

① Case 1.  $K = Q = X + E$ .

Score  $K^T Q = (X + E)^T (X + E)$   
 $= (X^T + E^T) (X + E)$   
 $= (X^T X + X^T E + E^T X + E^T E)$   
 $= (X^T X + E^T E) + X^T E + E^T X$

terms meaning  $\rightarrow$

$X^T X$  and  $E^T E \rightarrow$  Captures correlations between different features for both feature and positional embedding space.

$E^T X \rightarrow$  this matrix calculates projection of each positional embedding vector in the feature space.

$X^T E \rightarrow$  this matrix calculates projection of each sample in embedding space.

Case 2  $\rightarrow K = Q = \text{Cat}(X, E)$ .

$$K = \begin{bmatrix} X & E \end{bmatrix}$$

Sort of like additional samples in features space.

Clearly  $K^T Q$  now will be the matrix which calculates covariance matrix but now with  $2N$  samples.