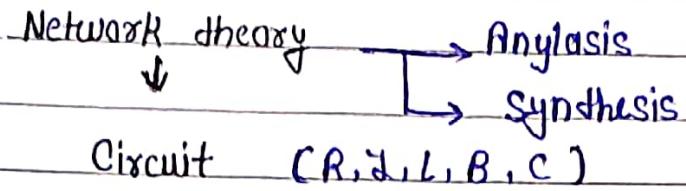
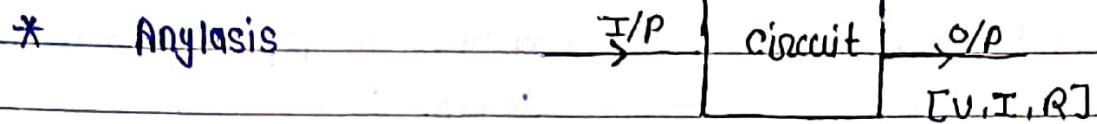


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## Basic electrical & electronics



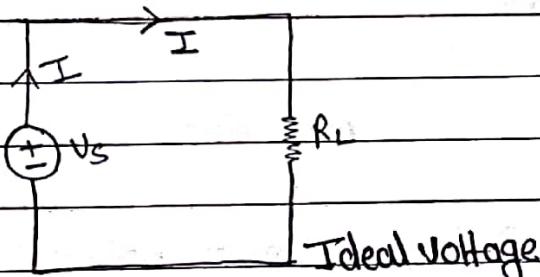
Circuit  $\rightarrow$  It can be made by electrical elements like as (Register, Inductor, Capacitor, Voltage, current, Power) etc.



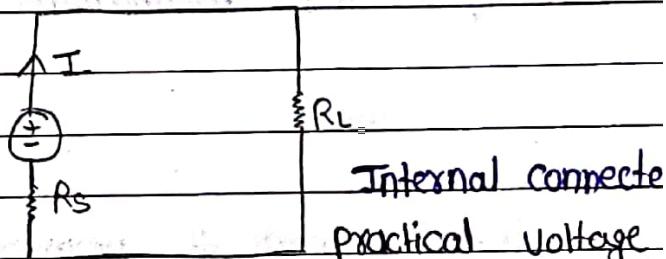
Network  $\rightarrow$  Network may be or may not be their in closest loop but circuit are always in close loop-

Ideal and practical source (V/I)

Ideal and practical voltage source



No internal resistance  
Delivers always constant  
Voltage across the  
load.



It has some voltage drop  
across the internal resistor  
So can not deliverse constnt  
voltage

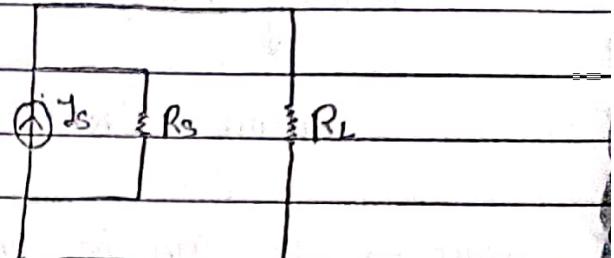
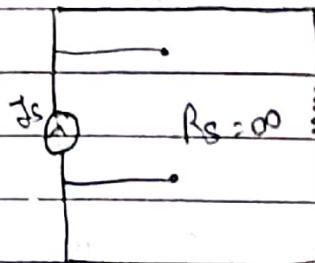
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## Ideal & Practical current Sources :-



Ideal current source

Practical current source

- ① It has  $\infty$  resistance in parallel across current source  $Is$ .
- ② It delivers constant current to load  $R_L$ .

- ① It has finite resistance  $R_s$  connected in parallel to current source  $Is$ .
- ② It cannot give constant current to load  $R_L$  because current goes through  $R_s$  internal resistance.

## \* Classification of network :-

There are four types of network :-

- 1. Linear and non linear network
- 2. Bilateral and unilateral network
- 3. active and passive network
- 4. lumped and distribution network

linear

non linear

for linear network the parameter of the network will not change with respect to temperature, voltage or current no as linear current ex  $R, L, C$  or  $A$ .

for non linear network parameter of network will change respect to temp, voltage or current known as non linear current ex - diode, transistor, FET

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### Biletral

- for biletral network behaviour remains same when current flows from both direction.



### Uniletral

- In uniletral networks behaviour depend to direction of current.



### Active

- for active network it contains elements which deliver power ex. voltage source, current source in a network

### Passive

- for passive network it does not contain element which deliver power.

Eg RLC circuit.

### Jumped

- jumped networks work at low frequency

### Distributed

- It is work as high frequency and micro frequency.

- \* Electric charge & electric current
- electric charge

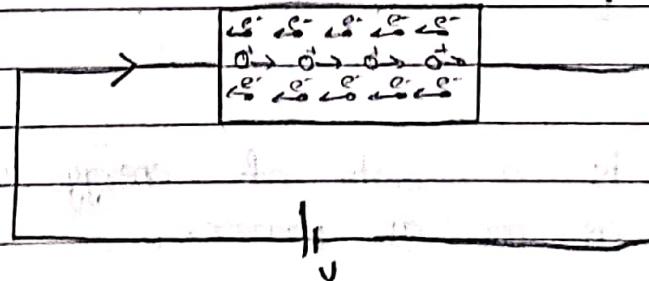
$$p^+ = +ve = 1.6 \times 10^{-19} C$$

n - no charge

$$e^- = -ve = -1.6 \times 10^{-19} C$$



### Electric current



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\* Electric current is rate of change charge w.r.t time is known as electric current.

$$I = \frac{dQ}{dt}$$

$\therefore Q$  = charge

$$\int dQ = \int I \cdot dt$$

$$Q = \int I \cdot dt$$

(Q) If charge is a function of time as per  $Q(t) = 2t^2 + 3t + 5$  then find current at 0.1 s.

$$I = \frac{dQ}{dt}$$

$$I = \frac{d(2t^2 + 3t + 5)}{dt}$$

$$I = 4t + 3$$

$$I = 4(0.1) + 3 = 3.4 \text{ Amp}$$

= Voltage (Potential) : It is a amount of work required to be done to bring 1 unit charge from infinite to given point.

Unit of voltage = Joule / Coulomb

$$V = \frac{dq}{dq}$$

$\therefore V$  = Work / Energy

power & energy

Power  $\rightarrow$  It is a state of energy with respect to time as man as power.

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$$P_1 \frac{dw}{dt}$$

Joule  
sec

watt

$$mW = 10^{-3} \text{ watt}$$

$$uW = 10^{-6} \text{ watt}$$

$$mW = 10^{-9} \text{ watt}$$

$$kW = 10^3 \text{ watt}$$

$$mW = 10^6 \text{ watt}$$

$$GW = 10^9 \text{ watt}$$

$$P = \frac{dw \times dt}{dt}$$

$$P_1 V I$$

$$P_2 V^2 / R$$

$$P_3 I^2 R$$

# Energy : If it is a capacity of workdone is non as energy.

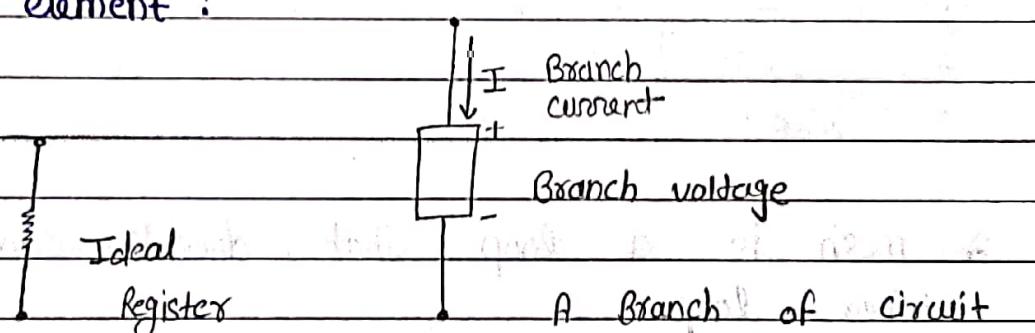
$$P_1 \frac{dw}{dt}$$

$$\int dw, \int P \cdot dt$$

$$W, \int P \cdot dt$$

Joule.

# Branch of circuit : A branch is any portion of the circuit with two terminals connected to it. A branch may consist of one or more circuit element.



Battery

In Branch

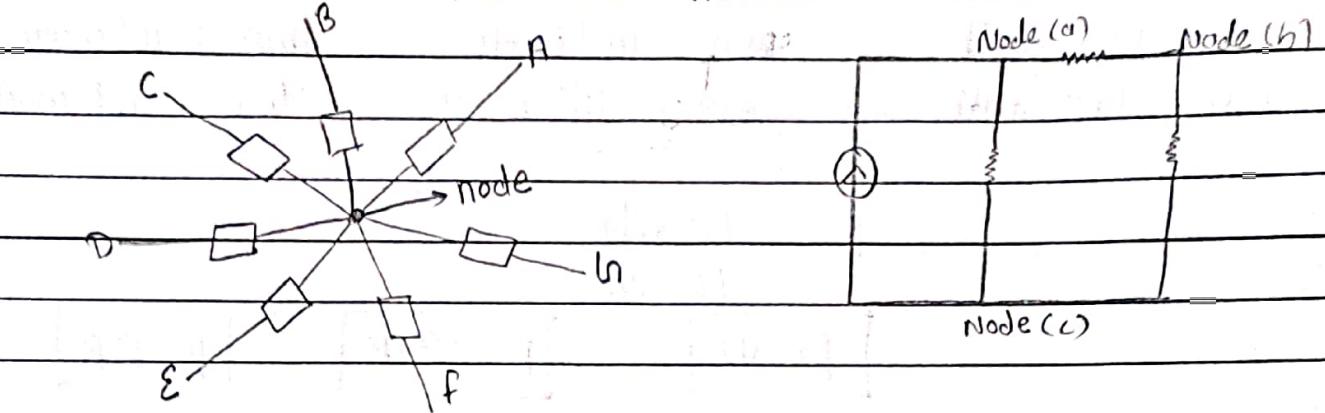


Practical  
ammeter

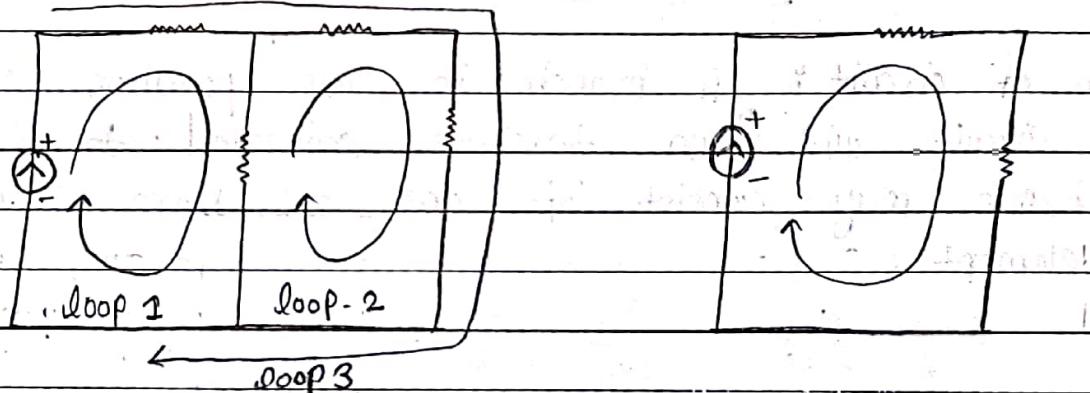
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# Node :- A node is the junction of two or more branches non as node.



# Loop :- A loop is a close path by starting a node passing through a set of nodes and returning to the starting node, without passing through any node more than once.

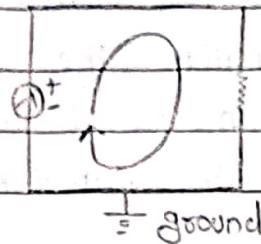


= mesh :- A mesh is a loop that doesn't contain other loop.

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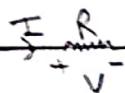
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Circuit ground :



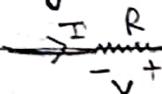
\* Ohm's law  $\rightarrow$  The voltage across the element is directly proportional to the current flowing through it

$$V \propto I$$



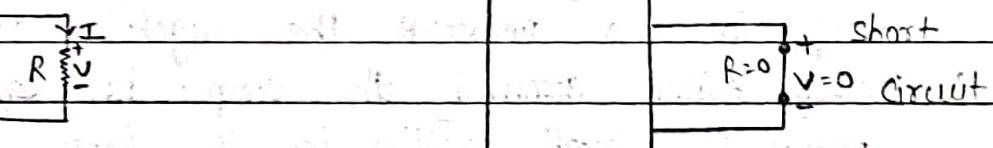
$$V = IR$$

If polarity change so

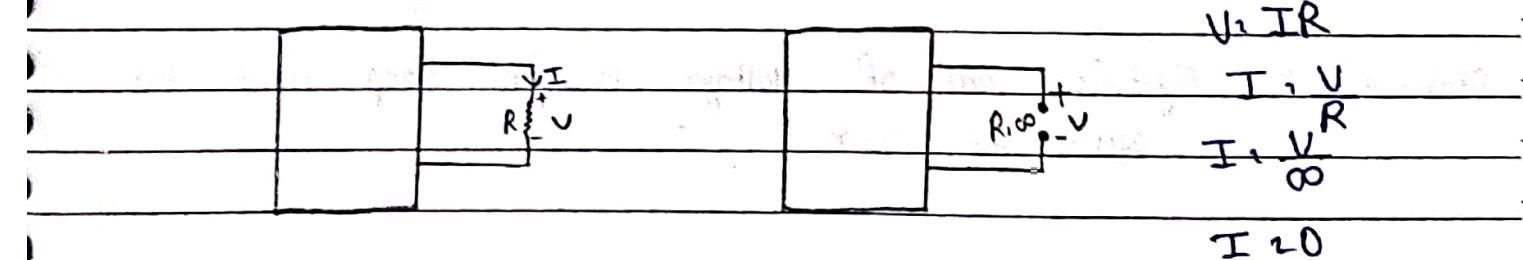


$$V = -IR$$

\* Short circuit  $\rightarrow$  An element with  $R=0$  is called short circuit.



