

2-0x

1 October 2023

Arrays - (medium) :-

1. \rightarrow { Two sum }

arr[] = { 2, 6, 5, 8, 11 } target = 14

{ 8 + 6 }

Brute :-

```
for (int i = 0; i < n; i++) {
```

```
    for (int j = 0; j < n; j++) {
```

```
        if (i != j) {
```

```
            if (target == arr[i] + arr[j]) {
```

```
                cout << "Yes"
```

```
                break;
```

```
            }
```

```
        }
```

```
    }
```

T.C $\rightarrow O(n^2)$

S.C $\rightarrow O(1)$

Better :- Hashing --- D

T.C $O(n)$

map<int, int> mapp;

S.C $O(n)$

for (int i = 0; i < size(n); i++)

int find = target - arr[i];

if (mapp[find])

cout << "Yes" << endl;

}

else {

mapp[arr[i]]++;

}

return NO;

}

Approach 2

target = 14

T.C $O(N) +$

$O(N \log N)$

Sort \rightarrow 2, 6, 5, 8, 11

↑

↓

$i + j = 13 < 14$ then increase small one

$(i+1) + j = 6 + 11 = 17 > 14$ then decrease big one

$6 + 8 = 14$ --- found

if (i < j) cout << "no".

2 \rightarrow { sort 0's, 1's and 2's }

Brute

sort (Merge sort)

T.C $\rightarrow N \log N$

S.C $\rightarrow N$

Bucket

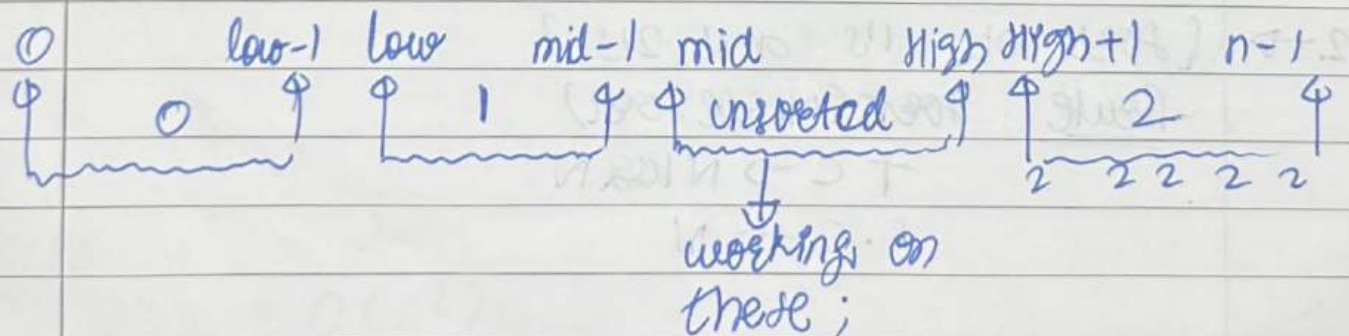
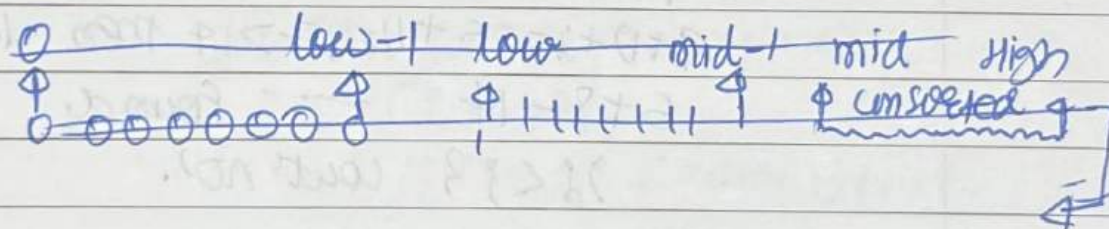
count 0's, 1's and 2's TC $O(N)$ -- TC $O(2N)$
 for (0-0's) 0 } SC $O(1)$.
 (0's-1's) 1 } N
 (1's-2's) 2 } for counting N & $2N$
 for distributing N

Optional

Dutch National flag Algorithm :- T.C $\rightarrow O(N)$
 S.C $\rightarrow O(1)$.

low
 mid
 high } Pointers

$[0 \dots \text{low}-1] \rightarrow 0$ extreme left
 $[\text{low} \dots \text{mid}-1] \rightarrow 1$
 $[\text{high}+1, n-1] \rightarrow 2$ extreme right



