

DESIGN AND ANALYSIS OF ALGORITHMS
LAB WORKBOOK WEEK – 6

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CLASS: CSE-B

Quick Sort (First element as pivot)

Code:

```
//CH.SC.U4CSE24120
#include <stdio.h>
int Partition(int a[], int low, int high) {
    int pivot = a[low];
    int i = low + 1;
    int j = high;
    while (1) {
        while (i <= high && a[i] <= pivot)
            i++;
        while (a[j] > pivot)
            j--;
        if (i >= j)
            break;
        int temp = a[i];
        a[i] = a[j];
        a[j] = temp;
    }
    int temp = a[low];
    a[low] = a[j];
    a[j] = temp;
    return j;
}
void quickSort(int a[], int low, int high) {
    if (low < high) {
        int p = Partition(a, low, high);
        quickSort(a, low, p - 1);
        quickSort(a, p + 1, high);
    }
}
int main() {
    int a[] = {157, 110, 147, 122, 111, 149, 151, 141, 123, 112, 117, 133};
    int n = sizeof(a) / sizeof(a[0]);

    quickSort(a, 0, n - 1);

    printf("Sorted array:\n");
    for (int i = 0; i < n; i++)
        printf("%d ", a[i]);

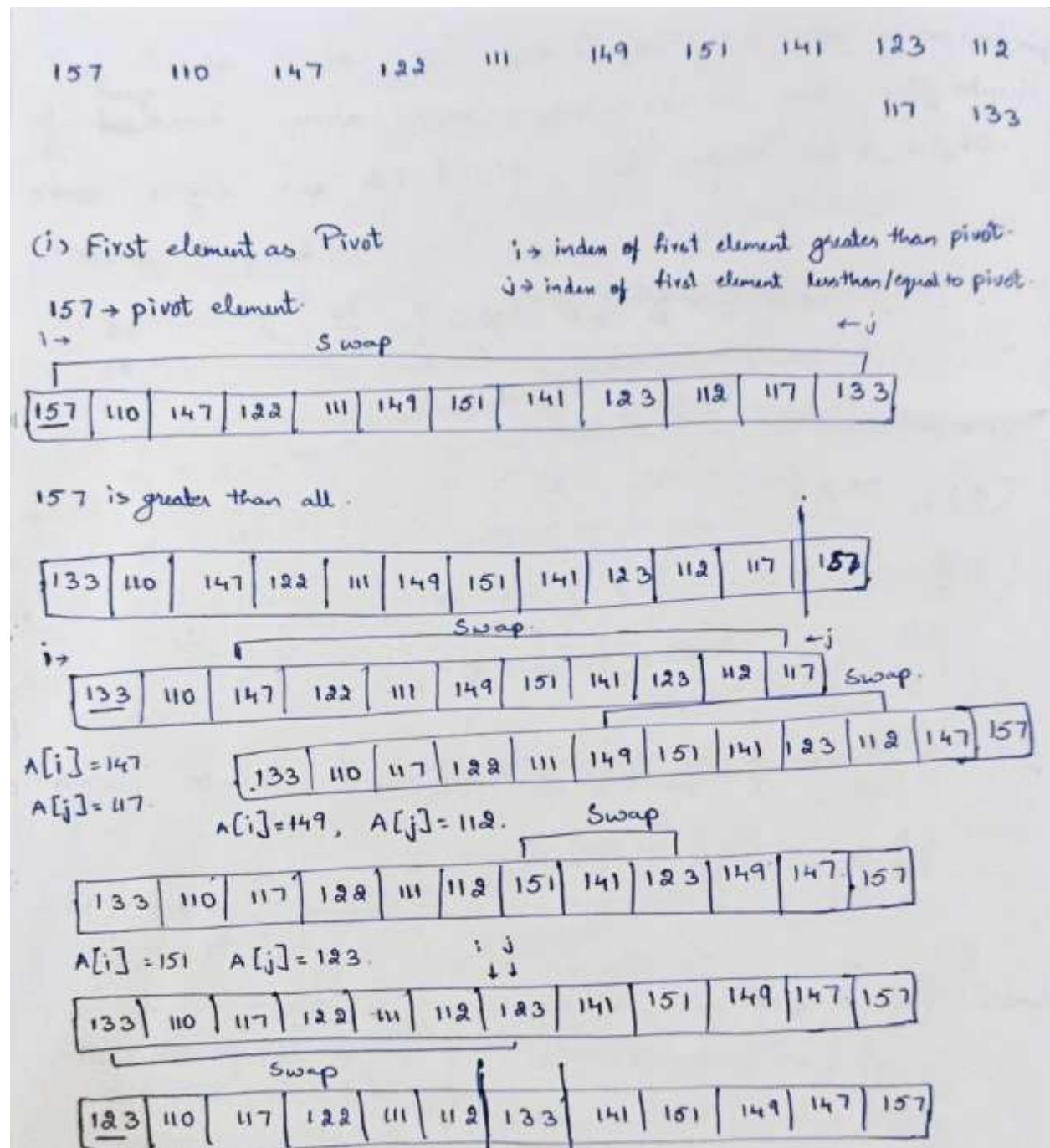
    return 0;
}
```

