

- 1) a) ii (Recursively Enumerable)  
 b) iv (Infinite tape)  
 c)  $L = \{ \text{many addition} \}$   
 d) Transition rules

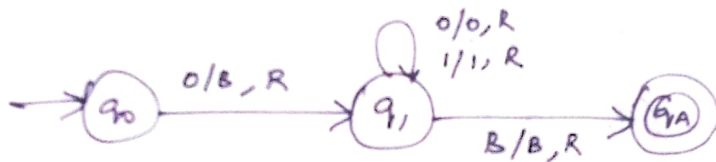
1)  $\delta(q_0, 0) = (q_1, B, R)$

2)  $\delta(q_1, 0) = (q_1, 0, R)$

3)  $\delta(q_1, 1) = (q_1, 0, R)$

4)  $\delta(q_1, B) = (q_A, B, R)$

c)



	0	1	B
→ q <sub>0</sub>	(q <sub>1</sub> , B, R)	-	-
q <sub>1</sub>	(q <sub>1</sub> , 0, R)	(q <sub>1</sub> , 0, R)	(q <sub>A</sub> , B, R)
* q <sub>A</sub>	-	-	-

f) Computing device

g)  $w = 000001000$

$q_0 000001000 B \vdash B q_1 00001000 B \vdash B 0 q_1 0001000 B$   
 $\vdash B 0 0 q_1 001000 B \vdash B 0 0 0 q_1 01000 B \vdash B 0 0 0 0 q_1 1000 B$   
 $\vdash B 0 0 0 0 0 q_1 000 B \vdash B 0 0 0 0 0 0 0 q_1 00 B \vdash B 0 0 0 0 0 0 0 0 q_1 0 B$   
 $\vdash B 0 0 0 0 0 0 0 0 0 q_1 B \vdash B 0 0 0 0 0 0 0 0 0 B q_A B$

∴ TM halts and input is computed.

Set A:

2) a) iv (Recursive)

b) iv) (L is recursive)

