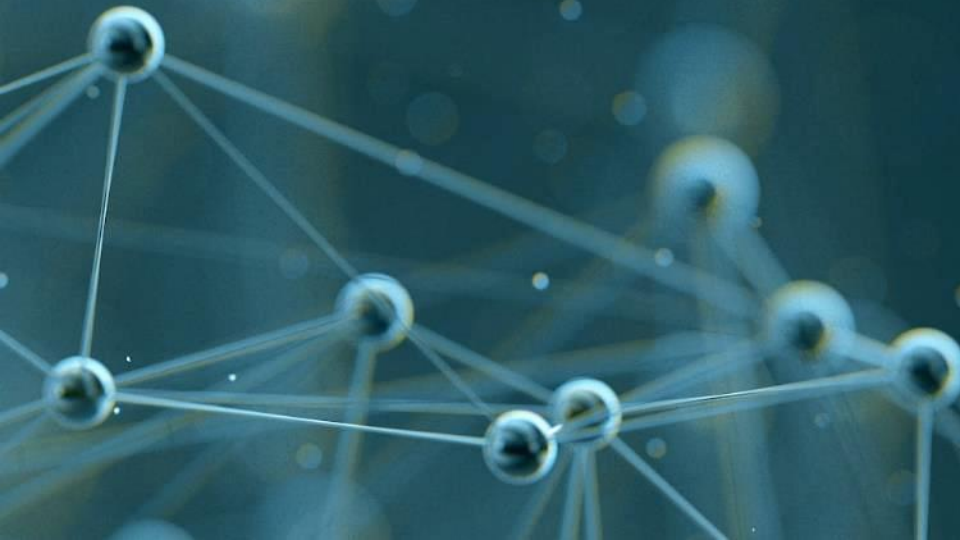
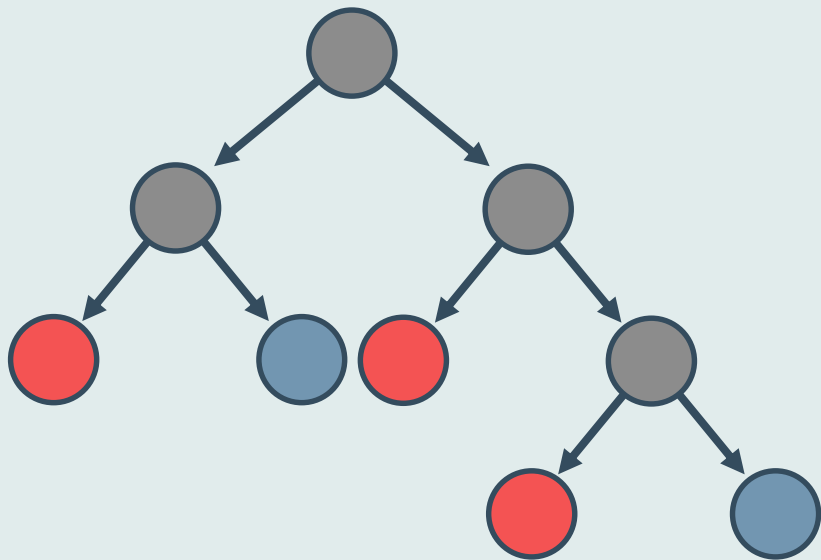