\* Open circuit  $\rightarrow$  An element with  $R=\infty$  is known as open circuit.



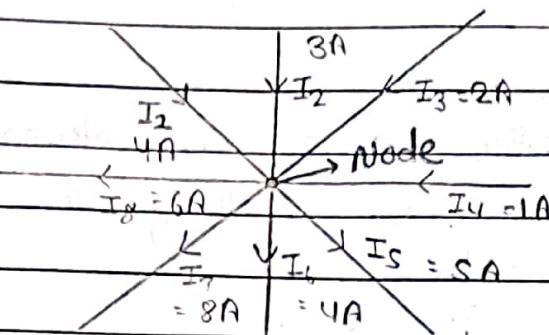
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- \* KCL (Kirchhoff current law)  $\rightarrow$  KCL states that at any junction (node) in an electric circuit the total current flowing towards that junction is equal to the total current flowing away from the junction.



at any node

$$\sum \text{Income} = \sum \text{Outgoing}$$

$$I_1 + I_2 + I_3 + I_4 = I_5 + I_6 + I_7 + I_8$$

$$3 + 4 + 2 + 1 = 5 + 4 + 8 + 6$$

$$4 + 3 + 2 + 1 - 5 - 4 - 8 - 6$$

$$-13 = \text{Ans}$$

- \* KVL (Kirchhoff voltage law)  $\rightarrow$  KVL states that in any closed loop in a network the algebraic sum of the voltage drop taken around the loop is equal to the resultant emf active in the loop.

Note :- Kirchhoff current law is based on law of charge conservation.

Statement :- Algebraic sum of voltage is in loop must be equal to zero.

Date.....

$$V = V$$

$$V = -IR$$

$$V = -\frac{1}{C} \int I \cdot dt$$

$$V = \frac{1}{C} \int I \cdot dt$$

$$V - IR_1 - IR_2 - IR_3 = 0$$

$$\underline{V = IR_1 + IR_2 + IR_3}$$

Sum of  
Voltage rise      sum of  
Voltage drop

$$I_0 = IS + IOI + IST$$

$$I = \frac{10}{30}$$

$I = 0.33A$

$$V_b = 10V$$

$$R_1 = 5\Omega$$

$$V_b = V_d - IR_1$$

$$= 10 - 0.33$$

$$= 8.67V$$

$$V_d = 10V$$

$$R_2 = 10\Omega$$

$$V_c = IR_3$$

$$R_3 = 5\Omega$$

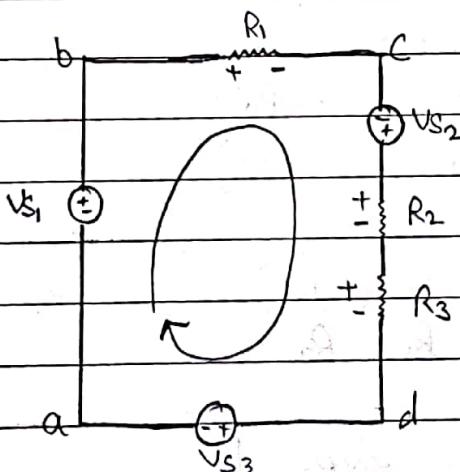
$$\approx 1V$$

$$V_c = V_b - IR_2$$

$$= 8.67 - 0.33$$

$$= 8.34V$$

Ques



$$VS_1 - IR_1 + VS_2 - IR_2 - IR_3 - VS_3 = 0$$

$$VS_1 + VS_2 - VS_3 = IR_1 + IR_2 + IR_3$$

Spiral



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\* Registers in series :

$R_1 \parallel R_2 \parallel R_3$

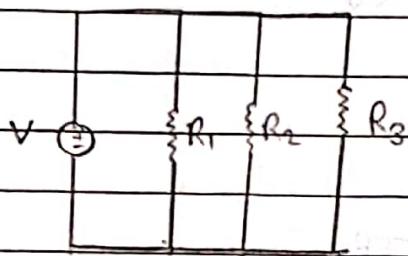
(+) v

$$R_{eq} = R_1 + R_2 + R_3$$

$$R_{eq} = R_1 + R_2 + R_3$$

(+)

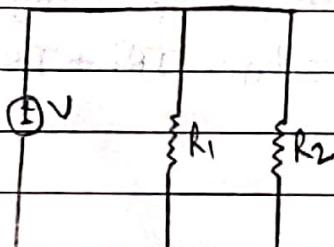
\* Registers in parallel :



$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\leftarrow \text{Power in Series} = \frac{P_1}{P_1} + \frac{P_2}{P_2} + \frac{P_3}{P_3} + \dots + \frac{P_n}{P_n}$$

$$\leftarrow \text{Power in parallel} = P_1 + P_2 + P_3 + \dots + P_n$$



$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_{eq} = \frac{R_1 \times R_2}{R_1 + R_2}$$

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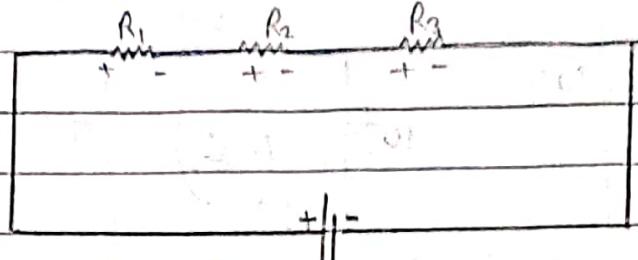


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\* Voltage divider rule :-

Current source



Apply KVL in loop I

$$V - IR_1 - IR_2 - IR_3 - \dots - IR_n = 0$$

$$V = IR_1 + IR_2 + IR_3 + IR_4 + \dots + IR_n$$

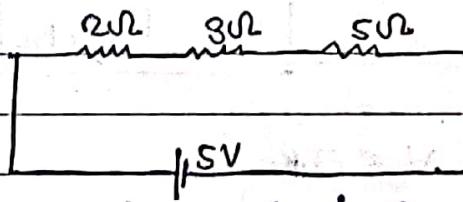
$$\boxed{I = \frac{V}{R_1 + R_2 + \dots + R_n}}$$

$$V_1 = IR_1 = \frac{R_1}{R_1 + R_2 + \dots + R_n} V$$

$$V_2 = IR_2 = \frac{R_2}{R_1 + R_2 + \dots + R_n} V$$

$$V_n = IR_n = \frac{R_n}{R_1 + R_2 + \dots + R_n} V$$

Ques find V



$$V_1 = \left( \frac{9}{9+3+5} \right) \times 5 = \frac{9 \times 5}{17} = 2.7 \text{ V}$$

$$V_2 = \frac{3 \times 8}{10 \times 2} = 1.5 \text{ V}$$

$$V_3 = \frac{8 \times 5}{10 \times 2} = 2.5 \text{ V}$$

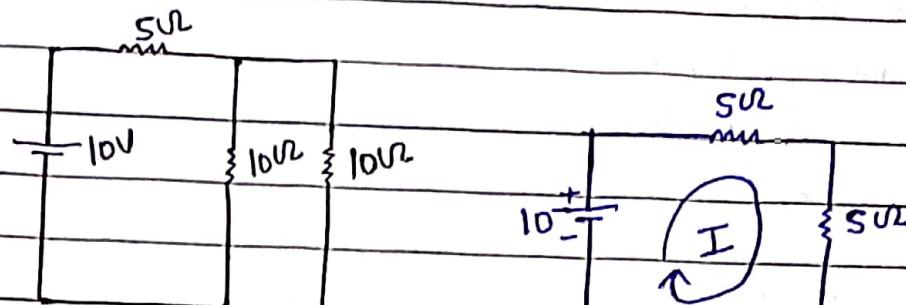
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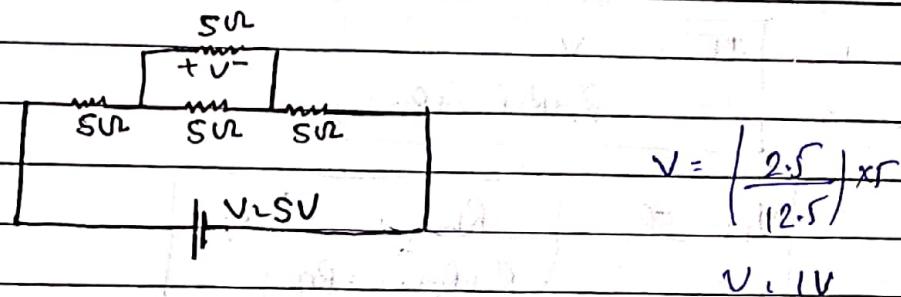
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Ques Find  $V$



$$\left( \frac{R_1}{R_1 + R_2} \right) V_2 = \frac{5 \times 10}{10} = 5V$$

Ques find  $V$



$$V = \left( \frac{2.5}{12.5} \right) \times r$$

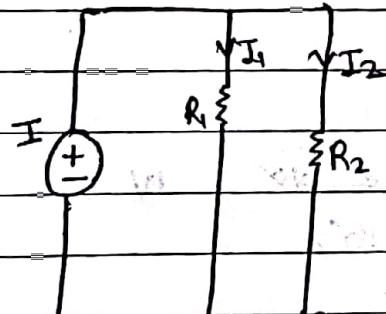
$$V = 1V$$

- Current divider rule :- across the  $R_1$  &  $R_2$ , in parallel
- Voltage  $R_1$  &  $R_2$  is same

$$V_1 = V_2 = V_T$$

$V_T$  is Reg. I

$$V_T = \left( \frac{R_1 R_2}{R_1 + R_2} \right) I$$



$$V = I_1 R_1$$

$$\left( \frac{R_1 R_2}{R_1 + R_2} \right) I = I_1 R_1$$

$$I_1 = \left( \frac{R_2}{R_1 + R_2} \right) I$$

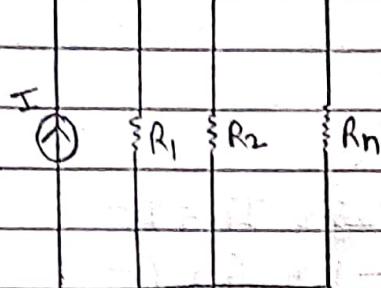
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$$V_2 = I_2 R_2$$

$$\left( \frac{R_1 R_2}{R_1 + R_2} \right) I = I_2 R_2$$

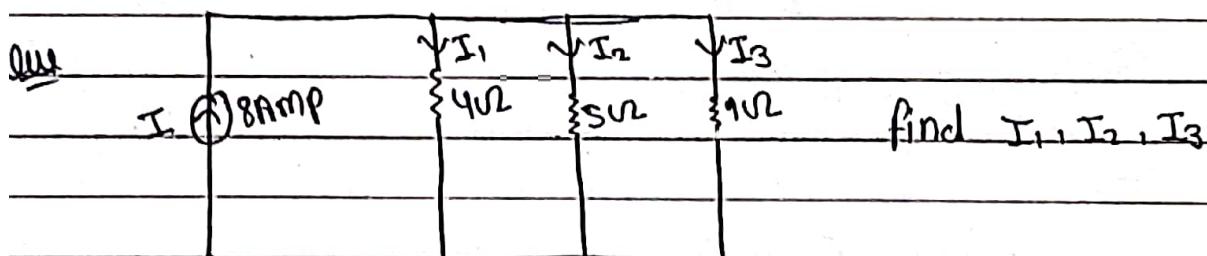
$$I_2 = \left( \frac{R_1}{R_1 + R_2} \right) I$$



When more than two Registers are connected in parallel then current divider rule is apply as.

$$I_1 = \left( \frac{Y_{R_1}}{Y_{R_1} + Y_{R_2}} \right) I$$

$$I_n = \left( \frac{Y_{R_n}}{Y_{R_1} + Y_{R_2} + \dots + Y_{R_n}} \right) I$$



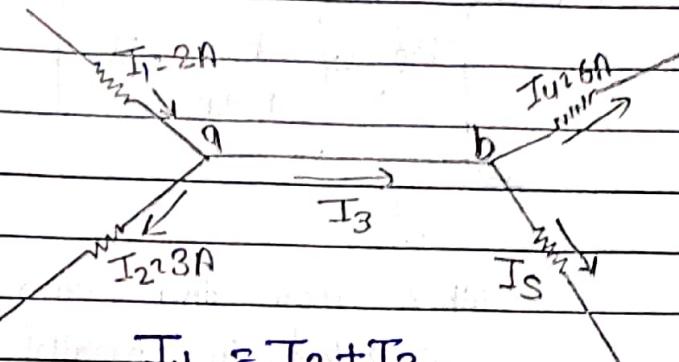
$$I_1 = \left( \frac{1/4}{1/4 + 1/5 + 1} \right) \times 8$$

$$= \left( \frac{1/4}{\frac{5+4+20}{20}} \right) \times 8$$

$$= \frac{\frac{1/4}{29}}{20^5} \times 8 = \frac{40}{29}$$

Date.....

