

# CSE 4/586: Project 2

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## 1 Dijkstra's 4-state token ring program

Consider Dijkstra's 4-state token ring algorithm described in the class. There are  $N+1$  nodes numbered  $0..N$ . Each node has two boolean variables,  $up$  and  $c$ . By definition,  $0.up = \text{True} \ \& \ N.up = \text{False}$  always hold.<sup>1</sup>

**At process 0:**

$0.c = 1.c \wedge \neg up.1 \longrightarrow 0.c := \neg 0.c$

**At process N:**

$N.c \neq (N-1).c \longrightarrow N.c := (N-1).c$

**At process j,  $j \neq 0 \wedge j \neq N$ :**

$j.c \neq (j-1).c \longrightarrow j.c := (j-1).c; j.up := \text{True}$

$j.c = (j+1).c \wedge j.up \wedge \neg (j+1).up \longrightarrow j.up := \text{False}$

### 1.1 Write a Pluscal program to represent this algorithm (20 points)

Write the algorithm in Pluscal and let TLA+ tool to translate this to TLA+. (You can study and learn from the ProcessTokenRing.tla for Dijkstra's classic token ring algorithm. See the Piazza post.)

### 1.2 Model check for invariant properties (10 points)

Provide a tight invariant property "InvProp == ??" for the program and model check the invariant.

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<sup>1</sup>The original description of the algorithm appears here <https://www.cs.utexas.edu/users/EWD/ewd04xx/EWD426.PDF>

### 1.3 Model check for stabilization (10 points)

Model check the program for stabilizing to the invariant. For this you can define the "Stabilization ==  $\Diamond$  InvProp" temporal property and add it in the "Properties" section of TLA+ model. In order to simulate arbitrarily corrupted initial state of the program, you can initialize the variables arbitrarily.<sup>2</sup>

### 1.4 Determine a suitable variant function to prove stabilization (10 points)

Provide a suitable variant property "sVariant==???" for the program and use model checking to show these properties:

- It never increases,
- It always eventually,  $\Box\Diamond$ , decreases (unless it hits the lowerbound)

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<sup>2</sup>While model-checking for stabilization, you should uncheck the "InvProp" from the Invariants of TLA+ model, otherwise you will get an invariant violation error, duh!

## 2 Dijkstra's 3-state token ring program

Consider Dijkstra's 3-state token ring algorithm described in the class. There are  $N+1$  nodes numbered  $0..N$ . Each node has a counter  $c$  with three possible values: 0,1,2. Let  $a +_3 1 \equiv (a + 1) \text{ modulo } 3$

**At process 0:**

$0.c +_3 1 = 1.c \longrightarrow 0.c := 1.c +_3 1$

**At process N:**

$(N-1).c = 0.c \wedge N.c \neq (N-1).c +_3 1 \longrightarrow N.c := (N-1).c +_3 1$

**At process  $j, j \neq 0 \wedge j \neq N$ :**

$j.c (+) 1 = (j-1).c \longrightarrow j.c := (j-1).c$

$j.c (+) 1 = (j+1).c \longrightarrow j.c := (j+1).c$

### 2.1 Write a Pluscal program to represent this algorithm (20 points)

Write the algorithm in Pluscal and let TLA+ tool to translate this to TLA+.

### 2.2 Model check for invariant properties (10 points)

Provide a tight invariant property "InvProp==???" for the program and model check the invariant.

### 2.3 Model check for stabilization (10 points)

Model check the program for stabilizing to the invariant. For this you can define the "Stabilization ==  $\Diamond$  InvProp" temporal property and add it in the "Properties" section of TLA+ model. In order to simulate arbitrarily corrupted initial state of the program, you can initialize the variables arbitrarily. <sup>3</sup>

### 2.4 Determine a suitable variant function to prove stabilization (10 points)

Provide a suitable variant property "sVariant==???" for the program and use model checking to show the three properties: It never increases, it always eventually,  $\Box\Diamond$ , decreases (unless it hits the lowerbound).

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<sup>3</sup>While model-checking for stabilization, you should uncheck the "InvProp" from the Invariants of TLA+ model, otherwise you will get an invariant violation error, duh!

### 3 Submission

Your TLA+ files should be named "4state.tla" and "3state.tla". Your model's name should be the default name *Model\_1* (do not name your model file differently).

Generate a pdf print of your two TLA+ programs using the "Produce Pdf version" from the TLA+ menu. (This will get included in your submission automatically.)

Now create a zip file from the two ".tla" files and the corresponding ".toolbox" directories. **Name the zipfile as: proj2.zip**

Not following these directions will cause you to lose points.

You will use the submit command (*submit\_cse486* or *submit\_cse586* respectively) to submit your work. The submit command instructions are here: <https://wiki.cse.buffalo.edu/services/content/submit-script>