Output:

Sorted array:

110 111 112 117 122 123 133 141 147 149 151 157

Working:



123	110	117	122	111	112
-----	-----	-----	-----	-----	-----

112	110	117	122	111	123
-----	-----	-----	-----	-----	-----

112	110	111	122	117	123
-----	-----	-----	-----	-----	-----

111	110	112	122	117	123
-----	-----	-----	-----	-----	-----

110	111
-----	-----

117	122	123
-----	-----	-----

110	111	112	117	122	123
-----	-----	-----	-----	-----	-----

141	151	149	147	157
-----	-----	-----	-----	-----

151	149	147	157
-----	-----	-----	-----

147	149	151	157
-----	-----	-----	-----

141	147	149	151	157
-----	----------------	-----	-----	-----

Final:-

110	111	112	117	122	123	133	141	147	149	151	157
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

Quick Sort (Last element as pivot)

Code:

```
//CH.SC.U4CSE24120
#include <stdio.h>
int PartitionLast(int a[], int low, int high) {
    int pivot = a[high];
    int i = low;
    int j = high - 1;
    while (1) {
        while (i <= j && a[i] <= pivot)
            i++;
        while (j >= i && a[j] > pivot)
            j--;
        if (i >= j)
            break;
        int temp = a[i];
        a[i] = a[j];
        a[j] = temp;
    }
    int temp = a[i];
    a[i] = a[high];
    a[high] = temp;
    return i;
}
void quickSort(int a[], int low, int high) {
    if (low < high) {
        int p = PartitionLast(a, low, high);
        quickSort(a, low, p - 1);
        quickSort(a, p + 1, high);
    }
}
int main() {
    int a[] = {157, 110, 147, 122, 111, 149, 151, 141, 123, 112, 117, 133};
    int n = sizeof(a) / sizeof(a[0]);
    quickSort(a, 0, n - 1);
    printf("Sorted array:\n");
    for (int i = 0; i < n; i++)
        printf("%d ", a[i]);

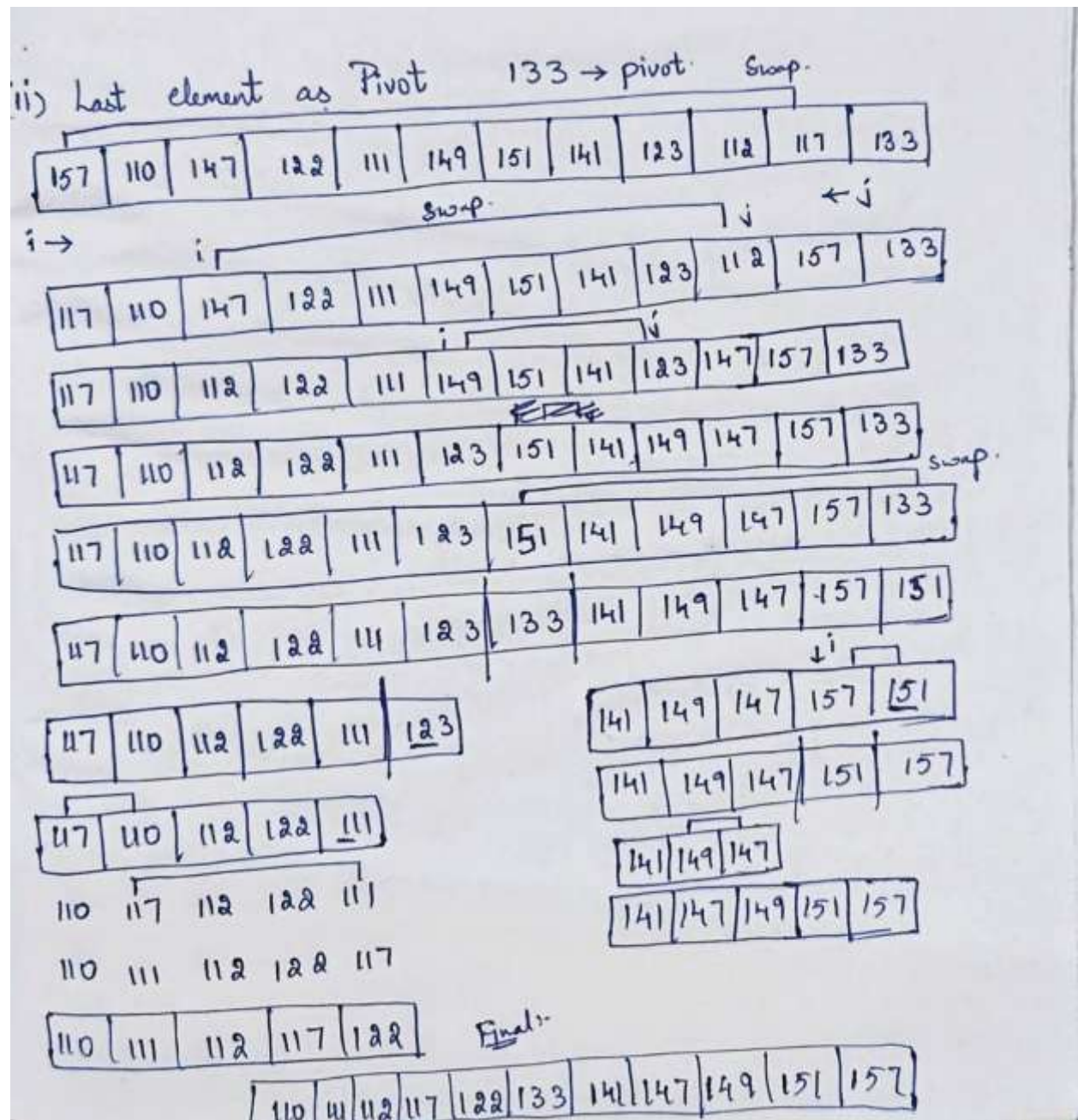
    return 0;
}
```