BAGGING

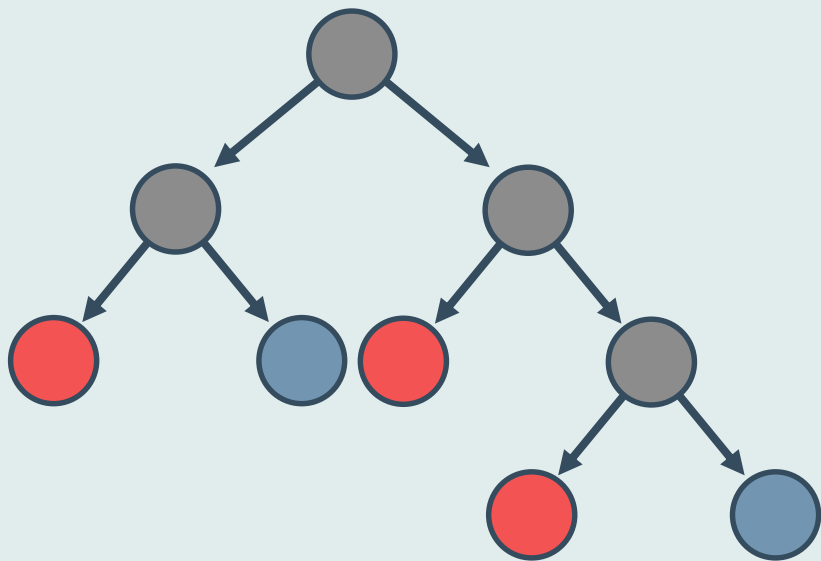


DECISION TREES ARE HIGH VARIANCE



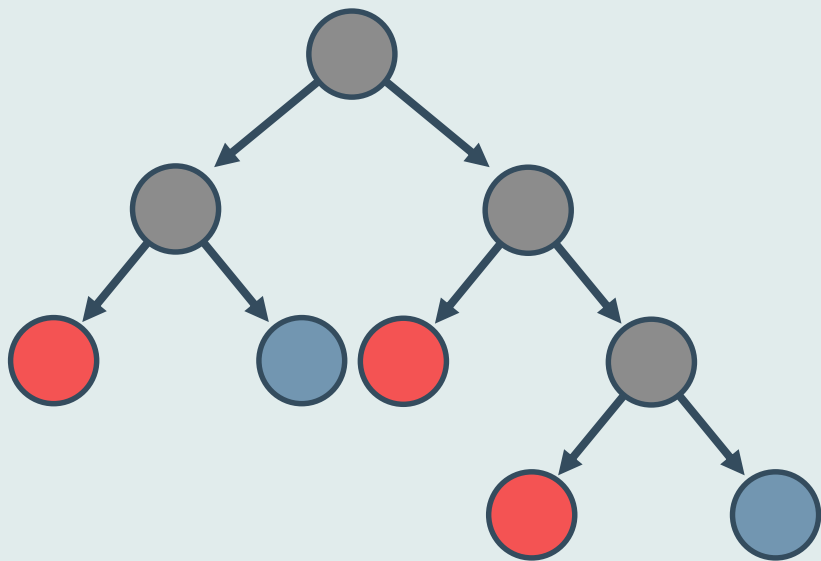
- Problem: decision trees tend to overfit

DECISION TREES ARE HIGH VARIANCE



- Problem: decision trees tend to overfit
- Pruning helps reduce variance to a point

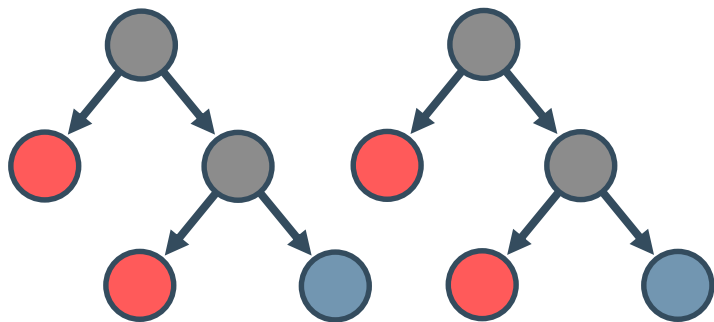
DECISION TREES ARE HIGH VARIANCE



- Problem: decision trees tend to overfit
- Pruning helps reduce variance to a point
- Often not significant for model to generalize well

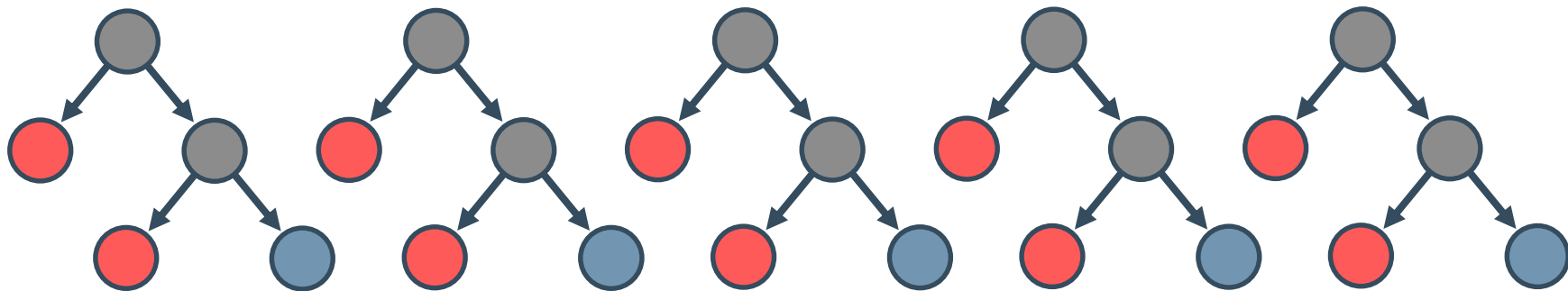
IMPROVEMENT: USE MANY TREES

Create many different trees.



