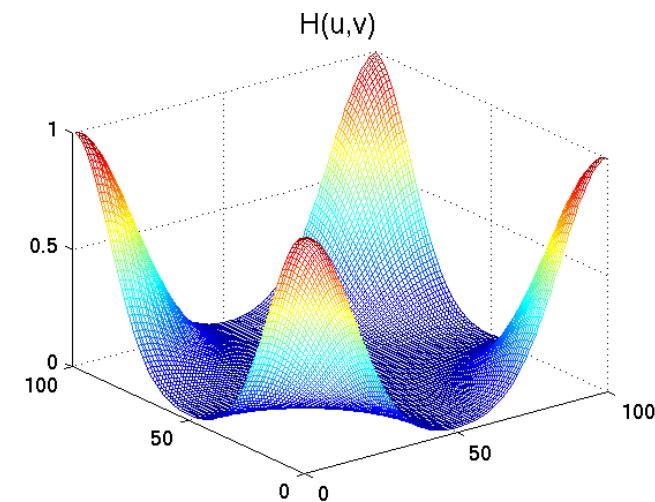
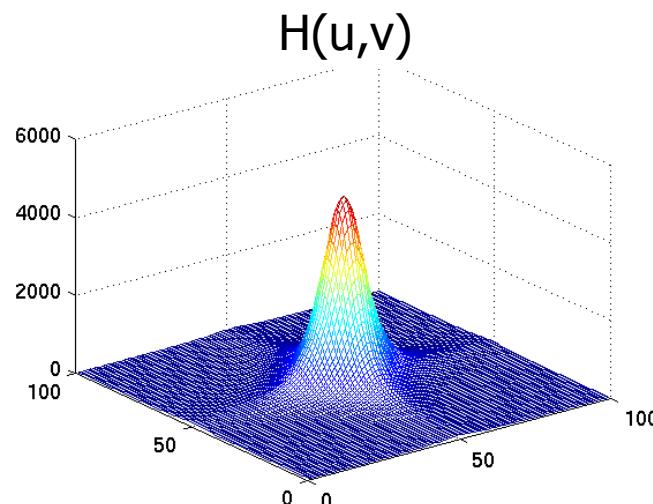
**FIGURE 3** (a) Fringe elements of discrete out-of-focus blur that are calculated by integration; (b) PSF in the Fourier domain, showing  $|D(u, v)|$ , for  $R = 2.5$ .

# inverse filter

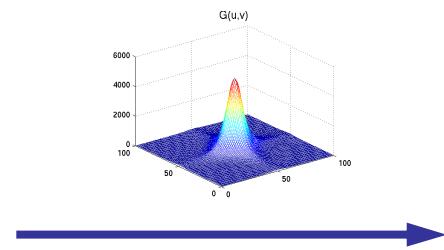
- assume  $h$  is known: low-pass filter  $H(u,v)$



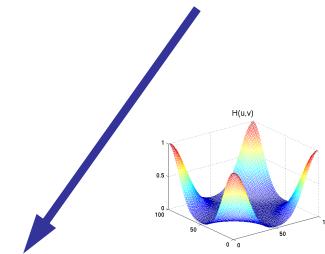
- inverse filter  $\hat{H}(u, v) = 1/H(u, v)$
- recovered image  $\hat{F}(u, v) = G(u, v)\hat{H}(u, v)$