Output:

Sorted array:

110 111 112 117 122 123 133 141 147 149 151 157

Working:



Quick Sort (Random element as pivot)

Code:

```
//CH.SC.U4CSE24120
#include <stdio.h>
int PartitionLast(int a[], int low, int high) {
    int pivot = a[high];
    int i = low;
    int j = high - 1;
    while (1) {
        while (i <= j && a[i] <= pivot)
            i++;
        while (j >= i && a[j] > pivot)
            j--;
        if (i >= j)
            break;
        int temp = a[i];
        a[i] = a[j];
        a[j] = temp;
    }
    int temp = a[i];
    a[i] = a[high];
    a[high] = temp;
    return i;
}
void quickSort(int a[], int low, int high) {
    if (low < high) {
        int p = PartitionLast(a, low, high);
        quickSort(a, low, p - 1);
        quickSort(a, p + 1, high);
    }
}
int main() {
    int a[] = {157, 110, 147, 122, 111, 149, 151, 141, 123, 112, 117, 133};
    int n = sizeof(a) / sizeof(a[0]);
    quickSort(a, 0, n - 1);
    printf("Sorted array:\n");
    for (int i = 0; i < n; i++)
        printf("%d ", a[i]);

    return 0;
}
```

Output:

Sorted array:

110 111 112 117 122 123 133 141 147 149 151 157

Working:

iii) Random element as pivot. Pivot $\rightarrow 123$.
Choose any random element & swap it with first element.

157	110	147	122	111	149	151	141	123	112	117	133
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

$i \rightarrow$ $j \rightarrow$

123	110	147	122	111	149	151	141	157	112	117	133
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

123	110	117	122	111	149	151	141	157	112	147	133
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

123	110	117	122	111	112	151	141	157	149	147	133
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

111	110	117	122	112	123	151	141	157	149	147	133
-----	-----	-----	-----	----------------	-----	-----	-----	-----	-----	-----	-----

111	110	117	122	112
-----	-----	-----	-----	-----

151	141	157	149	147	133
-----	-----	-----	-----	-----	-----

149	141	157	151	147	133
-----	-----	-----	-----	-----	-----

149	141	133	151	147	157
-----	-----	-----	-----	-----	-----

149	141	133	147	151	157
-----	-----	-----	-----	-----	-----

147	141	133	149	151	157
-----	-----	-----	-----	-----	-----

147	141	133
-----	-----	-----

133	141	147	151	157
-----	-----	-----	-----	-----

112	110	111	117	122
-----	-----	-----	-----	-----

110	111	112	117	122
-----	-----	-----	-----	-----

Final:-

110	111	112	117	122	123	133	141	147	151	157
-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----

Time Complexity:

Recursive partitioning divides the array into subarrays.

The recursion depth depends on how balanced the partitions are.

Balanced partitions give logarithmic depth.

Unbalanced partitions lead to linear depth.

- Best / Average Case = **$O(n \log n)$**
- Worst Case = **$O(n^2)$**

Space Complexity:

Recursion is used for partitioning.

Recursion depth depends on the height of the recursion tree.

Average recursion depth is logarithmic.

- Average Case = **$O(\log n)$**
- Worst Case = **$O(n)$**