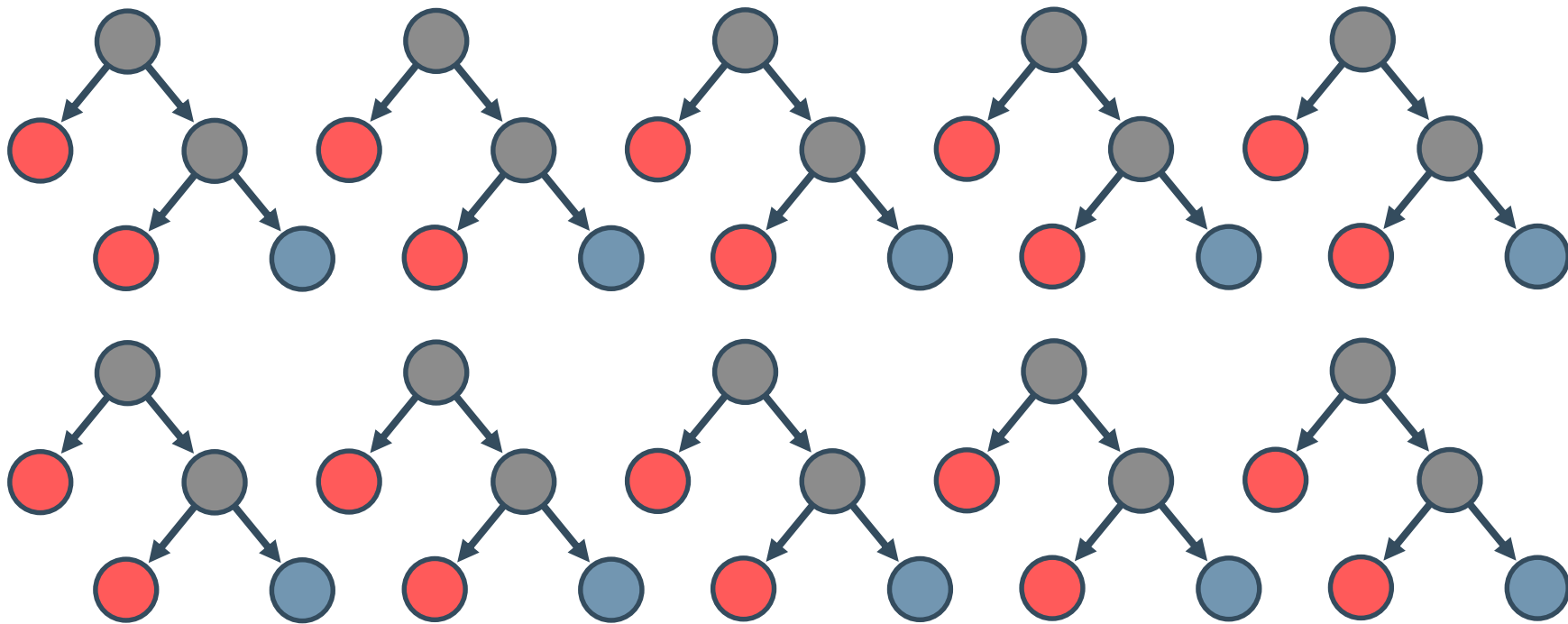
IMPROVEMENT: USE MANY TREES

Create many different trees.



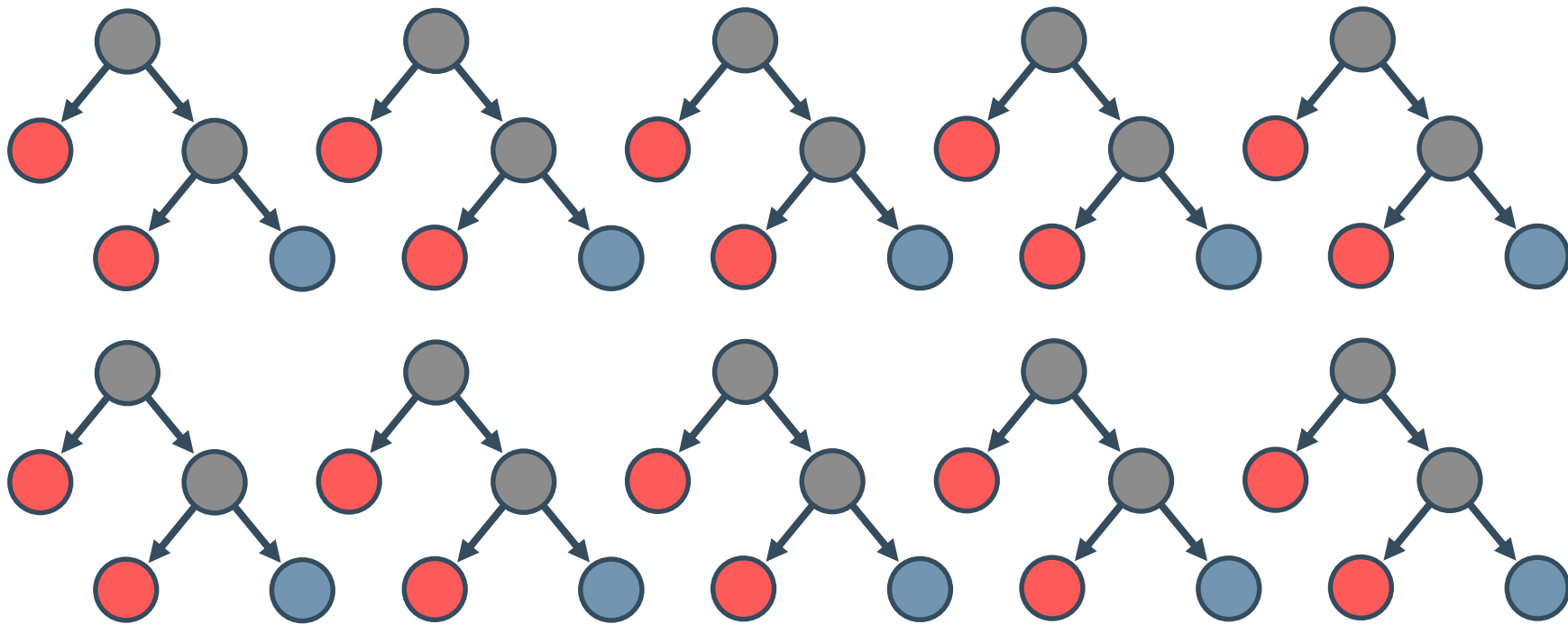
IMPROVEMENT: USE MANY TREES

Create many different trees.