c) ~~proof~~

Let's assume red as a  
yellow as b

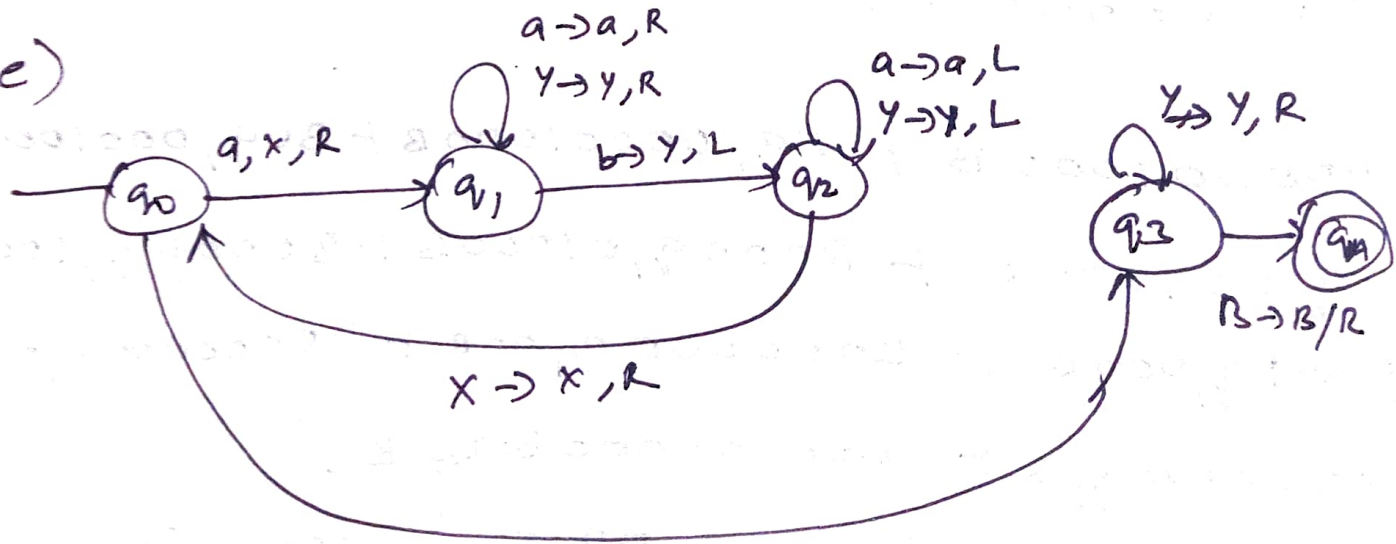
$$L = \{a^n b^n \mid n \geq 1\}.$$

## 1) Transition rules

- 1)  $\delta(q_0, a) = (q_1, x, R)$
- 2)  $\delta(q_1, a) = (q_1, a, R)$
- 3)  $\delta(q_1, b) = (q_2, y, L)$
- 4)  $\delta(q_2, a) = (q_2, a, L)$
- 5)  $\delta(q_2, x) = (q_0, x, R)$
- 6)  $\delta(q_1, y) = (q_1, y, R)$
- 7)  $\delta(q_2, y) = (q_2, y, L)$
- 8)  $\delta(q_0, y) = (q_3, y, R)$
- 9)  $\delta(q_3, y) = (q_3, y, R)$
- 10)  $\delta(q_3, b) = (q_A, b, R)$

d) transition diagram & table

e)



yellow as b

$$L = \{a^n b^n \mid n \geq 1\}.$$

d) transition diagram & table

e) encode the message.

Lets assume

$q_0 - 0$

$a - 0$

$L - 0$

$q_1 - 00$

$b - 00$

$R - 00$

$q_2 - 000$

$X - 000$

$q_3 - 0000$

$Y - 0000$

$q_A - 00000$

For each transition encode: ~~the~~ and the coded M

~~0~~ 01010010001001100101001010011

0010010001000010110001010001010

Similarly encode all transitions.

f) 

<u>List A</u>	<u>List B</u>
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RYX

YYYR

YYR

YRYR

RR

RRY

YY

YRY

a t have evolution because all the perm

yellow as b

$$L = \{a^n b^n \mid n \geq 1\}.$$

d) transition diagram & table

e) encode the message.

Let's assume

$q_0 - 0$

$a - 0$

$L - 0$

$q_1 - 00$

$b - 00$

$R - 00$

$q_2 - 000$

$X - 000$

$q_3 - 0000$

$Y - 0000$

$q_A - 00000$

For each transition encode: ~~the~~ and the coded

$\Rightarrow 01010010001001100101001010011$

$0010010001000010110001010001010$

Similarly encode all transitions.

f)

List A

List B

RYX

YYXR

YYR

YRYR

RR

RRY

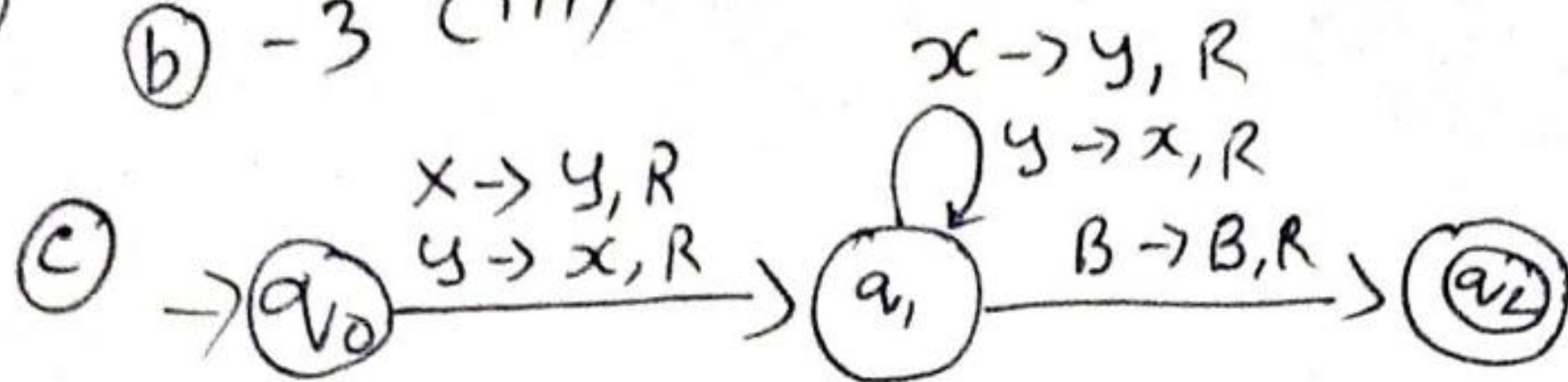
YY

YRY

Doesn't have solution. Because all the permutations  
combination doesn't give solution.