# inverse filtering example



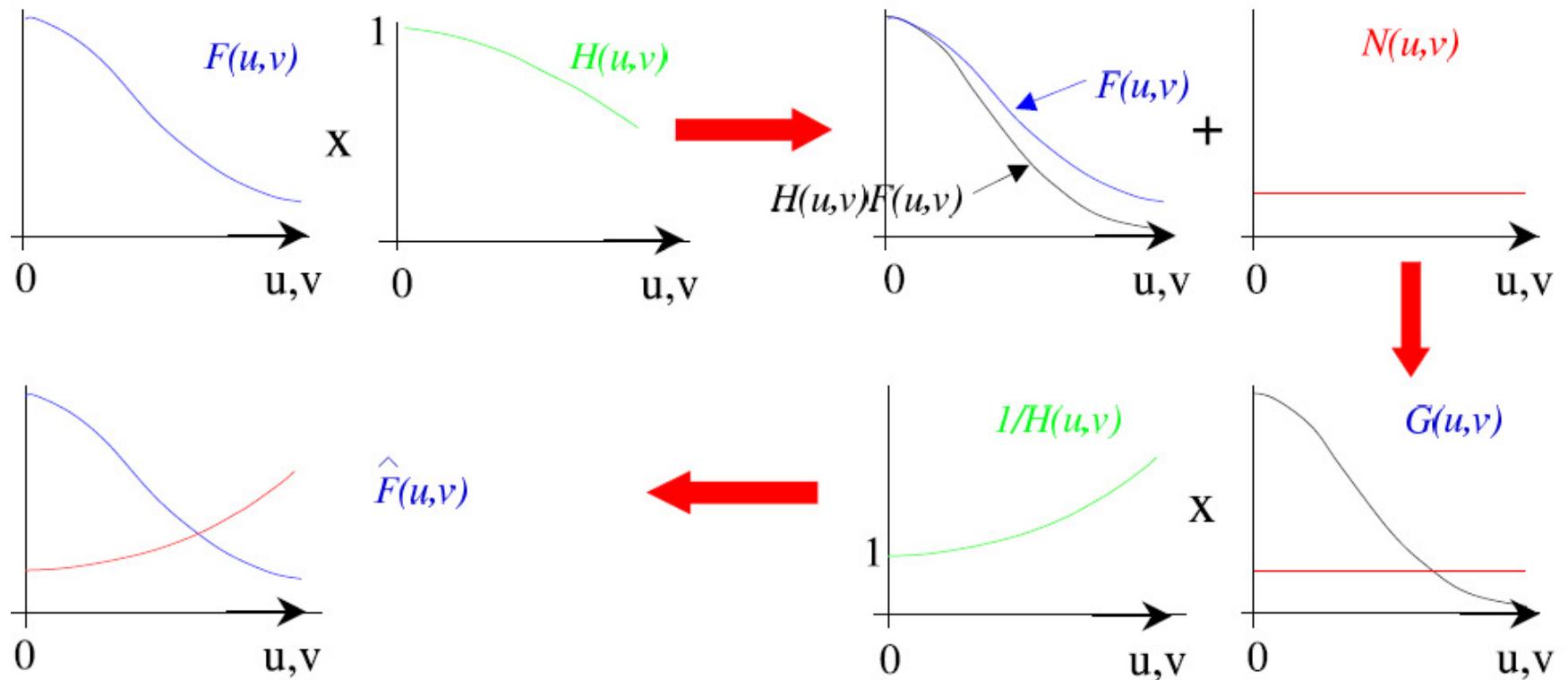
loss of  
information



# the problem of noise amplification

$$G(u, v) = F(u, v)H(u, v) + N(u, v) \quad \hat{H}(u, v) = 1/H(u, v)$$

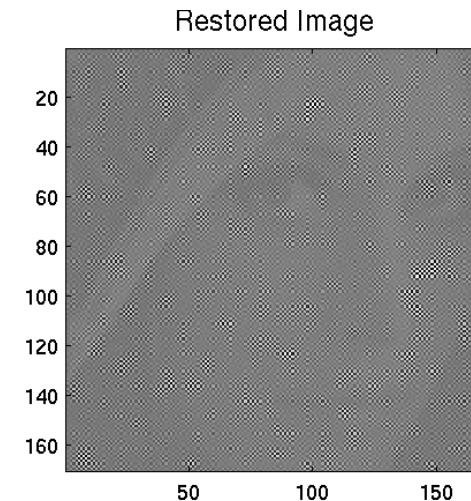
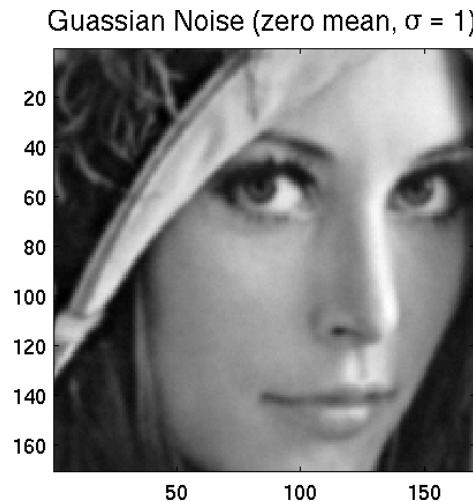
$$\hat{F}(u, v) = G(u, v)\hat{H}(u, v) = F(u, v) + \frac{N(u, v)}{\hat{H}(u, v)}$$



# noise amplification example

$$G(u, v) = F(u, v)H(u, v) + N(u, v) \quad \hat{H}(u, v) = 1/H(u, v)$$

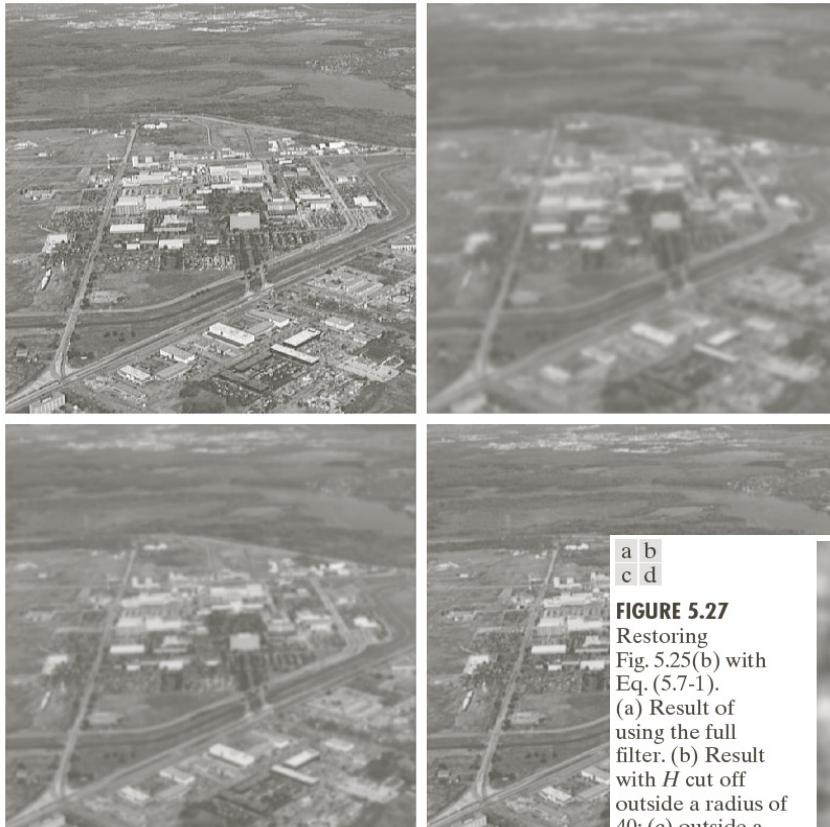
$$\hat{F}(u, v) = G(u, v)\hat{H}(u, v) = F(u, v) + \frac{N(u, v)}{H(u, v)}$$



a	b
c	d

**FIGURE 5.25**

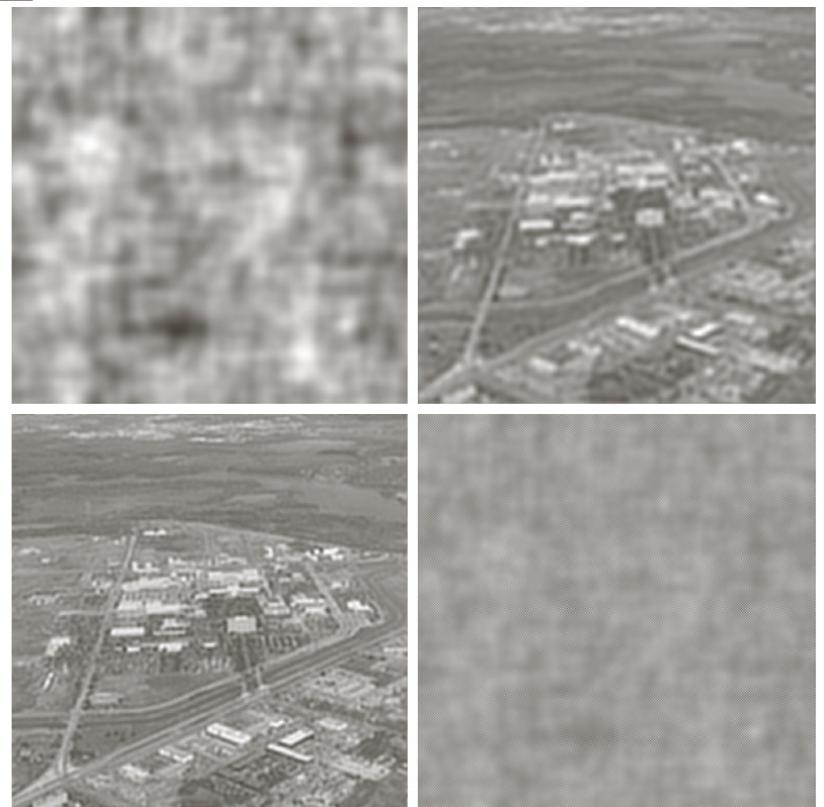
Illustration of the atmospheric turbulence model.  
 (a) Negligible turbulence.  
 (b) Severe turbulence,  
 $k = 0.0025$ .  
 (c) Mild turbulence,  
 $k = 0.001$ .  
 (d) Low turbulence,  
 $k = 0.00025$ .  
 (Original image courtesy of NASA.)



a	b
c	d

**FIGURE 5.27**

Restoring Fig. 5.25(b) with Eq. (5.7-1).  
 (a) Result of using the full filter. (b) Result with  $H$  cut off outside a radius of 40; (c) outside a radius of 70; and (d) outside a radius of 85.



