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# Visually Grounded Reasoning about Temporal Concepts in Selective Attention Memory

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## Abstract

1 Visual reasoning in videos requires understanding temporal concepts in addition  
2 to the objects and their relations in a given frame. In analogy with human reason-  
3 ing, we present Selective Attention Memory network (SAMNet), an end-to-end  
4 differentiable recurrent model equipped with external memory. SAMNet can per-  
5 form multi-step reasoning on a frame-by-frame basis, and dynamically control  
6 information flow to the memory to store context-relevant representations to answer  
7 questions. We tested our model on the COG dataset (a multi-frame visual question  
8 answering test), and outperformed the state of the art baseline for hard tasks and in  
9 terms of generalization.

## 10 1 Introduction

11 Integration of vision and language in deep neural network models allows the system to learn joint  
12 representations of objects, concepts, and relations. Potentially, this approach can address Harnad’s  
13 “symbol grounding problem” [Har03] and lead to visually grounded language learning.

14 Starting with the Visual Question Answering (VQA) dataset [AAL<sup>+</sup>15], a variety of tasks that  
15 integrate vision and language have emerged in the past several years [MKK19]. Going beyond  
16 classification and object detection, the core emphasis in these tasks is *visual reasoning* that tackles  
17 spatial aspects such as comparison of object attributes, counting and other relational questions.

18 In contrast to VQA, which comes with static image and question pairs, another emerging direction is  
19 Video QA [], that provides an additional opportunity to work on *temporal* relations and reasoning.  
20 As evident from human cognition, attention and memory are the key competencies required to solve  
21 these problems, and unsurprisingly, the AI research is rapidly growing in these areas.

22 The ability to deal with time can pose a challenge for natural language processing (NLP), e.g. in  
23 question answering (QA) and dialog applications. Current NLP solutions, in certain problem settings,  
24 work around this challenge by processing the entire text input and reason over it multiple times  
25 using attention [VSP<sup>+</sup>17] or other mechanisms. For example, solutions to the bAbI reasoning task  
26 (e.g. Memory Networks [WBC<sup>+</sup>15]), typically involve processing the supporting facts all at once,  
27 which reside in memory and available to provide answers. Similarly, in Visual Dialog [DKG<sup>+</sup>17] the  
28 system keeps the whole history of the dialog in memory. In real-time dialog or video QA, there may  
29 not be such an opportunity to have the question and entire visual data all at once in the beginning.

30 Video reasoning datasets such as SVQA (Synthetic Video Question Answering) [SSCH18] and  
31 COG [YGW<sup>+</sup>18] have limited number of frames (e.g. 4-16 frames), and therefore manageable by the  
32 neural net models to process and represent all of the visual information. As an example, according  
33 to [SSCH18] the authors extracted visual features from each frame and aggregated features of all  
34 clips from one video to form a sequential video representation.

**Contributions.** Inspired by human cognitive capacity to selectively pay attention and store salient information in memory, we introduce a new model that can dynamically process video input frame-by-frame, reason over images and remember the salient concepts to answer questions. Our results based on the COG dataset [YGW<sup>+</sup>18] indicate that the model is capable of: (1) learning the temporal association, i.e., grounding the time-related words with meaning; (2) learning complex, multi-step reasoning that involves grounding of words and visual representations of objects/attributes; (3) selectively control the flow of information to and from the memory to answer questions; and (4) updating the memory only with relevant visual information depending on the temporal context.

## 2 Selective Attention Memory (SAM) Network

SAM Network (SAMNet for short) is an end-to-end differentiable recurrent model equipped with an external memory (Figure 1). The model makes a single pass over the frames in temporal order, accessing one frame at a time. The memory locations store relevant objects representing contextual information about words in text and visual objects extracted from video. Each location of the memory stores a  $d$ -dimensional vector. The memory can be accessed through either content-based addressing, via dot-product attention, or location-based addressing. Using gating mechanisms, correct objects can be retrieved in order to perform multi-step spatio-temporal reasoning over text and video.

The core of SAMNet is a recurrent cell called a SAM Cell (Figure 2). Unrolling a new series of  $T$  cells for every frame enables  $T$  steps of compositional reasoning. Information flows between frames through the external memory. During the  $t$ -th reasoning step, for  $t = 1, 2, \dots, T$ , SAM Cell maintains the following information as part of its recurrent state:

(a)  $c_t \in \mathbb{R}^d$ , the control state used to drive the reasoning over objects in the frame and memory; and (b)  $so_t \in \mathbb{R}^d$ , the summary visual object representing the relevant object for step  $t$ . Let