//_

low

arr

0	1	1	0	1	2	1	2	0	0	0
---	---	---	---	---	---	---	---	---	---	---

mid high

$a[mid] = 0$ swap(arr[low], arr[mid]);
low++; mid++;

$a[mid] = 1$ mid++;

$a[mid] = 2$ swap(arr[mid], arr[high]);
~~mid++~~ high--;

1) swap(arr[low], arr[mid]) low++, mid++;

0, 1, 1, 0, 1, 2, 1, 2, 0, 0, 0

↑ ↑
low mid

2) $a[mid] = 1$ mid++;

0, 1, 1, 0, 1, 2, 1, 2, 0, 0, 0

↑ ↑
low mid

3) $a[mid] = 1$ mid++

0, 1, 1, 0, 1, 2, 1, 2, 0, 0, 0

↑ ↑
low mid

6) $a[mid] = 0$ swap(arr[low], arr[mid],
low++, mid++.

0, 0, 1, 1, 1, 2, 1, 2, 0, 0, 0

0, 0, 1, 1, 1, 2, 1, 2, 0, 0, 0

↑ ↑ ↑
low mid mid

7) $a[mid] = 1$ mid++

8) $arr[mid] = 2$

$swap(arr[mid], arr[high]);$

$high--$

0, 0, 1, 1, 1, 0, 1, 2, 0, 0, 2

low mid high

9) $arr[mid] = 0$ $mid++$ $swap(low, mid)$

0, 0, 0, 1, 1, 1, 1, 2, 0, 0, 2

low mid high

10) $mid++$ { because 1 }

11) $mid++$

0, 0, 0, 1, 1, 1, 1, 2, 0, 0, 2

low mid high

12) $swap(mid, high)$ $arr[mid] = 2$

0, 0, 0, 1, 1, 1, 1, 0, 2, 2

low mid high

13) $arr[mid] = 0$

0, 0, 0, 0, 1, 1, 1, 1, 0, 2, 2

low mid

$arr[mid] = 0$ mid, high

swap with low

14)

{ 0, 0, 0, 0, 0, 1, 1, 1, 1, 2, 2 }

Sorted

3. \rightarrow Majority element ($> \frac{N}{2}$ times)

arr[] = { 2, 2, 3, 3, 1, 2, 2 }

ans = 4

Brute

for (i \rightarrow n)

for (j = i+1 to n)

$O(n^2)$

Better

{ use map }

unordered map

$N \log N$

T.C $O(N) + N \log N$

Optimal

Moore's Voting Algorithm :-

If the element is greater than $> \frac{N}{2}$ times its count in different sub-array can't be zero.

{ 7, 7, 5, 7, 5, 1, 5, 7, 5, 5, 7, 7, 5, 5, 5, 5 }

ele = 7

ele = 5

cnt = 2 2 0 1 0

2 0 1 2 3 4

{ 7 7 5 7 5 1 } { 5 7 }

5 5 7 7 5 5 5 5

{ cnt = 4 is not cancelled }

check that element occurs $> \frac{N}{2}$ time in array again.

{ Moore Voting Algo }

```
int majorityElement (vector<int> &v)
```

```
    int cnt = 0;
```

```
    int el;
```

```
    for (int i = 0; i < n; i++) {
```

```
        if (cnt == 0) {
```

```
            el = v[i]; cnt = 1;
```

```
        }
```

```
        if (v[i] == el) {
```

```
            cnt++;
```

```
        }
```

```
    } else {
```

```
        cnt--;
```

```
    }
```

```
}
```

```
// again iterate
```

```
for (int i = 0; i < n; i++)
```

```
    if (el == v[i]) count++;
```

```
}
```

```
if (count > (v.size() / 2))
```

```
    return el;
```

```
}
```

```
return -1;
```

```
}
```

T.C $\rightarrow O(N) + O(N)$

S.C $\rightarrow O(1)$

21 sept 2023

LOVE BABBAR DIA SHEET / A23

Largest subarray Sum Problem

Kadane algorithm

{ -2, -3, 4, -1, -2, 1, 5, 3 }

~~max-so-far = INT_MIN;~~

~~max ending here = 0;~~

~~i=0, a[0] = -2~~

~~max ending here += (-2);~~

~~max ending here = 0 -- because~~

~~max-end-here < 0~~

~~set max-so-far = -2~~

~~i=1, a[1] = -3~~

~~max ending here += (-3)~~

~~-4 = 0 < 0~~

~~max~~

int maxSubarraySum(int arr[], int n)

int mini = INT_MIN;

for(int i=0; i<n; i++){

for(int j=i; j<n; j++){

int sum = 0;