$$\hat{F}(u, v) = G(u, v)\hat{H}(u, v)$$

$$\hat{H}(u, v) = \begin{cases} 1/H(u, v), & |u^2 + v^2| \leq \eta \\ 0, & |u^2 + v^2| > \eta \end{cases}$$

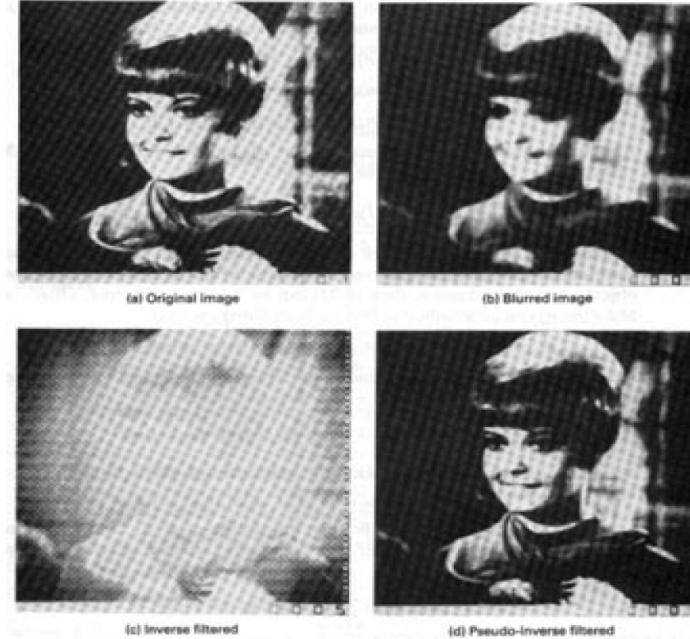
$$H(u, v) = e^{-k(u^2 + v^2)}$$

# pseudo-inverse filtering

- in reality, we often have
  - $H(u,v) = 0$ , for some  $u, v$ . e.g. motion blur
  - noise  $N(u,v) \neq 0$

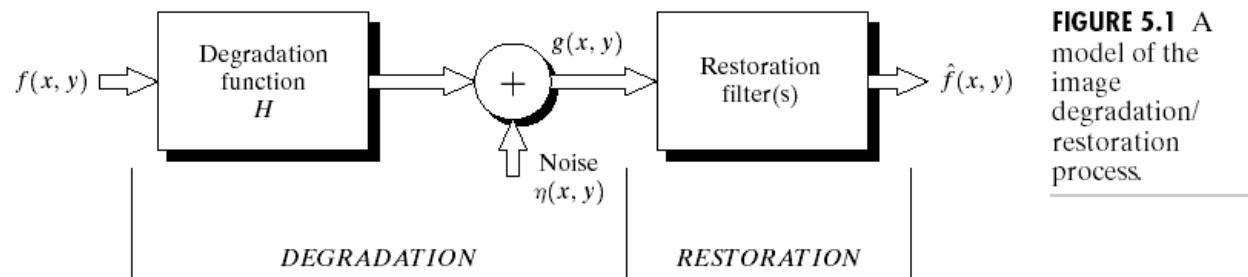
To mitigate the effect of zeros in the degradation function, we have:

$$\hat{H}(u, v) = \begin{cases} 1/H(u, v), & |H(u, v)| \geq \epsilon \\ 0, & |H(u, v)| < \epsilon \end{cases}$$



[Jain, Fig 8.10]

# back to the original problem



**FIGURE 5.1** A model of the image degradation/restoration process

Inverse filter with cut-off:

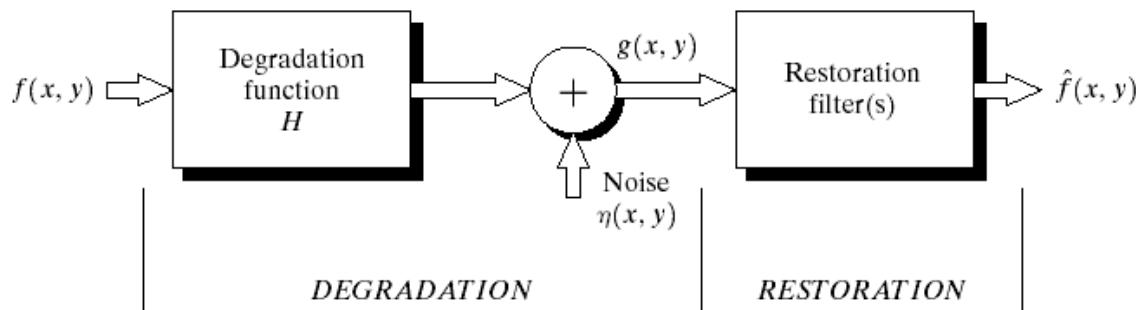
$$\hat{H}(u, v) = \begin{cases} 1/H(u, v), & |u^2 + v^2| \leq \eta \\ 0, & |u^2 + v^2| > \eta \end{cases}$$

Pseudo-inverse filter:

$$\hat{H}(u, v) = \begin{cases} 1/H(u, v), & |H(u, v)| \geq \epsilon \\ 0, & |H(u, v)| < \epsilon \end{cases}$$

- Can the filter take values between  $1/H(u,v)$  and zero?
- Can we model noise directly?

# Wiener filter



**FIGURE 5.1** A model of the image degradation/restoration process.

$$g(x, y) = f(x, y) * h(x, y) + n(x, y)$$

$$W(u, v)$$

$$\hat{f}(x, y) = w(x, y) * g(x, y)$$

- goal: restoration with expected minimum mean-square error (MSE)

$$\min_W e^2 = E\{(f - \hat{f})^2\} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} [f(x, y) - \hat{f}(x, y)]^2 dx dy$$

- optimal solution (nonlinear):

$$\hat{f}(x, y) = E\{f(x, y)|g(m, n), \forall (m, n)\}$$

- restrict to linear space-invariant filter

$$\hat{f}(x, y) = w(x, y) * g(x, y)$$

- find “optimal” linear filter  $W(u, v)$  with min. MSE ...

Derived by Norbert Wiener ~1942, published in 1949

Wiener, Norbert (1949), *Extrapolation, Interpolation, and Smoothing of Stationary Time Series*. New York: Wiley

## Wiener filter defined

$$W(u, v) = \frac{H^*(u, v)}{|H(u, v)|^2 + S_{\eta\eta}(u, v)/S_{ff}(u, v)}$$

$$W(u, v) = \frac{H^*(u, v)}{|H(u, v)|^2 + K(u, v)}$$

- If no noise,  $S_{\eta\eta} \rightarrow 0$        $W(u, v)|_{S_{\eta\eta} \rightarrow 0} = \begin{cases} \frac{1}{H(u, v)}, & H(u, v) \neq 0 \\ 0, & H(u, v) = 0 \end{cases}$   
 $\rightarrow$  Pseudo inverse filter
- If no blur,  $H(u, v) = 1$  (Wiener smoothing filter)

$$W(u, v)|_{H=1} = \frac{1}{1 + S_{\eta\eta}(u, v)/S_{ff}(u, v)} = \frac{SNR(u, v)}{SNR(u, v) + 1}$$

$\rightarrow$  More suppression on noisier frequency bands

- If  $K(u, v) \gg |H(u, v)|$  for large  $u, v \rightarrow$  suppress high-freq.

