

Assignment 8

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Title: Shortest Path Finding

Aim: To implement shortest path using Dijkstra's algorithm.

Problem Statement: Represent a graph of city using adjacency matrix / adjacency list. Nodes should represent the distance between them. Find the shortest path using Dijkstra's algo from single source to all destination.

Theory:

What is shortest path?

In graph theory the shortest path is the path between 2 vertices as such that the sum of the weight of its edge is minimized. The problem of finding the shortest path in a graph from one vertex to another. Shortest can be least number of edges least total weight, etc.

Various algorithm to find shortest path:

- 1) Dijkstra's algorithm.
- 2) Bellman-ford algorithm.
- 3) Floyd-Warshall algorithm.
- 4) Johnson algorithm.
- 5) Warli algorithm.

- Greedy approach -

An algorithm is designed to achieve optimum solution for a given problem. In greedy algorithm approach, decisions are made from given solution domain. As being greedy the closest solution that seems to provide an optimized solution is chosen.

Greedy algorithm builds up solution piece by ~~part~~^{piece} always choosing the next piece that offers the most obvious and immediate benefits.

- Dijkstra's algorithm -

It is an algorithm for finding the shortest path between nodes in graph. The algorithm creates a ~~tree~~ ^{tree} of shortest path from starting vertex (source) to all other points in graph. Dijkstra's algorithm finds the shortest path till from a single source node by building a set of nodes that have minimum distance from source.

Real time uses of Dijkstra's Algorithm:

- 1) Social Networking appliance.
- 2) Telephone Network.
- 3) Digital Mapping service in Google map.
- 4) IP routing to find open shortest path first.
- 5) Fighting agenda.

* Algorithm for Dijkstra's single source to multiple destination:

Procedure Dijkstra's:

// src is source vertex

for $i = 0$ to v

// find initial distance

if $\text{weight}[\text{src}][i] \neq 0$

$\text{dis}[i] = \text{weight}[\text{src}][i]$

else

$\text{dis}[i] = 32767$

$\text{path}[i] = \text{src}$

$\text{visited}[i] = 0$

End for

// take source as current vertex and make it visited

$\text{current} = \text{src}$

$\text{visited}[\text{src}] = 1$

// repeat for all vertices

for $j = 0$ to $v - 1$

$\text{min_dist} = 32767$

// find min dist from current to all other

for $i = 0$ to v

if $\text{visited}[i] = 0$ & $\text{dis}[i] < \text{min_dist}$

$\text{min_dist} = \text{dis}[i]$

$\text{current} = i$

End for

// make current as visited

$\text{visited}[\text{current}] = 1$

// find shortest path from current

for $i = 0$ to v

if $\text{visited}[i] = 0$ and $(\text{dis}[\text{current}] + \text{weight}[\text{current}][i] < \text{dis}[i])$

$\text{dis}[i] = \text{dis}[\text{current}] + \text{weight}[\text{current}][i]$

```
path[i] = current
End for
End for
```

// display shortest path.

```
for i = 0 to v
```

```
if i  $\neq$  src
```

```
print i, dis[i]
```

```
int j = 1
```

```
do
```

```
j = path[j]
```

```
print path[j]
```

```
while j  $\neq$  src
```

```
End for
```

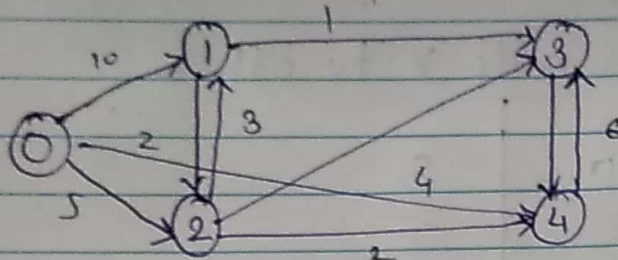
END.

Validation:

- 1) No. of vertices & edges are positive
- 2) Weight of an edge is not negative.
- 3) Remove parallel edge at higher cost.

Test cases:

1) For directed Graph:



Node	From node V_0 to other
V_1	10
V_2	5
V_3	∞
V_4	∞
best	

2) Find shortest path to neck 0:

Node 2 selected.

Node	From node V_0 to other
V_1	10
V_2	5
V_3	∞
V_4	∞
best	V_2

3) Recalculate path to other node (Node V_4):

Node	From node V to other	
V_1	10	8
V_2	5	5
V_3	∞	14
V_4	∞	7
best	V_2	V_4

4) Find shortest path to Node 0, Node V selected:

Node	From node V_0 to other		
V_1	10	8	8
V_2	5	5	5
V_3	∞	14	13
V_4	∞	7	7
best	V_2	V_4	V_1

5) Find shortest path to node 0, node 3 selected:

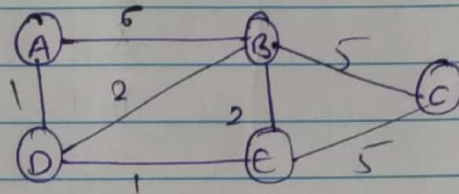
Node	From node V_0 to other			
V_1	10	8	8	8
V_2	5	5	5	5
V_3	∞	14	13	9
V_4	∞	7	7	7
best	V_2	V_4	V_1	V_3

∴ Shortest path can be calculated as

$$V_0 \rightarrow V_2 \rightarrow V_4 \rightarrow V_1 \rightarrow V_3$$

Cost = 11

2) For Undirected graph:



From current vertex = A, examine unvisited neighbours:

Vertex	Shortest dist	Path
A	0	
B	6	A
C	∞	
D	1	A
E	∞	

Current vertex = D Examine unvisited neighbours:

Vertex	Shortest dist	Path
A	0	
B	3	D
C	2	
D	1	A
E	2	D

Current Vertex = E

Vertex	Shortest dist	Path
A	0	
B	3	D
C	7	E
D	1	A
E	2	D

Current vertex = B

Vertex	Shortest dist	Path
A	0	
B	3	D
C	7	E
D	1	A
E	2	D

Path :-

A → D → E → B → C

Cost = 9



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Conclusion:

We successfully implemented a graph and choose a path using Dijkstra's algorithm.

Time complexity = $O(E \log V)$

Space complexity = $O(V)$