IMPROVEMENT: USE MANY TREES

Combine predictions to reduce variance.



HOW TO CREATE MULTIPLE TREES?

Use bootstrapping: sample data with replacement.

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
0	2013-11-02 The Hunger Games: Catching Fire	130000000	424668047	Francis Lawrence	PG-13	146
1	2013-05-03 Iron Man 3	200000000	409013694	Shane Black	PG-13	129
2	2013-11-02 Frozen	150000000	400738009	Chris BuckJennifer Lee	PG	108
3	2013-07-03 Despicable Me 2	76000000	368061265	Pierre CoffinChris Renaud	PG	98
4	2013-08-14 Man of Steel	225000000	291043518	Zack Snyder	PG-13	143
5	2013-10-04 Gravity	100000000	274289705	Alfonso Cuarón	PG-13	91
6	2013-06-21 Monsters University	NaH	268492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	NaH	236366855	Peter Jackson	PG-13	161
8	2013-05-04 Fast & Furious 6	160000000	238679650	Justin Lin	PG-13	130
9	2013-03-08 Oz: The Great and Powerful	215000000	234811825	Sam Raimi	PG	127
10	2013-05-16 Star Trek Into Darkness	180000000	228778661	J.J. Abrams	PG-13	123
11	2013-11-08 Thor: The Dark World	170000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	190000000	202359711	Marc Forster	PG-13	116
13	2013-03-02 The Croods	135000000	187168425	Kirk De MicoChris Sanders	PG	98
14	2013-06-28 The Heat	43000000	195682188	Paul Feig	R	117
15	2013-08-07 We're the Millers	37000000	150394119	Rawson Marshall Thurber	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

HOW TO CREATE MULTIPLE TREES?

Create multiple bootstrapped samples.

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
0	2013-11-02 The Hunger Games: Catching Fire	13000000	42468047	Francis Lawrence	PG-13	146
1	2013-05-03 Iron Man 3	20000000	409013694	Shane Black	PG-13	129
2	2013-11-02 Frozen	15000000	400738009	Chris BuckJennifer Lee	PG	108
3	2013-07-03 Despicable Me 2	76000000	368061265	Pierre CoffinChris Renaud	PG	98
4	2013-06-14 Man of Steel	22000000	291045818	Zack Snyder	PG-13	143
5	2013-06-04 Gravity	10000000	274089705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	23636955	Peter Jackson	PG-13	161
8	2013-03-04 Fast & Furious 6	16000000	236679650	Justin Lin	PG-13	130
9	2013-03-08 Oz: The Great and Powerful	21500000	234911825	Sam Rami	PG	127
10	2013-05-16 Star Trek Into Darkness	18000000	228778961	J.J. Abrams	PG-13	123
11	2013-11-08 Thor: The Dark World	17000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	19000000	202359711	Marc Forster	PG-13	116
13	2013-03-02 The Croods	13000000	187168425	Kirk De MicoChris Sanders	PG	98
14	2013-06-28 The Heat	43000000	195982188	Paul Feig	R	117
15	2013-06-07 We're the Millers	37000000	103094119	Ressan Marshall Thuermer	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	10500000	144840419	Baz Luhrmann	PG-13	143

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
0	2013-11-02 The Hunger Games: Catching Fire	13000000	42468047	Francis Lawrence	PG-13	146
1	2013-05-03 Iron Man 3	20000000	409013694	Shane Black	PG-13	129
2	2013-11-02 Frozen	15000000	400738009	Chris BuckChris Renaud	PG	108
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4	2013-06-14 Man of Steel	22000000	291045818	Zack Snyder	PG-13	143
5	2013-06-04 Gravity	10000000	274089705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	23636955	Peter Jackson	PG-13	161
8	2013-03-04 Fast & Furious 6	16000000	236679650	Justin Lin	PG-13	130
9	2013-03-08 Oz: The Great and Powerful	21500000	234911825	Sam Rami	PG	127
10	2013-05-16 Star Trek Into Darkness	18000000	228778961	J.J. Abrams	PG-13	123
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12	2013-06-21 World War Z	19000000	202359711	Marc Forster	PG-13	116
13	2013-03-02 The Croods	13000000	187168425	Kirk De MicoChris Sanders	PG	98
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5	2013-06-04 Gravity	10000000	274089705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	23636955	Peter Jackson	PG-13	161
8	2013-03-04 Fast & Furious 6	16000000	236679650	Justin Lin	PG-13	130
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11	2013-11-08 Thor: The Dark World	17000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	19000000	202359711	Marc Forster	PG-13	116
13	2013-03-02 The Croods	13000000	187168425	Kirk De MicoChris Sanders	PG	98
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5	2013-06-04 Gravity	10000000	274089705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
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HOW TO CREATE MULTIPLE TREES?

