

Binary Classification:

In this our dependent variable (y) is a discrete variable where it takes two values i.e. $y \in \{0,1\}$ where 0 represents negative class and 1 represents a positive class.

Examples:

Email : Spam or not ?

Online Transactions : Fraud or not ?

Tumor : malignant or Benign ?

Threshold classifier output : We use linear regression and map all predictions greater than 0.5 as a 1 and all less than 0.5 as a 0. However, this method doesn't work well because classification is not actually a linear function.

What if we use linear reg for classification problem ?

If we use linear regression model then our predicted output might be <0 or sometimes it might be >1 , both the cases are not suitable for classification problem.

We can use classification algorithms such as **logistic Regression** for the binary classification.

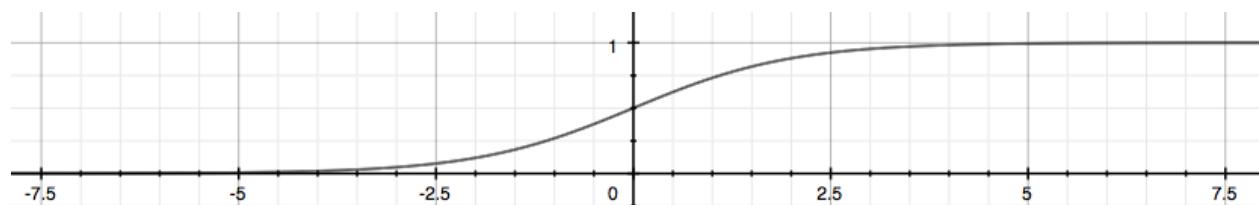
Logistic Regression :

Our goal is to have our hypothesis function between 0 to 1, i.e. $0 \leq h_{\theta}(x) \leq 1$.

θ

For Logistic regression we modify our hypothesis function as $h_{\theta}(x) = g(h_{\theta}(x))$, i.e. $h_{\theta}(\theta^T X) = \frac{1}{1+e^{-\theta^T X}}$

where $g(z)$ is a logistic/sigmoid function, where $g(z) = \frac{1}{1+e^{-z}}$, the graph looks like below.



Interpretation of Hypothesis Output:

$h_{\theta}(x)$ = estimated probability that $y=1$ on input x .

Example of cancer prediction : $h_{\theta}(x) = 0.7 \rightarrow$ it tells that 70% chance of tumor being malignant tumor.

Another way of notation is $h_{\theta}(x) = P(y=1/x; \theta) \rightarrow$ "probability that $y=1$, given x , parameterized by θ "

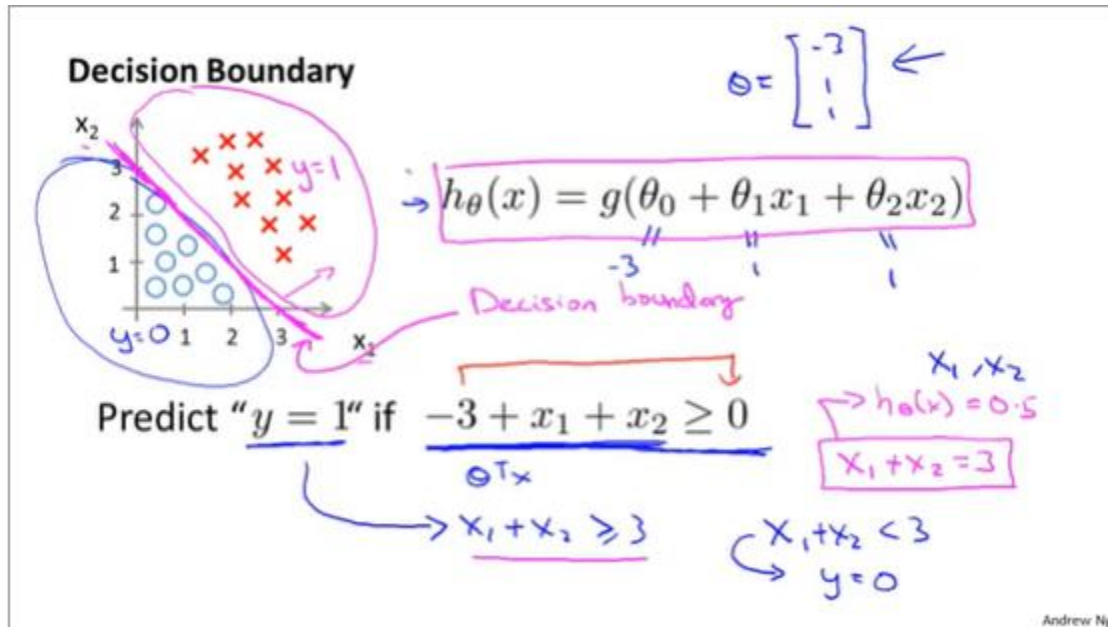
Also, $P(y=1/x; \theta) + P(y=0/x; \theta) = 1$.