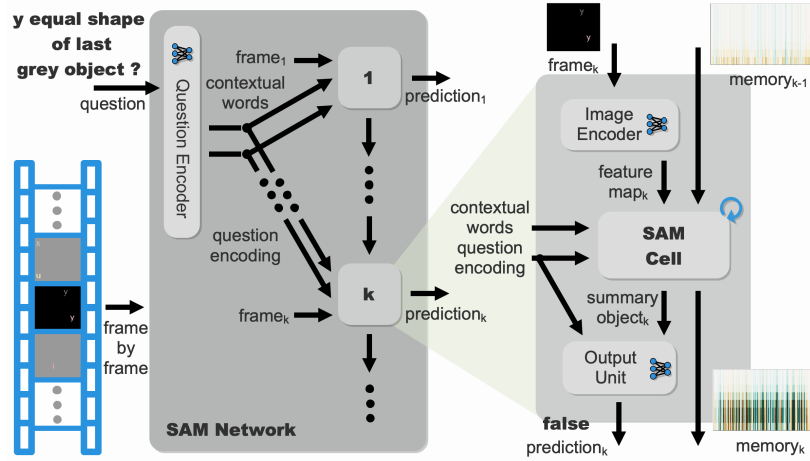


Figure 1: General architecture of SAMNet

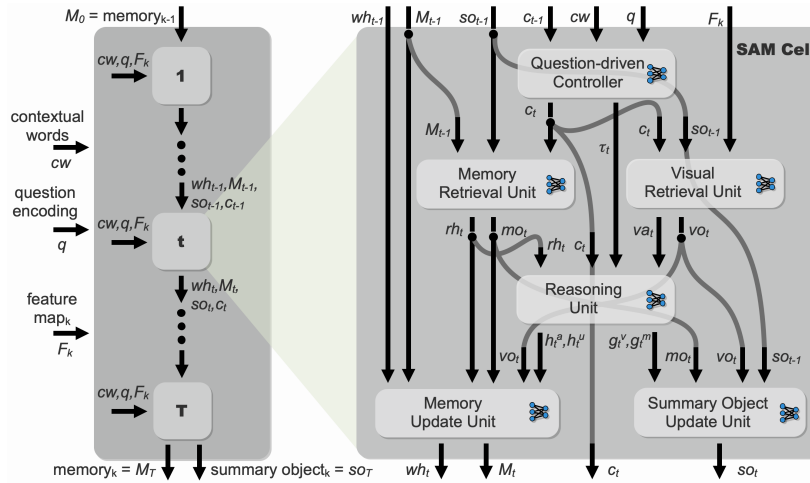


Figure 2: Single reasoning step in SAMCell

91  $M_t \in \mathbb{R}^{N \times d}$  denote the external memory with  $N$  slots at the end of step  $t$ . Let  $wh_t \in \mathbb{R}^N$  denote  
 92 an attention vector over the memory locations; in a trained model,  $wh_t$  points to the location of first  
 93 empty slot in memory for adding new objects.

94 **Question-driven Controller.** This module drives attention over the question to produce  $k$  control  
 95 states, one per reasoning operation. The control state  $c_t$  at step  $t$  is then fed to a *temporal classifier*, a  
 96 two-layer feedforward network with ELU activation used in the hidden layer of  $d$  units. The output  
 97  $\tau_t$  of the classifier is intended to represent the different temporal contexts (or lack thereof) associated  
 98 with the word in focus for that step of reasoning. For the COG dataset we pick 4 classes to capture  
 99 the terms labeled “last”, “latest”, “now”, and “none”.

100 The visual retrieval unit uses the information generated above to extract a relevant object  $vo_t$  from the  
 101 frame. A similar operation on memory yields the object  $mo_t$ . The memory operation is based on an  
 102 attention mechanism, and resembles content-based addressing on memory. Therefore, we obtain an  
 103 attention vector over memory addresses that we interpret to be the *read head*, denoted by  $rh_t$ . Note  
 104 that the returned objects may be invalid, e.g., if the current reasoning step focuses on the phrase “last  
 105 red square”,  $vo_t$  is invalid even if the current frame contains a red square.

106 **Reasoning Unit.** This module is the backbone of SamNet that determines what gating operations  
 107 need to be performed on the external memory, as well as determining the location of the correct  
 108 object for reasoning.

109 To determine whether we have a valid object from frame (and similarly for memory), we execute  
 110 the following reasoning procedure. First, we take the visual attention vector  $va_t$  of dimension  $L$ ,  
 111 where  $L$  denotes the number of feature vectors for the frame, and compute a simple aggregate  
 112  $vs_t = \sum_{i=1}^L [va_t(i)]^2$ . It can be shown mathematically that the more localized the attention vector  
 113 is, the higher is the aggregate value. We perform a similar computation on the read head  $rh_t$  over  
 114 memory locations. We feed these 2 values along with the temporal class weights  $\tau_t$  to a 3-layer  
 115 feedforward classifier with hidden ELU units to extract 4 gating values in  $[0, 1]$  modulated for the  
 116 current reasoning step: (a)  $g_t^v$ , which determines whether there is a valid visual object; (b)  $g_t^m$ ,  
 117 which determines whether there is a valid memory object. (c)  $h_t^r$ , which determines whether the  
 118 memory should be updated by replacing a previously stored object with a new one; and (d)  $h_t^a$ , which  
 119 determines whether a new object should be added to memory. We stress that the network has to learn  
 120 via training how to correctly implement these behaviors.

