

Order Statistics Algorithm

Problem Description

Implementing a randomized algorithm to find the k th order statistic in an unsorted array of integers. The k th order statistic represents the element that would be at the k th position if the array were sorted in ascending order.

Suggested solution: Floyd-Rivest algorithm

The Floyd-Rivest algorithm is a randomized selection algorithm used to find the k -th smallest element in an unsorted array efficiently. It is an extension of the quickselect algorithm and offers an improved worst-case time complexity (we discussed in class that improving performance is one benefit of randomized algorithms). The algorithm works by recursively partitioning the input array into subarrays based on a randomly selected pivot element. It then narrows down the search range by focusing on the relevant subarray that contains the desired element. This process continues until the k -th smallest element is found. What sets the Floyd-Rivest algorithm apart is its ability to achieve a good average-case performance while also providing a worst-case time complexity of $O(n)$, where n is the size of the input array. This is achieved by carefully selecting the pivot element and performing a series of partitioning steps. By combining randomization and efficient partitioning techniques, the Floyd-Rivest algorithm offers a reliable and fast solution for finding the k -th smallest element. It is commonly used in applications where an efficient selection of elements is required, such as order statistics, approximate median finding, and more.

Requirements

- Write a program that takes three parameters: an integer **k**, an integer **size** (length of the array), and an integer array **arr**. The program should return only one value, the k th order statistic.
- The program should handle cases where **k** is out of bounds (less than 0 or greater than **size** - 1) and return -1 appropriately.
- Use an **efficient randomized algorithm**.
- Test your implementation with different arrays and values of **k** to ensure correctness.
- Use comments to explain your code.

Instructions

- Submission format: single Python file named as your roll number. Example: M20AIE200.py
- The program should take the input from the command line arguments.
Example: `python M20AIE200.py 2 7 1 4 6 2 8 5 7`
Where **k** = 2, **size** = 7 and **arr** = {1, 4, 6, 2, 8, 5, 7}
- Note that the array **arr** may have repeated elements and the variable **k** takes values from 0 to **size** - 1. That is when **k**=0, the program would return the smallest element in the array.
- Ensure the efficiency. Using a naive method to solve the problem will not be accepted.

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- In the following program, the three variables are already assigned values from command line arguments and they are passed to the function `kthOrderStatistic`. Complete the program by only implementing the function `kthOrderStatistic`.

```
#-----
import random
import sys

def kthOrderStatistic(k, size, arr):
    return

if len(sys.argv) < 4:
    print("Usage: python roll_no.py K size arr[1] arr[2] ... arr[size]")
    sys.exit(1)

k = int(sys.argv[1])
size = int(sys.argv[2])
args = sys.argv[3:]
arr = [int(arg) for arg in args]

result = kthOrderStatistic(k, size, arr)
print(result)
#-----
```

- Examples:
\$ python M20AIE200.py 2 7 1 4 6 2 8 5 6
4
\$ python M20AIE200.py 5 7 1 4 6 2 8 5 6
6
\$ python M20AIE200.py 2 10 5 6 8 5 8 4 7 1 5 9
5
- To ensure the correctness and efficiency of your implementation, compare the time required for your implementation against the time required by a naive method (sorting the array then returning the kth element). Repeat the comparison while increasing array size (**This exercise carries no marks and does not require any submission**).
- Plagiarism of any form will result in 0 marks being awarded and result in disciplinary action being taken.