

# Day 1: Introduction to Data Science

Kenneth Benoit and Slava Mikhaylov

Introduction to Data Science and Big Data Analytics

15 August 2016

# Day 1 Outline

Data Science

Course outline and logistics

Statistical learning

## **Data Science**





# Data Scientist:

## *The Sexiest Job of the 21st Century*

Meet the people who  
can coax treasure out of  
messy, unstructured data.  
by Thomas H. Davenport  
and D.J. Patil

**W**hen Jonathan Goldstein arrived for work in June 2008 at LinkedIn, the business networking site, the place still felt like a start-up. The company had just under 8 million accounts, and the number was growing quickly as existing members invited their friends and colleagues to join. But some weren't making out connections with the people who were already on the site at the rate executives had expected. Something was apparently missing in the social experience. As one LinkedIn manager put it, "It was like arriving at a conference reception and realizing you don't know anyone. So you just stand in the corner sipping your drink—and you probably leave early."

98 Harvard Business Review October 2009



"I keep saying the sexy job in the next ten years will be statisticians. People think I'm joking, but who would've guessed that computer engineers would've been the sexy job of the 1990s?"  
Hal Varian (Chief Economist at Google, 2009).

# Statistical Learning Problems

- ▶ Identify the risk factors for prostate cancer.
- ▶ Predict whether someone will have a heart attack on the basis of demographic, diet and clinical measurements.
- ▶ Customize an email spam detection system.
- ▶ Identify the numbers in a handwritten post code.
- ▶ Classify a tissue sample into one of several cancer classes, based on a gene expression profile.
- ▶ Establish the relationship between salary and demographic variables in population survey data.
- ▶ Classify the pixels in a satellite photo of Earth's surface by agricultural usage.

# The Supervised Learning Problem

Starting point:

- ▶ Outcome measurement  $Y$  (also called dependent variable, response, target).
- ▶ Vector of  $p$  predictor measurements  $X$  (also called inputs, regressors, covariates, features, independent variables).
- ▶ In the **regression problem**,  $Y$  is quantitative (e.g price, blood pressure).
- ▶ In the **classification problem**,  $Y$  takes values in a finite, unordered set (survived/died, digit 0-9, cancer class of tissue sample).
- ▶ We have training data  $(x_1, y_1), \dots, (x_N, y_N)$ . These are observations (examples, instances) of these measurements.



# Objectives

On the basis of the training data we would like to:

- ▶ Accurately predict unseen test cases.
- ▶ Understand which inputs affect the outcome, and how.
- ▶ Assess the quality of our predictions and inferences.

# Philosophy

- ▶ It is important to understand the ideas behind the various techniques, in order to know how and when to use them.
- ▶ One has to understand the simpler methods first, in order to grasp the more sophisticated ones.
- ▶ It is important to accurately assess the performance of a method, to know how well or how badly it is working (simpler methods often perform as well as fancier ones!).
- ▶ This is an exciting research area, having important applications in science, industry and policy.
- ▶ Statistical learning is a fundamental ingredient in the training of a modern **data scientist**.

# Unsupervised learning

- ▶ No outcome variable, just a set of predictors (features) measured on a set of samples.
- ▶ objective is more fuzzy – find groups of samples that behave similarly, find features that behave similarly, find linear combinations of features with the most variation.
- ▶ difficult to know how well you are doing.
- ▶ different from supervised learning, but can be useful as a pre-processing step for supervised learning.

# The Netflix prize

- ▶ competition started in October 2006. Training data is ratings for 18,000 movies by 400,000 Netflix customers, each rating between 1 and 5.
- ▶ training data is very sparse – about 98% missing.
- ▶ objective is to predict the rating for a set of 1 million customer-movie pairs that are missing in the training data.
- ▶ Netflix's original algorithm achieved a root MSE of 0.953. The first team to achieve a 10% improvement wins one million dollars.
- ▶ is this a supervised or unsupervised problem?

# Netflix Prize

COMPLETED

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## Leaderboard

Showing Test Score. [Click here to show quiz score](#)

Display top  leaders.

Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos				
1	<a href="#">BellKor's Pragmatic Chaos</a>	0.8567	10.06	2009-07-26 18:18:28
2	<a href="#">The Ensemble</a>	0.8567	10.06	2009-07-26 18:38:22
3	<a href="#">Grand Prize Team</a>	0.8582	9.90	2009-07-10 21:24:40
4	<a href="#">Opera Solutions and Vandelay United</a>	0.8588	9.84	2009-07-10 01:12:31
5	<a href="#">Vandelay Industries !</a>	0.8591	9.81	2009-07-10 00:32:20
6	<a href="#">PragmaticTheory</a>	0.8594	9.77	2009-06-24 12:06:56
7	<a href="#">BellKor in BigChaos</a>	0.8601	9.70	2009-05-13 08:14:09
8	<a href="#">Dace</a>	0.8612	9.59	2009-07-24 17:18:43

BellKor's Pragmatic Chaos wins, beating The Ensemble by a narrow margin.

# Statistical Learning versus Machine Learning

- ▶ Machine learning arose as a subfield of Artificial Intelligence.
- ▶ Statistical learning arose as a subfield of Statistics.
- ▶ There is much overlap – both fields focus on supervised and unsupervised problems:
  - ▶ Machine learning has a greater emphasis on **large scale** applications and **prediction accuracy**.
  - ▶ Statistical learning emphasizes **models** and their interpretability, and **precision** and **uncertainty**.
- ▶ But the distinction has become more and more blurred, and there is a great deal of “cross-fertilization”.
- ▶ Machine learning has the upper hand in **Marketing!**

## **Course outline and logistics**

# Pitch of this course

- ▶ Whom this class is for
  - ▶ (typically) graduate-level applied researchers with some prior experience in quantitative methods
  - ▶ those requiring the fundamentals of data science
  - ▶ people working with typically large datasets and databases
  - ▶ those seeking a practical introduction to data analysis using R
- ▶ Prerequisites
  - ▶ at least one prior course in quantitative methods or statistics
  - ▶ familiarity, or willingness to learn, R
  - ▶ ability to use a text editor and spreadsheet is helpful
  - ▶ (optional) ability to process data files in a programming language such as Python



# Learning objectives

- ▶ an overview of data science and the challenges of working with big data
- ▶ learning the R statistical package and practical methods for manipulating and analyzing data
- ▶ formulating research questions using data analytics
- ▶ how to acquire, process, store, and use data, both structured and unstructured
- ▶ the basics of statistical inference including probability and probability distributions, modelling, experimental design

## Learning objectives (cont.)

- ▶ an overview of classification methods and methods for assessing model fit
- ▶ supervised learning approaches, including linear and logistic regression, decision trees, and naive Bayes
- ▶ unsupervised learning approaches, including clustering, association rules, and principal components analysis
- ▶ quantitative methods of text analysis, including mining social media and other online resources

# Who we are

- ▶ In the lectures:
  - ▶ Ken Benoit, London School of Economics  
kbenoit@lse.ac.uk
  - ▶ Slava Mikhaylov, University College London  
s.mikhaylov@ucl.ac.uk
- ▶ In the labs:
  - ▶ Jack Blumenau, j.blumenau@lse.ac.uk
- ▶ Course homepage: <http://github.com/kbenoit/ME414>

## Class schedule: Typical day

10:00–11:15 Lecture part 1 (NAB Thai Theatre)

11:25–12:45 Lecture part 2 (NAB Thai Theatre)

14:00–15:30 Lab Group 1 (TW2.4.02)

15:30–17:00 Lab Group 2 (TW2.4.02)

# Essential course resources

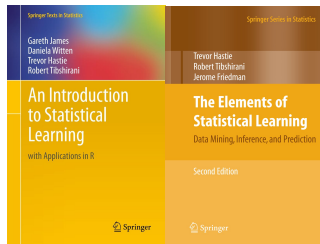
- ▶ On-line course resources

GitHub repository <http://github.com/kbenoit/ME414>

Moodle page <https://shortcourses.lse.ac.uk/course/view.php?id=158>

- ▶ Using GitHub and forking the course repo
- ▶ RStudio and GitHub integration
- ▶ How to complete (and submit) assignments
  - ▶ For a brief on-line introduction to RMarkdown, which we will use for completing the exercises for the course, see <https://goo.gl/Zq0wUe>

# Course Texts



- ▶ The course will cover most of the material in ISLR. Each chapter ends with an R lab, in which examples are developed. An electronic version of this book is available for free from the authors' websites.
- ▶ For statistical learning component of the course we closely follow ISLR, including figures and lecture materials, as made available by the authors.
- ▶ ESL is a more advanced treatment of similar topics, so may be useful for those who have previous data science training. Similarly, a free electronic version of the book is available from the authors' websites.

