



AMRITA
VISHWA VIDYAPEETHAM
DEEMED TO BE UNIVERSITY UNDER SECTION 3 OF UGC ACT, 1956

SCHOOL OF
COMPUTING

DESIGN AND ANALYSIS OF ALGORITHMS
LAB WORKBOOK
WEEK - 7

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ROLL NO : CH.SC.U4CSE24120

CLASS : CSE-B

Question 1: Let there be 14 jobs with the profit of
22,19,29,28,30,21,27,25,24,26,14,27,19,11 with deadlines
3,3,8,6,7,5,10,4,6,12,13,2,14,1

Implement the greedy algorithm for the Job Sequencing with Deadlines and determine the optimal sequence of jobs that maximizes total profit.

Job sequencing

Let there be 14 Jobs with the profit of [22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11] and job completion times [3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1]

Huffman Coding

DATA ANALYTICS AND INTELLIGENCE LABORATORY

D - 2	Y - 2	G - 1
A - 7	I - 3	B - 1
T - 4	C - 2	O - 2
N - 4	S - 1	R - 2
L - 4	E - 3	

Job Sequencing

Q) Let there be 14 Jobs with the profit of [22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11] with job completion time [3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1].

Given,

$$\text{No. of jobs (n)} = 14$$

$$\text{Profits} = (P_1 \text{ to } P_{14}) = (22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11)$$

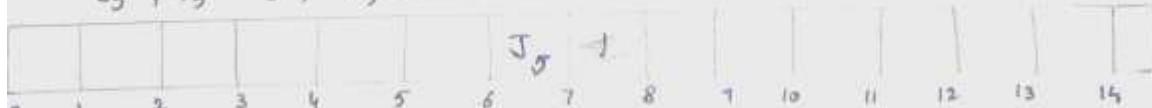
$$\text{Deadlines} = (D_1 \text{ to } D_{14}) = (3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1).$$

Step 1:- Arrange the jobs in descending order based on profits and write corresponding deadlines.

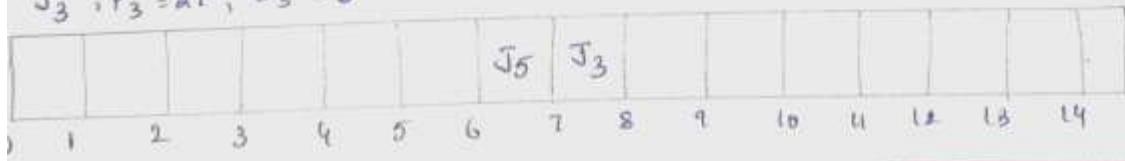
30	29	28	27	27	26	25	24	24	21	19	19	14	11
7	8	6	10	2	12	4	6	3	5	3	14	13	1
J ₅	J ₃	J ₄	J ₇	J ₁₂	J ₁₀	J ₈	J ₉	J ₁	J ₆	J ₂	J ₁₃	J ₁₁	J ₁₄

Step 2:- Create slots and Assign jobs

$$J_5, P_5 = 30, D_5 = 7$$



$$J_3, P_3 = 29, D_3 = 8$$



$$J_4, P_4 = 28, D_4 = 6$$

						J ₄	J ₅	J ₃						
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$$J_7, P_7 = 27, D_7 = 10$$

					J ₄	J ₅	J ₃		J ₇					
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$$J_{12}, P_{12} = 27, D_{12} = 2$$

	J ₁₂				J ₄	J ₅	J ₃		J ₇					
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$$J_{10}, P_{10} = 26, D_{10} = 12$$

	J ₁₂				J ₄	J ₅	J ₃		J ₇		J ₁₀			
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$$J_8, P_8 = 25, D_8 = 4$$

	J ₁₂		J ₈		J ₄	J ₅	J ₃		J ₇		J ₁₀			
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$J_9, P_9 = 24, D_9 = 6$, As slot 5-6 is filled check 4-5, As it is empty allot it with J_9 .

	J ₁₂		J ₈	J ₉	J ₄	J ₅	J ₃		J ₇		J ₁₀			
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$$J_1, P_1 = 22, D_1 = 3$$

	J ₁₂	J ₁	J ₈	J ₉	J ₄	J ₅	J ₃		J ₇		J ₁₀			
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$J_6, P_6 = 21, D_6 = 5$, As 5-6 slot is already filled, check previous slots, As only

J_6 is free allot it with J_6

	J ₆	J ₁₂	J ₁	J ₈	J ₉	J ₄	J ₅	J ₃		J ₇		J ₁₀		
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

$J_2, P_2 = 19, D_2 = 3$. All the slots before deadline i.e., 3 are allotted already. So no slot for J_2 so we reject J_2 .