# Sketch derivation of Wiener Filter

Aim is to find filter which minimizes

$$\mathcal{E} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (f(x, y) - \hat{f}(x, y))^2 dx dy$$

$$\begin{aligned} \mathcal{E} &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |f(x, y) - \hat{f}(x, y)|^2 dx dy \\ &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |F(u, v) - \hat{F}(u, v)|^2 du dv \quad \text{Parseval's Theorem} \end{aligned}$$

$$\hat{F} = WG = WHF + WN$$

$$F - \hat{F} = (1 - WH)F - WN$$

$$\begin{aligned} \mathcal{E} &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} |(1 - WH)F - WN|^2 du dv \\ &= \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \{|(1 - WH)F|^2 + |WN|^2\} du dv \quad \text{since } f(x, y) \text{ and } \eta(x, y) \text{ uncorrelated} \end{aligned}$$

- Note, integrand is sum of two squares

# Sketch derivation of Wiener Filter (contd)

Minimize integral if integrand minimum for all  $(u,v)$

NB  $\frac{\partial}{\partial z}(zz^*) = 2z^*$

$$\frac{\partial}{\partial z} \rightarrow 2(-(1 - W^*H^*)H|F|^2 + W^*|N|^2) = 0$$

$$W^* = \frac{H|F|^2}{|H|^2|F|^2 + |N|^2}$$

$$W = \frac{H^*}{|H|^2 + |N|^2/|F|^2}$$

Note: filter is defined in the Fourier domain

# Alternative derivation of Wiener filter

- goal: restoration with minimum mean-square error (MSE)

$$\min_W e^2 = E\{(f - \hat{f})^2\}$$

$$\hat{f}(x, y) = w(x, y) * g(x, y)$$

- find “optimal” linear filter  $W(u, v)$  with min. MSE

→ orthogonal condition  $E\{g(f - \hat{f})\} = 0$

→ wide-sense-stationary (WSS) signals

$$R_{fg}(x_1, y_1, x_2, y_2) = E\{f(x_1, y_1)g(x_2, y_2)\} \xrightarrow{WSS} R_{fg}(x_1 - x_2, y_1 - y_2)$$

→ correlation function  $R_{fg}(x, y) = w(x, y) * R_{gg}(x, y)$

→ Fourier Transform: from correlation to spectrum

$$S_{fg}(u, v) = \mathcal{F}\{R_{fg}(x, y)\}, \quad S_{gg}(u, v) = \mathcal{F}\{R_{gg}(x, y)\}$$

$$\Rightarrow W(u, v) = \frac{S_{fg}(u, v)}{S_{gg}(u, v)} = \frac{H^*(u, v)S_{ff}(u, v)}{|H(u, v)|^2S_{ff}(u, v) + S_{\eta\eta}(u, v)}$$

$S_{ff}$  and  $S_{\eta\eta}$  are the power spectra of the signal and noise, respectively

## 1-D Wiener Filter Shape

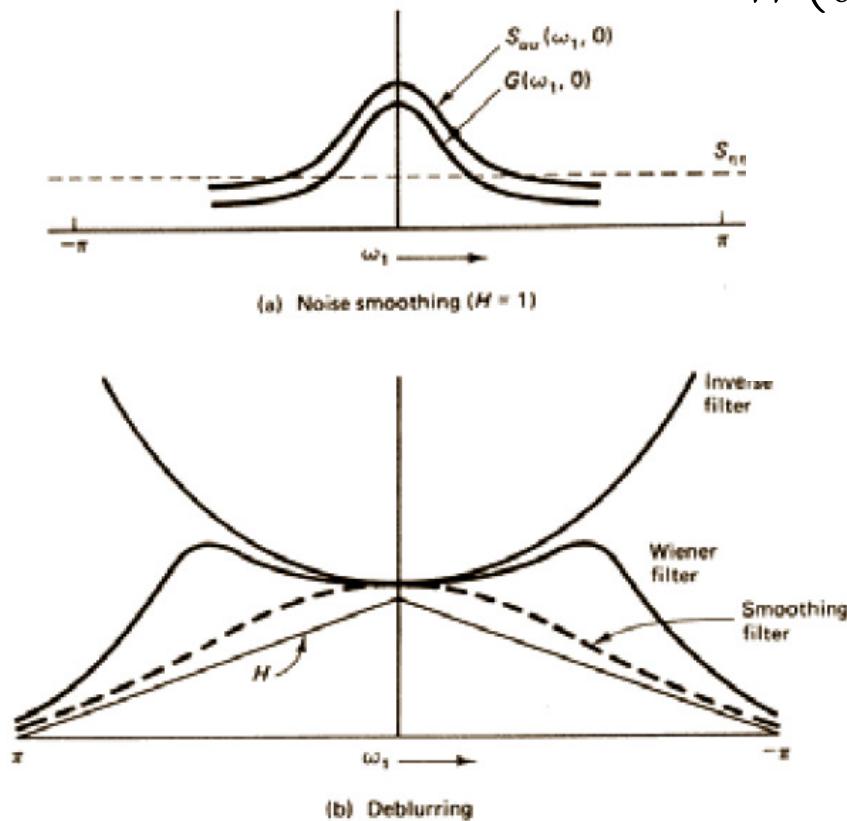


Figure 8.11 Wiener filter characteristics.

