

**SCHOOL OF  
COMPUTING**

**DESIGN AND ANALYSIS OF ALGORITHMS**

**LAB WORKBOOK**

**WEEK - 7**

**NAME : Konda Bhavani**

**ROLL NO : CH.SC.U4CSE24120**

**CLASS : CSE-B**

**Question 1:** Let there be 14 jobs with the profit of  
22,19,29,28,30,21,27,25,24,26,14,27,19,11 with deadlines  
3,3,8,6,7,5,10,4,6,12,13,2,14,1

Implement the greedy algorithm for the Job Sequencing with Deadlines and  
determine the optimal sequence of jobs that maximizes total profit.

## Job sequencing

Let there be 14 Jobs with the profit of [22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11] and job completion times [3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1]

## Huffman Coding

Data ANALYTICS AND INTELLIGENCE LABORATORY

|     |     |     |
|-----|-----|-----|
| D-2 | Y-2 | G-1 |
| A-7 | I-3 | B-1 |
| T-4 | C-2 | O-2 |
| N-4 | S-1 | R-2 |
| L-4 | E-3 |     |

## Job Sequencing

Q) Let there be 14 Jobs with the profit of [22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11] with job completion time [3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1].

Given,

No. of jobs (N) = 14

Profits = (P<sub>1</sub> to P<sub>14</sub>) = (22, 19, 29, 28, 30, 21, 27, 25, 24, 26, 14, 27, 19, 11)

Deadlines = (D<sub>1</sub> to D<sub>14</sub>) = (3, 3, 8, 6, 7, 5, 10, 4, 6, 12, 13, 2, 14, 1)

Step 1:- Arrange the jobs in descending order based on profits and write corresponding deadlines.

|                |                |                |                |                 |                 |                |                |                |                |                |                 |                 |                 |
|----------------|----------------|----------------|----------------|-----------------|-----------------|----------------|----------------|----------------|----------------|----------------|-----------------|-----------------|-----------------|
| 30             | 29             | 28             | 27             | 27              | 26              | 25             | 24             | 22             | 21             | 19             | 19              | 14              | 11              |
| 7              | 8              | 6              | 10             | 2               | 12              | 4              | 6              | 3              | 5              | 3              | 14              | 13              | 1               |
| J <sub>5</sub> | J <sub>3</sub> | J <sub>4</sub> | J <sub>7</sub> | J <sub>12</sub> | J <sub>10</sub> | J <sub>8</sub> | J <sub>9</sub> | J <sub>1</sub> | J <sub>6</sub> | J <sub>2</sub> | J <sub>13</sub> | J <sub>11</sub> | J <sub>14</sub> |

Step 2:- Create slots and Assign jobs

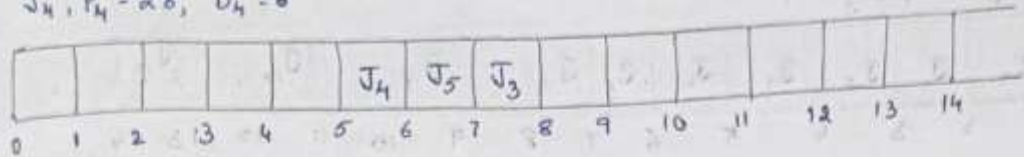
J<sub>5</sub>, P<sub>5</sub> = 30, D<sub>5</sub> = 7.

|   |   |   |   |   |   |                |   |   |   |    |    |    |    |    |
|---|---|---|---|---|---|----------------|---|---|---|----|----|----|----|----|
|   |   |   |   |   |   | J <sub>5</sub> |   |   |   |    |    |    |    |    |
| 0 | 1 | 2 | 3 | 4 | 5 | 6              | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |

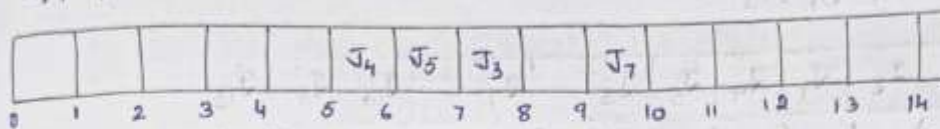
J<sub>3</sub>, P<sub>3</sub> = 29, D<sub>3</sub> = 8

|   |   |   |   |   |   |                |                |   |    |    |    |    |    |  |
|---|---|---|---|---|---|----------------|----------------|---|----|----|----|----|----|--|
|   |   |   |   |   |   | J <sub>5</sub> | J <sub>3</sub> |   |    |    |    |    |    |  |
| 1 | 2 | 3 | 4 | 5 | 6 | 7              | 8              | 9 | 10 | 11 | 12 | 13 | 14 |  |

