

AI-1110 Assignment-1

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12.13.1.11 Question: A fair die is rolled.

Consider events $E = \{1,3,5\}$, $F = \{2,3\}$ and $G = \{2,3,4,5\}$ Find

- 1) $P(E|F)$ and $P(F|E)$
- 2) $P(E|G)$ and $P(G|E)$
- 3) $P((E \cup F)|G)$ and $P((E \cap F)|G)$

Solution: Sample space when a die is rolled $= \{1,2,3,4,5,6\}$. We have $E = \{1,3,5\}$, $F = \{2,3\}$ and $G = \{2,3,4,5\}$. So, $P(E) = 3/6$, $P(F) = 2/6$ and $P(G) = 4/6$

$$\implies P(E) = 1/2$$

$$\implies P(F) = 1/3$$

$$\implies P(G) = 2/3$$

Answer:

$$P(E|F) = 1/2,$$

$$P(F|E) = 1/3,$$

$$P(E|G) = 1/2,$$

$$P(G|E) = 2/3,$$

$$P((E \cup F)|G) = 3/4,$$

$$P((E \cap F)|G) = 1/4$$

$$\begin{aligned} 1) \quad a) P(E|F) &= \frac{P(E \cap F)}{P(F)} \\ E \cap F &= \{3\} \\ \implies P(E \cap F) &= 1/6 \\ \therefore P(E|F) &= \frac{1/6}{1/3} = 1/2 \end{aligned}$$

$$\begin{aligned} b) P(F|E) &= \frac{P(E \cap F)}{P(E)} \\ \therefore P(F|E) &= \frac{1/6}{1/2} = 1/3 \end{aligned}$$

$$\begin{aligned} 2) \quad a) P(E|G) &= \frac{P(E \cap G)}{P(G)} \\ E \cap G &= \{3, 5\} \\ \implies P(E \cap G) &= 2/6 = 1/3 \\ \therefore P(E|G) &= \frac{1/3}{2/3} = 1/2 \end{aligned}$$

$$\begin{aligned} b) P(G|E) &= \frac{P(E \cap G)}{P(E)} \\ \therefore P(G|E) &= \frac{1/3}{1/2} = 2/3 \end{aligned}$$

$$\begin{aligned} 3) \quad a) P((E \cup F)|G) &= \frac{P((E \cup F) \cap G)}{P(G)} \\ (E \cup F) \cap G &= \{2, 3, 5\} \\ \implies P((E \cup F) \cap G) &= 3/6 = 1/2 \\ \therefore P((E \cup F)|G) &= \frac{1/2}{2/3} = 3/4 \end{aligned}$$

$$\begin{aligned} b) P((E \cap F)|G) &= \frac{P((E \cap F) \cap G)}{P(G)} \\ (E \cap F) \cap G &= \{3\} \\ \implies P((E \cap F) \cap G) &= 1/6 \\ \therefore P((E \cap F)|G) &= \frac{1/6}{2/3} = 1/4 \end{aligned}$$