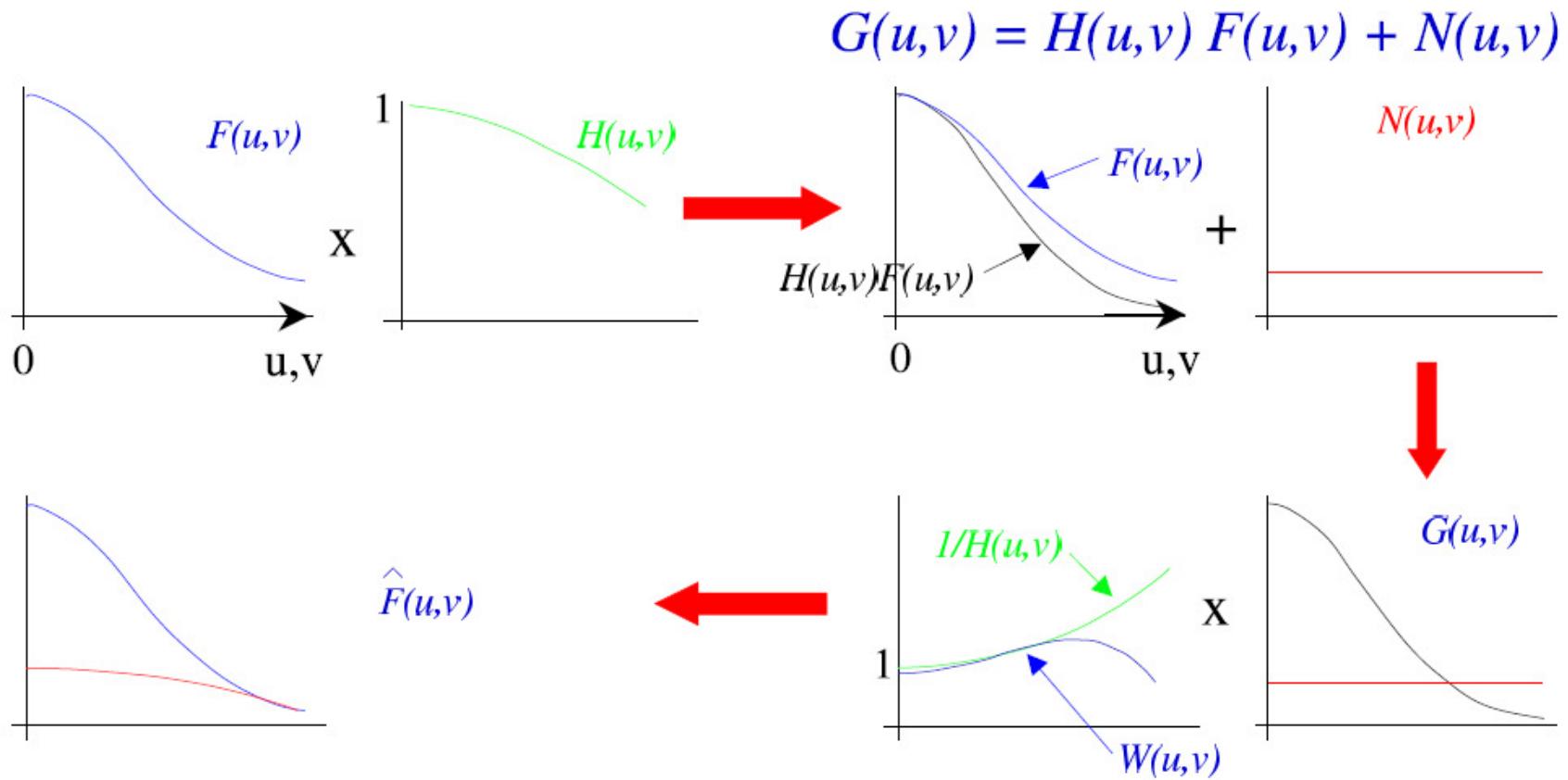
## Wiener Filter implementation

$$\begin{aligned}
 W(u, v) &= \frac{H^*(u, v)S_{ff}(u, v)}{|H(u, v)|^2S_{ff}(u, v) + S_{\eta\eta}(u, v)} \\
 &= \frac{H^*(u, v)}{|H(u, v)|^2 + \frac{S_{\eta\eta}}{S_{ff}}} \\
 &= \frac{H^*(u, v)}{|H(u, v)|^2 + K}
 \end{aligned}$$

$|F(u,v)|$  and  $|N(u,v)|$  are known approximately, or  
 $K$  is a constant (w.r.t.  $u$  and  $v$ ) chosen empirically to our knowledge of the noise level.

[Jain, Fig 8.11]

