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NCERT 11.9.2.3

EE23BTECH11043 - BHUVANESH SUNIL NEHETE*

QUESTION

In an A.P. the first term is 2 and the sum of the first five terms is one-fourth of the next five terms. Show that 20^{th} term is -112.

SOLUTION

Parameter	Value/Formula	description
x(0)	2	First term
x(19)	-112	20th term
x(n)	(x(0) + nd)u(n)	$(n+1)^{\text{th}}$ term of AP
d	-6	common difference

TABLE 0 Input data

General term can be written as

$$x(n) = (x(0) + nd) u(n)$$
 (1)

The corresponding Z-transform can be written as

$$X(z) = \frac{x(0)}{1 - z^{-1}} + \frac{dz^{-1}}{(1 - z^{-1})^2}$$
 (2)

Given,

$$\sum_{n=0}^{4} x(n) = \frac{1}{4} \sum_{n=5}^{9} x(n)$$
 (3)

Simplifying:

$$5x(0) + 10d = \frac{1}{4}(5x(0) + 35d) \tag{4}$$

$$\implies x(0) = \frac{-d}{3} \tag{5}$$

$$\implies d = -6$$
 (6)

From (6) and Table 0

$$x(19) = x(0) + 19d \tag{7}$$

$$= 2 + 19(-6) \tag{8}$$

$$= -112 \tag{9}$$

From (6) and Table 0:

$$\implies x(n) = (2 - 6n)u(n) \tag{10}$$

From (2) and (10):

$$X(z) = \frac{2}{1 - z^{-1}} - \frac{6z^{-1}}{(1 - z^{-1})^2} \quad |z| > 1$$
 (11)

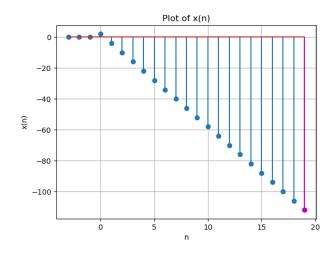


Fig. 1. graph of x(n) = 2 - 6n