	J ₆	J ₁₂	J ₁	J ₈	J ₉	J ₄	J ₅	J ₃		J ₇		J ₁₀		
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14

J_{13} , $P_{13} = 19$, $D_{13} = 14$

J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3	J_7	J_{10}	J_{11}	J_{13}
0	1	2	3	4	5	6	7	8	9	10	11

P_{14} , J_{11} , $P_{11} = 14$, $D_{11} = 13$

J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3	J_7	J_{10}	J_{11}	J_{13}
0	1	2	3	4	5	6	7	8	9	10	11

J_{14} , $P_{14} = 11$, $D_{14} = 1$

as deadline for P_{14} is 1, it has no empty slots. So Reject J_{14} .

J_6	J_{12}	J_1	J_8	J_9	J_4	J_5	J_3	J_7	J_{10}	J_{11}	J_{13}
0	1	2	3	4	5	6	7	8	9	10	11

Final Job sequence :- $[J_5, J_3, J_4, J_7, J_{12}, J_{10}, J_8, J_9, J_1, J_6, J_{13}, J_{11}]$

$$\begin{aligned}\text{Total profit} &= 21 + 27 + 22 + 25 + 24 + 28 + 30 + 29 + 27 + 26 + 14 + 17 \\ &= 292\end{aligned}$$

CODE:

```
//CH.SC.U4CSE24120
#include <stdio.h>
#define MAX 100
struct Job
{
    int id;
    int profit;
    int deadline;
};
void sortJobs(struct Job jobs[], int n)
{
    int i, j;
    struct Job temp;

    for(i = 0; i < n - 1; i++)
    {
        for(j = 0; j < n - i - 1; j++)
        {
            if(jobs[j].profit < jobs[j + 1].profit)
            {
                temp = jobs[j];
                jobs[j] = jobs[j + 1];
                jobs[j + 1] = temp;
            }
        }
    }
}
int findMaxDeadline(struct Job jobs[], int n)
{
    int i, max = jobs[0].deadline;

    for(i = 1; i < n; i++)
    {
        if(jobs[i].deadline > max)
        {
            max = jobs[i].deadline;
        }
    }
    return max;
```

```
}

int main()
{
    struct Job jobs[MAX];
    int n, i, j;

    printf("Enter number of jobs: ");
    scanf("%d", &n);
    printf("Enter profits:\n");
    for(i = 0; i < n; i++)
    {
        jobs[i].id = i + 1;
        scanf("%d", &jobs[i].profit);
    }
    printf("Enter deadlines:\n");
    for(i = 0; i < n; i++)
    {
        scanf("%d", &jobs[i].deadline);
    }
    sortJobs(jobs, n);
    int maxDeadline = findMaxDeadline(jobs, n);
    int slot[MAX];
    for(i = 1; i <= maxDeadline; i++)
    {
        slot[i] = -1;
    }
    int totalProfit = 0;
    for(i = 0; i < n; i++)
    {
        for(j = jobs[i].deadline; j >= 1; j--)
        {
            if(slot[j] == -1)
            {
                slot[j] = jobs[i].id;
                totalProfit += jobs[i].profit;
                break;
            }
        }
    }
}
```

```

        printf("\nSlot Arrangement:\n");
    for(i = 1; i <= maxDeadline; i++)
    {
        if(slot[i] == -1)
            printf("Slot %d : _\n", i);
        else
            printf("Slot %d : J%d\n", i, slot[i]);
    }
    printf("\nMaximum Profit = %d\n", totalProfit);
    return 0;
}

```

OUTPUT:

```

Enter number of jobs: 14
Enter profits:
22 19 29 28 30 21 27 25 24 26 14 27 19 11
Enter deadlines:
3 3 8 6 7 5 10 4 6 12 13 2 14 1

Slot Arrangement:
Slot 1 : J6
Slot 2 : J12
Slot 3 : J1
Slot 4 : J8
Slot 5 : J9
Slot 6 : J4
Slot 7 : J5
Slot 8 : J3
Slot 9 : _
Slot 10 : J7
Slot 11 : _
Slot 12 : J10
Slot 13 : J11
Slot 14 : J13

Maximum Profit = 292

```

Time Complexity:

1. Sorting the jobs by profit

We used Bubble Sort in the program.

Time complexity: $O(n^2)$

2. Finding maximum deadline

We check all jobs once.

Time complexity: $O(n)$

3. Assigning jobs to slots

For each job, we may check up to d slots. $O(n^2)$

Total Time Complexity

$$O(n^2) + O(n) + O(n^2) = O(n^2)$$

Space Complexity

We use:

- Job array $\rightarrow O(n)$
- Slot array $\rightarrow O(d)$

Total Space: $O(n)$