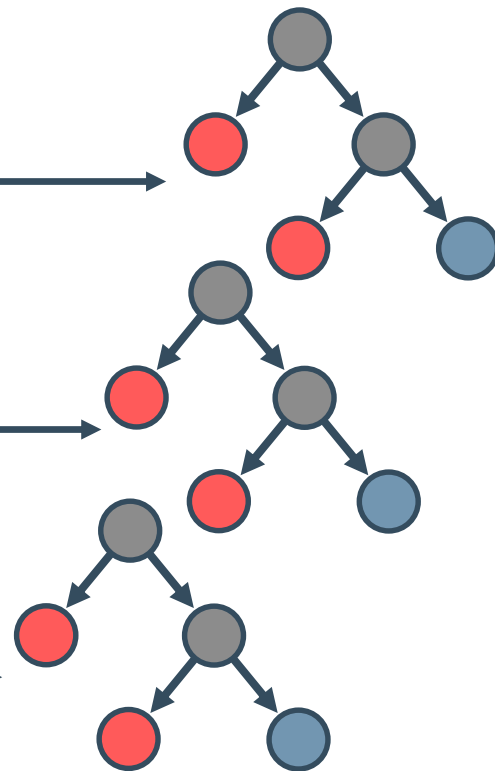
Grow decision tree from each bootstrapped sample.

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
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1	2013-05-03 Iron Man 3	200000000	409013694	Shane Black	PG-13	129
2	2013-11-02 Frozen	150000000	400738009	Chris Buck/Chris Renaud	PG	108
3	2013-07-03 Despicable Me 2	76000000	368061265	Pierre Coffin/Chris Renaud	PG	98
4	2013-06-14 Man of Steel	220000000	291045518	Zack Snyder	PG-13	143
5	2013-10-04 Gravity	100000000	274080705	Alfonso Cuarón	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	236369555	Peter Jackson	PG-13	161
8	2013-03-04 Fast & Furious 6	160000000	236879650	Justin Lin	PG-13	130
9	2013-03-08 Oz: The Great and Powerful	215000000	234811825	Sam Raimi	PG	127
10	2013-05-16 Star Trek Into Darkness	180000000	228778961	J.J. Abrams	PG-13	123
11	2013-11-08 Thor: The Dark World	770000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	190000000	20259711	Marc Forster	PG-13	116
13	2013-03-02 The Croods	130000000	187168425	Kirk De Mico/Chris Sanders	PG	98
14	2013-06-28 The Heat	43000000	195682188	Paul Feig	R	117
15	2013-06-07 We're the Millers	37000000	103094119	Ressan Marshall Thuermer	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
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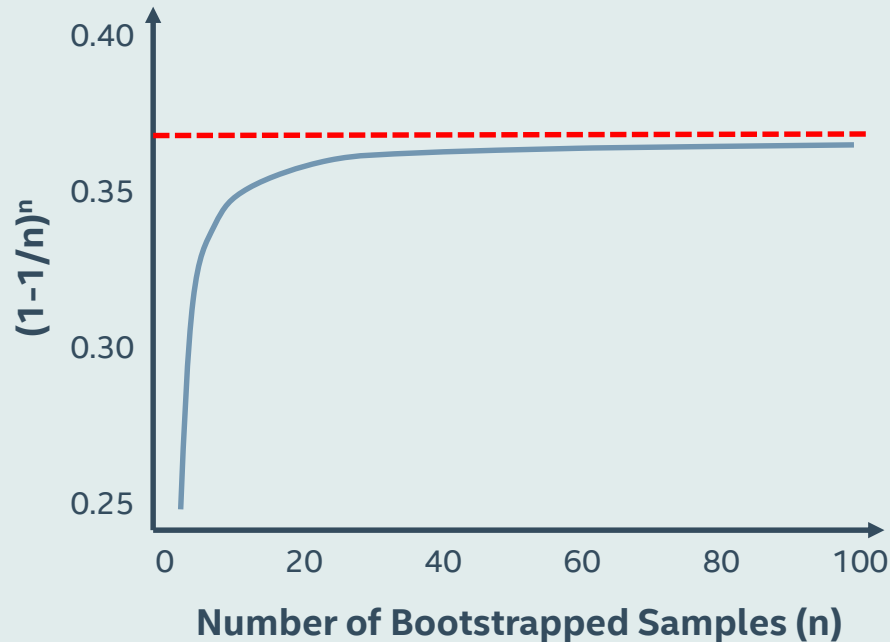
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4	2013-06-14 Man of Steel	220000000	291045518	Zack Snyder	PG-13	143
5	2013-10-04 Gravity	100000000	274080705	Alfonso Cuarón	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	236369555	Peter Jackson	PG-13	161
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4	2013-06-14 Man of Steel	220000000	291045518	Zack Snyder	PG-13	143
5	2013-10-04 Gravity	100000000	274080705	Alfonso Cuarón	PG-13	91
6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	236369555	Peter Jackson	PG-13	161
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6	2013-06-21 Monsters University	N/A	238492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	N/A	236369555	Peter Jackson	PG-13	161
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12	2013-06-21 World War Z	190000000	20259711	Marc Forster	PG-13	116
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16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