Determined the magnitude and correct direction of the current  $I_3$  &  $I_5$  for a network?



$$I_1 = I_2 + I_3$$

$$2 - 3 = I_3$$

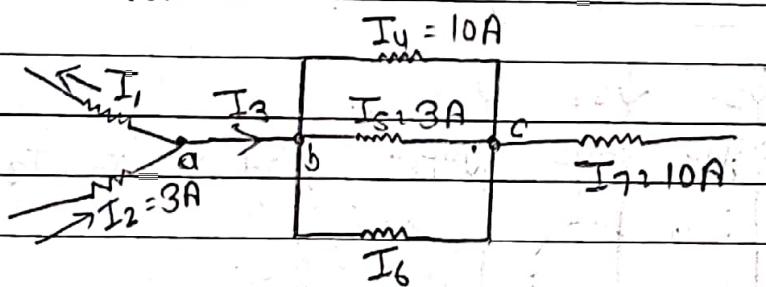
$$I_3 = -1A$$

$$I_3 = I_4 + I_5$$

$$-1 = 6 + I_5$$

$$I_5 = -7A$$

Find the magnitude of the unknown current for the circuit?



$$I_1 = I_2 + I_3$$

$$I_3 = I_5 + I_4 + I_6$$

$$I_4 + I_5 + I_6 = I_7$$

$$10 + 3 + I_6 = 10$$

$$I_6 = -3A$$

$$I_3 = 8 + 10A - 3A$$

$$I_3 = 10A$$

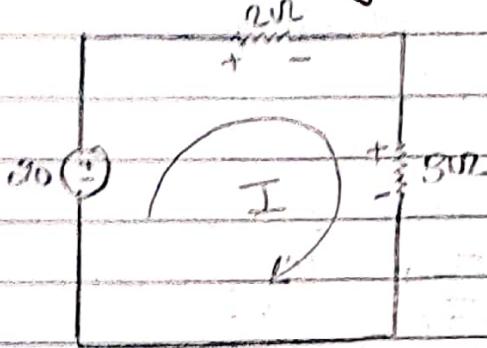
$$I_1 = 3 + 10$$

$$I_1 = 13A$$

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Q11. For the circuit in figure find voltage  $V_1$  &  $V_2$ ?



$$20 - IR_1 + IR_2 = 0$$

$$20 = 2I + 3I$$

$$20 = 5I$$

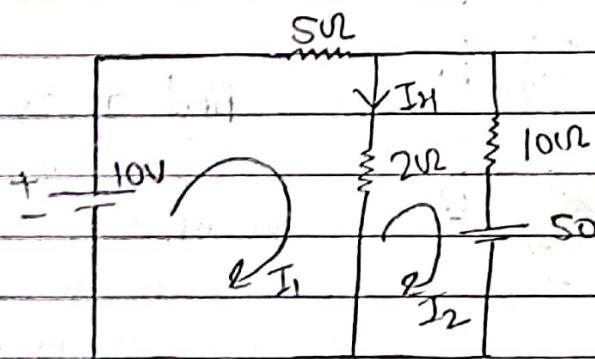
$$I = 4A$$

$$V_{1,2} = \left( \frac{R_1}{R_1 + R_2} \right) I$$

$$V_{1,2} = \left( \frac{2}{5} \right) \times 4 = 4V$$

Ans

\* Mesh analysis :-



KVL in ① loop

$$10 = 2I_1 + 2(I_1 - I_2)$$

$$10 = 2I_1 + 2I_1 - 2I_2$$

$$10 = 4I_1 - 2I_2 \quad \text{(1)}$$

KVL in ② loop

$$-50 = 2(I_2 - I_1) + 10I_2$$

$$-50 = 2I_2 - 2I_1 + 10I_2$$

$$-50 = 12I_2 - 2I_1 \quad \text{(2)}$$

Date.....

Solve the eqn (1) & (2)

$$(10 - 7I_1 - 2I_2) \times 6 \\ 60 = 42I_1 + 12I_2 \\ \underline{60 = 12I_2 - 2I_1}$$

$$10 = 40I_1$$

$$I_1 = \frac{10}{40} = 0.25A$$

Put the value of  $I_1$  in eqn (1)

$$10 = 7 \times 0.25 - 2I_2$$

$$10 = 1.75 - 2I_2$$

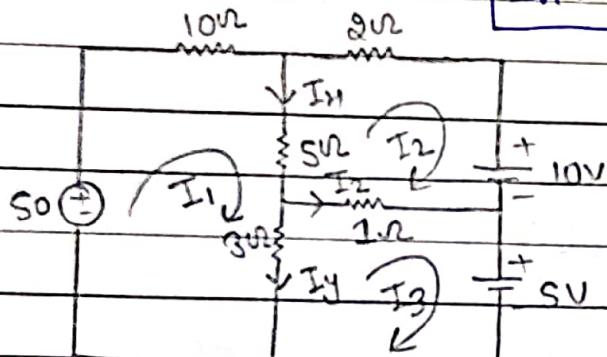
$$I_2 = \frac{10 - 1.75}{2}$$

$$\underline{I_2 = 4.125 A}$$

$$I_H = I_1 - I_2$$

$$I_H = 0.25 + 4.125$$

$$\boxed{I_H = 4.375 A}$$



find  $I_x, I_y$  &  $I_z$

KVL in loop (1)

$$So - 10I_1 - 5(I_1 - I_2) - 3(I_2 - I_3) = 0$$

$$So = 10I_1 + 5I_2 - 5I_2 + 3I_3$$

$$So = 10I_1 + 8I_2 - 3I_3 \quad (1)$$

KVL in loop (2)

$$-10 = 1(I_2 - I_3) + 5(I_2 - I_1) + 2I_2$$

$$-10 = 1I_2 - 4I_3 + 5I_2 - 5I_1 + 2I_2$$

$$-10 = 8I_2 - I_3 - 5I_1 \quad (2)$$

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KVL in loop ③

$$-S = 3(I_3 - I_1) + 1(I_3 - I_2)$$

$$-S = 3I_3 + I_3 - I_2 + 3I_1$$

$$-S = 4I_3 - I_2 + 3I_1 \quad \text{---(1)}$$

$$S_0 = 10I_1 + 8I_2 - 3I_3 \quad \text{---(2)}$$

$$-10 = 8I_2 - I_3 - SI_1 \quad \text{---(3)}$$

$$-S = 4I_3 - I_2 + 3I_1 \quad \text{---(1)}$$

$$D = \begin{vmatrix} 18 & 8 & -3 \\ -8 & 8 & -1 \\ 3 & -1 & 4 \end{vmatrix} = \frac{18(32-1) + 8(-20+3) - 3(5+24)}{-8(18) + 8(-27) - 3(+19)} = \frac{-810 + 16}{-144 - 216 - 57} = 356$$

$$D_{1,2} = \begin{vmatrix} S_0 & -S & -3 \\ 10 & -8 & 1 \\ S & 1 & -4 \end{vmatrix} = \frac{1175}{356} \quad D_2 = \begin{vmatrix} 18 & S_0 & -3 \\ S & 10 & 1 \\ 3 & S & -4 \end{vmatrix} = 355$$

$$D_3 = \begin{vmatrix} 18 & -S & S_0 \\ S & -8 & 10 \\ 3 & 1 & 5 \end{vmatrix} = 525 \quad I_1 = \frac{D_1}{D} = \frac{1175}{356} = 3.3A$$

$$I_2 = \frac{D_2}{D} = \frac{355}{356} = 0.99A$$

$$I_{x2} = I_1 - I_2$$

$$I_x = 3.3 - 0.99$$

$$I_x = 2.31 A$$

$$I_3 = \frac{D_3}{D} = \frac{525}{356} = 1.47A$$

$$I_y = I_1 - I_3$$

$$= 3.3 - 1.47$$

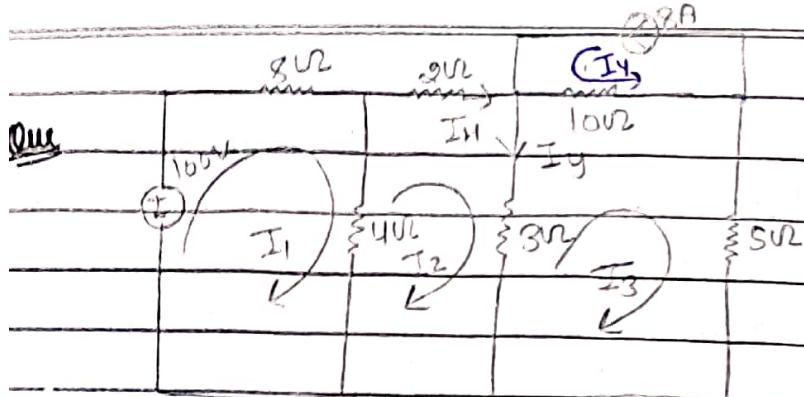
$$= 1.83 A$$

$$I_2 = I_3 - I_2$$

$$= 1.47 - 0.99$$

$$= 0.47 A$$

Date.....



Find  $I_{11}$  &  $I_y$

$$100 = 8I_1 + 4(I_1 - I_2)$$

$$100 = 8I_1 + 4I_1 - 4I_2$$

$$100 = 12I_1 - 4I_2 \quad \text{--- (1)}$$

Apply KVL in Loop (2)

$$0 = 4(I_2 - I_1) + 2I_2 + 3(I_2 - I_3)$$

$$= 4I_2 - 4I_1 + 2I_2 + 3I_2 - 3I_3$$

$$= 9I_2 - 4I_1 - 3I_3 \quad \text{--- (2)}$$

Apply KVL in Loop (3)

$$0 = 3(I_3 - I_2) + 10(I_3 + I_4) + 5I_3$$

$$= 3I_3 - 3I_2 + 10I_3 + 10I_4 + 80 + 5I_3$$

$$= 18I_3 + 80 - 3I_2 \quad \text{--- (3)}$$

$$100 = 12I_1 - 4I_2 \quad \text{--- (1)}$$

$$0 = 9I_2 - 4I_1 - 3I_3 \quad \text{--- (2)}$$

$$0 = 18I_3 + 80 - 3I_2 \quad \text{--- (3)}$$

$$\begin{array}{c|cc|c} & 12 & -4 & 0 \\ \Delta_2 & -4 & 9 & -3 \\ & 0 & -3 & 18 \end{array} \quad \begin{array}{l} 12(162 + 9) + 4(-72) \\ = 12(153) + 288 \\ 1836 - 288 = 1548 \end{array}$$

$$\Delta_1 = \begin{array}{c|cc|c} & 100 & -4 & 0 \\ & 0 & 9 & -3 \\ & -80 & -3 & 18 \end{array} \quad \begin{array}{l} 100(162 + 9) + 4(-240) \\ = 100(171) + 4(-240) \\ 17100 - 960 \\ 14340 \end{array}$$

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$$\Delta_{2,2} = \begin{vmatrix} 12 & 100 & 0 \\ -4 & 0 & -3 \\ 0 & -80 & 18 \end{vmatrix} = \frac{12(-240) - (100)(-72)}{-880 - 720} = \frac{3600}{1600} = 4320$$

$$\Delta_3 = \begin{vmatrix} 12 & -4 & 100 \\ -4 & 9 & 0 \\ 0 & -3 & -80 \end{vmatrix} = \frac{12(-720) - 4(-320) + 100(12)}{-6160}$$

$$I_{1,2} = \frac{\Delta_1}{D} = \frac{14340}{1548} = 9.26 \text{ A}$$

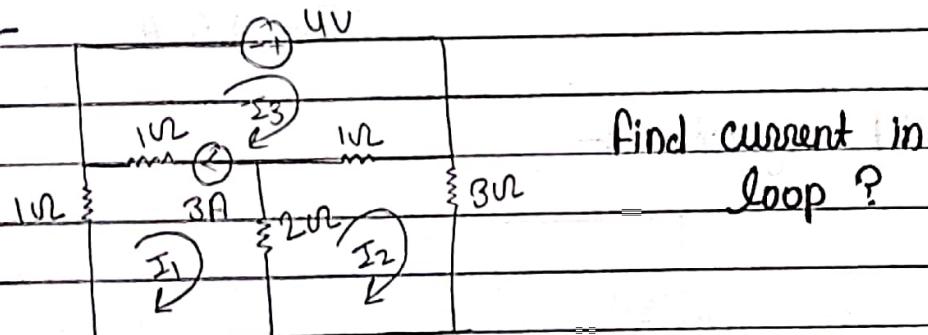
$$I_{2,2} = \frac{\Delta_2}{D} = \frac{4340}{1548} = 2.79 \text{ A}$$

$$I_3 = \frac{-6160}{1548} = -3.97 \text{ A}$$

$$I_{H2} = I_2 = 2.79 \text{ A}$$

$$I_y = I_2 - I_3 \\ \approx 6.76 \text{ A}$$

\* Super mesh :-



$$3 = I_3 - I_1 \quad (1)$$

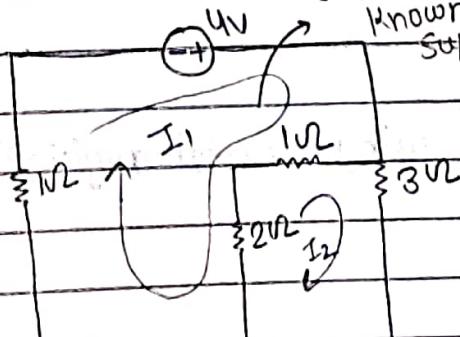
This mesh is known as super mesh

Apply in KVL in super mesh

$$4 = 9(I_1 - I_2) + 2(I_1 - I_2) + I_1$$

$$4 = I_1 - I_2 + 2I_1 + 2I_2 + I_1$$

$$4 = 4I_1 - 3I_2$$



Spiral

Date.....

