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### **Practical no. 3**

**Aim:** Write a program to recognize strings under 'a\*', 'a\*b+', 'abb'.

#### **Theory :**

##### **Automata – What is it?**

The term "Automata" is derived from the Greek word "αὐτόματα" which means "self-acting". An automaton (Automata in plural) is an abstract self-propelled computing device which follows a predetermined sequence of operations automatically.

An automaton with a finite number of states is called a Finite Automaton (FA) or Finite State Machine (FSM).

##### **Formal definition of a Finite Automaton**

An automaton can be represented by a 5-tuple  $(Q, \Sigma, \delta, q_0, F)$ , where –

- $Q$  is a finite set of states.
- $\Sigma$  is a finite set of symbols, called the alphabet of the automaton.
- $\delta$  is the transition function.
- $q_0$  is the initial state from where any input is processed ( $q_0 \in Q$ ).
- $F$  is a set of final state/states of  $Q$  ( $F \subseteq Q$ ).

#### **Related Terminologies**

##### **Alphabet**

- Definition – An alphabet is any finite set of symbols.
- Example –  $\Sigma = \{a, b, c, d\}$  is an alphabet set where 'a', 'b', 'c', and 'd' are symbols.

##### **String**

- Definition – A string is a finite sequence of symbols taken from  $\Sigma$ .
- Example – 'cabcad' is a valid string on the alphabet set  $\Sigma = \{a, b, c, d\}$

##### **Length of a String**

- Definition – It is the number of symbols present in a string. (Denoted by  $|S|$ ).
- Examples –
  - If  $S = \text{'cabcad'}$ ,  $|S| = 6$

- If  $|S|= 0$ , it is called an empty string (Denoted by  $\lambda$  or  $\epsilon$ )

### **Kleene Star**

- Definition – The Kleene star,  $\Sigma^*$ , is a unary operator on a set of symbols or strings,  $\Sigma$ , that gives the infinite set of all possible strings of all possible lengths over  $\Sigma$  including  $\lambda$ .
- Representation –  $\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \dots$  where  $\Sigma^p$  is the set of all possible strings of length  $p$ .
- Example – If  $\Sigma = \{a, b\}$ ,  $\Sigma^* = \{\lambda, a, b, aa, ab, ba, bb, \dots\}$

### **Kleene Closure / Plus**

- Definition – The set  $\Sigma^+$  is the infinite set of all possible strings of all possible lengths over  $\Sigma$  excluding  $\lambda$ .
- Representation –  $\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \cup \dots$   
 $\Sigma^+ = \Sigma^* - \{\lambda\}$
- Example – If  $\Sigma = \{a, b\}$ ,  $\Sigma^+ = \{a, b, aa, ab, ba, bb, \dots\}$

### **Language**

- Definition – A language is a subset of  $\Sigma^*$  for some alphabet  $\Sigma$ . It can be finite or infinite.
- Example – If the language takes all possible strings of length 2 over  $\Sigma = \{a, b\}$ , then  $L = \{ab, aa, ba, bb\}$

### **Deterministic Finite Automaton**

Finite Automaton can be classified into two types –

- Deterministic Finite Automaton (DFA)
- Non-deterministic Finite Automaton (NFA / NFA)

### **Deterministic Finite Automaton (DFA)**

In DFA, for each input symbol, one can determine the state to which the machine will move. Hence, it is called Deterministic Automaton. As it has a finite number of states, the machine is called Deterministic Finite Machine or Deterministic Finite Automaton.

### **Graphical Representation of a DFA**

A DFA is represented by digraphs called state diagram.

- The vertices represent the states.
- The arcs labeled with an input alphabet show the transitions.
- The initial state is denoted by an empty single incoming arc.
- The final state is indicated by double circles.