121 **Memory Update Unit.** We first determine the exact location where an object could be added to the  
 122 memory using the following equation:

$$w_t = h^r \cdot rh_t + h^a \cdot wh_{t-1}$$

123 Above,  $w_t$  denotes the pseudo-attention vector that represents the “location” where the memory  
 124 update should happen. The sum of components of  $w$  is at most equal to 1; and  $w_t$  can even equal 0  
 125 whenever neither condition of adding a new object nor replacing an existing object holds true. We  
 126 then update the memory accordingly as:

$$M_t = M_{t-1} \odot (J - w_t \otimes \mathbf{1}) + w_t \otimes vo_t,$$

127 where  $vo_t$  denotes the object returned by the visual retrieval unit. Here  $J$  denotes the all ones matrix,  
 128  $\odot$  denotes the Hadamard product and  $\otimes$  denotes the Kronecker product. Note that the memory is  
 129 unchanged in the case where  $w_t = 0$ , i.e.,  $M_t = M_{t-1}$ . We finally update the write head so that it  
 130 points to the succeeding address if an object was added to memory or otherwise stay the same. Let  
 131  $wh'_{t-1}$  denote the circular shift to the right of  $wh_{t-1}$  which corresponds to the soft version of the  
 132 head update. Then:

$$wh_t = h^a \cdot wh'_{t-1} + (1 - h^a) \cdot wh_{t-1}$$

133 **Summary Update Unit.** This unit updates the (recurrent) summary object to equal the outcome of  
 134 the  $t$ -th reasoning step. We first determine whether the relevant object  $ro_t$  should be obtained from  
 135 memory or the frame according to:

$$ro_t = g_t^v \cdot vo_t + g_t^m \cdot mo_t$$

136 Note that  $ro_t$  is allowed to be a null object (i.e. 0 vector) in case neither of the gates evaluate to true.  
 137 Finally,  $so_t$  is the output of a simple linear layer whose inputs are  $ro_t$  and the previous summary  
 138 object  $so_{t-1}$ . This serves to retain additional information that was in  $so_{t-1}$ , e.g., if it held the partial  
 139 result of a complex query with Boolean connectives.

140 For more details of the various modules, please see the appendix.

### 3 Experiments

We evaluated SAMNet on the COG dataset [YGW<sup>+</sup>18]. Our experiments were designed to study SAMNet’s performance as well as its generalization abilities in different settings. For this purpose, we used two different variants of the COG dataset: an easy one (Canonical) and a Hard version to explore a wide range of difficulties. The main differences are the number of frames in the input sequence (4 vs. 8) and the maximum number of distractors (i.e., objects not relevant for the answer) per frame (1 vs. 10).

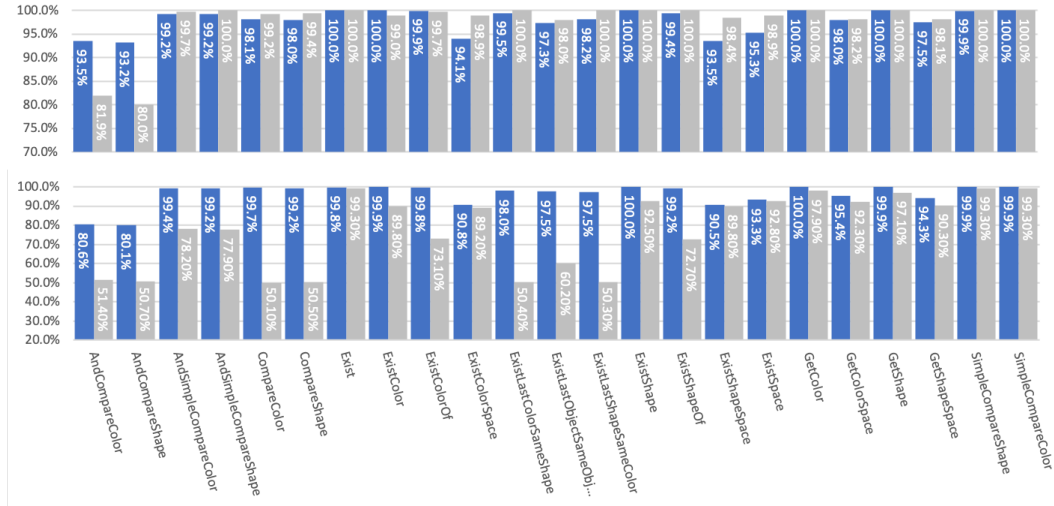


Figure 3: Comparison of test set accuracies of SAMNet (blue) with original results achieved by the COG model (gray) on Canonical (top) and Hard (bottom) variants of the COG dataset.

We have implemented and trained our SAMNet model using MI-Prometheus [KMM<sup>+</sup>18], a framework based on Pytorch [?]. In our experiments, we have focused on 22 classification tasks and compared our results with the baseline model, as presented in Figure 3. For the Canonical variant (top row), we have achieved similar accuracies for the majority of tasks (with the total average accuracy of 98.0% in comparison of 97.6% achieved by the COG model), with significant improvements (around 13 points) for *AndCompare* tasks. As those tasks focus on compositional questions referring to two objects, we hypothesize that our model achieved better accuracy due to the ability to selectively pick and store the relevant objects from the past frames in the memory. Despite there are some tasks in which our model reached slightly lower accuracies, when comparing performances on the Hard variant, it dominates COG baseline on all tasks, with improvements varying from 0.5 to more than 30 points.