Apply KVL in Loop 2

$$0 = 2(I_2 - I_1) + 1(I_2 - I_1) + 3I_2$$

$$= 8I_2 - 2I_1 + I_2 - I_1 + 3I_2$$

$$0 = GI_2 - 3I_1$$

$$4 = UI_1 - 3I_2 \times 2$$

$$8 = 8I_1 - 6I_2$$

$$0 = 6I_2 - 3I_1$$

$$\frac{8}{5} = SI_1$$

$$GI_2 - 3I_1 = 0 \quad I_1 = \frac{8}{5} = 1.6 A$$

$$GXI_2 = 3 \times \frac{8}{5}$$

$$I_2 = \frac{3 \times 8}{5} = 0.8 A$$

$$3 = I_3 - I_1$$

$$I_3 = 3 + 1.6$$

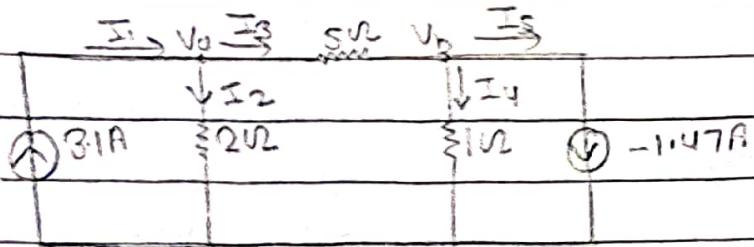
$$I_3 = 4.6 A$$

\* Nodal Analysis :-

		SUR		
		+ V -		
(1)	3A	$\sum 2V_L$	$\sum V_L$	(2) 14.7A

find V using nodal analysis?

Date.....



Apply KCL at node a

Apply KCL at node b

$$I_3 = I_1 + I_2$$

$$\frac{V_a - V_b}{S} = V_b + 1.47$$

$$I_1 + I_2 + I_3$$

$$3I = \frac{V_a}{2} + \frac{V_a - V_b}{S}$$

$$3I = SV_a + 2V_a - 2V_b$$

$$\frac{V_a - V_b - V_b}{S} = 1.4$$

10

$$3I = 7V_a - 2V_b = 0$$

$$V_b - 6V_b = 7 \quad \text{(1)}$$

$$3I = 7V_a - 2V_b$$

$$4V_a = -7V_a + 42V_b$$

$$8V_a = 40V_b$$

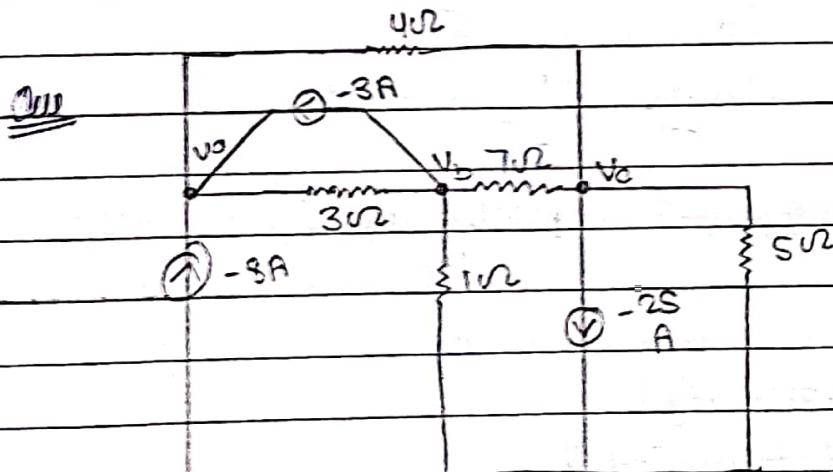
$$V_b = 2V$$

$$-7 = V_a = 6 \times 2$$

$$V_a = 5V$$

$$V_b = V_a - V_b$$

$$V = S - 2 = 3V$$



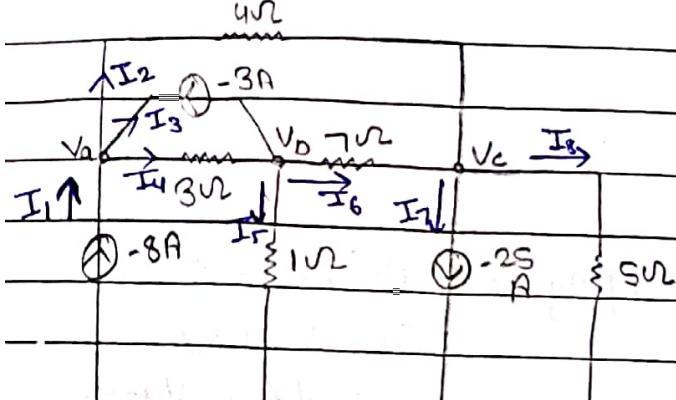
find  $V_a, V_b \& V_c$

Spiral



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Date.....



Apply KCL at node 'a'

$$I_1 = I_2 + I_3 + I_4$$

$$-8 = \frac{V_a - V_c}{4} + 3 + \frac{V_a - V_b}{3}$$

$$-8 \times 12 = 3V_a - 9V_b + 36 + 4V_a - 4V_b$$

$$-8 \times 12 = 7V_a - 8V_b + 36 - 4V_b$$

$$-96 - 36 = 7V_a - 3V_c - 4V_b$$

$$-132 = 7V_a - 3V_c - 4V_b \quad (i)$$

Apply KCL at node 'b'

$$I_3 + I_4 = I_5 + I_6$$

$$3 + \frac{V_a - V_b}{3} = \frac{V_b + V_b - V_c}{7}$$

$$3 = \frac{7V_b + V_b - V_c}{7} + \frac{V_b - V_a}{3}$$

$$3 = \frac{8V_b + 3V_b - 3V_c + 7V_b - 7V_a}{21}$$

$$63, 3V_b - 7V_a - 3V_c \quad (ii)$$

Apply KCL at node 'c'

$$I_2 + I_6 = I_7 + I_8$$

$$\frac{V_a - V_c}{4} + \frac{V_b - V_c}{7} = -\frac{2S + V_c}{5}$$

$$\frac{V_a - V_c}{4} + \frac{V_b - V_c}{7} - \frac{V_c}{5} = -2S$$

$$8V_a - 3SV_a - 3SV_c + 20V_b - 20V_c + 28V_b = -25 \\ 140$$

$$8SV_a - 8SV_c + 20V_b = -3500$$

$$-132 - 7V_a - 4V_b - 3V_c \quad (i)$$

$$63 = 3V_b - 7V_a - 3V_c \quad (ii)$$

$$-8500 = 3SV_a + 20V_b - 83V_c \quad (iii)$$

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$$D_2 = \begin{vmatrix} 7 & -4 & -3 \\ -7 & 31 & -3 \\ 35 & 20 & -83 \end{vmatrix} = -11172$$

$$D_1 = \begin{vmatrix} -132 & -4 & -3 \\ 63 & 31 & -3 \\ -3500 & 20 & -83 \end{vmatrix} = -60480$$

$$D_2 = \begin{vmatrix} 7 & -4 & -132 \\ -7 & 31 & 63 \\ 35 & 20 & -3500 \end{vmatrix} = -517440$$

$$V_{a1}, \frac{D_1}{D} = \frac{-60480}{-11172} = 5.41V$$

$$V_b = \frac{D_2}{D} = \frac{-86436}{-11172} = 7.73V$$

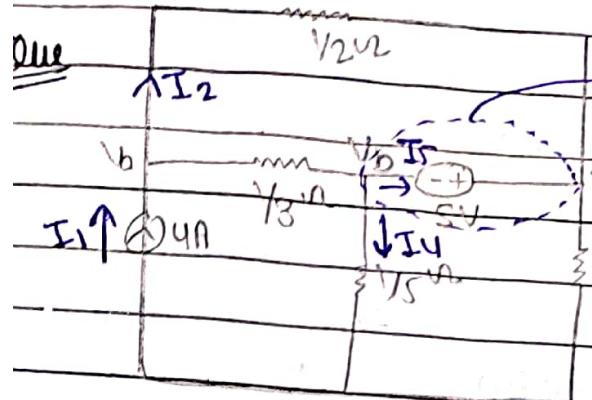
$$V_{c1}, \frac{D_3}{D} = \frac{-517440}{-11172} = 46.31V$$

\* Super node :- If is a node which a combination of two nodes known as Super node.  
when you apply KCL at super node at a time complete network of Super node consider

- a) One node entering current of super node equal to out going current of super node

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Find  $V_a, V_b, V_c$

$$SV = V_c - V_b \quad \text{---(1)}$$

Apply KCL at supernode

$$I_2 + I_3 = I_4 + I_5$$

$$\left(\frac{V_a - V_c}{1/2}\right) + \left(\frac{V_a - V_b}{1/3}\right) = \frac{V_b}{1/5} + V_c$$

$$2(V_a - V_c) + 3(V_a - V_b) = 5V_b + V_c$$

$$2V_a - 2V_c + 3V_a - 3V_b = 5V_b + V_c$$

$$SV_a - 8V_b - 3V_c = 0 \quad \text{---(2)}$$

Apply KCL at node a

$$I_1 = I_2 + I_3$$

$$I_1 = \left(\frac{V_a - V_c}{1/2}\right) + \left(\frac{V_a - V_b}{1/3}\right)$$

$$I_1 = 2V_a - 2V_c + 3V_a - 3V_b$$

$$I_1 = SV_a - 8V_b - 2V_c \quad \text{---(3)}$$

$$D_1 = \begin{vmatrix} 0 & -1 & 1 \\ 5 & -8 & -3 \\ 5 & -3 & -2 \end{vmatrix} = 30$$

$$D_1 = \begin{vmatrix} S & -1 & 1 \\ 0 & 8 & -3 \\ 4 & -3 & -2 \end{vmatrix} = 79$$

$$D_2 = \begin{vmatrix} 0 & S & 1 \\ S & 0 & -3 \\ S & 4 & -2 \end{vmatrix} = -S \quad D_3 = \begin{vmatrix} 0 & -1 & S \\ S & -8 & 0 \\ S & -3 & 4 \end{vmatrix} = 145$$

$$V_a = \frac{D_1}{D} = \frac{79}{30} = 2.63 \text{ Volt}$$

$$V_c = \frac{D_3}{D} = \frac{145}{30} = 4.85 \text{ Volt}$$

$$V_b = \frac{D_2}{D} = \frac{-5}{-30} = 0.16 \text{ Volt}$$

Spiral

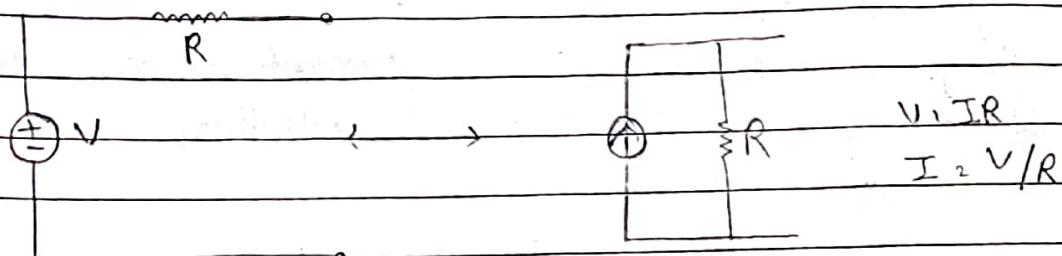


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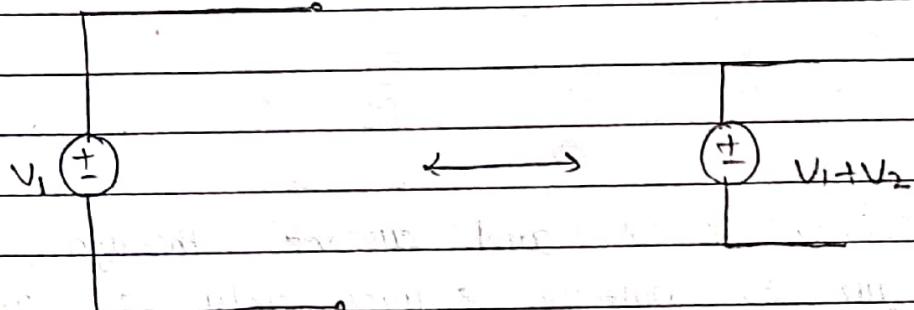
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\* Source information :-