- ③ a - 3 (iii)  
b - 3 (iii)



d)  $\delta(q_0, x) = (q_1, y, R)$

$\delta(q_0, y) = (q_1, x, R)$

$\delta(q_1, x) = (q_1, y, R)$

$\delta(q_1, y) = (q_1, x, R)$

$\delta(q_1, B) = (q_2, B, R)$

step 1 = 
$$\frac{\#}{\#q_0 w \#}$$

step 2: Right moves

$$\frac{|x|}{q_0} = \frac{|y|}{q_1}$$

$$\frac{q_0 x}{y q_1} \quad \frac{q_0 y}{x q_1} \quad \frac{q_1 x}{y q_1} \quad \frac{q_1 y}{x q_1}$$

③  $\frac{x}{x} \quad \frac{y}{y} \quad \frac{B}{B}$

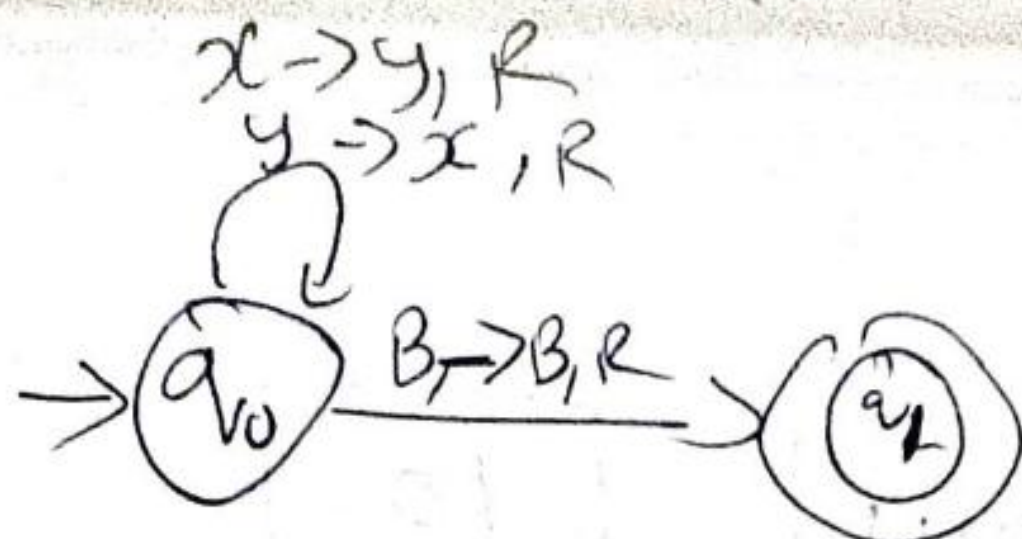
④  $\frac{x q_2}{q_2} \quad \frac{q_2 x}{q_2} \quad \frac{y q_2}{q_2} \quad \frac{q_2 y}{q_2}$

⑤  $\frac{\#}{\#} \quad \frac{\#}{B \#} \quad \text{⑥} \quad \frac{q_2 \# \#}{\#}$



(28)

①



$$\delta(q_0, x) = (q_0, y, R)$$

$$\delta(q_0, y) = (q_0, x, R)$$

$$\delta(q_0, B) = (q_1, \epsilon, R)$$

step 1 :  $\frac{\#}{\# q_0 w \#}$

step 2 :

$$\frac{q_0 x}{y q_0}$$

$$\frac{q_0 y}{x q_0}$$

③

$$\frac{x}{x}$$

$$\frac{y}{y}$$

$$\frac{B}{B}$$

④

$$\frac{x q_1}{q_1}$$

$$\frac{q_1 x}{q_1}$$

$$\frac{y q_1}{q_1}$$

$$\frac{q_1 y}{q_1}$$

⑤

$$\frac{\#}{\#}$$

$$\frac{\#}{B \#}$$

⑥

$$\frac{q_1 \# \#}{\#}$$



(e)

x	y	x	B
---	---	---	---

↑  
 $a_0$

y	y	x	B
---	---	---	---

↑  
 $a_1$

y	x	x	B
---	---	---	---

↑  
 $a_1$

y	x	y	B
---	---	---	---

↑  
 $a_2$

(or)

x	y	x	B
---	---	---	---

↑  
 $a_0$

y	y	x	B
---	---	---	---

↑  
 $a_0$

y	x	x	B
---	---	---	---

↑  
 $a_0$

y	x	y	B
---	---	---	---

↑  
 $a_1$



⑧

$$w = xyx$$

$$\frac{\#}{\# q_0 w \#}$$

$$\frac{\#}{\# q_0 x y x \#}$$

$$\frac{\#}{\# q_0 x y x \#}$$

$$\frac{q_0 x}{y q_1}$$

$$\frac{y}{y}$$

$$\frac{x}{x}$$

$$\frac{\#}{\#}$$

$$\frac{\#}{\#}$$

$$\frac{\#}{\#}$$

$$\frac{q_0 x}{y q_1}$$

...

It

loops