$N^2 \rightarrow$ sum takes

for(int k=i; k<=j; k++){

sum += arr[k];

}

mini = max(mini, sum);

}

return mini;

}

$\{ > O(N^2) \}$

arr[] = {-2, -3, 4, -1, -2, 1, 5, -3}

maxi = ~~INT_MIN~~ -2, 4, 7

sum = 0 -3, 4

-2, 0, 3

0

4
2

7, 4

sum < 0

long long maxSub (int arr[], int n)

long long sum = 0, maxi = LONG_MIN;

for (int i = 0; i < n; i++)

sum += arr[i]; if (sum == 0)

start = i;

if (sum > maxi)

maxi = sum; --o (and start

= start;

and end = i)

if (sum < 0)

sum = 0;

return maxi;

4. \rightarrow Rearrange array element by sign

arr1[] = {3, 1, -2, -5, 2, -4}

arr2[] = {3, -2, 1, -5, 2, -4}

Brute:-

marking two array positive, negative

T.C $O(N) + O(N)$

S.C $O(N)$

Optimal:

T.C $\rightarrow O(N)$

S.C $\rightarrow O(1)$

{3, 1, -2, -5, 2, -4}

↓ ↓ ↓ ↓ ↓
3 -2 1 -5 2 -4
0 1 2 3 4 5

function (vector<int> &v) {

vector<int> ans;

int i = 0, j = 1;

if (v[i] < 0) {

ans[j] = v[i];

j += 2;

}

else {

ans[i] = v[j];

i += 2;

}

}

return ans;



5. Next Permutation

arr[] = [3, 1, 2]

1, 2, 3

ans \rightarrow [3, 2, 1]

1, 3, 2

2, 1, 3

3, 1, 2

3, 2, 1

Brute : generate all permutations

then linear search

between then index for index next to that

TC $N! N >>>$

Better : next-permutation (arr, begin, arr.end());

inside the \downarrow

Optional :

1. longer prefix match ($a[i] < a[i+1]$)

arr = [2, 1, 5, 4, 3, 0, 0]

2. first greater than $arr[i]$ but

2 1 < 3

smallest one

2, 3 {5, 4, 1, 0, 0}

3. sort

sort

dip

{1, 2, 3, 4, 5}

{2, 3, 0, 0, 4, 5}

{5, 4, 3, 2, 1}

last permutation

$$\begin{array}{ccc} & p & n-1 \\ 0 & 0 & 0 \\ n-2 & & \end{array} \quad \{p < n-1\}$$

index = -1;

for (p = n-2; p >= 0; i--)

if (arr[p] < arr[p+1])

index = p;

break;

}

if (index == -1)

reverse(arr);

else

{ 2, 1, 5, 4, 3, 0, 0 }

// first element greater element at index
// but mark it one

p > index

for (p = n-1; p >= 0; i--)

if (arr[p] > arr[index])

swap(arr[p], arr[index]);

break;

}

// 2, 3, 5, 4, 1, 0, 0

arr[end-1]

reverse(arr, begin + index + 1, n-1);

TC - O(N^2)

SC - O(1)

6. \rightarrow

Headline in the array

{ 10, 22, 12, 3, 0, 6 }

{ 22, 12, 6 }

everything in the eight
must be smaller

brute

for (i = 0 \rightarrow n)

for (j = i + 1 \rightarrow n)

T.C $\rightarrow O(N^2)$

S.C $\rightarrow O(1)$

--- storing $O(N)$

Optimal

Start from backward and maintain maxi.

Store in array

sort ---

T.C \rightarrow ~~$O(N^2)$~~ $O(N \log N)$

S.C $\rightarrow O(N)$

03 octomber 2023

Longest consecutive sequence in an array :-

Brute :-

```
for (int i = 0; i < n; i++) {
    int start = arr[i];
    int cnt = 1;
    while (bool (start + 1, arr)) {
        start++;
        cnt++;
    }
    ans = max (cnt, ans);
}
return ans;
```

```
bool bools ? {
    for (int i = 0; i < n; i++) {
        if (start == arr[i])
            return true;
    }
    return false;
}
```

$O(N^2)$ TC
 $O(1)$ SC

{ 1, 1, 1, 2, 2, 2, 3, 3, 4, 100, 100, 101, 101 }

Better :-

bools ?

