

* Yash is busy with
 some personal work
 & wouldn't be available for a couple
 of lectures.
 * Will start by 9.00pm.



$A(4 \times 5)$

`int T[][] A = new int[4][5];`

0 3 0 4

↓ ↓
rows cols.

A

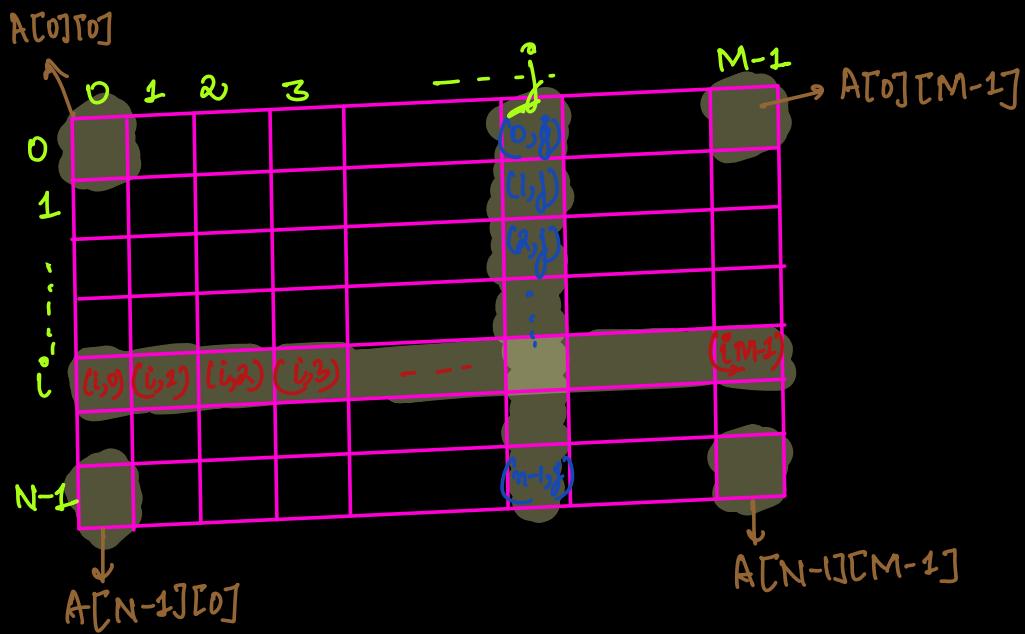
0	1	2	3	4
0				
1				
2				
3				

$\rightarrow A[1][3]$

0 M-1

$mat[N][M]$

0 N-1



Obs :-

When iterating over a row :-
 → row index $\rightarrow [0, N-1]$
 → col index $\rightarrow [0, M-1]$

When iterating over a col
 → col index $\rightarrow [0, M-1]$
 → row index $\rightarrow [0, N-1]$

Q Given a matrix (N, M) . Print row wise sum.

I/P:- mat[3][4]

O/P:-

		0	1	2	3	
		4	3	1	7	15
		6	2	3	4	15
		5	3	2	7	17.
0	1	2	3	4	5	6

```

void printRowWise( int mat[ ][ ] mat, int rows, int cols ) {
    for( int i=0; i<rows; i++ ) {
        // now I need to calculate sum for ith row.
        int sum = 0;
        for( int j=0; j<cols; j++ ) {
            sum = sum + mat[i][j];
        }
        print( sum );
    }
}

```

}

$O(M \times N)$

\downarrow rows

cols =

SC $\in O(1)$

		print colwise sum.			
		0	1	2	3
0	0	4	3	1	7
	1	6	2	3	4
2	5	3	2	7	
	15	8	6	18	

```

for( int j=0; j<cols; j++ ) {
    // need to calculate sum of jth col.
    int sum = 0;
    for( int i=0; i<rows; i++ ) {
        sum = sum + mat[i][j];
    }
    print( sum );
}

```

Q. Given a square matrix.
no. of rows = no. of cols.
Print all the diagonals.

mat[4][4].

	0	1	2	3.
0	(0,0)			
1		(1,1)		
2			(2,2)	
3				(3,3)

```
for(int i=0; i<n; i++) {
    for(int j=0; j<n; j++) {
        if( i==j ) {
            print(mat[i][j]);
        }
    }
}
```

$\underline{\underline{O(N)}}$ \leftarrow S.C $\rightarrow O(1)$.

```
int i=0, j=0;
while( i<N & j<N ) {
    print( mat[i][j] );
    i++; j++;
}
```

$i, j \rightarrow 0$
mat[0][0].

