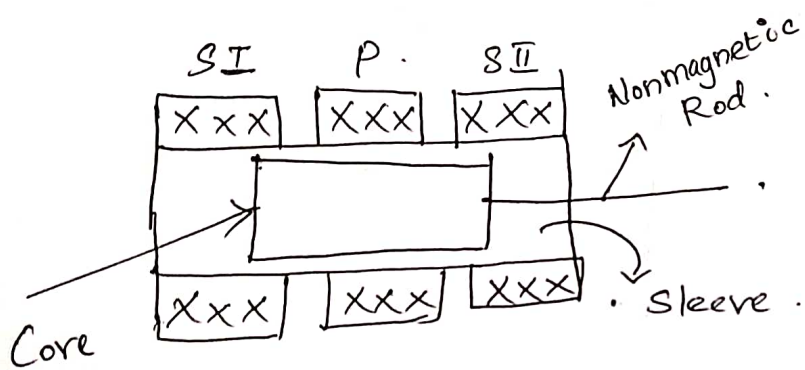


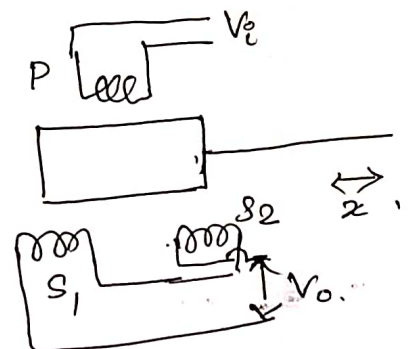
Linear Variable Differential Transformer (LVDT).

- Modified version of plunger type sensors
- arranged with two sets of coils, one as the primary and the other set as secondary having two coils connected differentially for providing the o/p.
- The coupling between primary and secondaries varies with the core plunger moving linearly.
- An alternating supply V_i and frequency f is impressed across the primary coil and depending on the position of the core w.r. to primary and two secondaries, an o/p voltage V_o is obtained from the secondaries.
- The induction in one secondary coil, according to the law is
$$V_{os} = - \frac{n d\phi}{dt} = - M \frac{di_p}{dt} \quad \text{--- (1)}$$
 - n → no of turns in the coil of secondary
 - ϕ → magnetic flux
 - M → Mutual Inductance b/w primary & secondary
 - i_p → primary current.

Scheme of an LVDT



equivalent model



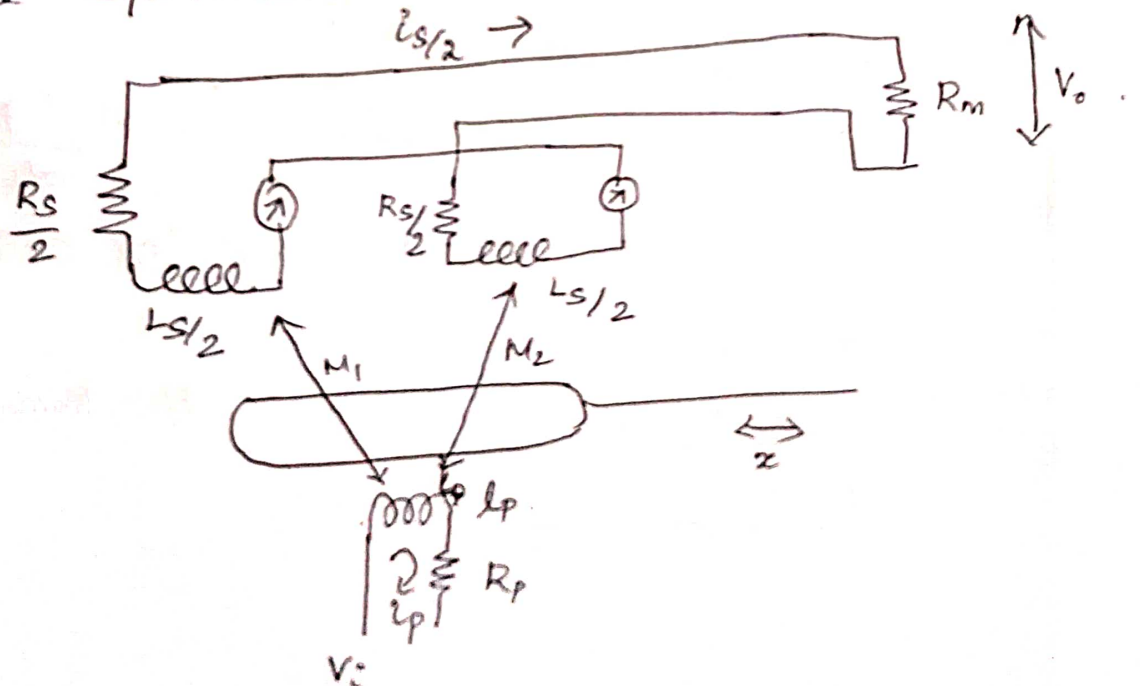
For the two coils differentially connected,

$$V_o = V_{os1} - V_{os2} = (M_1 - M_2) \frac{di_p}{dt} \quad - (2)$$

Both M_1 & M_2 being functions of x ,
 $M_1 - M_2 = M(x)$. If the function is linear
 over a certain range, $M(x) = kx$ so that

$$x = \frac{V_o}{k \left(\frac{di_p}{dt} \right)} \quad - (3)$$

Loss components are to be considered for
 obtaining o/p V_o per unit displacement of the core.
 The when arranged in a bridge in a
 differential manner, loss components be
 compensated by appropriate circuit components.
 The equivalent circuit of LVDT is



Solving for the magnitude ratio per unit displacement

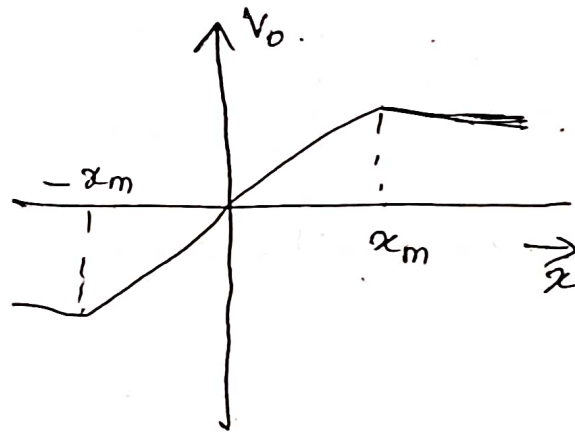
$\left| \frac{V_o}{V_i} \right| / \alpha$, angle by which the o/p voltage V_o ,
lags the i/p voltage V_i at $f = \frac{\omega}{2\pi}$ and
if the meter load is R_m , we get.

$$\left| \frac{V_o}{V_i} \right| \frac{1}{\alpha} = \frac{k \omega R_m / \{ (R_s + R_m) R_p \}}{\sqrt{[1 - \omega^2 (\tau_m^2 + \tau_p \tau_s)]^2 + \omega^2 (\tau_p + \tau_s)^2}}$$

$$\phi = 90^\circ - \tan^{-1} \frac{\omega (\tau_p + \tau_s)}{1 - \omega^2 (\tau_m^2 + \tau_p \tau_s)}$$

Where $\tau_m = \frac{M_1 - M_2}{\sqrt{(R_s + R_m) R_p}}$ $\tau_p = \frac{L_p}{R_p}$ $\tau_s = \frac{L_s}{R_s + R_m}$

The phase rectified secondary opp voltage V_o with x is shown in fig.



For a given V_o , linear range limits are indicated by $\pm x_m$. This limitation is inherent in all differential systems.