Decision Boundary :

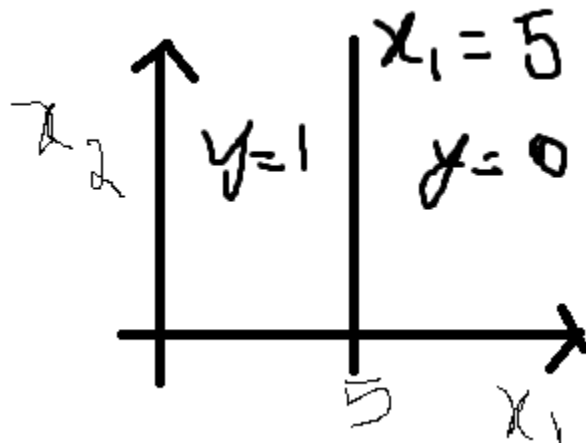
From sigmoid graph, we can say that $g(z) \geq 0.5$ when $z \geq 0$, suppose if $z=0 \rightarrow g(z) = 1/2$

That is

- for $y=1$, $\rightarrow g(\theta^T X) \geq 0.5$ i.e. $(\theta^T X) \geq 0$. Similarly
- for $y=0 \rightarrow g(\theta^T X) < 0.5$ i.e. $(\theta^T X) < 0$.

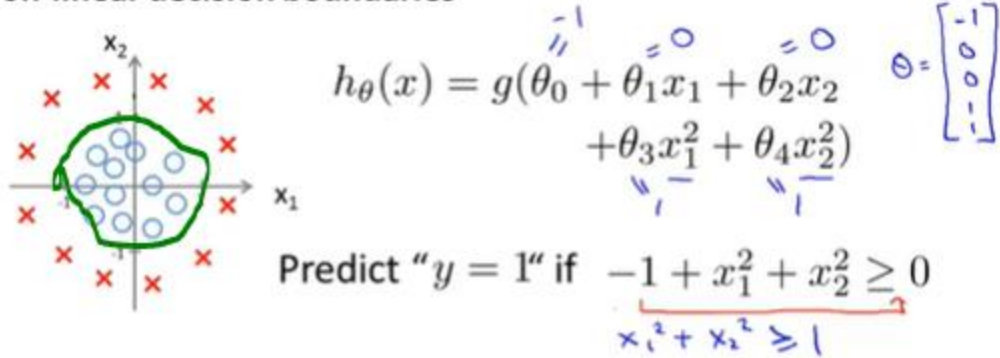


- Consider logistic regression with two features x_1 and x_2 . Suppose $\theta_0 = 5$, $\theta_1 = -1$ and $\theta_2 = 0$, so that $h_\theta(x) = g(5 - x_1)$. Which of these shows the decision boundary of $h_\theta(x)$?
- For $y=1$, $\theta^T X$ i.e. $5 - x_1 \geq 0 \rightarrow x_1 \leq 5$ is the required decision Boundary equation.



- The decision boundaries might not always be linear, it can also be non-linear as well.

Non-linear decision boundaries



Cost Function for Logistic Regression:

Training set : $\{(x^1, y^1), (x^2, y^2), \dots, (x^m, y^m)\}$, m examples and we have our $X \in \begin{bmatrix} x^0 \\ \vdots \\ x^n \end{bmatrix}$ i.e. a $(n+1)$ dimensional vector and $y \in \{0, 1\}$.

Our hypothesis/Objective function, $h_{\theta}(\theta^T X) = \frac{1}{1 + e^{-\theta^T X}}$

Now how to choose parameters θ ?

Out Scope : Usage of 1x1 convolution ?

We can shrink the number of channels, based on the number of 1x1 convolutional filters.