# Course reading materials

- ▶ The R statistical package resources on <https://cran.r-project.org/doc/manuals>
- ▶ Key readings
- ▶ Additional readings – recommended but we understand that this course will be intensive

## **Statistical learning and this course**



# Statistical learning

- ▶ **Statistical learning** refers to a vast set of tools for *understanding data*.
- ▶ For a quantitative response  $Y$  and a set of predictors  $X$ :

$$Y = f(X) + \epsilon$$

- ▶ Here,  $f$  represents the *systematic* information that  $X$  provides about  $Y$ .
- ▶ Statistical learning refers to a set of approaches for estimating  $f$ .
- ▶ Most of the course we'll spend talking about different ways to estimate  $f$  and how to evaluate whether we've done a good job with it.

## Where does this course fit in?

- ▶ Supervised versus unsupervised learning.
- ▶ Regression versus classification.
- ▶ No single *best* method. We'll spend a lot of time choosing the most appropriate tool for a given dataset using different measures of the quality of fit. E.g. MSE

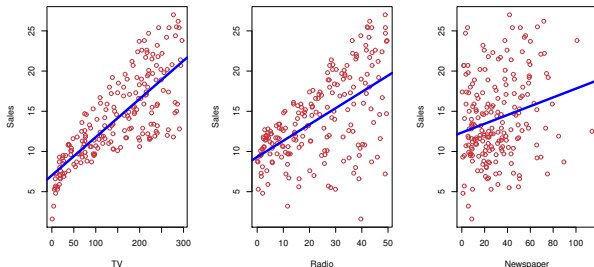
$$MSE_{training} = \frac{1}{n} \sum_{i=1}^n (y_i - \hat{f}(x_i))^2$$

$$MSE_{test} = \text{Ave}(\hat{f}(x_0) - y_0)^2$$

# Why should we bother with $f$ ?

1. **Prediction:**  $\hat{Y} = \hat{f}(X)$ , where  $\hat{f}$  is a *black box*.
2. **Inference:** How  $Y$  is changing as a function of  $X$ .
  - ▶ Depending on whether the ultimate goal is prediction, inference or a mix of both, we may deploy different methods for estimating  $f$ .
  - ▶ Also depending on the ultimate goal you may or may not care about evaluating the causal relationship between  $Y$  and  $X$ .

# What is Statistical Learning?



- ▶ Shown are Sales vs TV, Radio and Newspaper, with a blue linear-regression line fit separately to each.
- ▶ We can predict Sales using a model

$$Sales \approx f(TV, Radio, Newspaper)$$

## Notation

- ▶ Here Sales is a *response* or *target* that we wish to predict. We generically refer to the response as  $Y$ .
- ▶ TV is a *feature*, or *input*, or *predictor*, we name it  $X_1$ .
- ▶ Likewise name Radio as  $X_2$ , and so on.
- ▶ We can refer to the input vector collectively as

$$X = (X_1, X_2, X_3)$$

- ▶ Now we write our model as

$$Y = f(X) + \epsilon$$

where  $\epsilon$  captures measurement errors and other discrepancies.

## What is $f(X)$ good for?

- ▶ With a good  $f$  we can make predictions of  $Y$  at new points  $X = x$ .
- ▶ We can understand which components of  $X = (X_1, X_2, \dots, X_p)$  are important in explaining  $Y$ , and which are irrelevant. For example, Seniority and Years of Education have a big impact on Income, but Marital Status typically does not.
- ▶ Depending on the complexity of  $f$ , we may be able to understand how each component  $X_j$  of  $X$  affects  $Y$ .

- ▶ Is there an ideal  $f(X)$ ? In particular, what is a good value for  $f(X)$  at any selected value of  $X$ , say  $X = 4$ ?
- ▶ There can be many  $Y$  values at  $X = 4$ . A good value is

$$f(4) = E(Y|X = 4)$$

- ▶  $E(Y|X = 4)$  means expected value (average) of  $Y$  given  $X = 4$ .
- ▶ This ideal  $f(x) = E(Y|X = x)$  is called the regression function.