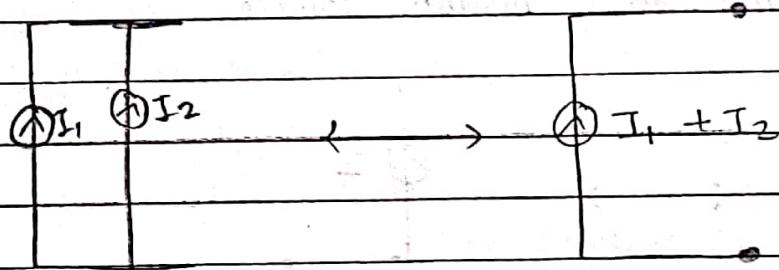
① Voltage Source to current source :-



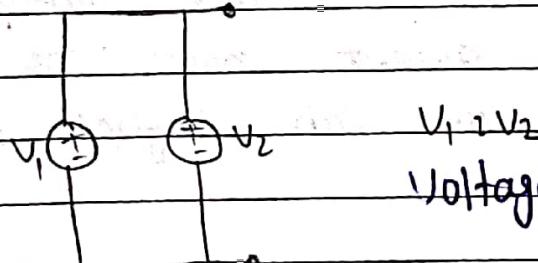
② Voltage Source in Series :-



③ if current source are in parallel :-



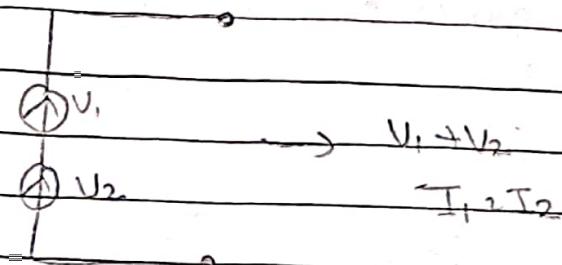
④ Voltage Source in parallel :-



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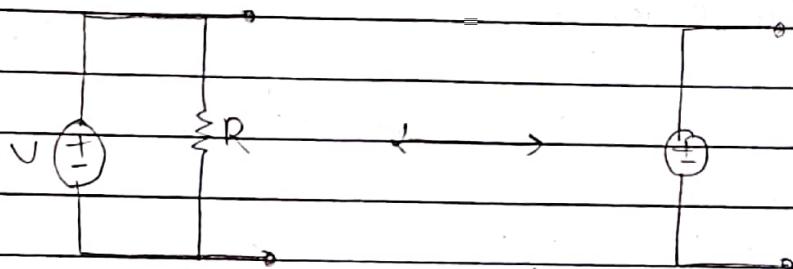
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### ⑤ Current Source in series :-



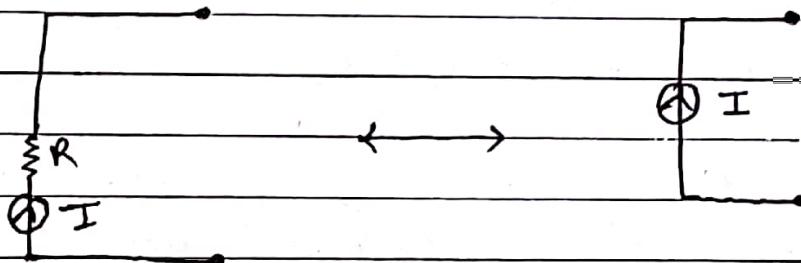
current source will be identical

### \* Network element parallel in voltage source :-



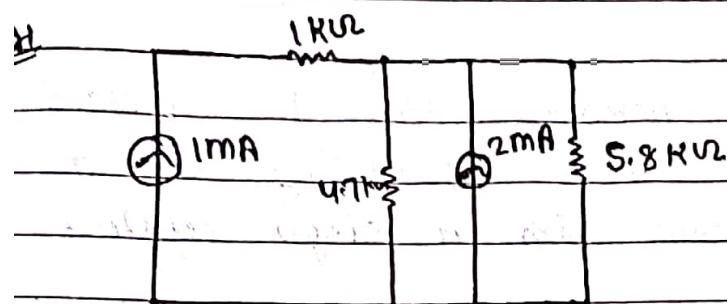
Voltage across are is ' $V$ ' and current through register is  $V/R$  due to voltage source only so we can neglect registers in network.

### \* Network element series to current source



Current across are is ' $I$ ' and Voltage across is  $(V = IR)$  due to current source. The resultant electrical network we can neglect the resistance.

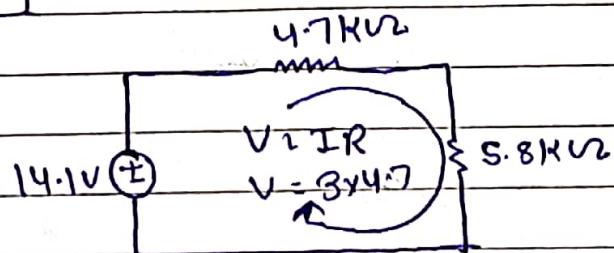
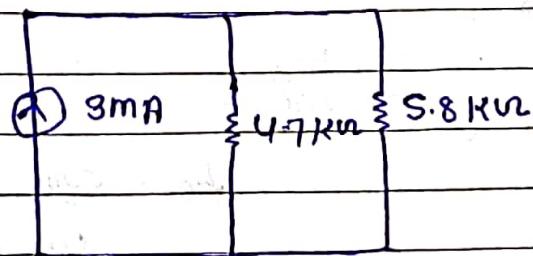
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find

power dissipation

across 5.8 kΩ



$$14.1 = 4.7 \times 10^3 + 5.8 \times 10^3$$

$$14.1 - 14.1 = 1.4$$

$$4.7 \times 10^3 + 5.8 \times 10^3$$

$$I = 1.34 \times 10^{-3} \text{ A}$$

$$P = I^2 R$$

$$P = (1.34 \times 10^{-3})^2 \times 5.8 \times 10^3$$

$$P = 10.4 \times 10^{-3} \text{ W}$$

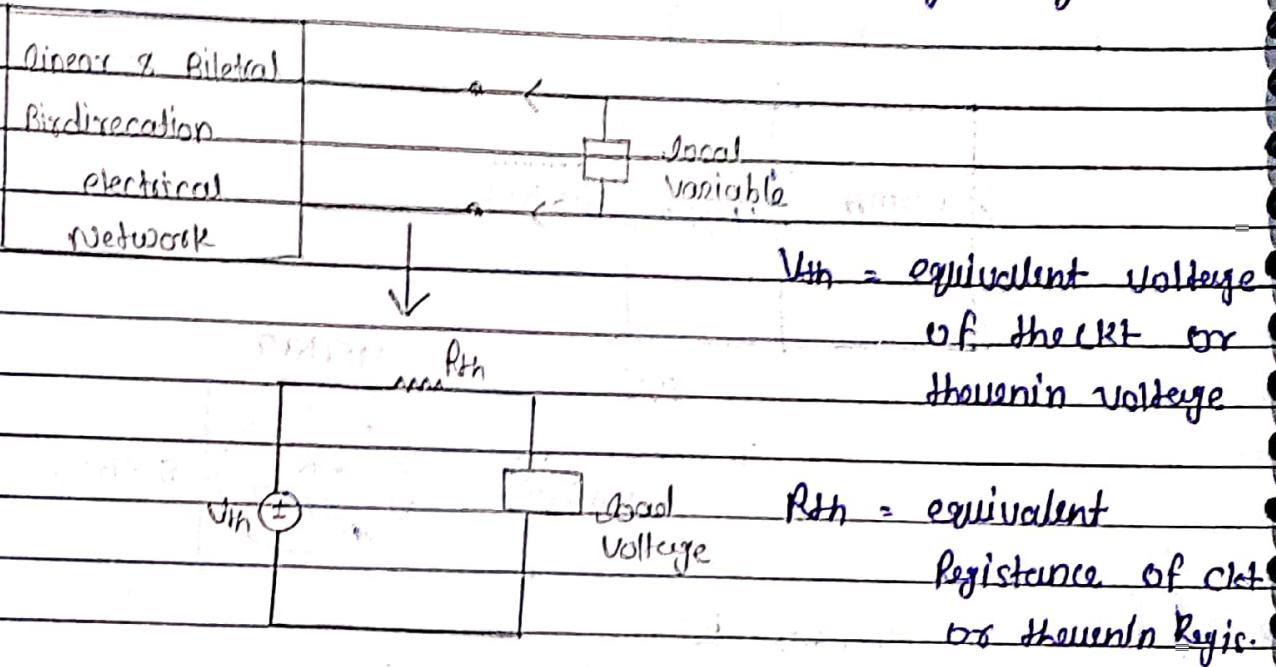
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Jmp.

### - Thévenin's theorem

A linear bilateral to terminal network can be reduced to a simplified to terminal circuit consisting of a single voltage source in series with a single register.



Steps to apply Thévenin theorem

Remove (open) the load and find the open circuit voltage at the terminal by any method - this open circuit voltage equal to Thévenin voltage.

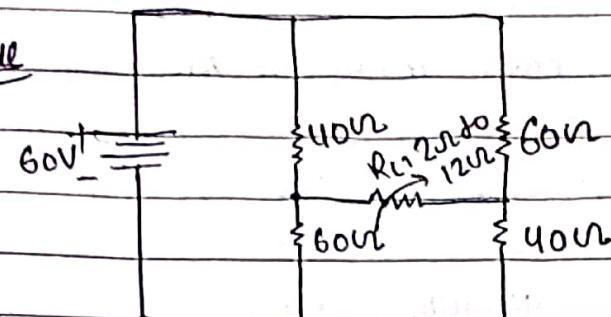
In the circuit of independent voltage source are short circuited and all independent current source are open circuited and obtain equivalent resistance  $R_{th}$  of the circuit

$[R_{th}, R_{eq}]$

Now replace the linear circuit with its Thévenin equivalent and find voltage and current of the given circuit

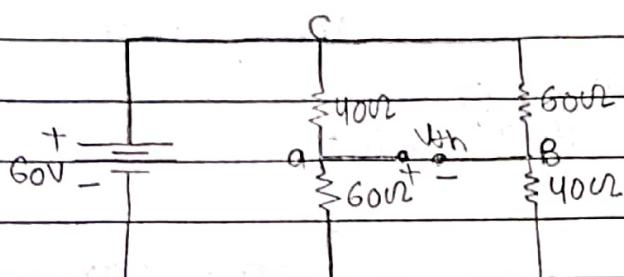
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find the range of current  
R<sub>L</sub> using thevenin theorem?

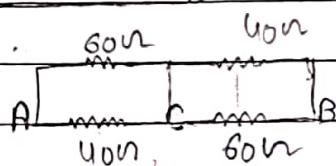
find V<sub>th</sub>



$$V_{th} = V_a - V_b$$

$$= 60 \left( \frac{60}{100} \right) - 6 \left( \frac{40}{100} \right)$$

$$= 12 \text{ Volt}$$



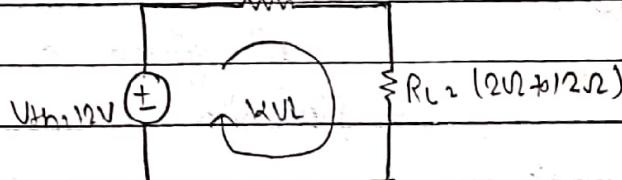
$$40 \times 160 + 60 \times 40$$

$$\frac{60 \times 40}{100} + \frac{60 \times 40}{100}$$

thevenin equivalent circuit :

$$R_{th} = 48\Omega$$

$$R_h = 48\Omega$$



Apply the KVL in ckt

$$12 = R_{th} I_L + J_C R_L$$

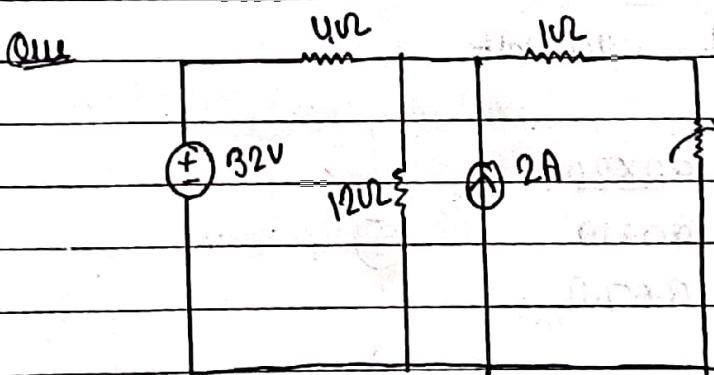
$$J_C = 12$$

$$R_{th} + R_L$$

$$I_L = \frac{12}{48+12} = 0.24 \text{ Amp}$$

$$48+12$$

$$J_L = \frac{12}{48+12} = \frac{12}{60} = 0.2 \text{ Amp}$$



$$R_L (6\Omega \text{ to } 12\Omega)$$

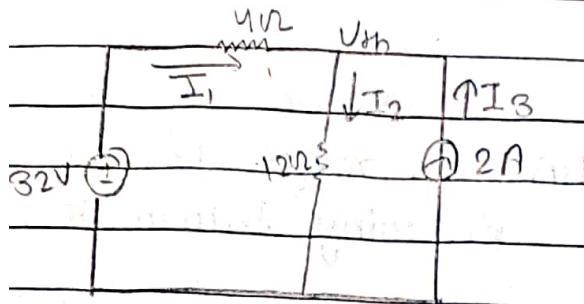
Find the Range of  
current in R<sub>L</sub> usir  
thevenin ?