$i, j \rightarrow 1$
mat[1][1]

$i, j \rightarrow 2$
mat[2][2]

$i, j \rightarrow 3$
mat[3][3]

$\cancel{i, j \rightarrow 4}$

right to left.

Obs.

1. rowIndex $\uparrow \rightarrow$ (by 1)
2. colIndex $\downarrow \rightarrow$ (by -1)

0	1	2	3
0			(0,3)
1			(1,2)
2		(2,1)	
3	(3,0)		

$n \times n$.

$i \rightarrow 0$
 $j \rightarrow n-1$

T.C $\rightarrow O(N)$
S.C $\rightarrow O(1)$

`int i=0; int j = n-1;`
while (
 $i < n$ $j >= 0$
 {
 $i++$
 $j--$
 }

'i' is within bounds

'j' is within bounds

`print(mat[i][j]);`

}

Q. Given a rectangular matrix.
Iterate over diagonals. (Right \rightarrow Left)

`mat[N][M]`

`mat[a][b]`.

$m \rightarrow 6$
 $b \rightarrow m-1$

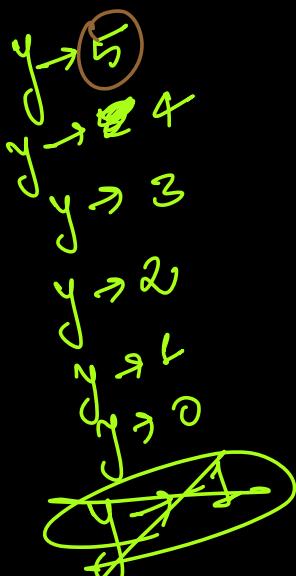
0

0 ... 1 ... 2 ... 3 ... 4 ... 5

						1st diagonal	2nd diagonal
						(i, j)	(i, j)
						$(0, 0)$	$(0, 4)$
0	0	$(0, 1)$	$(0, 2)$	$(0, 3)$	$(0, 4)$	$(0, 5)$	
1	$(1, 0)$	$(1, 1)$	$(1, 2)$	$(1, 3)$	$(1, 4)$		$(0, 5)$
2	$(2, 0)$	$(2, 1)$	$(2, 2)$	$(2, 3)$			$(1, 4)$
3	$(3, 0)$	$(3, 1)$	$(3, 2)$				$(2, 3)$

$\rightarrow I \text{ want } i < n \text{ and } j \geq 0$

5	9	13
4	8	12
3	7	11
2	6	
1		



```
for(int y=m-1; y>=0; y--) {
```

int i=0] point diagonal with starting indices as (i, j)
int j=y]

```
while( i < n && j >= 0 ) {
```

```
    point( mat[i][j] );
    i++;
    j--;
}
```

j	1st diagonal	2nd diagonal
	(i, j)	(i, j)
	$(0, 5)$	$(0, 4)$
	$(1, 4)$	$(1, 3)$
	$(2, 3)$	$(2, 2)$
	$(3, 2)$	$(3, 1)$
	$(4, 1)$	$(4, 0)$

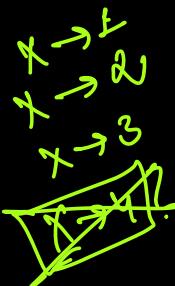
	0	1	2	3	4	5
0	(0,0)	(0,1)	(0,2)	(0,3)	(0,4)	(0,5)
1	(1,0)	(1,1)	(1,2)	(1,3)	(1,4)	(1,5)
2	(2,0)	(2,1)	(2,2)	(2,3)	(2,4)	(2,5)
3	(3,0)	(3,1)	(3,2)	(3,3)	(3,4)	(3,5)

$i \downarrow$ $j \rightarrow$

1st diagonal
 (i, j)
 $(1, 5)$
 $(2, 4)$
 $(3, 3)$

2nd diagonal
 (i, j)
 $(2, 5)$
 $(3, 4)$

$$\frac{N=4}{3?}$$



```
for(int x=1; x<N; x++) {
```

int i=x point diagonal with starting index as (i, j)
 int j=M-1

```
while( i < n && j >= 0) {
```

```
    point( mat[i][j] );
    i++;

```

} $\frac{\text{1st diagonal}}{(i,j)}$ $\frac{\text{2nd diagonal}}{(i,j)}$

$(0,5)$ $(0,4)$

$(1,4)$ $(1,3)$

$(2,3)$ $(2,2)$

$(3,2)$ $(3,1)$

$\boxed{(4,0)}$ $(4,0)$

OVERALL
CODE:

```
for(int y=m-1; y>=0; y--) {
```

 int i = 0] point diagonal with starting
 int j = y indices as (i,j)

```
    while( i < n && j >= 0) {
```

 point(mat[i][j]);
 i++;
 j--;

```
    }
```

T.C $\rightarrow O(N+N)$
↓
cols rows.