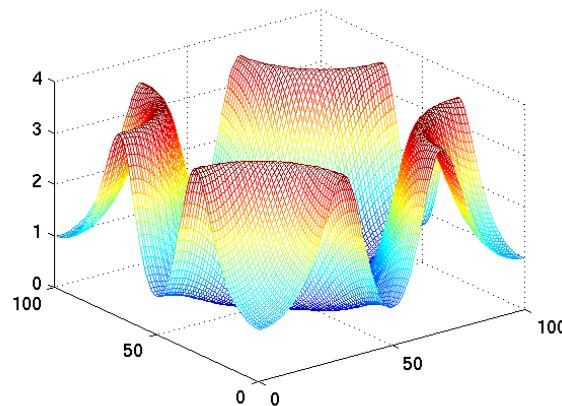
# Schematic effect of Wiener filter



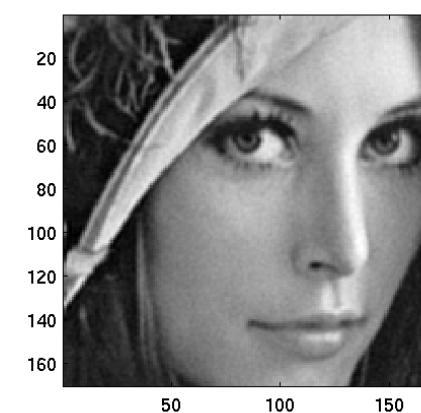
# Wiener Filter example

$$W(u, v) = \frac{H^*(u, v)}{|H(u, v)|^2 + K}$$

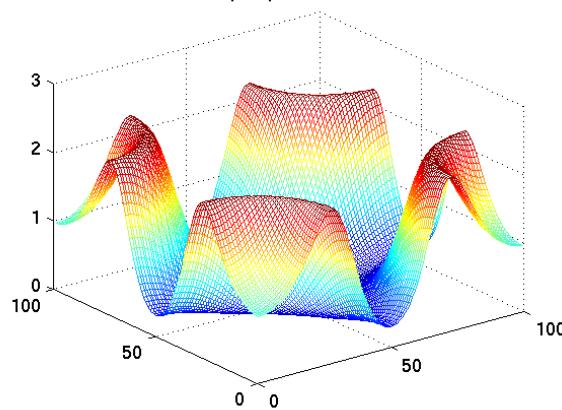
$G(u, v), K=0.02$



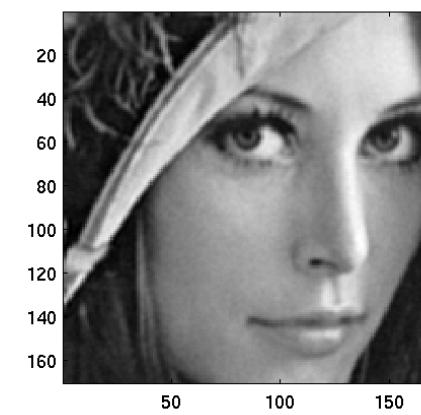
$K=0.02$



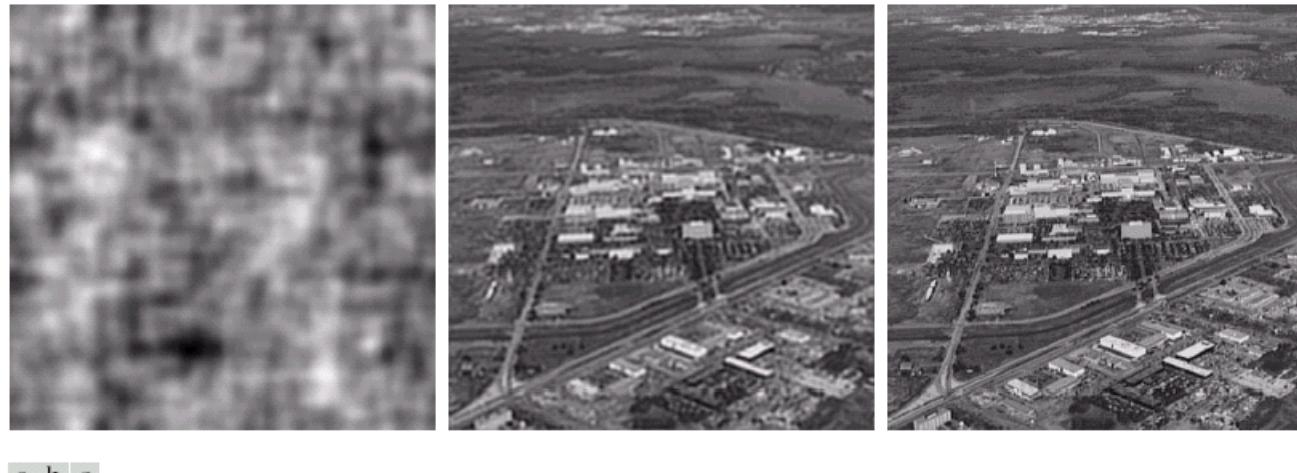
$G(u, v), K=0.05$



$K=0.05$



## Wiener filter example



a b c

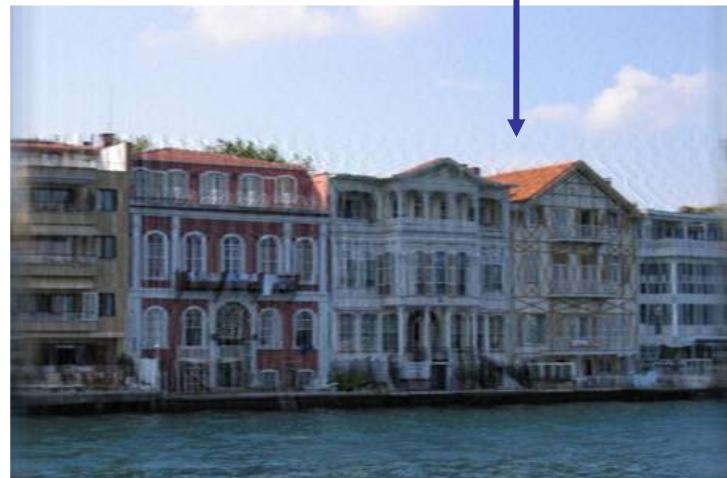
**FIGURE 5.28** Comparison of inverse- and Wiener filtering. (a) Result of full inverse filtering of Fig. 5.25(b). (b) Radially limited inverse filter result. (c) Wiener filter result.

- Wiener filter is more robust to noise, and preserves high-frequency details.

# Wiener filter example



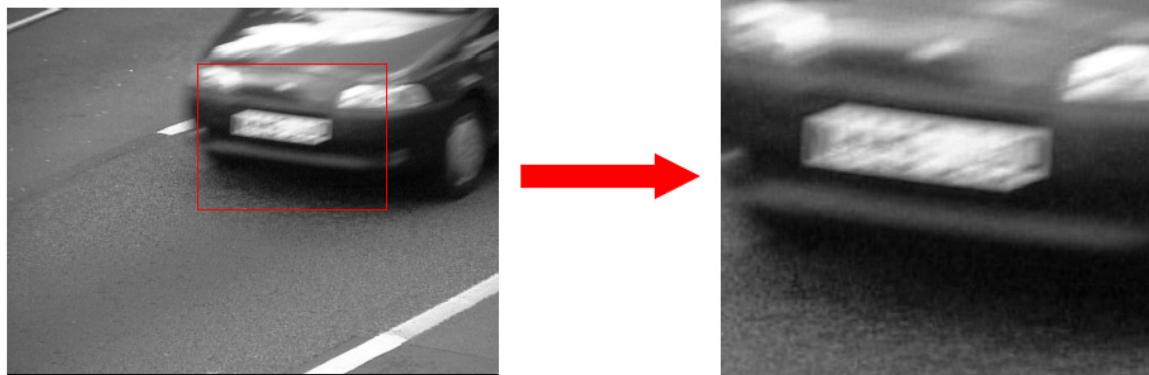
Ringing effect visible, too many high frequency components?



(a) Blurry image (b) restored w. regularized pseudo inverse  
(c) restored with wiener filter

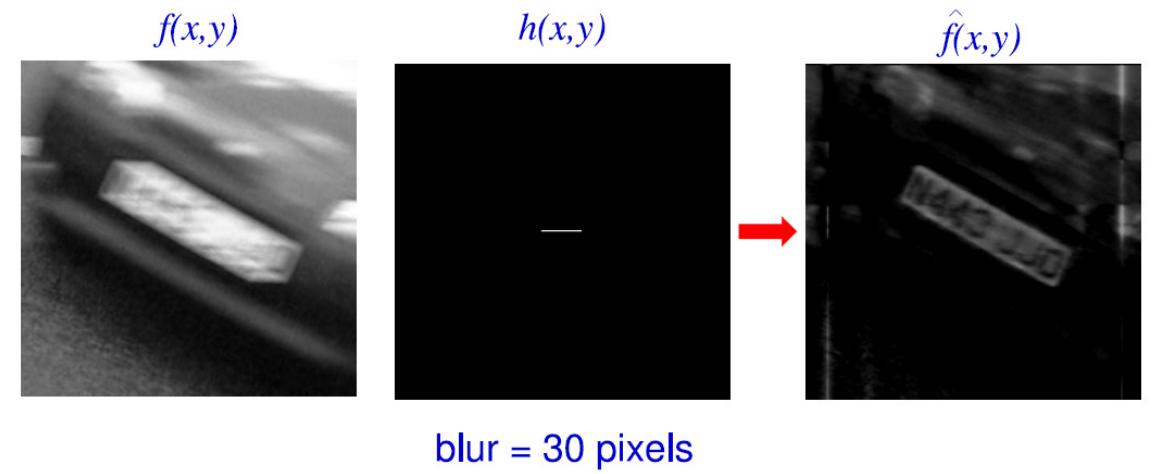
[UMD EE631]

# Another example: reading licence plates



## Algorithm

1. Rotate image so that blur is horizontal
2. Estimate length of blur
3. Construct a bar modelling the convolution
4. Compute and apply a Wiener filter
5. Optimize over values of K



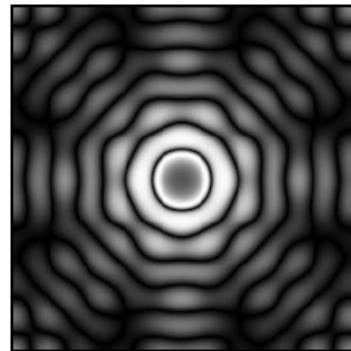
# Wiener filter: when does it not work?

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How much de-blurring is just enough?