Spiral



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Apply nodal analysis at node  $V_{th}$

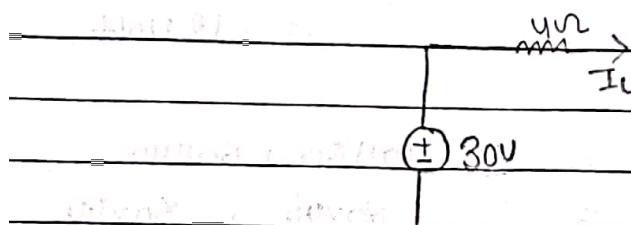
$$I_1 + I_3 = I_2$$

$$\frac{32 - V_{th}}{12} + 2 = \frac{V_{th}}{12}$$

$$96 - 4V_{th} + 24 = V_{th}$$

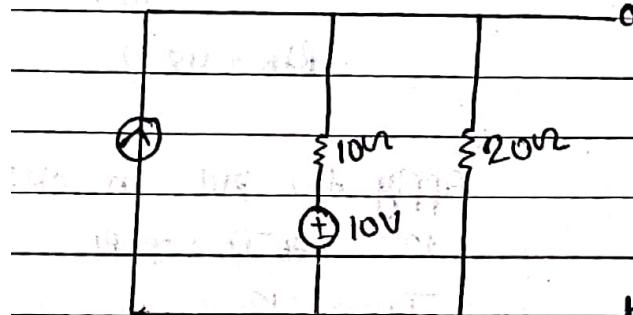
$$V_{th} = 30 \text{ Volt}$$

$$\frac{4 \times 12}{16} + 1 = V_{th}$$



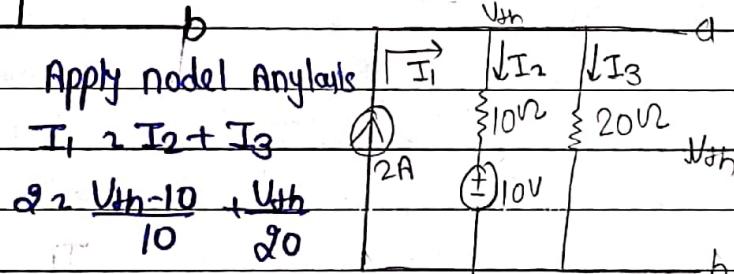
$$I_L = \frac{30}{4+6} = 3 \text{ Amp}$$

$$I_L = \frac{30}{4+12} = 1.8 \text{ Amp}$$



Find the Thevenin equivalent of given circuit?

Find  $V_{th}$



Apply nodal Analysis

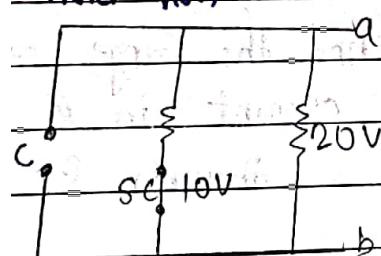
$$I_1 = I_2 + I_3$$

$$2 = \frac{V_{th} - 10}{10} + \frac{V_{th}}{20}$$

$$2 \times 20 = V_{th} - 20$$

$$V_{th} = 20 \text{ Volt}$$

Find  $R_{th}$



$R_{th} = \frac{20 \times 20}{10+20}$

$$= 8 \Omega$$

$$= 8.67 \Omega$$

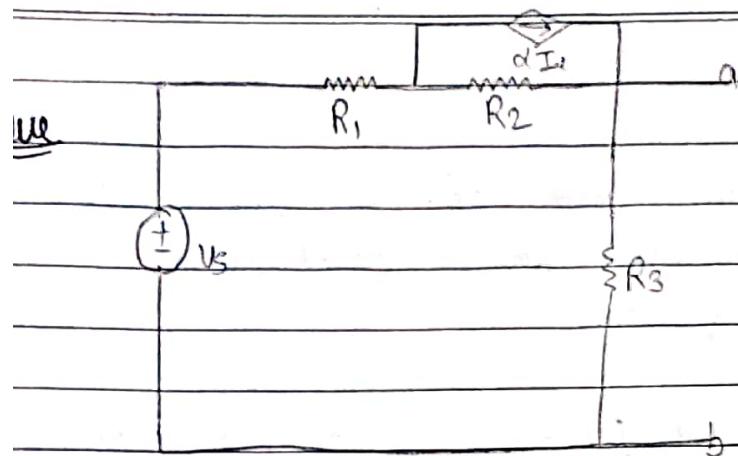
$$R_{th} = 8.67 \Omega$$

Spiral



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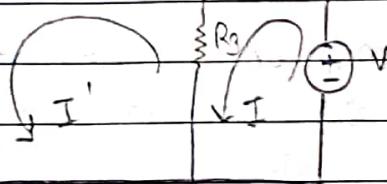
Date.....



Thévenin equivalent  
Resistance ?  
Find  $V_{th}$

Find  $R_{th}$

$$V_{th} = V_s \left( \frac{R_3}{R_1 + R_2 + R_3} \right)$$



Apply KVL in loop I'

$$-dI_H R_2 + R_1 I' + R_2 I' + R_3 I' - R_3 J$$

$$-dI_H R_2 = R_1 I' + R_2 I' + R_3 I' - R_3 J$$

$$-dI_H R_2 = I' (R_1 + R_2 + R_3) - R_3 J$$

$$V = R_3 (J' - J) \quad \text{---(1)}$$

put the value of eqn(1)

$$R_3 J + dI_H R_2 = I' (R_1 + R_2 + R_3)$$

$$R_3 \left( \frac{I (dR_2 + R_3)}{R_1 + R_2 + R_3} - J \right)$$

$$I (dR_2 + R_3) = I' (R_1 + R_2 + R_3)$$

$$I' = \frac{I (dR_2 + R_3)}{R_1 + R_2 + R_3} \quad \text{---(2)}$$

$$V = R_3 \times I \left( \frac{1 - dR_2 + R_3}{R_1 + R_2 + R_3} \right)$$

$$\frac{V}{I} = R_{th} = R_3 \left( \frac{R_1 + R_2 + R_3 - dR_2 - R_3}{R_1 + R_2 + R_3} \right)$$

$$R_{th} = R_3 \left( \frac{R_1 + R_2 - dR_2}{R_1 + R_2 + R_3} \right)$$

$$R_{th} = R_3 \left( \frac{R_1 + R_2 (1-d)}{R_1 + R_2 + R_3} \right)$$

$$V_{th} = V_s \left( \frac{R_3}{R_1 + R_2 + R_3} \right)$$

b

Spiral



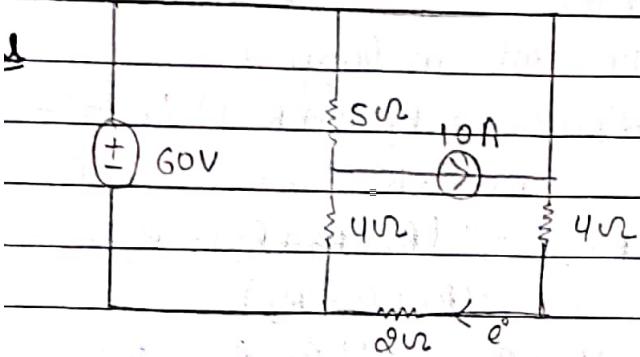
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Superposition theorem  $\rightarrow$

The total current / Voltage in part of a linear circuit equals to the algebraic sum of the current / voltage produced by each source separately.

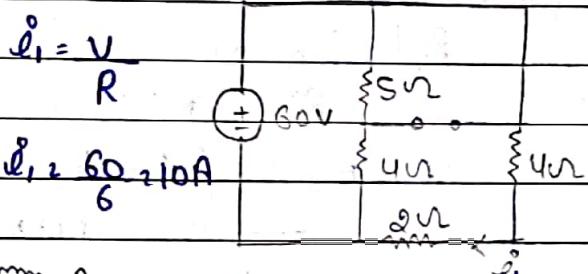
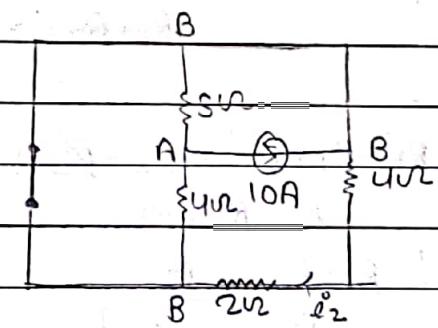
Note :- To evaluate the current / Voltage replace all other Voltage source by short circuit & current source by open circuit.



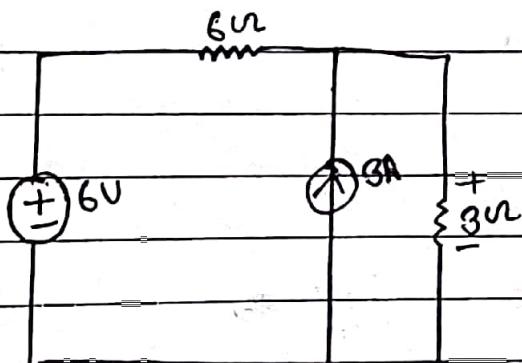
Find the current of 'i' through our register using super position theorem?

Consider 60V voltage source.

Consider 10A current source



$$i_1 = \frac{60}{6} = 10A$$
$$i_2 = i_1 + i_2$$
$$i = 10 + 10$$
$$i = 20A$$



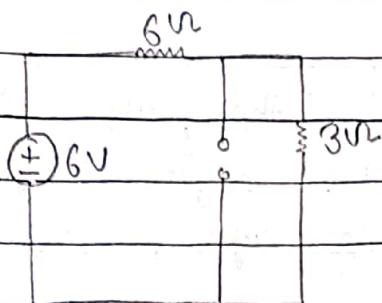
Find voltage across 3Ω register?

Spiral



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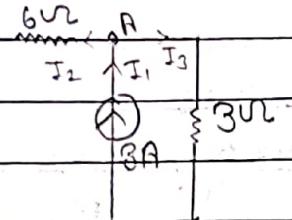
Date.....



Apply Voltage divider rule

$$V_1 = V \left( \frac{R_L}{R_1 + R_2} \right)$$

$$V_1 = 6 \left( \frac{3}{6+3} \right) = 2V$$



Consider 3A current source in the circuit.  
Apply nodal analysis.

$$I_1 = I_2 + I_3$$

$$3 = \frac{V_{out} - 0}{6} + \frac{V_{out} - 0}{3}$$

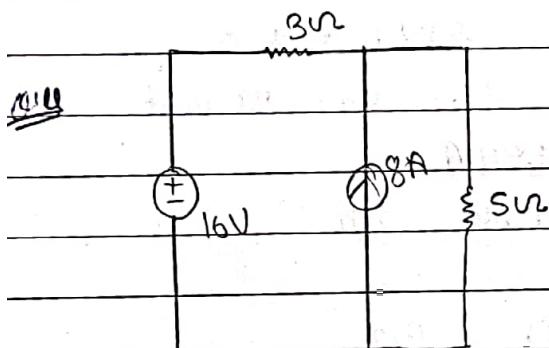
$$V_{total} = V_1 + V_2$$

$$= 2 + 6$$

$$3 \times 6 = 3 V_{out}$$

$$= 8 \text{ Volt}$$

$$V_{out} = 6 \text{ Volt}$$



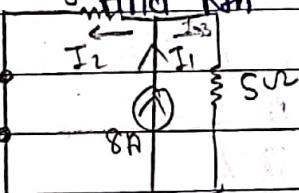
find  $V_{th}$

$$V_1 = V \left( \frac{R_1}{R_1 + R_2} \right)$$

$$V_1 = 16 \times \frac{5}{8}$$

$$V_1 = 10V$$

find  $R_{th}$



$$I_1 = I_2 + I_3$$

$$8 = \frac{V_{out}}{3} + \frac{V_{out}}{5}$$

$$V_{th} = 15 + 10$$

$$8 \times 15 = 80$$

$$= 25 \text{ Volt}$$

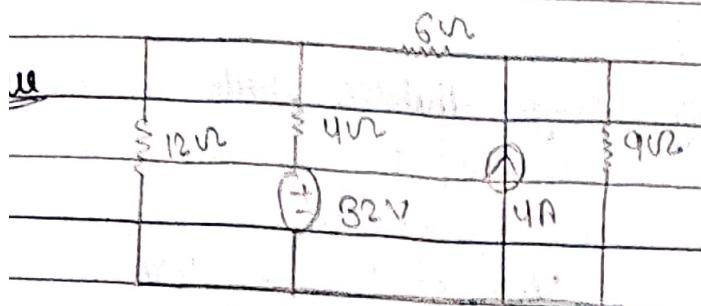
$$15 \text{ Volt}$$

Spiral



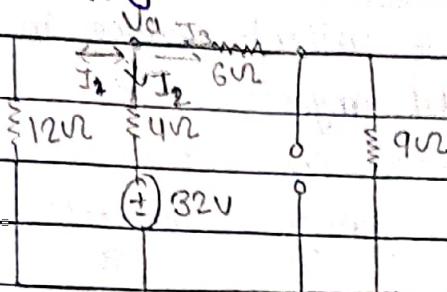
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determine the power dissipate  
in  $9\Omega$  register of circuit  
using super position theorem