# The regression function $f(x)$

- ▶ Is also defined for vector  $X$ ; e.g.  
 $f(x) = f(x_1, x_2, x_3) = E(Y|X_1 = x_1, X_2 = x_2, X_3 = x_3)$
- ▶ Is the **ideal** or **optimal** predictor of  $Y$  with regard to mean-squared prediction error:  $f(x) = E(Y|X = x)$  is the function that minimizes  $E[(Y - g(X))^2|X = x]$  over all functions  $g$  at all points  $X = x$ .
- ▶  $\epsilon = Y - f(x)$  is the **irreducible** error – i.e. even if we knew  $f(x)$ , we would still make errors in prediction, since at each  $X = x$  there is typically a distribution of possible  $Y$  values.
- ▶ For any estimate  $\hat{f}(x)$  of  $f(x)$ , we have

$$E[(Y - \hat{f}(X))^2|X = x] = \underbrace{[f(x) - \hat{f}(x)]^2}_{\text{Reducible}} + \underbrace{\text{Var}(\epsilon)}_{\text{Irreducible}}$$



## How to estimate $f$

- ▶ Typically we have few if any data points with  $X = 4$  exactly.
- ▶ So we cannot compute  $E(Y|X = x)$ !
- ▶ Relax the definition and let

$$\hat{f}(x) = \text{Ave}(Y|X \in N(x))$$

where  $N(x)$  is some **neighborhood** of  $x$ .

- ▶ Nearest neighbor averaging can be pretty good for small  $p$  – i.e.  $p \leq 4$  and large-ish  $N$ .
- ▶ We will discuss smoother versions, such as kernel and spline smoothing later in the course.
- ▶ Nearest neighbor methods can be lousy when  $p$  is large.  
Reason: the **curse of dimensionality**. Nearest neighbors tend to be far away in high dimensions.
  - ▶ We need to get a reasonable fraction of the  $N$  values of  $y_i$  to average to bring the variance down – e.g. 10%.
  - ▶ A 10% neighborhood in high dimensions need no longer be local, so we lose the spirit of estimating  $E(Y|X = x)$  by local averaging.

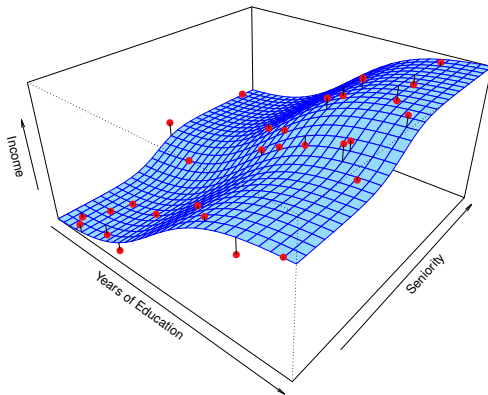
# Parametric and structured models

The **linear** model is an important example of a parametric model:

$$f_L(X) = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \cdots + \beta_p X_p.$$

- ▶ A linear model is specified in terms of  $p + 1$  parameters  $\beta_0, \beta_1, \beta_2, \dots, \beta_p$ .
- ▶ We estimate the parameters by fitting the model to training data.
- ▶ Although it is **almost never correct**, a linear model often serves as a good and interpretable approximation to the unknown true function  $f(X)$ .

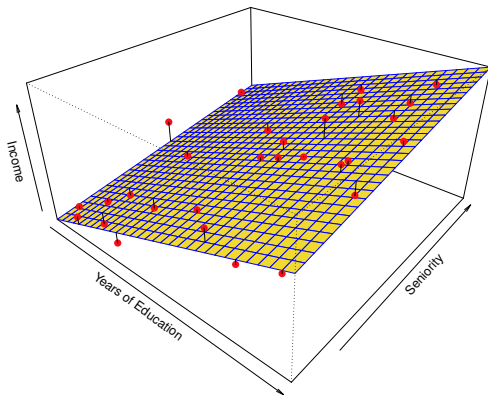
## Simulated example



Red points are simulated values for `income` from the model

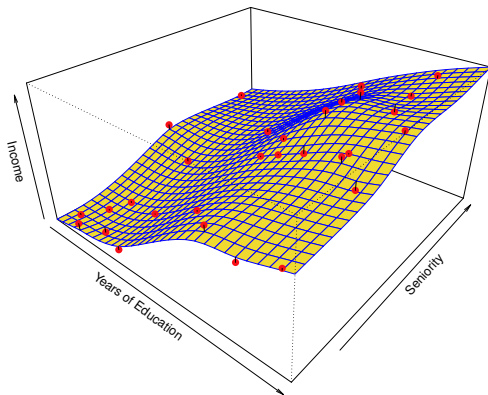
$$\text{income} = f(\text{education}, \text{seniority}) + \epsilon$$

$f$  is the blue surface.