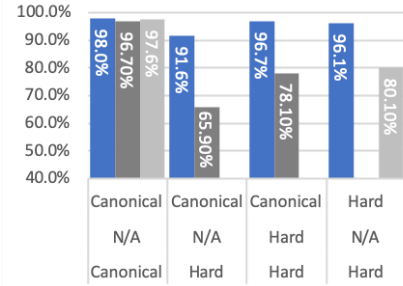


Figure 4: Total accuracies of SAMNet (blue) and COG models (light/dark gray) when testing generalization from Canonical to Hard variants of the dataset.

The goal of the next set of experiments was to test the generalization ability concerning the sequence length and number of distractors. For that purpose, we have compared the accuracies of both models when trained on the Canonical variant and tested on Hard (Figure 4). As the original paper does not include such experiments, we have performed them on our own. The light gray color indicates the original results, whereas dark gray indicates the accuracies of COG models that we have trained (fine-tuning/testing) using the original code provided by the authors. For sanity check, in the first column, we report both the best-achieved score and the score reported in the paper when training and testing on Canonical variant, without any fine-tuning (N/A in the second row from the bottom). In a pure *transfer learning* setup (second column), our model shows enormous generalization ability, reaching 91.6% accuracy on the test set. We have also tested both models in a setup where the model

176 trained on a Canonical variant underwent additional fine-tuning (for a single epoch) on the Hard  
177 variant (third column). In this case, the SAMNet model also reached much better performance, and,  
178 interestingly, achieved better scores from the model trained and tested exclusively on the Hard variant.  
179 In summary, the results clearly indicate that the mechanisms introduced in SAMNet enable it to learn  
180 to operate independently of the total number of frames or number of distractions, and allow it to  
181 generalize to longer videos and more complex scenes.

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## 210 4 Appendix

## 211 5 VWM model

212 *Notation.* Treat 1D tensors as column vectors and 2D tensors as matrices, where appropriate. We use  
 213 lower case to represent both 1D and 2D tensors but occasionally use upper case for 2D tensors where  
 214 matrix operations are involved.

- 215 1. Let  $\Delta^d = \{(x_0, x_1, \dots, x_d) : x_0 + x_1 + \dots + x_d = 1, x_i \geq 0, i = 0, 1, \dots, d\}$  denote the  
 216 standard  $d$ -simplex.
- 217 2. Let  $\circ$  denote concatenation of two tensors with identical shape except possibly for their last  
 218 dimensions  $d_1$  and  $d_2$ , respectively, resulting in a tensor with last dimension of  $d_1 + d_2$ .
- 219 3. Let  $\odot$  denote element-wise product of two tensors of same shape, i.e., Hadamard product for  
 220 vectors/matrices.
- 221 4. Let  $\otimes$  denote tensor product of two tensors, i.e. Kronecker product for vectors/matrices.

## 222 6 Basic layers/modules

### 223 Linear (Affine) Layer

224 **Inputs:** A tensor  $x$  with last dimension  $n$ .

225 **Parameter:** An affine function  $\mathcal{G} : \mathbb{R}^n \rightarrow \mathbb{R}^m$  with weight and bias parameters.

226 **Output:** A tensor  $y$  with last dimension  $m$ , and remaining dimensions same as that of  $x$ , obtained  
 227 by applying  $\mathcal{G}$  to each 1D slice of  $x$  along the last dimension.

### 228 Attention Module

229 **Inputs:**

- 230 1. Query:  $q \in \mathbb{R}^d$
- 231 2. Keys:  $K \in \mathbb{R}^{N \times d}$
- 232 3. Values:  $V \in \mathbb{R}^{N \times d}$ . By default  $V = K$ , unless mentioned explicitly.

233 **Parameter:** Weight  $w \in \mathbb{R}^d$

234 **Outputs:**

- 235 1. Content vector:  $h = V^T u \in \mathbb{R}^d$
- 236 2. Attention vector:  $w = \text{softmax}(K(w \odot q)) \in \mathbb{R}^N$

### 237 Interaction Module

238 **Inputs:**

- 239 1. Base object:  $b \in \mathbb{R}^d$
- 240 2. Feature objects:  $f \in \mathbb{R}^{M \times d}$

241 **Parameters:**

- 242 1. Base object projection linear layer:  $\mathcal{G} : \mathbb{R}^d \rightarrow \mathbb{R}^d$
- 243 2. Feature objects projection linear layer:  $\mathcal{K} : \mathbb{R}^{M \times d} \rightarrow \mathbb{R}^{M \times d}$
- 244 3. Modifier linear layer:  $\mathcal{H} : \mathbb{R}^{M \times 2d} \rightarrow \mathbb{R}^{M \times d}$

245 **Output:** Modified feature objects  $f' = \mathcal{H}(\mathcal{K}(f) \odot (\mathbf{1} \otimes \mathcal{G}(b))) \in \mathbb{R}^{M \times d}$

246

## 247 7 VWM cell

248 The VWM recurrent cell is executed for  $T$  reasoning steps for every frame in the temporal order.  
 249 Within a single frame, the cell state at the end of each reasoning step  $t = 1, 2, \dots, T$  is denoted by  
 250  $(c_t, M_t, o_t)$ , where:

- 251 1.  $c_t \in \mathbb{R}^d$  is the control state;
- 252 2.  $M_t \in \mathbb{R}^{N \times d}$  is the visual working memory with  $N$  slots;
- 253 3.  $w_t \in \mathbb{R}^N$  is the write head; and
- 254 4.  $so_t \in \mathbb{R}^d$  is the summary visual object.

