Training Discriminator

$$\max_{D} V(D) = \mathbb{E}_{x \sim p_{data}(x)}[log D(x)] + \mathbb{E}_{z \sim p_{z}(z)}[log(1 - D(z))]$$

Training Generator

$$\max_{G} V(G) = \mathbb{E}_{z \sim p_z(z)}[log(1 - D(G(z)))]$$

GAN for Image Colorization

$$\min_{\theta_G} J^{(G)}(\theta_D, \theta_G) = \min_{\theta_G} - \mathbb{E}_z[log(D(G(0_z|x)))] + \lambda \parallel G(0_z|x) - y \parallel 1$$

$$\max_{\theta_G} J^{(D)}(\theta_D, \theta_G) = \max_{\theta_D} (\mathbb{E}_y[log(D(y|x))] + \mathbb{E}_z[log(1 - D(G(0_x|x)|x))])$$