*image 'blurrl'*



*wiener filter*



*restored license plate*

# Variations of Wiener filters

- geometric mean filters

$$W(u, v) = \left[ \frac{H * (u, v)}{|H(u, v)^2|} \right]^\alpha \left[ \frac{H^*(u, v)}{|H(u, v)|^2 + \beta \frac{S_{\eta\eta}(u, v)}{S_{ff}(u, v)}} \right]^{1-\alpha}$$

- Constrained Least Squares
  - Wiener filter emphasizes high-frequency components, while images tend to be smooth

$$\min_f |g - H\hat{f}|^2 + \alpha |C\hat{f}|^2$$

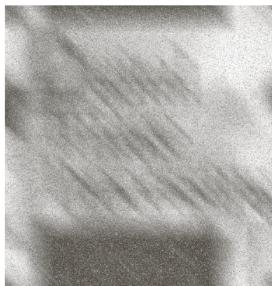
$\hat{f}$ : the estimate for undegraded image

$C\hat{f}$ : a high-passed version of  $\hat{f}$

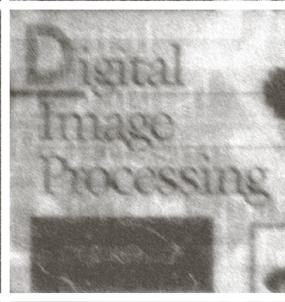
degraded    inverse-filtered    Wiener-filtered

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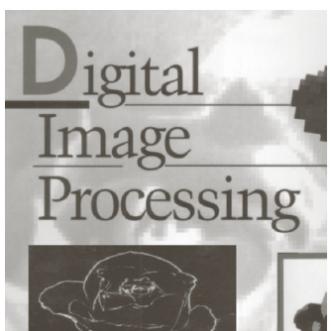
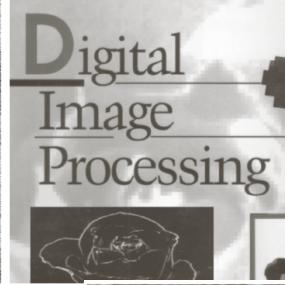
motion blur  
+ noise



$\text{noise} \times 10^{-1}$



$\text{noise} \times 10^{-5}$



a b c

**FIGURE 5.30** Results of constrained least squares filtering. Compare (a), (b), and (c) with the Wiener filtering results in Figs. 5.29(c), (f), and (i), respectively.

# Improve Wiener Filter

- Blind deconvolution

Wiener filter assumes both the image and noise spectrum are known (or can be easily estimated), in practice this becomes trial-and-error since noise and signal parameters are often hard to obtain.

$$\log |H|^2 = \log(S_{gg} - S_{\eta\eta}) - \log S_{ff}$$

$$S_{\eta\eta} \approx 0 \quad \Rightarrow \quad \log |H| \approx \frac{1}{M} \sum_{k=1}^M [\log|G_k| - \log|F_k|]$$

# Maximum-Likelihood (ML) Estimation

- $h(x,y)$   $H(u,v)$  unknown
- Assume parametric models for the blur function, original image, and/or noise
- Parameter set  $\theta$  is estimated by

$$\theta_{\text{ml}} = \arg\{\max_{\theta} p(y | \theta)\}$$

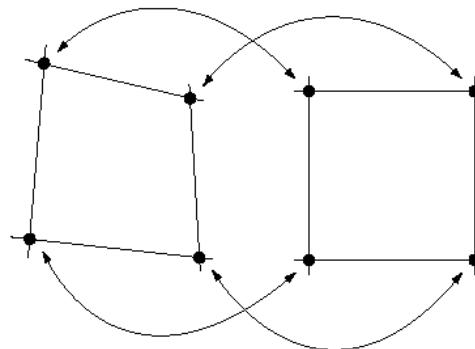
- Solution is difficult in general
- Expectation-Maximization algorithm
  - Guess an initial set of parameters  $\theta$
  - Restore image via Wiener filtering using  $\theta$
  - Use restored image to estimate refined parameters  $\theta$
  - ... iterate until local optimum

# geometric distortions

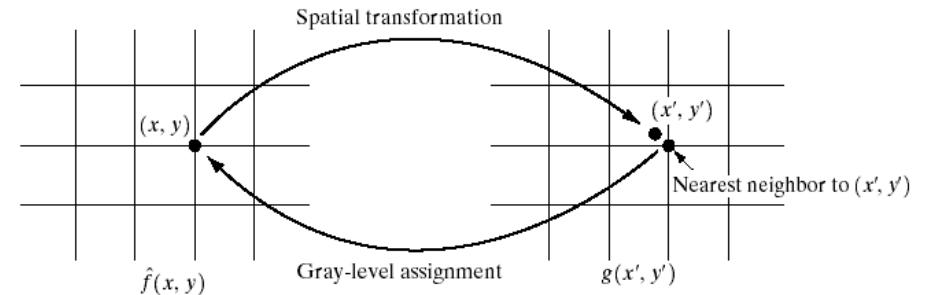
- Modify the spatial relationships between pixels in an image
- a. k. a. “rubber-sheet” transformations
- Two basic steps
  - Spatial transformation
  - Gray-level interpolation