255 The initial state is such that both  $c_0$  and  $so_0$  are initialized to a fixed value at the start of each frame.  
 256 However  $M_0$  is initialized only once at the start of the first frame and otherwise taken to be the value  
 257 of  $M_T$  at the end of the previous frame.

### 258 Question-driven Controller

259 The Question-driven Controller plays an important role in the reasoning process. It drives the attention  
 260 over the question and produces the new control states. Each new control state defines a new reasoning  
 261 operation. The inputs of this unit are the past control state, the question encoding and the contextual  
 262 words (see Question Encoding Unit). It uses the dot product attention between the contextual words  
 263 and the combination of the past control states and the question encoding. This attention layer produces  
 264 the new control state.

265 This unit also outputs the temporal class weights that will be used in the Reasoning Unit. It gives  
 266 access to a temporal information for the current words (last, latest, now, none temporal).

#### 267 Inputs:

- 268 1. Reasoning step  $t = 1, 2, \dots, T$
- 269 2. Previous control state:  $c_{t-1} \in \mathbb{R}^d$
- 270 3. Contextual words:  $cw \in \mathbb{R}^{L \times d}$
- 271 4. Question encoding:  $q \in \mathbb{R}^d$

#### 272 Parameters:

- 273 1. Reasoning step-dependent linear layer:  $\mathcal{G}_t : \mathbb{R}^d \rightarrow \mathbb{R}^d$ , depending on  $s$
- 274 2. Concatenation linear layer:  $\mathcal{H} : \mathbb{R}^{2d} \rightarrow \mathbb{R}^d$
- 275 3. Attention module  $\mathcal{A}$
- 276 4. Temporal classifier:  $\mathcal{K} : \mathbb{R}^d \rightarrow \Delta^3$ . A two-layer feedforward network with ELU activation in the  
 277 hidden layer of  $d$  units. The classes for the temporal context are labeled “last”, “latest”, “now”,  
 278 as well as a fourth class label “none” indicating no temporal context. If  $\tau \in \Delta^3$  is the output of  
 279 the classifier, we denote the components by  $\tau^{\text{last}}$ ,  $\tau^{\text{latest}}$ ,  $\tau^{\text{now}}$  and  $\tau^{\text{none}}$ .

#### 280 Outputs:

- 281 1. Control state  $c_t \in \mathbb{R}^d$
- 282 2. Control attention  $ca_t \in \mathbb{R}^L$
- 283 3. Temporal class weights  $\tau_t \in \mathbb{R}^4$

#### 284 Equations:

- 285 1. Modulation:  $y = \mathcal{H}([c_{t-1}, \mathcal{G}_t(q)])$
- 286 2. Control state and attention:  $c_t, ca_t = \mathcal{A}(y, cw)$
- 287 3. Temporal classification:  $\tau_t = \mathcal{K}(c_t)$

### 288 Visual Retrieval Unit

289 The visual retrieval unit is responsible to extract visual information from the current image given  
 290 a control state coming from the Question-driven Controller. It is first projecting the past summary  
 291 object and the feature maps together using the interaction module. It is then using the attention  
 292 module as follow. The query are the control states and the keys and are the feature maps coming from  
 293 the image encoder. The results of this attention is applied on the modified features maps coming from  
 294 the interaction module. This unit outputs the extracted object and the visual attention.



**Inputs:**

1. Control state:  $c_t \in \mathbb{R}^d$
2. Previous summary object:  $so_{t-1} \in \mathbb{R}^d$
3. Feature map of current frame:  $F \in \mathbb{R}^{H \times W \times d}$

**Parameters:**

1. Interaction module  $\mathcal{I}$
2. Attention module  $\mathcal{A}$

**Outputs:**

1. Visual object:  $vo_t \in \mathbb{R}^d$
2. Visual attention:  $va_t \in \mathbb{R}^{H \times W \times d}$

**Equations:**

1. Modified feature map:  $\hat{F} = \mathcal{I}(so_{t-1}, F)$
2. Visual object and attention:  $vo_t, va_t = \mathcal{A}(y, \hat{F}, M_{t-1})$

*Note.* Appropriate flatten/unflatten operations are performed to match the signature of the modules.

**Memory Retrieval Unit**

The role of the memory retrieval unit is to read and extract object from memory). As the Visual Retrieval Unit, it uses the combination of the two following submodules. The interaction module blends together the extracted object and the content of the memory. The attention module then extract the corresponding object in memory if present. This unit outputs the extracted object and its corresponding location, we call it the "read head".