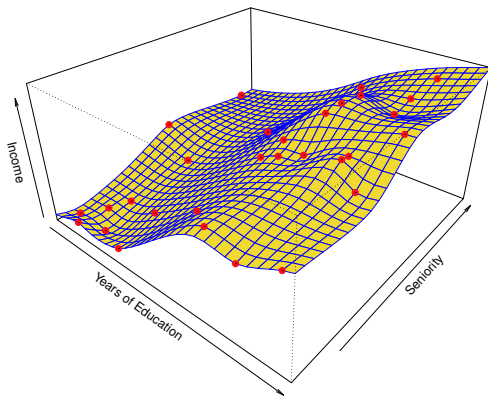


Linear regression model fit to the simulated data.

$$\hat{f}_L(\text{education}, \text{seniority}) = \hat{\beta}_0 + \hat{\beta}_1 \times \text{education} + \hat{\beta}_2 \times \text{seniority}$$



- ▶ More flexible regression model  $\hat{f}_S(\text{education}, \text{seniority})$  fit to the simulated data.
- ▶ Here we use a technique called a **thin-plate spline** to fit a flexible surface.
- ▶ We control the roughness of the fit.

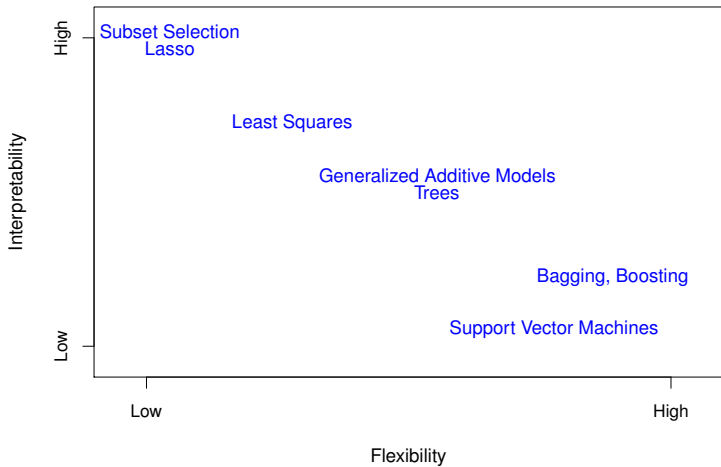


- ▶ Even more flexible spline regression model  $\hat{f}_S(\text{education}, \text{seniority})$  fit to the simulated data.
- ▶ Here the fitted model makes no errors on the training data!
- ▶ Also known as **overfitting**.

# Some trade-offs

- ▶ Prediction accuracy versus interpretability.
  - ▶ Linear models are easy to interpret; thin-plate splines are not.
- ▶ Good fit versus over-fit or under-fit.
  - ▶ How do we know when the fit is just right?
- ▶ Parsimony versus black-box.
  - ▶ We often prefer a simpler model involving fewer variables over a black-box predictor involving them all.





# Assessing Model Accuracy

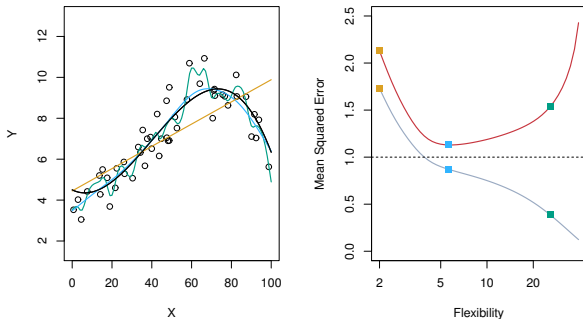
- ▶ Suppose we fit a model  $\hat{f}(x)$  to some training data  $Tr = \{x_i, y_i\}_1^N$ , and we wish to see how well it performs.
- ▶ We could compute the average squared prediction error over  $Tr$ :

$$MSE_{Tr} = Ave_{i \in Tr} [y_i - \hat{f}(x_i)]^2$$

This may be biased toward more overfit models.