TC $\rightarrow N \log N$
SC $\rightarrow O(1)$

```
for (int i = 0; i < n; i++) {
    if (arr[i] - 1 == last smaller) {
        cnt++;
        last smaller = arr[i];
    }
    else if (arr[i] != last smaller) {
        cnt = 1;
        last smaller = arr[i];
    }
    longest = max (cnt, longest);
}
return longest;
```


Optional :-

```
longest (vector<int> a) {
```

```
    if (!a.size()) return 0;
```

```
    int longest = 1;
```

```
    unordered_set<int> st;
```

```
    for (int i = 0; i < n; i++)
```

```
        st.insert(a[i]);
```

```
}
```

```
pre (auto it, st) {
```

```
    if (st.find(it-1) != st.end()) {
```

```
        int cnt = 1;
```

```
        int x = it;
```

```
        while (st.find(x-1) != st.end()) {
```

```
            cnt = 1;
```

```
            cnt++;
```

```
            x++;
```

```
        }
```

```
        longest = max(longest, cnt);
```

```
    }
```

```
    return longest;
```

TC $\rightarrow O(3N)$

SC $\rightarrow O(N)$

Set matrix Zero

Brute:-

```
for (int i = 0 to n) {  
    for (int j = 0 to m) {  
        if (arr[i][j] == 0) {  
            markRow(i);  
            markCol(j);  
        }  
    }  
}
```

```
markRow(i) {  
    if (arr[i]  
    for (int j = 0 to m) {  
        if (arr[i][j] != 0) {  
            arr[i][j] = -1;  
        }  
    }  
}
```

```
markCol(j) {  
    for (i = 0 to n) {  
        if (arr[i][j] != 0) {  
            arr[i][j] = -1;  
        }  
    }  
}
```

Put all zero where -1 exists } $n \times m$

T.C $\rightarrow (n \times m) \times (n + m)$
 $+ (n \times m)$

$\approx n^3$

S.C $\approx O(1)$

Better

maintain two set

```
for (-D) {
```

```
{st1, st2}
```

```
for (-D) {
```

```
if (matrix[i][j] == 0) {
```

```
Row.push =
```

```
st1.insert(i);
```

```
st2.insert(i);
```

```
}
```

```
}
```

```
for (-D) {
```

```
for (-D) {
```

```
if (st1.find(i) != st1.end()) {
```

```
matrix[i][j] = 0;
```

```
}
```

```
if (st2.find(j) != st2.end()) {
```

```
matrix[i][j] = 0;
```

```
}
```

```
}
```

TC $\rightarrow O(2n \times m)$

SC $\rightarrow O(n) + O(m)$.

Optional

```
int col0 = 1;
for (int i = 0; i < n; i++) {
    for (int j = 0; j < m; j++) {
        if (matrix[i][j] == 0) {
            // mark pth row
            matrix[i][0] = 0;
            if (j != 0) {
                matrix[0][j] = 0;
            }
        }
    }
}
```

col0 = 0;

TC $\rightarrow O(n \times m)$

SC $\rightarrow O(1)$.

```
for (int i = 1; i < n; i++) {
    for (int j = 1; j < m; j++) {
        if (matrix[i][j] != 0) {
            // check col & row
            if (matrix[0][j] == 0 || matrix[i][0] == 0) {
                matrix[i][j] = 0;
            }
        }
    }
}

if (matrix[0][0] == 0) {
    // set j = 0 to m matrix[0][j] = 0;
    if (col0 != 0) {
        for (int i = 0; i < n; i++) {
            matrix[i][0] = 0;
        }
    }
}
```


Rotate Matrix :-

Brute?

TC
DO(N²)
SC
DO(N²)

	0	1	2	3
0	1	2	3	4
1	5	6	7	8
2	9	10	11	12
3	13	14	15	16

	0	1	2	3
0	13	9	5	1
1	14	10	6	2
2	15	11	7	3
3	16	12	8	4

$[0,0] \rightarrow [0,3]$ $[0,1] \rightarrow [0,2]$
 $[0,1] \rightarrow [1,3]$ $[1,1] \rightarrow [1,2]$
 $[0,2] \rightarrow [2,3]$ $[1,2] \rightarrow [2,2]$
 $[0,3] \rightarrow [3,3]$ $[1,3] \rightarrow [3,2]$
 (i,j) (i,do)

$(i) = (n-1) - i$
 $do =$

$ans[do] = arr[i][j]$
 $arr[i][j] = ans[do]$

Brute / Optional :-

	0	1	2	3	Team score
0	1	2	3	4	→ 1 5 9 13
1	5	6	7	8	2 6 10 14
2	9	10	11	12	3 7 11 15
3	13	14	15	16	4 8 12 16

reverse each row

13	9	5	1
14	10	6	2
15	11	7	3
16	12	8	4

func()

for (int i=0 to n)

for (j=i+1 to m)

swap(mat[i][j], mat[j][i]);