**Inputs:**

1. Control state:  $c_t \in \mathbb{R}^d$
2. Previous summary object:  $so_{t-1} \in \mathbb{R}^d$
3. Previous VWM  $M_{t-1} \in \mathbb{R}^{N \times d}$

**Parameters:**

1. Interaction module  $\mathcal{I}$
2. Attention module  $\mathcal{A}$

**Outputs:**

1. Memory object:  $mo_t \in \mathbb{R}^d$
2. Read head:  $rh_t \in \mathbb{R}^N$

**Equations:**

1. Modified VWM:  $\hat{M}_t = \mathcal{I}(so_{t-1}, M_{t-1})$
2. Memory object and attention:  $mo_t, rh_t = \mathcal{A}(y, \hat{M}_t, M_{t-1})$

**Reasoning Unit****Inputs:**

1. Control state:  $c_t \in \mathbb{R}^d$
2. Visual object:  $vo_t \in \mathbb{R}^d$
3. Memory object:  $mo_t \in \mathbb{R}^d$
4. Temporal class weights  $\tau \in \Delta^3$

**Parameters:** Validator modules  $\mathcal{G}, \mathcal{K} : \mathbb{R}^{2d} \rightarrow \mathbb{R}$ . Both  $\mathcal{G}, \mathcal{K}$  are two-layer networks of  $2d$  hidden units, using ELU activation in the hidden layer, and sigmoid in the output layer.

**Output:** Predicate gates for the current reasoning step

1. Object match predicate gates (i) image:  $g_t^v \in [0, 1]$  and (ii) memory:  $g_t^m \in [0, 1]$ .
2. Memory update predicate gates (i) add:  $h_t^a \in [0, 1]$  and (ii) replace:  $h_t^r \in [0, 1]$

**Equations:**

- 340 1.  $g_t^v \in [0, 1]$ : It's true if there is a valid visual object. This assumes that the current reasoning step  
341 refers to either “now” or “latest”.
- 342 2.  $g_t^m \in [0, 1]$ : It's true if there is a valid memory object. This assumes that the current reasoning  
343 step refers to either “last”, or alternatively “latest” but there is no matching visual object.
- 344 3.  $h_t^a$ :
- 345 4.  $h_t^r$ :

### 346 Memory Update Unit

347 This unit is meant to update the content of the memory.

348 Three actions can happen:

- 349 • There is no object to be added to memory, the memory remains unchanged
- 350 • There is one object that needs to be added to memory, but a similar object is already in memory at  
351 a given location. The new object will replace the old object at this location
- 352 • There is one object that needs to be added to memory, and it is a new object. It is added at the write  
353 head location.

354 This module also updates the position of the write head. If a new object as been added to the current  
355 write head position, the right head shifts right to a new empty slot. If the object has been replaced,  
356 the write head doesn't move.

#### 357 Inputs:

- 358 1. Visual object:  $vo_t \in \mathbb{R}^d$
- 359 2. Memory object:  $mo_t \in \mathbb{R}^d$
- 360 3. Memory update predicate gates:  $h_t^a, h_t^r \in [0, 1]$
- 361 4. Read head:  $rh_t \in \mathbb{R}^N$
- 362 5. Previous VWM  $M_{t-1} \in \mathbb{R}^{N \times d}$
- 363 6. Previous write head:  $wh_{t-1} \in \mathbb{R}^N$

#### 364 Outputs:

- 365 1. VWM  $M_t \in \mathbb{R}^{N \times d}$
- 366 2. Read head:  $rh_t \in \mathbb{R}^N$
- 367 3. Write head:  $wh_t \in \mathbb{R}^N$

### 368 Summary Object Update Unit

369 The Summary Unit is the last unit of the SAMCell. It is responsible to output the new summary  
370 object. It first picks which object is relevant between the object extracted from memory and the visual  
371 object extracted from the image. Once the relevant object is picked, it is combined with the former  
372 summary object through a linear layer to become the new summary object. It is the final step of the  
373 SAMCell reasoning cycle.

