## AI25BTECH11003 - Bhavesh Gaikwad

**Question**: The approximate eigenvalue of the matrix

$$\mathbf{A} = \begin{pmatrix} 15 & 4 & 3 \\ 10 & 12 & 6 \\ 20 & 4 & 2 \end{pmatrix}$$

obtained after two iterations of Power method, with the initial vector  $\begin{pmatrix} 1 & 1 & 1 \end{pmatrix}^T$  is (MA 2012)

(a) 7.768

(b)9.468

(c)10.548

(d)19.468

## **Solution:**

Given:

$$\mathbf{A} = \begin{pmatrix} 15 & 4 & 3 \\ 10 & 12 & 6 \\ 20 & 4 & 2 \end{pmatrix}$$

Let the initial vector be  $\mathbf{x}_0 = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$ 

$$\mathbf{x}_1 = \mathbf{A}\mathbf{x}_0 = \begin{pmatrix} 22\\28\\26 \end{pmatrix} \tag{0.1}$$

Let Normalization vector:  $\mathbf{y}_i = \frac{1}{x_{max}} \mathbf{x}_i$  where,  $x_{max}$  is the largest element in  $\mathbf{x}_i$ 

$$\mathbf{y}_1 = \frac{1}{28} \mathbf{x}_1 \tag{0.2}$$

$$\mathbf{x}_2 = \mathbf{A}\mathbf{y}_1 = \frac{1}{7} \begin{pmatrix} 260 \\ 356 \\ 302 \end{pmatrix} \tag{0.3}$$

$$\mathbf{y}_2 = \frac{1}{356} \mathbf{x}_2 = \frac{1}{1246} \begin{pmatrix} 130 \\ 178 \\ 151 \end{pmatrix} \tag{0.4}$$

Let  $\lambda$  be the Dominant eigenvalue.

By Rayleigh-Quotient,

$$\lambda = \frac{\mathbf{y}_2^{\mathsf{T}} \mathbf{A} \mathbf{y}_2}{\mathbf{y}_2^{\mathsf{T}} \mathbf{y}_2} \tag{0.5}$$

$$\lambda = 24.1453$$

Thus, all the given options are incorrect.