Apply KCL node  $V_a$



$$I_1 = I_2 + I_3$$

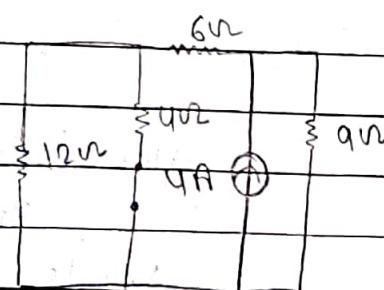
$$-\frac{V_a}{12} = \frac{V_a - 32}{4} + \frac{V_a}{15}$$

$$\frac{V_a - 32}{4} + \frac{V_a}{15} + \frac{V_a}{12} = 0$$

$$15V_a - 82(15) + 4V_a + 5V_a = 0$$

apply ohm's law

$$V_a / R = 20 \text{ volt}$$



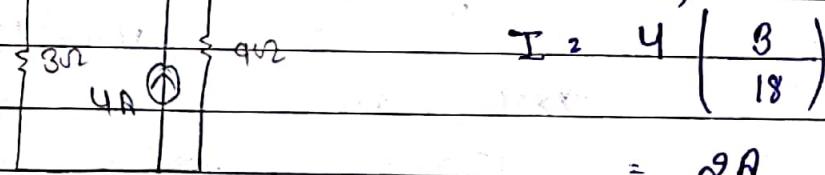
$$\frac{20}{15} = I \quad I = 1.333 \text{ A}$$

Apply current divider rule

12 || 4

$$12 \times 4 = 3.333$$

$$I = I_1 \left( \frac{R_2}{R_1 + R_2} \right) = 1.333$$



$$I = 4 \left( \frac{3}{15} \right)$$

$$= 0.833 \text{ A}$$

$$P = I^2 R$$

$$P = \frac{0.833^2}{3} \times 20 \times 9^2$$

$$I = I_1 + I_2$$

$$= 1.333 + 0.833$$

$$= 2.166 \text{ A}$$

$$= 2.166 \text{ A}$$

$$P = (2.166)^2 \times 9$$

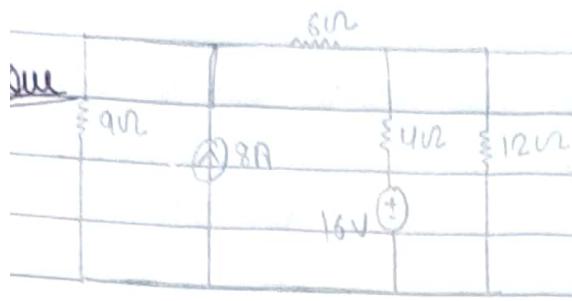
$$= 100 \text{ watt}$$

Spiral



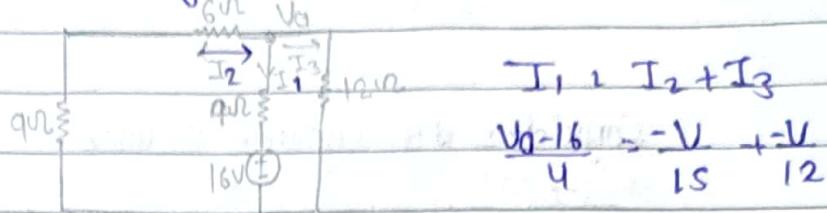
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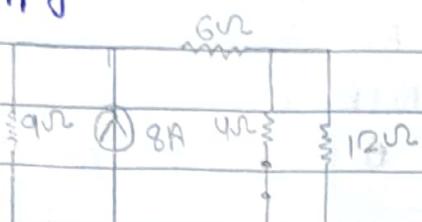


Ques Determine the power in resistance 9 Ω.

Apply nodal analysis V<sub>a</sub>



Apply current divider



$$I = I_1 \left( \frac{R_2}{R_1 + R_2} \right)$$

$$I = 8 \left( \frac{9}{18} \right)$$

$$\frac{16 - V_a}{4} + \frac{V_a}{15} + \frac{V_a}{12} = 0$$

$$\frac{16V_a - 15(16) + 4V_a + 5V_a}{60} = 0$$

$$8V_a = 240$$

$$V_a = 10V$$

$$I_1 = I_1 + I_2$$

$$V_a = IR$$

$$I_1 = \frac{10}{15} + 4$$

$$\frac{10}{15} = I_1$$

$$I_{\text{total}} = \frac{70}{15} \text{ Amp}$$

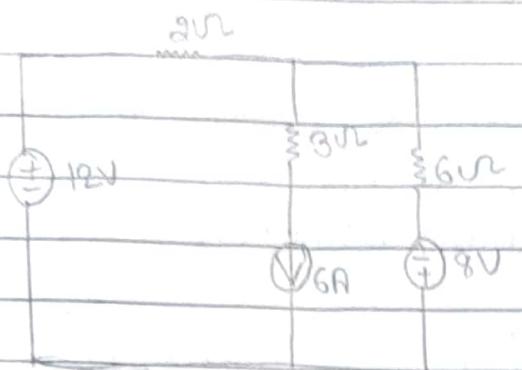
$$P_2 = I^2 R$$

$$P_2 = \frac{70}{15} \times \frac{10}{15} \times 9^2 = 196 \text{ watt}$$

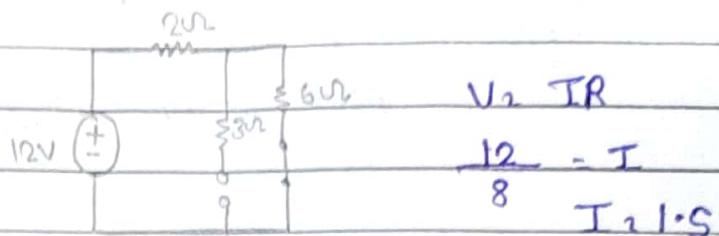
Ques Using superposition theorem find current in 2Ω register shown in figure. when the polarities of voltage source are reversed. what is the value of current across 2Ω register?

Spiral

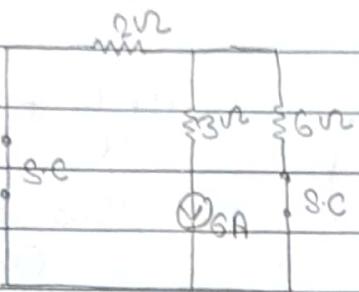
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Consider 12 V Voltage Source



Consider 6A current source

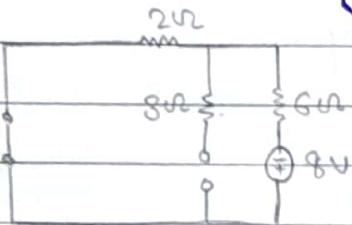


$$I = I_1 \left( \frac{R_2}{R_1 + R_2} \right)$$

$$I = 6 \left( \frac{8}{8+6} \right) = 6 \left( \frac{8}{14} \right) = 6 \left( \frac{4}{7} \right) = \frac{24}{7} \text{ Amp}$$

Consider 8V Voltage Source

$$I = \frac{9}{2} \text{ Amp}$$



$$V_2 / R$$

$$\frac{8}{8+2} = I$$

$$I = 4 \text{ Amp}$$

$$I_t = I_1 + I_2 + I_3$$

$$= 1.5 + 4.5 + 1$$

$$= 7 \text{ Amp}$$

if Voltage Source are reversed

$$1.5 + 4.5 - 1$$

$$= 5 \text{ Amp.}$$

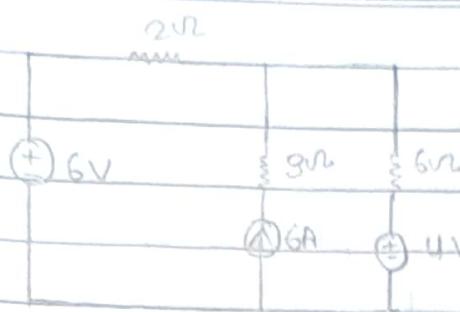
Ques Using super position to find current 2Ω register in the shown in figure. When the polarities voltage source are reverse what is the value of current across 2Ω register?

Spiral

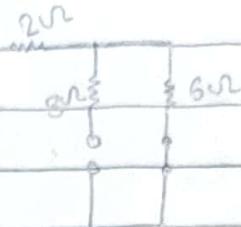


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Consider 6V voltage source.

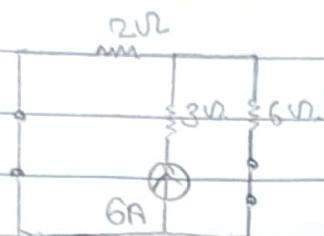


$$V = IR$$

$$\frac{6}{8} = I \cdot \frac{3}{4}$$

$$I = \frac{3}{4} \text{ A.}$$

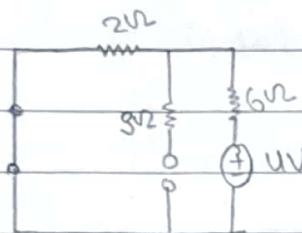
Consider 6A current source



$$I_2, I_1 \left( \frac{R_2}{R_1 + R_2} \right)$$

$$= 6 \left( \frac{6}{11} \right) = \frac{36}{11} \text{ Amp.}$$

Consider 4V voltage source.



$$V = IR$$

$$\frac{4}{8} = I$$

$$I = \frac{1}{2} \text{ Amp.}$$

$$I_{\text{Total}} = I_1 + I_2 + I_3$$

$$= \frac{3}{4} + \frac{36}{11} + \frac{1}{2}$$

$$I_t = \frac{33 + 44 + 22}{44} = \frac{199}{44} = 4.52$$

If voltage source are reverse

$$I_t = \frac{3}{4} + \frac{36}{11} - \frac{1}{2}$$

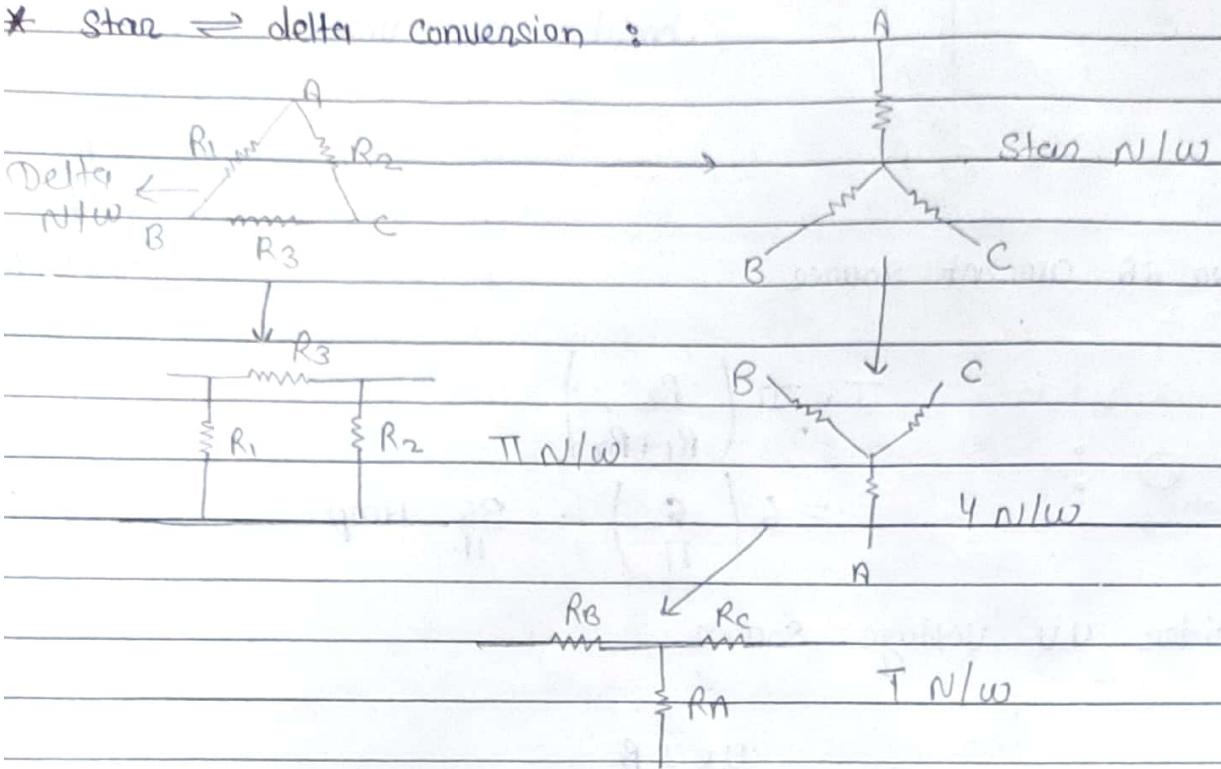
$$= \frac{33 + 44 - 22}{44}$$

$$= \frac{55}{44} \text{ Amp.}$$

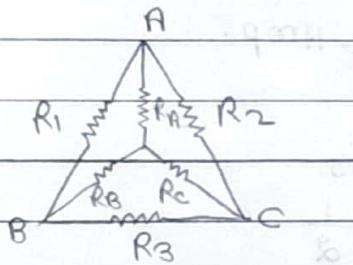
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Date.....