374 The image encoder, question encoder and output unit are described in the appendix.

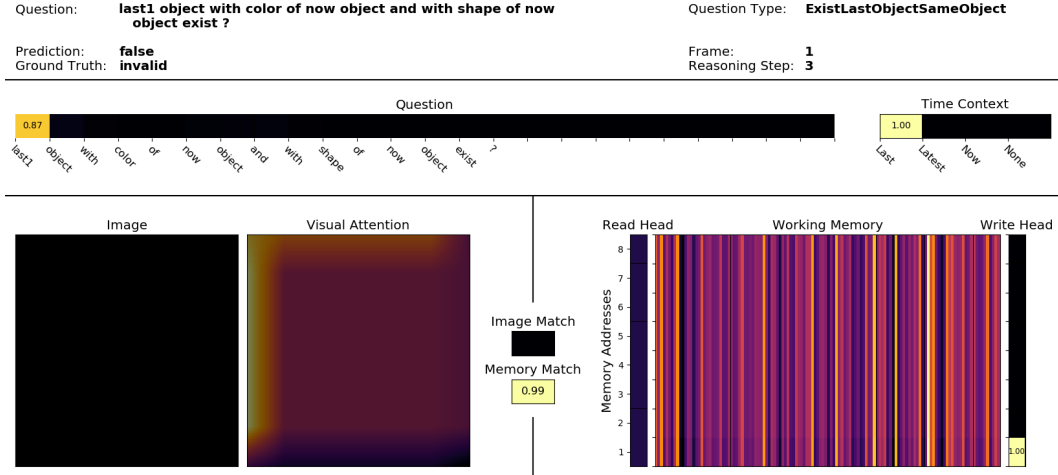
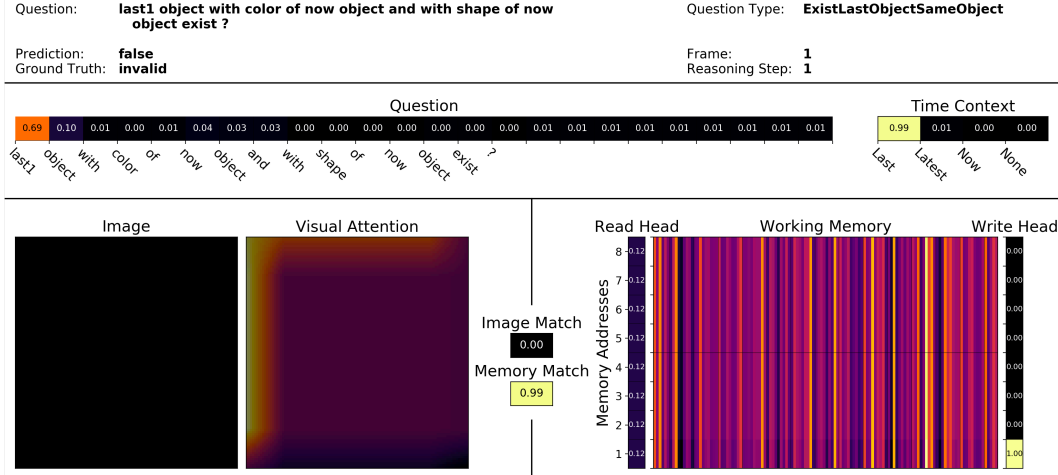
#### 375 Inputs:

- 376 1. Previous summary object:  $so_{t-1} \in \mathbb{R}^d$
- 377 2. Visual object:  $vo_t \in \mathbb{R}^d$
- 378 3. Memory object:  $mo_t \in \mathbb{R}^d$
- 379 4. Object predicate gates:  $g_t^v, g_t^m \in [0, 1]$

380 **Parameters:** Concatenation linear layer  $\mathcal{H}$

381 **Output:** New summary object:  $so_t = \mathcal{H}([so_{t-1}, (g_t^v * vo_t + g_t^m * mo_t)]) \in \mathbb{R}^d$

### 383 Image Encoder



384 **Inputs:** Images

385 **Output:** Features maps:  $F_k$

386 The Image Encoder unit is responsible to preprocess the sequence of images one at the time. It is a 4  
387 layer convolutional neural network. Every layer is composed of the following sequence of operations:

- 388 1. 2D convolution ( $stride = 1$ )
- 389 2. 2D max pooling
- 390 3. 2D batch normalization
- 391 4. Relu (only for the first 3 layers)

392 The first layer has 3 inputs channels and 32 output channels. Layer 2 has 32 and 64. Layer 3 has  
393 64 and 64. Finally, layer 4 has 64 inputs channels and 128 output channels . The resulting tensor  
394 (feature maps) are of dimensions [batch size,  $H * W = 7 * 7$ ,  $dim=128$ ].

### 395 Question Encoder

396 **Inputs:** 1. question string  $question$

397 2. question lengths  $question_l$

398 **Output:** 1. contextual word embedding  $cw$   
399 2. question encoding  $q$

400 The strings questions are first embedded (*torch.NN.Embeddings*) and then passed through a  $d$ -  
401 dimensional biLSTM ( $d=128$ ). The final hidden state of the biLSTM becomes the question encoding  
402 representation  $q$ . Whereas the biLSTM outputs are projected via a linear layer to become the final  
403 words encodings named contextual words  $cw$ .

#### 404 **Output Unit**

405 **Inputs:** 1. question encoding  $q$   
406 2. summary object  $so_t$

407 **Output:** prediction

408 The output unit predicts the final answer to the question. It is a 2-linear-layer-ELU classifier that  
409 produces a distribution over the possible candidates. It is based on two inputs, the final summary  
410 object  $so_t$  and the question encoding  $q$  that are concatenated together.

## 411 **8 Training and Implementation Details**

### 412 **8.1 Training and testing Methodology**

413 SAMNet is implemented on IBM's Mi-Prometheus [KMM<sup>+</sup>18] framework based on Pytorch. We  
414 trained all our models using NVIDIA's GeForce GTX TITAN X GPUs. SAMNet was trained using  
415 8 reasoning steps and a hidden state size of 128. The external memory has 128-bit slots for all  
416 experiments. We trained our model until convergence but we also have set a training time limit of 80  
417 hours.

418 We compared our model to the original COG model [YGW<sup>+</sup>18] using their implementation  
419 (<https://github.com/google/cog>) and scores provided by the authors through personal communi-  
420 cations. We used the same training parameters detailed in the original paper and reproduced their  
421 results. For the generalization experiments from canonical to hard, we used the verified model and  
422 obtained new results that were not reported in the reference paper. In Table 1 COG section shows 4  
423 columns divided into two parts: "paper" and "ours" which distinguish between the results reported in  
424 the paper vs. our own experiments.