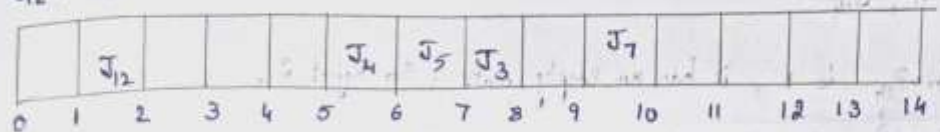
$$J_4, P_4 = 28, D_4 = 6$$



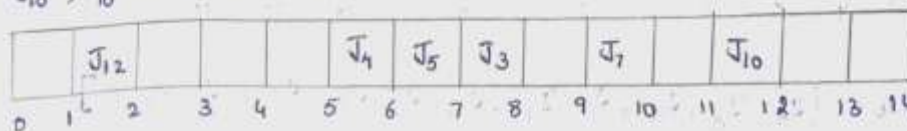
$$J_7, P_7 = 27, D_7 = 10$$



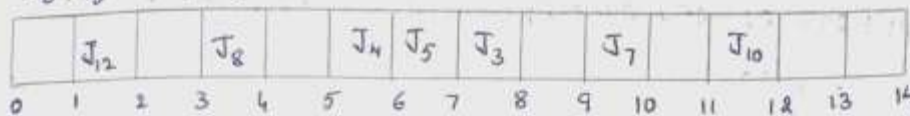
$$J_{12}, P_{12} = 27, D_{12} = 2$$



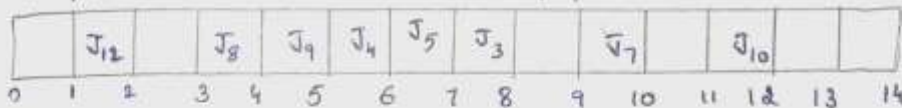
$$J_{10}, P_{10} = 26, D_{10} = 12$$



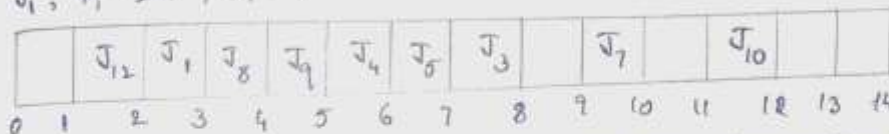
$$J_8, P_8 = 25, D_8 = 4$$



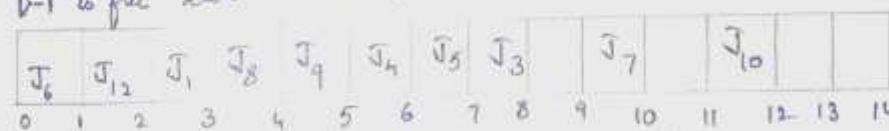
$J_9, P_9 = 24, D_9 = 6$ , As slot 5-6 is filled check 4-5, As it is empty slot it with  $J_9$ .



$$J_1, P_1 = 22, D_1 = 3$$



$J_6, P_6 = 21, D_6 = 5$ , As 5-4 slot is already filled, check previous slots, As only D-1 is free slot it with  $J_6$ .



$J_2, P_2 = 19, D_2 = 3$ . All the slots before deadline i.e., 3 are allotted already. So no slot for  $J_2$  so, we reject  $J_2$ .



$J_{13}, P_{13} = 19, D_{13} = 14$

|       |          |       |       |       |       |       |       |   |       |    |          |    |          |    |
|-------|----------|-------|-------|-------|-------|-------|-------|---|-------|----|----------|----|----------|----|
| $J_6$ | $J_{12}$ | $J_1$ | $J_8$ | $J_9$ | $J_4$ | $J_5$ | $J_3$ |   | $J_7$ |    | $J_{10}$ |    | $J_{13}$ |    |
| 0     | 1        | 2     | 3     | 4     | 5     | 6     | 7     | 8 | 9     | 10 | 11       | 12 | 13       | 14 |

Pr:  $J_{11}, P_{11} = 14, D_{11} = 13$

|       |          |       |       |       |       |       |       |   |       |    |          |          |          |    |
|-------|----------|-------|-------|-------|-------|-------|-------|---|-------|----|----------|----------|----------|----|
| $J_6$ | $J_{12}$ | $J_1$ | $J_8$ | $J_9$ | $J_4$ | $J_5$ | $J_3$ |   | $J_7$ |    | $J_{10}$ | $J_{11}$ | $J_{13}$ |    |
| 0     | 1        | 2     | 3     | 4     | 5     | 6     | 7     | 8 | 9     | 10 | 11       | 12       | 13       | 14 |