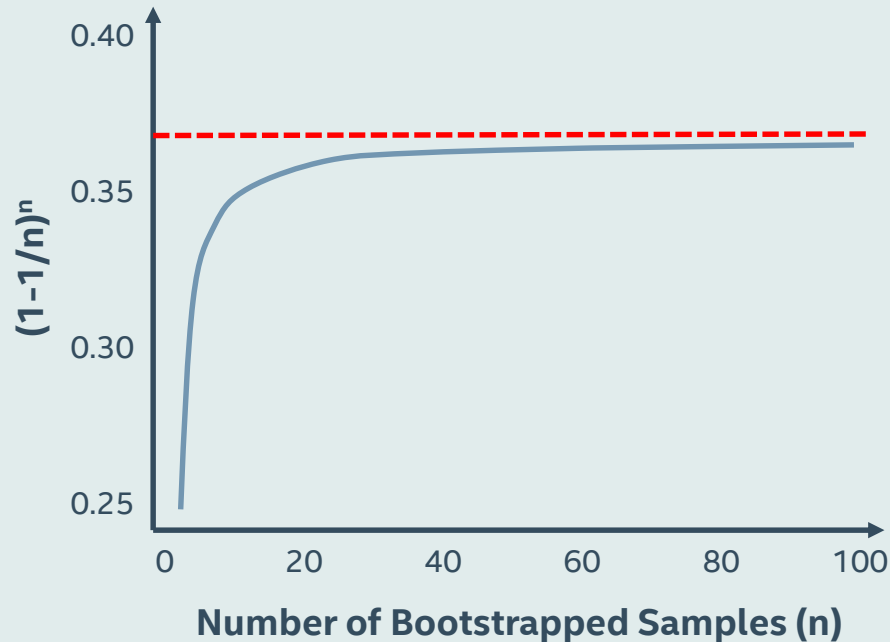


DISTRIBUTION OF DATA IN BOOTSTRAPPED SAMPLES



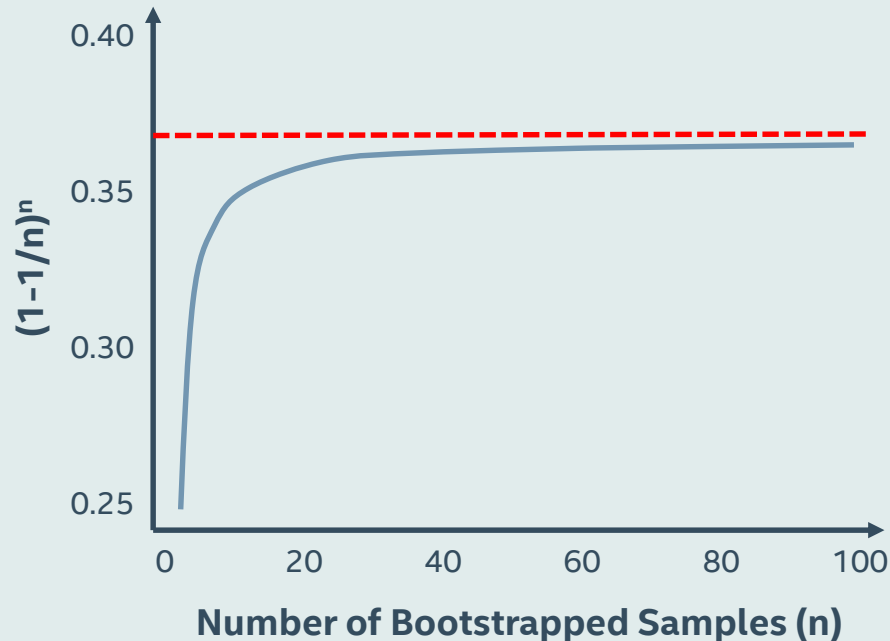
- Given a dataset, create n bootstrapped samples

DISTRIBUTION OF DATA IN BOOTSTRAPPED SAMPLES



- Given a dataset, create n bootstrapped samples
- For a given record x ,
 $P(\text{rec } x \text{ not selected}) = (1 - 1/n)^n$

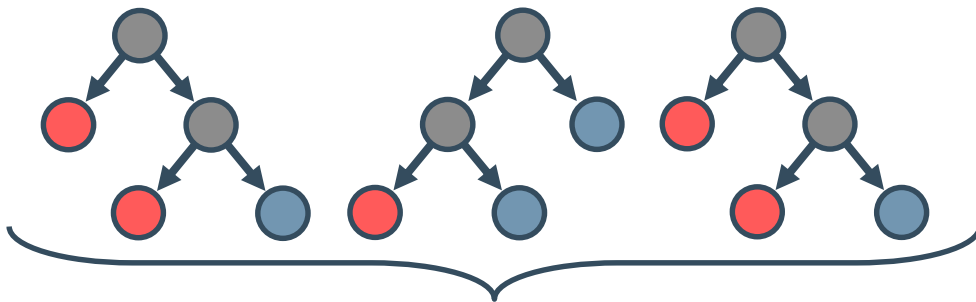
DISTRIBUTION OF DATA IN BOOTSTRAPPED SAMPLES