S.C $\rightarrow O(1)$

```
for(int x=1; x < N; x++) {
```

 int i = x point diagonal with starting
 int j = M-1 indices as (i,j)

```
    while( i < n && j >= 0) {
```

 point(mat[i][j]);
 i++;
 j--;

```
    }
```

Given a Mat[N][N]. Calculate Transpose
 → S.C. → O(1)

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

	0	1	2	3	4
0	1	6	11	16	21
1	2	7	12	17	22
2	3	8	13	18	23
3	4	9	14	19	24
4	5	10	15	20	25

$$x(i,j) \geq x(j,i)$$

$\begin{matrix} i \\ j \end{matrix} \geq \begin{matrix} j \\ i \end{matrix}$

$$6(1,0) \Leftrightarrow 6(0,1)$$

$$18(3,2) \Leftrightarrow 18(2,3)$$

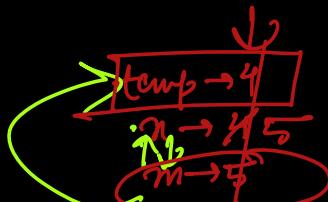
$\boxed{i,j}$

iterate in upper Δ or lower Δ.

for (int i=0; i < n; i++) { } → upper Δ
 for (int j=i; j < n; j++) { }
 swap(arr[i][j], arr[j][i]);
 }

S.C. = O(1)

swap(
 $\frac{4}{n}, \frac{5}{m}$)
 $\{$
 $\text{temp} = m;$
 $\boxed{n = m;}$
 $m = \text{temp};$;
 }



	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

$i \rightarrow 0 \text{ to } n-1$
 $j \rightarrow 0 \text{ to } n-1$
 $i=0, j \rightarrow [0, 1, 2, 3, 4]$
 $a[0][1] \rightarrow a[1, 0]$
 $a[0][2] \rightarrow a[2, 0]$
 $i=1, j \rightarrow [0, 1, 2, 3, 4]$
 $a[1][0] \rightarrow a[0, 1]$
 $\downarrow \quad \downarrow$
 $a \quad b$

Rectangular matrix. (you will need space)

($\frac{A}{2 \times 5}$)

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10

$A(i, j) \rightarrow AT(j, i)$

$A(m \times n)$

AT

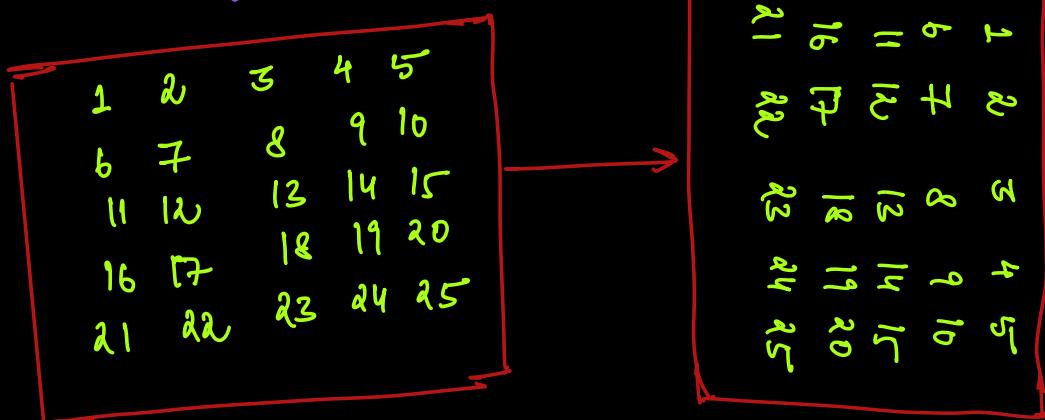
0	1	
1	6	
2	2	7
3	3	8
4		9
5		10

$t_{transpose} = \text{new int}[m][n];$
 $\{ \text{for (int } i=0; i < n; i++) \}$
 $\{ \text{for (int } j=0; j < m; j++) \}$
 $\{ \quad t[j][i] = arr[i][j]; \}$
 $\}$

$\Rightarrow S.C.$

Q.

Given a mat $N \times N$.
Rotate it by 90° in clockwise direction.



* Think in terms of transpose.
(of given array).