$J_{14}, P_{14} = 11, D_{14} = 1$

as deadline for  $P_{14}$  is 1, it has no empty slots. So Reject  $J_{14}$ .

|       |          |       |       |       |       |       |       |   |       |    |          |          |          |    |
|-------|----------|-------|-------|-------|-------|-------|-------|---|-------|----|----------|----------|----------|----|
| $J_6$ | $J_{12}$ | $J_1$ | $J_8$ | $J_9$ | $J_4$ | $J_5$ | $J_3$ |   | $J_7$ |    | $J_{10}$ | $J_{11}$ | $J_{13}$ |    |
| 0     | 1        | 2     | 3     | 4     | 5     | 6     | 7     | 8 | 9     | 10 | 11       | 12       | 13       | 14 |

Final Job sequence:  $[J_5, J_3, J_4, J_7, J_{12}, J_{10}, J_8, J_9, J_1, J_6, J_{13}, J_{11}]$

Total profit =  $21 + 27 + 22 + 25 + 24 + 28 + 30 + 29 + 27 + 26 + 14 + 17$   
 $= 292$

## CODE:

```
//CH.SC.U4CSE24120
#include <stdio.h>
#define MAX 100
struct Job
{
    int id;
    int profit;
    int deadline;
};
void sortJobs(struct Job jobs[], int n)
{
    int i, j;
    struct Job temp;

    for(i = 0; i < n - 1; i++)
    {
        for(j = 0; j < n - i - 1; j++)
        {
            if(jobs[j].profit < jobs[j + 1].profit)
            {
                temp = jobs[j];
                jobs[j] = jobs[j + 1];
                jobs[j + 1] = temp;
            }
        }
    }
}
int findMaxDeadline(struct Job jobs[], int n)
{
    int i, max = jobs[0].deadline;

    for(i = 1; i < n; i++)
    {
        if(jobs[i].deadline > max)
        {
            max = jobs[i].deadline;
        }
    }
    return max;
}
```

```

}
int main()
{
    struct Job jobs[MAX];
    int n, i, j;

    printf("Enter number of jobs: ");
    scanf("%d", &n);
    printf("Enter profits:\n");
    for(i = 0; i < n; i++)
    {
        jobs[i].id = i + 1;
        scanf("%d", &jobs[i].profit);
    }
    printf("Enter deadlines:\n");
    for(i = 0; i < n; i++)
    {
        scanf("%d", &jobs[i].deadline);
    }
    sortJobs(jobs, n);
    int maxDeadline = findMaxDeadline(jobs, n);
    int slot[MAX];
    for(i = 1; i <= maxDeadline; i++)
    {
        slot[i] = -1;
    }
    int totalProfit = 0;
    for(i = 0; i < n; i++)
    {
        for(j = jobs[i].deadline; j >= 1; j--)
        {
            if(slot[j] == -1)
            {
                slot[j] = jobs[i].id;
                totalProfit += jobs[i].profit;
                break;
            }
        }
    }
}

```



```

printf("\nSlot Arrangement:\n");
for(i = 1; i <= maxDeadline; i++)
{
    if(slot[i] == -1)
        printf("Slot %d : _\n", i);
    else
        printf("Slot %d : J%d\n", i, slot[i]);
}
printf("\nMaximum Profit = %d\n", totalProfit);
return 0;
}

```

#### OUTPUT:

```

Enter number of jobs: 14
Enter profits:
22 19 29 28 30 21 27 25 24 26 14 27 19 11
Enter deadlines:
3 3 8 6 7 5 10 4 6 12 13 2 14 1

Slot Arrangement:
Slot 1 : J6
Slot 2 : J12
Slot 3 : J1
Slot 4 : J8
Slot 5 : J9
Slot 6 : J4
Slot 7 : J5
Slot 8 : J3
Slot 9 : _
Slot 10 : J7
Slot 11 : _
Slot 12 : J10
Slot 13 : J11
Slot 14 : J13

Maximum Profit = 292

```



**Time Complexity:****1. Sorting the jobs by profit**

We used Bubble Sort in the program.

Time complexity:  $O(n^2)$

**2. Finding maximum deadline**

We check all jobs once.

Time complexity:  $O(n)$

**3. Assigning jobs to slots**

For each job, we may check up to d slots.  $O(n^2)$

**Total Time Complexity**

$$O(n^2) + O(n) + O(n^2) = O(n^2)$$

**Space Complexity**

We use:

- Job array  $\rightarrow O(n)$
- Slot array  $\rightarrow O(d)$

Total Space:  $O(n)$