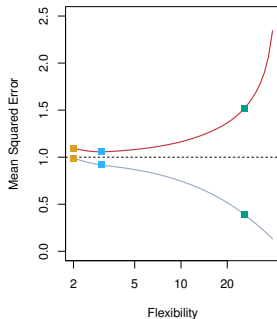
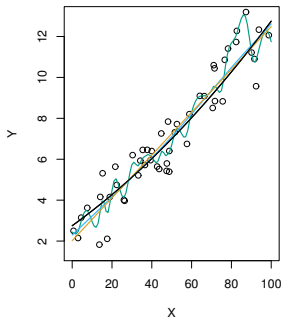
- ▶ Instead we should, if possible, compute it using fresh **test** data  $Te = \{x_i, y_i\}_1^M$ :

$$MSE_{Te} = Ave_{i \in Te} [y_i - \hat{f}(x_i)]^2$$

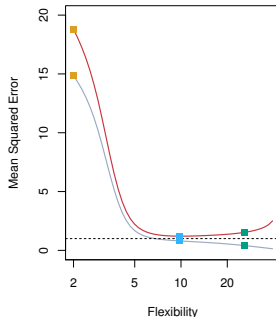
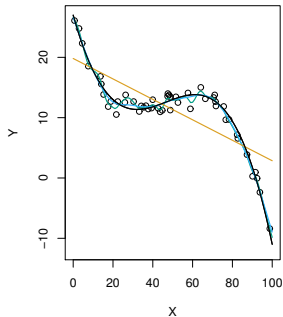


Data simulated from  $f$ , shown in black. Three estimates of  $f$  are shown: the linear regression line (orange curve), and two smoothing spline.

- ▶ Black curve is truth.
- ▶ Red curve on right is  $MSE_{Te}$ , grey curve is  $MSE_{Tr}$ .
- ▶ Orange, blue and green curves/squares correspond to fits of different flexibility.



- ▶ The setup as before, using a different true  $f$  that is much closer to linear. In this setting, linear regression provides a very good fit to the data.
- ▶ Here the truth is smoother, so the smoother fit and linear model do really well.



- ▶ Setup as above, using a different  $f$  that is far from linear.
- ▶ In this setting, linear regression provides a very poor fit to the data.
- ▶ Here the truth is wiggly and the noise is low, so the more flexible fits do the best.

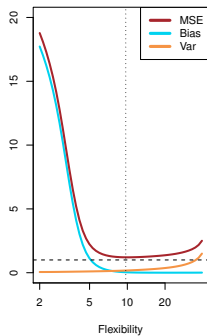
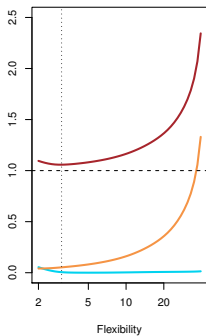
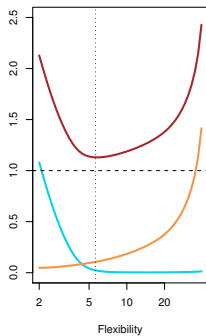
## Bias-Variance Trade-off

- ▶ Suppose we have fit a model  $f(x)$  to some training data  $Tr$ , and let  $(x_0, y_0)$  be a test observation drawn from the population.
- ▶ If the true model is  $Y = f(X) + \epsilon$  (with  $f(x) = E(Y|X = x)$ ), then

$$E(y_0 - \hat{f}(x_0)) = \text{Var}(\hat{f}(x_0)) + [\text{Bias}(\hat{f}(x_0))]^2 + \text{Var}(\epsilon).$$

- ▶ The expectation averages over the variability of  $y_0$  as well as the variability in  $Tr$ . Note that  $\text{Bias}(\hat{f}(x_0)) = E[\hat{f}(x_0)] - f(x_0)$ .
- ▶ Typically as the **flexibility** of  $\hat{f}$  increases, its variance increases, and its bias decreases.
- ▶ So choosing the flexibility based on average test error amounts to a **bias-variance trade-off**.

# Bias-variance trade-off for the three examples



# Classification Problems

Here the response variable  $Y$  is **qualitative** – e.g. email is one of  $\mathcal{C} = (\textit{spam}, \textit{ham})$  ( $\textit{ham} = \textit{goodemail}$ ), digitclass is one of  $\mathcal{C} = \{0, 1, \dots, 9\}$ . Our goals are to:

- ▶ Build a classifier  $\mathcal{C}(X)$  that assigns a class label from  $\mathcal{C}$  to a future unlabeled observation  $X$ .
- ▶ Assess the uncertainty in each classification
- ▶ Understand the roles of the different predictors among  $X = (X_1, X_2, \dots, X_p)$ .