425 Our experiments focused on the 22 classification tasks provided by the COG dataset. First we  
426 evaluated SAMNet's performance on the canonical setting and compared it with the COG Model.  
427 As shown in Table 1 we could achieve a small improvement in accuracy, from 97.6% for the COG  
428 model to 98% for SAMNet. Next we focused on the hard setting of the dataset which increases the  
429 number of distractors from 1 to 10 and the number of frames from 4 to 8.

430 The first approach was to train a model on the hard training set, and test it on the hard test set. This is  
431 the same approach used by the COG paper [YGW<sup>+</sup>18] to evaluate performance on the hard dataset.  
432 We achieve a test accuracy of 91.9 % which represents a 12% improvement from the COG model  
433 score (see Table 1).

434 The second approach was to see if the models can generalize from the easy to the hard setting. For  
435 this experiment, we trained a model on the canonical dataset, and directly tested on the hard dataset.  
436 This experiment highlighted the most significant difference between SAMNet and the baseline COG  
437 model.

438 Finally we trained a model on the canonical data set, fine-tuned it on the hard data set using only  
439 25k iterations, and tested on the hard dataset. Thanks to fine-tuning, we can observe a significant  
440 improvement from 91.6% to 96.5% test accuracy which represents the state of the art accuracy for  
441 the hard setting (classification tasks). After a short fine-tuning process, the transferred model could  
442 generalize well to harder tasks and even surpass the accuracy obtained in the first approach. We  
443 note that the third approach is also twice faster than the first one, and it is more effective in terms of  
444 accuracy.

Table 1: COG test set accuracies for SAMNet & COG models. Below ‘paper’ denotes results from [YGW<sup>+</sup>18] while ‘code’ denotes results of our experiments using their implementation [Gan18]

Model  Trained on Fine tuned on Tested on	SAMNet				COG			
	canonical - canonical	canonical - hard	canonical hard hard	hard - hard	paper	ours	ours	paper
					canonical - canonical	canonical - hard	canonical hard hard	hard - hard
Overall accuracy	98.0	91.6	96.5	96.1	97.6	65.9	78.1	80.1
AndCompareColor	93.5	82.7	89.2	80.6	81.9	57.1	60.7	51.4
AndCompareShape	93.2	83.7	89.7	80.1	80.0	53.1	50.3	50.7
AndSimpleCompareColor	99.2	85.3	97.6	99.4	99.7	53.4	77.1	78.2
AndSimpleCompareShape	99.2	85.8	97.6	99.2	100.0	56.7	79.3	77.9
CompareColor	98.1	89.3	95.9	99.7	99.2	56.1	67.9	50.1
CompareShape	98.0	89.7	95.9	99.2	99.4	66.8	65.4	50.5
Exist	100.0	99.7	99.8	99.8	100.0	63.5	96.1	99.3
ExistColor	100.0	99.6	99.9	99.9	99.0	70.9	99	89.8
ExistColorOf	99.9	95.5	99.7	99.8	99.7	51.5	76.1	73.1
ExistColorSpace	94.1	88.8	91.0	90.8	98.9	72.8	77.3	89.2
ExistLastColorSameShape	99.5	99.4	99.4	98.0	100.0	65.0	62.5	50.4
ExistLastObjectSameObject	97.3	97.5	97.7	97.5	98.0	77.5	61.7	60.2
ExistLastShapeSameColor	98.2	98.5	98.8	97.5	100.0	87.8	60.4	50.3
ExistShape	100.0	99.5	100.0	100.0	100.0	77.1	98.2	92.5
ExistShapeOf	99.4	95.9	99.2	99.2	100.0	52.7	74.7	72.70
ExistShapeSpace	93.4	87.5	91.1	90.5	97.7	70	89.8	89.80
ExistSpace	95.3	89.7	93.2	93.3	98.9	71.1	88.1	92.8
GetColor	100.0	95.8	99.9	100.0	100.0	71.4	83.1	97.9
GetColorSpace	98.0	90.0	95.0	95.4	98.2	71.8	73.	92.3
GetShape	100.0	97.3	99.9	99.9	100.0	83.5	89.2	97.1
GetShapeSpace	97.5	89.4	93.9	94.3	98.1	78.7	77.3	90.3
SimpleCompareShape	99.9	91.4	99.7	99.9	100.0	67.7	96.7	99.3
SimpleCompareColor	100.0	91.6	99.80	99.9	100.0	64.2	90.4	99.3

Table 2: COG Dataset parameters for the canonical setting and the hard setting

Dataset	number of frames	maximum memory duration	number of distractors	size of training set	size of validation/test set
Canonical setting	4	3	1	10000320	500016
Hard setting	8	7	10	10000320	500016

445 A more granular analysis of accuracy per task shows a major improvement for the two hardest tasks,  
 446 AndCompareShape and AndCompareColor. Those two tasks represent a higher level of difficulty  
 447 due to the number of objects to be remembered in order to answer the question correctly. As we  
 448 can see in Table 2 we could achieve a 12% improvement for the canonical data set and almost a  
 449 40% improvement for the hard dataset. The large improvement in these memory-intensive tasks  
 450 indicate that the SAMNet’s external memory plays a crucial role in our results. The training and  
 451 implementation details are in appendix.