$$x' = r(x, y)$$

$$y' = s(x, y)$$

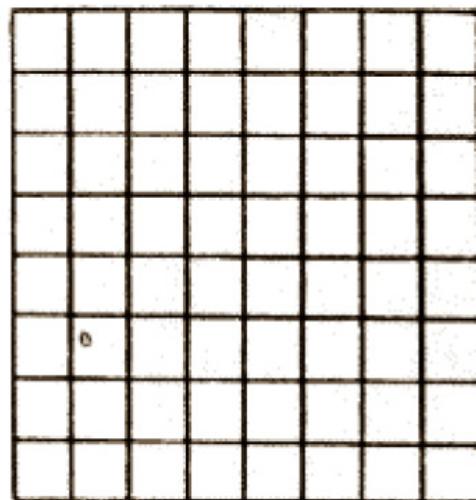


**FIGURE 5.32**  
Corresponding tiepoints in two image segments.

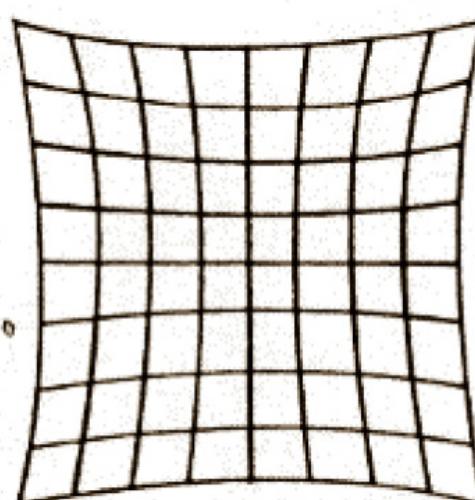


**FIGURE 5.33** Gray-level interpolation based on the nearest neighbor concept.

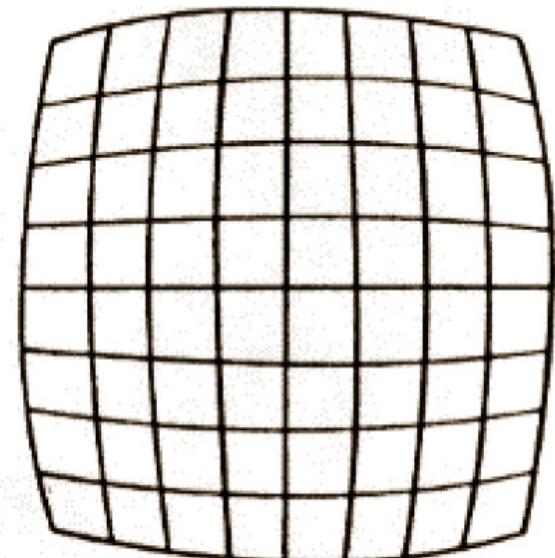
# geometric/spatial distortion examples



(a) Original



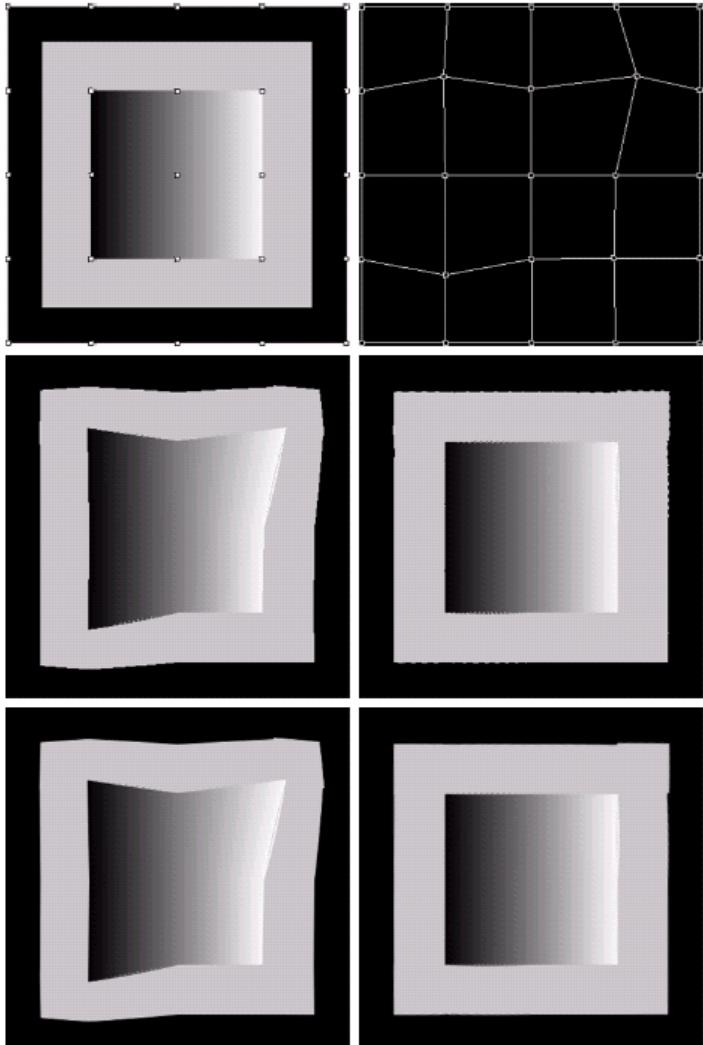
(b) Pincushion distortion



(c) Barrel distortion

**FIGURE 14.2-1.** Example of geometric distortion.

# recovery from geometric distortion



**FIGURE 5.34** (a) Image showing tiepoints. (b) Tiepoints after geometric distortion. (c) Geometrically distorted image, using nearest neighbor interpolation. (d) Restored result. (e) Image distorted using bilinear interpolation. (f) Restored image.

# recovery from geometric distortion



(a)



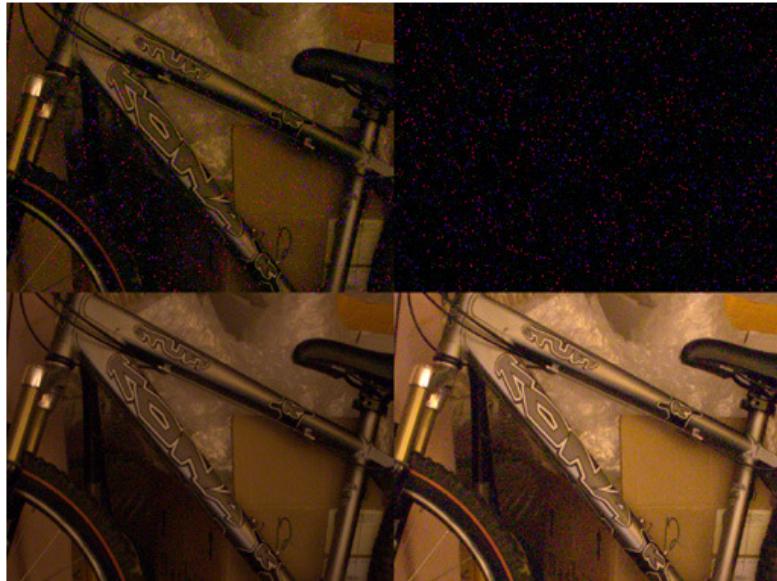
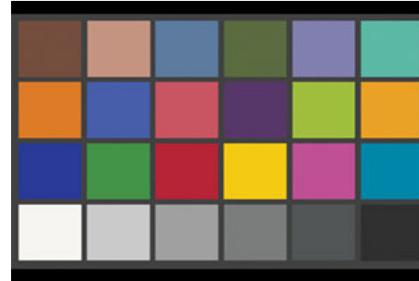
(b)

Fig. 5. (c) Image produced by a Comptar 2.5mm lens and a Comptar 1/3" CCD board camera. ( b ) Distortion parameters recovered via the minimization of  $\xi_3$  are used to map (a) to perspective image. Notice that straight lines in the scene, such as door edges, map to straight lines in the undistorted images.

Rahul Swaminathan, Shree K. Nayar: Nonmetric Calibration of Wide-Angle Lenses and Polycameras. IEEE Trans. Pattern Anal. Mach. Intell. 22(10): 1172-1178 (2000)

# estimating distortions

- calibrate
- use flat/edge areas
- ... ongoing work



a. Original  
 $BlurExtent = 0.0104$



b. Out-of-focus  
 $BlurExtent = 0.4015$



c. Original  
 $BlurExtent = 0.0462$



d. Linear-motion  
 $BlurExtent = 0.2095$

[http://photo.net/learn/dark\\_noise/](http://photo.net/learn/dark_noise/)

[Tong et. al. ICME2004]

# High-quality Motion Deblurring from a Single Image<sup>52</sup>

[Shan, Jia, and Agarwala, SIGGRAPH 2008]



"Our method computes a deblurred image using a unified probabilistic model of both blur kernel estimation and unblurred image restoration. ... include a model of the spatial randomness of noise in the blurred image, as well a new local smoothness prior that reduces ringing artifacts by constraining contrast in the unblurred image wherever the blurred image exhibits low contrast. Finally, we describe an efficient optimization scheme that alternates between blur kernel estimation and unblurred image restoration until convergence. As a result of these steps, we are able to produce high quality deblurred results in low computation time. "

# summary

- a image degradation model
- restoration from noise
- restoration from linear degradation
  - Inverse and pseudo-inverse filters, Wiener filter, constrained least squares
- geometric distortions
- readings
  - G&W Chapter 5.1 – 5.10, Jain 8.1-8.4 (at courseworks)

# who said distortion is a bad thing?



blur ...



noise ...



geometric ...

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