- ▶ Is there an ideal  $\mathcal{C}(X)$ ? Suppose the  $K$  elements in  $\mathcal{C}$  are numbered  $1, 2, \dots, K$ . Let

$$p_k(x) = \Pr(Y = k|X = x), k = 1, 2, \dots, K.$$

- ▶ These are the **conditional class probabilities** at  $x$ . Then the **Bayes optimal** classifier at  $x$  is

$$\mathcal{C}(x) = j \text{ if } p_j(x) = \max\{p_1(x), p_2(x), \dots, p_K(x)\}$$

- ▶ Nearest-neighbor averaging can be used as before.
- ▶ Also breaks down as dimension grows.
- ▶ However, the impact on  $\hat{\mathcal{C}}(x)$  is less than on  $\hat{p}_k(x)$ ,  $k = 1, \dots, K$ .

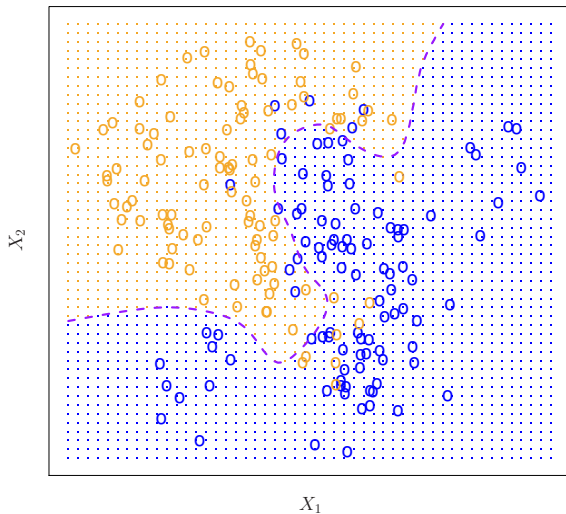
## Classification: some details

- ▶ Typically we measure the performance of  $\hat{\mathcal{C}}(x)$  using the misclassification error rate:

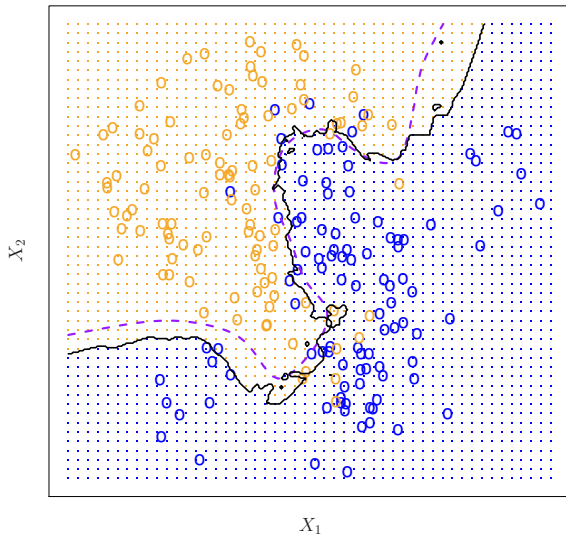
$$Err_{Te} = Ave_{i \in Te} \mathcal{I}[y_i \neq \hat{\mathcal{C}}(x_i)]$$

- ▶ The Bayes classifier (using the true  $p_k(x)$ ) has smallest error (in the population).
- ▶ Support-vector machines build structured models for  $\mathcal{C}(x)$ .
- ▶ We will also build structured models for representing the  $p_k(x)$ . For example, logistic regression, generalized additive models.

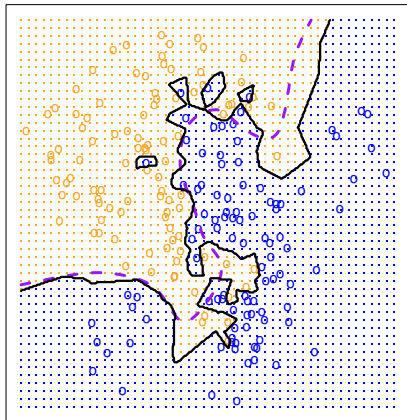
## Example: K-nearest neighbors in two dimensions



KNN: K=10



KNN:  $K=1$



KNN:  $K=100$