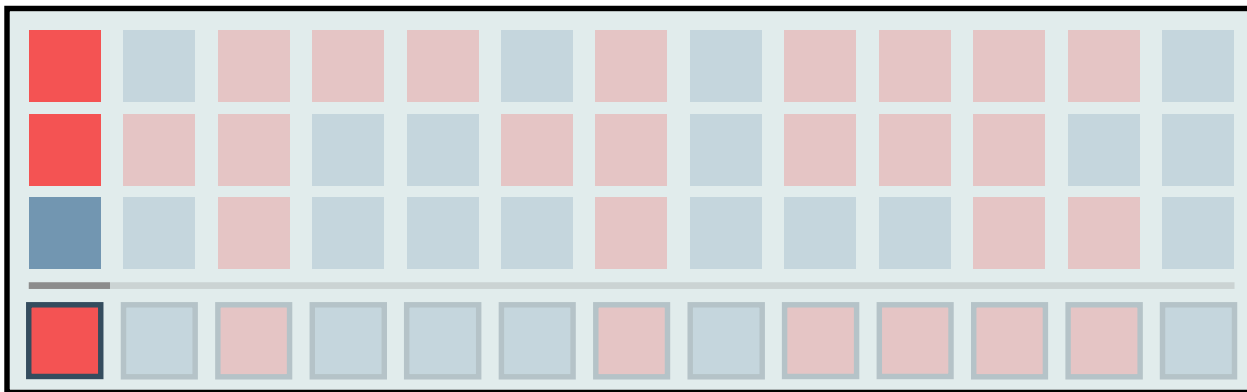
- Given a dataset, create n bootstrapped samples
- For a given record x ,
 $P(\text{rec } x \text{ not selected}) = (1 - 1/n)^n$
- Each bootstrap sample contains approximately $2/3$ of the records

AGGREGATE RESULTS

Trees vote on or average result for each data point.