\* Star  $\Rightarrow$  delta conversion :



Delta  $\rightarrow$  star



$$R_A = \frac{R_1 R_2}{R_1 + R_2 + R_3}$$

$$R_B = \frac{R_1 R_3}{R_1 + R_2 + R_3}$$

$$R_C = \frac{R_2 R_3}{R_1 + R_2 + R_3}$$

$$R_A = \frac{R_1 R_2}{R_1 + R_2 + R_3}$$

Proof :

Let us assume A, B, C are connected not any n/w

$$R_{ABN} = R_1 || (R_2 + R_3)$$

$$= \frac{R_1 (R_2 + R_3)}{R_1 + R_2 + R_3}$$

$$= \frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3}$$

$$R_{ABY} = R_A + R_B = \frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3} - ①$$

Spiral



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$$R_{ACD} = R_2 \parallel (R_1 + R_3)$$
$$= \frac{R_2(R_1 + R_3)}{R_1 + R_2 + R_3}$$

$$R_{ACV} = R_A + R_C = \frac{R_1 R_2 + R_2 R_3}{R_1 + R_2 + R_3} - \textcircled{11}$$

$$R_{BCD} = R_3 \parallel (R_2 + R_1)$$
$$= \frac{R_3(R_2 + R_1)}{R_1 + R_2 + R_3}$$

$$R_{BCV} = R_B + R_C = \frac{R_3 R_2 + R_1 R_3}{R_1 + R_2 + R_3} - \textcircled{111}$$

Add equation  $\textcircled{1} + \textcircled{2} + \textcircled{3}$

$$\alpha(R_A + R_B + R_C) = \alpha \left( \frac{R_1 R_2 + R_2 R_3 + R_1 R_3}{R_1 + R_2 + R_3} \right)$$

$$R_A + R_B + R_C = \frac{R_1 R_2 + R_2 R_3 + R_1 R_3}{R_1 + R_2 + R_3}$$

Subtract  $\textcircled{3} - \textcircled{1}$

$$R_C = \frac{R_1 R_3}{R_1 + R_2 + R_3}$$

Subtract  $\textcircled{4} - \textcircled{2}$

$$R_B = \frac{R_2 R_3}{R_1 + R_2 + R_3}$$

Subtract  $\textcircled{4} - \textcircled{3}$

$$R_A = \frac{R_1 R_2}{R_1 + R_2 + R_3}$$

Spiral

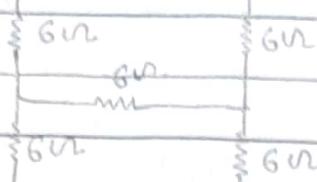


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A      6V

Que

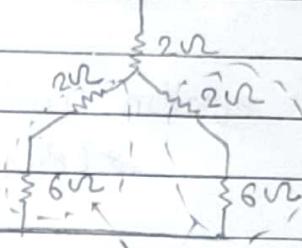
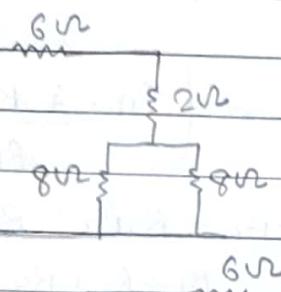
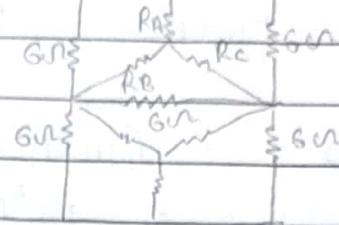


Find the Req in terminal A & B of given circuit.

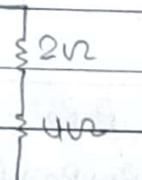
B

$$RA = RB = RC$$

$$= \frac{6 \times 6}{6+6+6} = 2\Omega$$

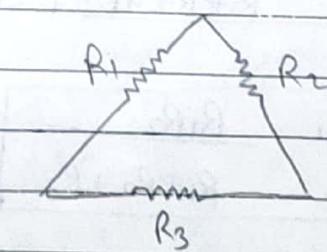
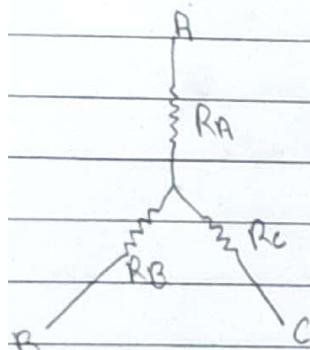


Series



$$B + 2 + 4 \\ Req = 12\Omega$$

Star to Delta conversion



$$R_1 = \frac{RA \cdot RB + RB \cdot RC + RA \cdot RC}{RC}$$

$$R_2 = \frac{RA \cdot RB + RB \cdot RC + RA \cdot RC}{RB}$$

Spiral



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$$R_3 \cdot \frac{RAR_B + RB R_C + R_C R_A}{R_A}$$

Proof :

We Know that value of  $R_A, R_B, R_C \rightarrow Y$

$$R_A = \frac{R_1 R_2}{R_1 + R_2 + R_3} - \textcircled{III}$$

$$R_B = \frac{R_1 R_3}{R_1 + R_2 + R_3} - \textcircled{II}$$

$$R_C = \frac{R_2 R_3}{R_1 + R_2 + R_3} - \textcircled{I}$$

Multiply eqn  $\textcircled{3}$  and  $\textcircled{2}$

$$RAR_B = \frac{R_1^2 R_2 R_3}{(R_1 + R_2 + R_3)^2} - \textcircled{A}$$

Multiply eqn  $\textcircled{3}$  and  $\textcircled{1}$

$$RAR_C = \frac{R_1 R_2^2 R_3}{(R_1 + R_2 + R_3)^2} - \textcircled{B}$$

Multiply eqn  $\textcircled{1}$  and  $\textcircled{2}$

$$RB R_C = \frac{R_1 R_2 R_3^2}{(R_1 + R_2 + R_3)^2} - \textcircled{C}$$

Add  $\textcircled{1} + \textcircled{2} + \textcircled{3}$

$$\begin{aligned} RAR_B + RA R_C + RB R_C &= \frac{R_1^2 R_2 R_3 + R_1 R_2^2 R_3 + R_1 R_2 R_3^2}{(R_1 + R_2 + R_3)^2} \\ &= \frac{(R_1 + R_2 + R_3) R_1 R_2 R_3}{(R_1 + R_2 + R_3)^2} \\ &= \frac{R_1 R_2 R_3}{R_1 + R_2 + R_3} - \textcircled{D} \end{aligned}$$

Put the value of  $\textcircled{D}$  into D

$$RAR_B + RA R_C + RB R_C = R_1 R_2 R_3$$

$$R_1 \cdot \frac{RAR_B + RB R_C + RA R_C}{R_1} = R_1 R_2 R_3$$

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Put the value of eqn ② into ①

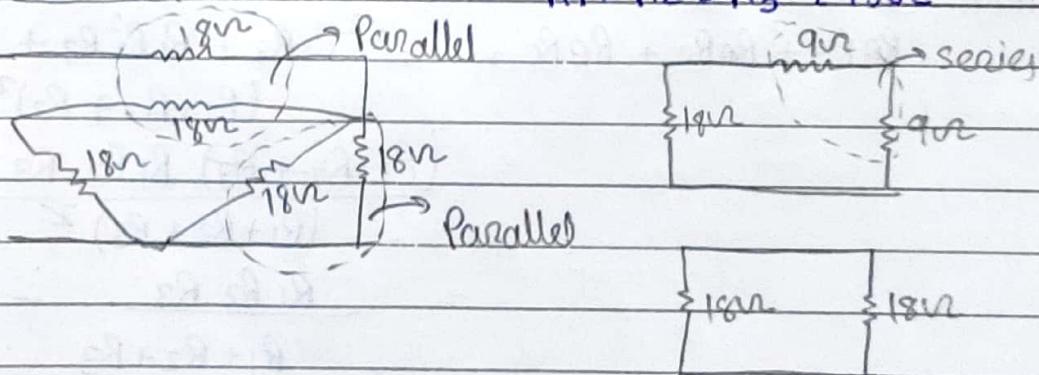
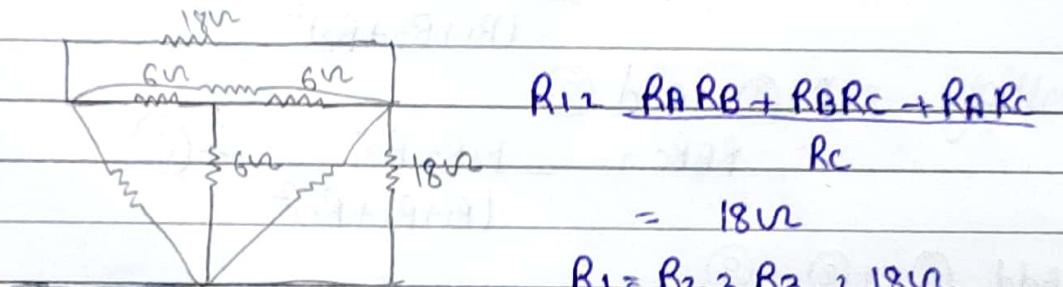
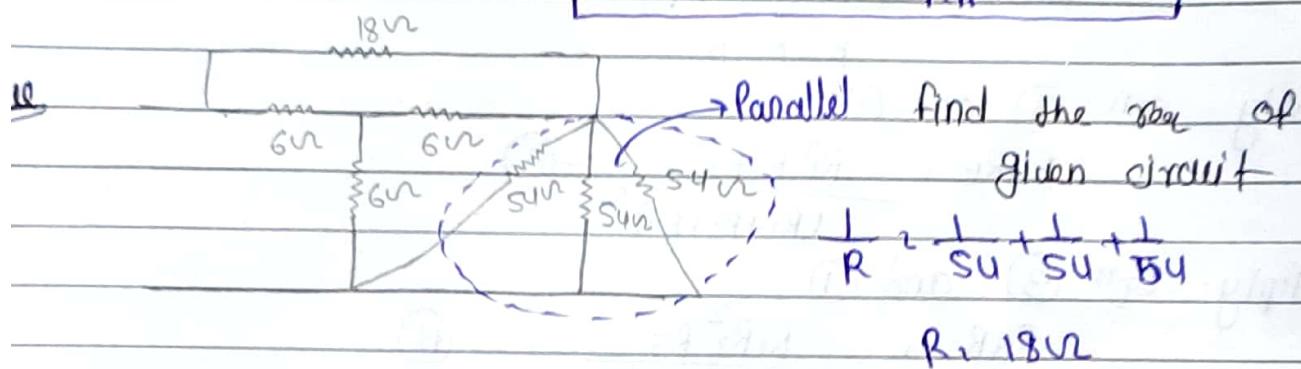
$$RAR_B + R_B R_C + R_A R_C = R_2 R_B$$

$$R_2 = \frac{RAR_B + R_B R_C + R_A R_C}{R_B}$$

Put the value of eqn ③ into ①

$$RAR_B + R_B R_C + R_A R_C = R_3 R_A$$

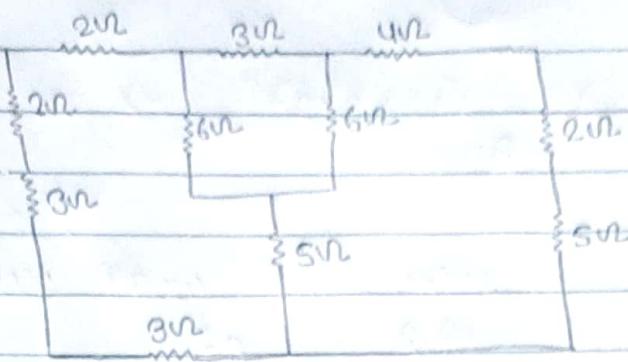
$$R_3 = \frac{RAR_B + R_B R_C + R_A R_C}{R_A}$$



$$R_{eq} = 9\Omega$$

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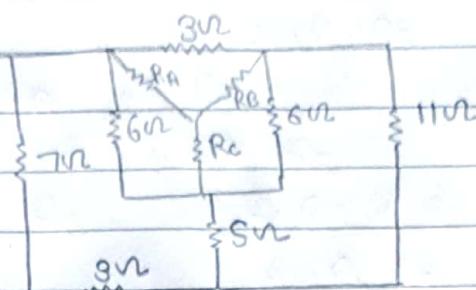
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Final Req.

$$\text{Req. } 4+2+5$$

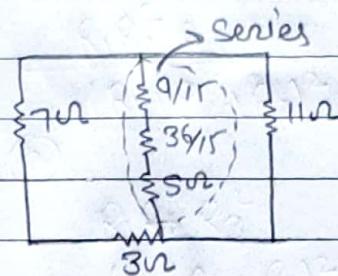
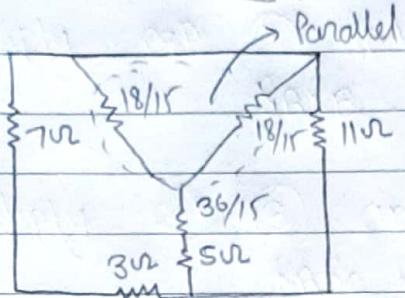
$$= 11\Omega$$



$$R_A = \frac{6 \times 3}{15} = \frac{18}{15}$$

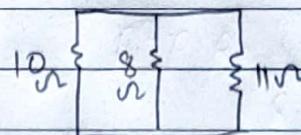
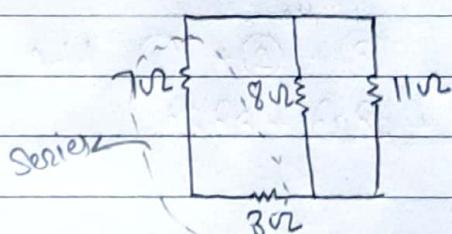
$$R_B = \frac{6 \times 6}{15} = \frac{36}{15}$$

$$R_C = \frac{6 \times 3}{15} = \frac{18}{15}$$



$$\frac{9}{15} + \frac{36}{15} + 5$$

$$9 + 36 + 75 = \frac{24}{15} = \frac{120}{15}$$



$$\text{Req. } R_1 + R_2 + R_3$$

$$\text{Req. } \frac{1}{10} + \frac{1}{8} + \frac{1}{11} = \frac{44 + 55 + 40}{440}$$

$$\text{Req. } = \frac{440}{139} = 3.16\Omega$$

Spiral