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AI25BTECH11003 - Bhavesh Gaikwad

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Question

Consider the following simultaneous equations (with c_1 and c_2 being constants)

$$3x_1 + 2x_2 = c_1$$

$$4x_1 + x_2 = c_2$$

The characteristic equation for these simultaneous equations is

(CE 2017)

a)
$$\lambda^2 - 4\lambda - 5 = 0$$

b)
$$\lambda^2 - 4\lambda + 5 = 0$$

c)
$$\lambda^2 + 4\lambda - 5 = 0$$

d)
$$\lambda^2 + 4\lambda + 5 = 0$$

Theoretical Solution

Given:

$$3x_1 + 2x_2 = c_1 \tag{1}$$

$$4x_1 + x_2 = c_2 \tag{2}$$

Let
$$\mathbf{A} = \begin{pmatrix} 3 & 2 \\ 4 & 1 \end{pmatrix}$$
, $\mathbf{x} = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$ and $\mathbf{c} = \begin{pmatrix} c_1 \\ c_2 \end{pmatrix}$
From Equation 0.1 and 0.2,

$$\mathbf{A}\mathbf{x} = \mathbf{c}$$

The characteristic equation is given by,

$$|\mathbf{A} - \lambda \mathbf{I}| = 0 \tag{4}$$

$$\begin{vmatrix} 3 - \lambda & 2 \\ 4 & 1 - \lambda \end{vmatrix} = 0$$
(5)

(6)

(3)

Theoretical Solution

$$\lambda^2 - 4\lambda - 5 = 0 \tag{7}$$

Thus, Option-A is correct.