}

}

for (int i=0 to n)

int start=0, end=mat[i].size()-1;

while (start < end)

swap(mat[i][start], mat[i][end]);

start++;

end--;

}

}

}

04 October 23

Spread Matrix

0 1 2 3 4 5

0 1 2 3 4 5 6 (0,5)

1 6 7 8 9 10 11 12 (1,5)

2 4 9 14 15 16 17 18

6/2 = 3

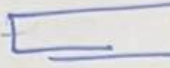
3 3 10 19 20 21 22 23 24

4 2 5 26 27 28 29 30

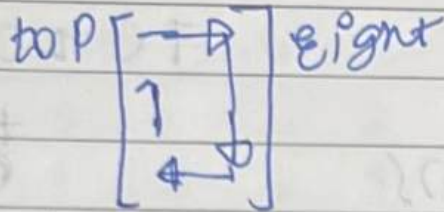
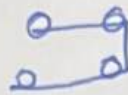
5 31 32 33 34 35 36 (5,5)

(5A)

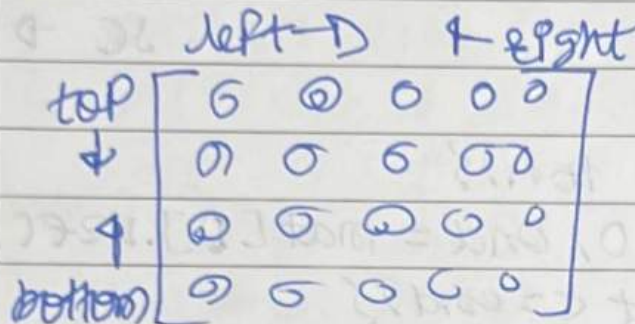
1	2	3	4	5
1	1	1	1	1
x	x	x	x	x
x	x	x	x	x

edge 

left



bottom



```
if (left <= right) {
    for (int i = bottom to top)
        ans.push_back
            (mat[i][
                ]
            )
}
```

bottom = mat.size() - 1

func() {

left = top = 0 right = mat[0].size() - 1

vector<int> ans;

while (left <= right and top <= bottom) {

for (int i = left; i <= right; i++) {

ans.push_back(mat[top][i]);

}

top++;

for (int i = top; i <= bottom; i++) {

ans.push_back(mat[i][right]);

}

right--;

{ edge case } if (top <= bottom) {

for (int i = right; i >= ~~left~~ left; i--) {

ans.push_back(mat[i][left]);

}

left++;

}



Number of sub-arrays with sum K

Brute:-

```
for (int i = 0 to n) {  
    for (int j = i to n) {  
        for (int k = i, k <= j; k++) {  
            sum += arr[k];  
        }  
        if (sum == k) {  
            ans++;  
        }  
    }  
}
```

TC = $O(N^3)$

```
for (int i = 0 to n) {  
    for (int sum = 0  
    for (int j = i to n) {  
        sum += arr[j];  
        if (sum == k) {  
            ans++;  
        }  
    }  
}
```

TC = $O(N^2)$

TC : $O(N \times 10^9 N)$
 SC : $O(N)$

Optimal approach with prefix sum :-

arr[] = { 1, 2, 3, -3, 1, 1, 1, 4, 2, -3 } {K=3}

prefsum = 0 1 3 0 3 4 5 8 10 12
 present 1 2 3 4 5 6 7 8 9

cnt = 0 0 1 2 3 4 6 8

arr[] = { 3, -3, 1, 1, 1 }

(9, 1)
(12, 1)
(10, 1)
(5, 1)
(4, 1)
(6, 2)
(3, 2)
(1, 1)
(0, 1)

without
 putting
 zero in
 prefix
 sum

PS = 3 0 1 2 3 0

cnt = 0 0 1

(2, 1)
(1, 1)
(0, 1)
(3, 1)

prefsum = 0 3 0 1 2 3

cnt = 0 1 2 2 2 4

{ 3 }, { 3, -3, 1, 1, 1 }
 { 1, 1, 1 } { -3, 1, 1, 1, 3 }

(2, 1)
(1, 1)
(3, 2)
(0, 2)

{ 1, -1, 0 } K=0

(0, 1)
(0, 1)

0, 1, 0 0
 1 2

prefsum = 0 1 0 0
 0 1 2 3