### Example

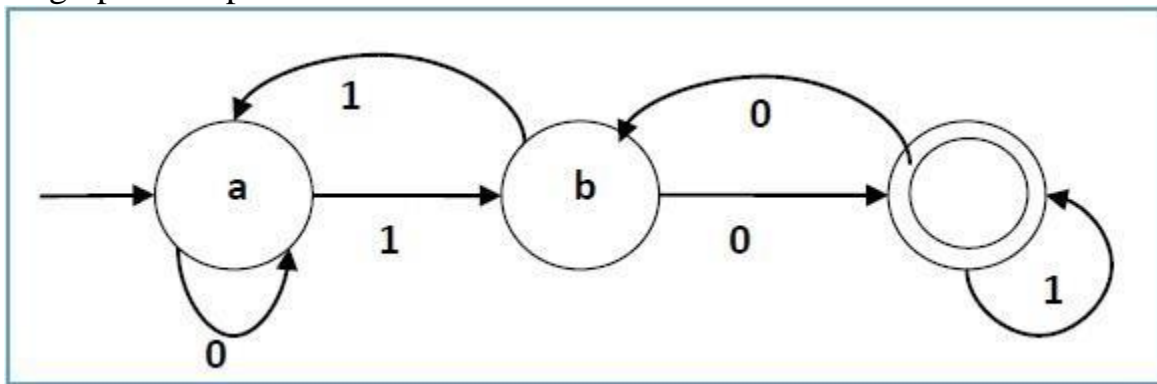
Let a deterministic finite automaton be  $\rightarrow$

- $Q = \{a, b, c\}$ ,
- $\Sigma = \{0, 1\}$ ,
- $q_0 = \{a\}$ ,
- $F = \{c\}$ , and

Transition function  $\delta$  as shown by the following table –

Present State	Next State for Input 0	Next State for Input 1
a	a	b
b	c	a
c	b	c

Its graphical representation would be as follows –



### Program Code:

```
#include<stdio.h>
#include<string.h>
#include<stdlib.h>
void main()
{
    char s[20],c;
    int state=0,i=0;
    printf("\n Enter a string :- ");
    gets(s);
    while(s[i]!='\0')
    {
        switch(state)
        {
```

```
case 0: c=s[i++];
        if(c=='a')
            state=1;
        else if(c=='b')
            state=2;
        else
            state=6;
break;
case 1: c=s[i++];
        if(c=='a')
            state=3;
        else if(c=='b')
            state=4;
        else
            state=6;
break;
case 2: c=s[i++];
        if(c=='a')
            state=6;
        else if(c=='b')
            state=2;
        else
            state=6;
break;
case 3: c=s[i++];
        if(c=='a')
            state=3;
        else if(c=='b')
            state=2;
        else
            state=6;
break;
case 4: c=s[i++];
        if(c=='a')
            state=6;
        else if(c=='b')
            state=5;
        else
            state=6;
break;
```

```

        case 5: c=s[i++];
                if(c=='a')
                    state=6;
                else if(c=='b')
                    state=2;
                else
                    state=6;
                break;
        case 6: printf("\n %s is not Recognised By the Automata.",s);
                exit(0);
            }
        }
    if((state==1)||(state==3))
        printf("\n %s is Accepted under rule 'a*'.",s);
    else if((state==2)||(state==4))
        printf("\n %s is Accepted under rule 'a*b+'.",s);
    else if(state==5)
        printf("\n %s is Accepted under rule 'abb'.",s);
    }
}

```

## Output:

Output

Clear

^

/tmp/D0cX2TbKZU.o

Enter a string :- aaaa

aaaa is Accepted under rule 'a\*'.

Output

Clear

^

/tmp/D0cX2TbKZU.o

Enter a string :- aaaabbbb

aaaabbbb is Accepted under rule 'a\*b+'.

```
Output Clear
/tmp/D0cX2TbKZU.o
Enter a string :- abb
abb is Accepted under rule 'abb'.|
```

```
Output Clear
/tmp/D0cX2TbKZU.o
Enter a string :- abbbb
abbbb is Accepted under rule 'a*b+'.|
```

```
Output Clear
/tmp/D0cX2TbKZU.o
Enter a string :- aabbaabba
aabbaabba is not Recognised By the Automata.|
```

**Conclusion :** In this practical we learnt how DFA recognizes patterns for identifiers, keywords.