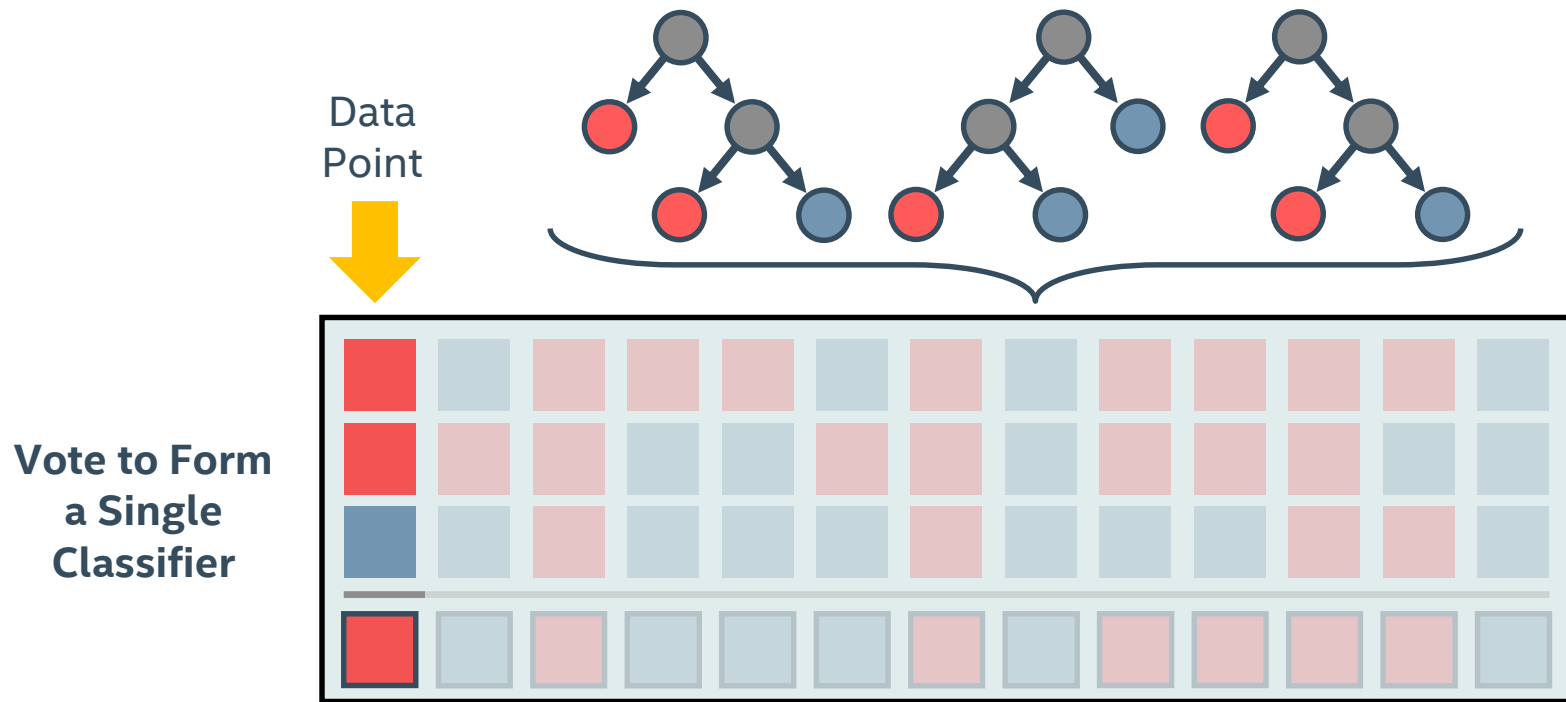


**Vote to Form
a Single
Classifier**



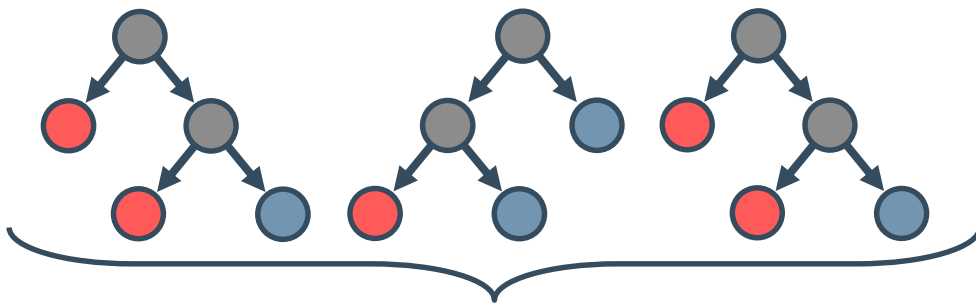
AGGREGATE RESULTS

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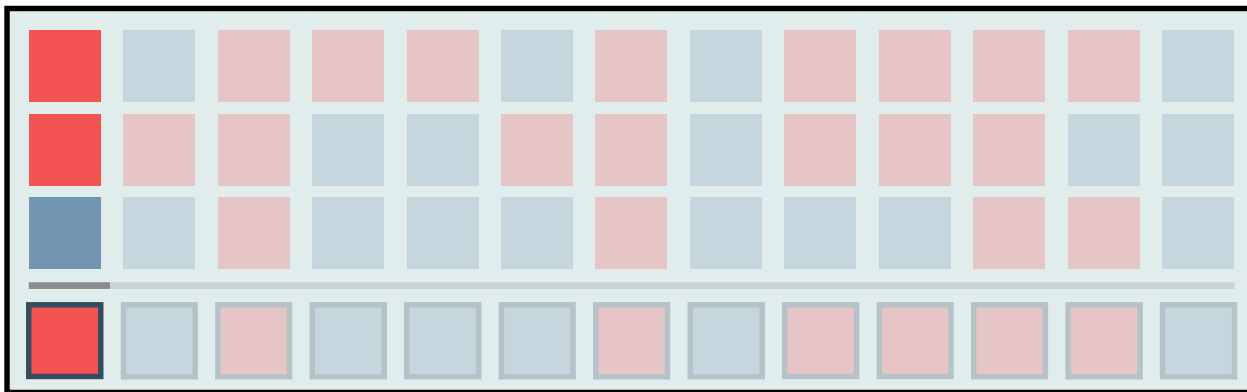
AGGREGATE RESULTS

Trees vote on or average result for each data point.



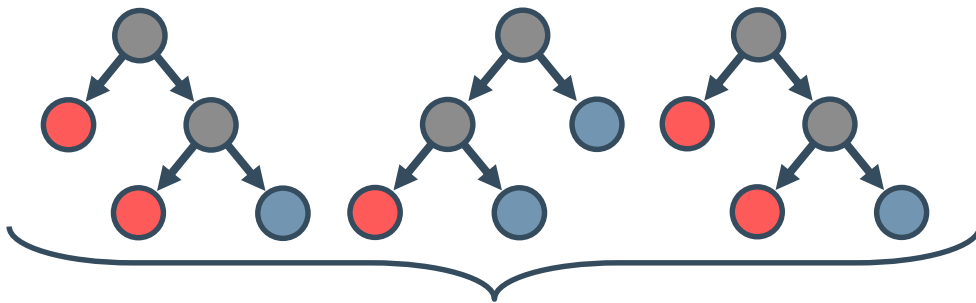
**Vote to Form
a Single
Classifier**

Results

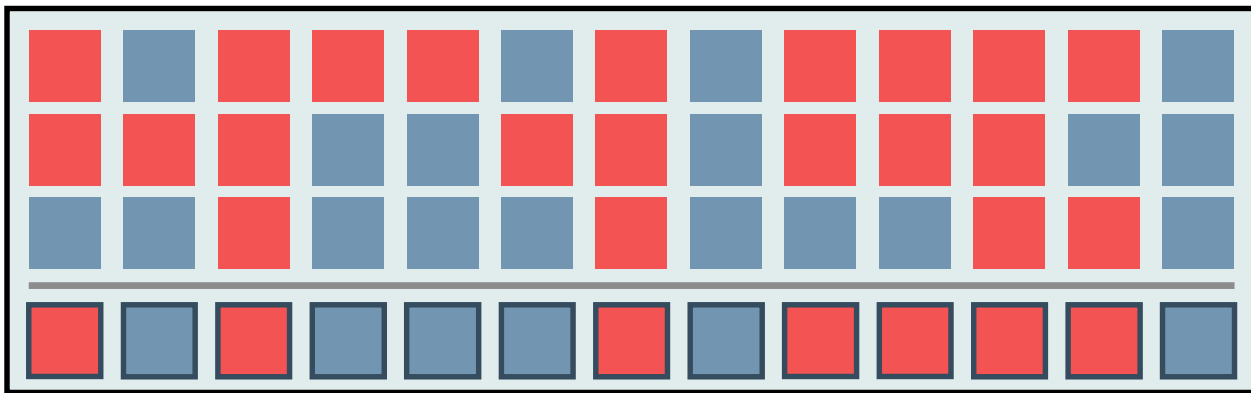


AGGREGATE RESULTS

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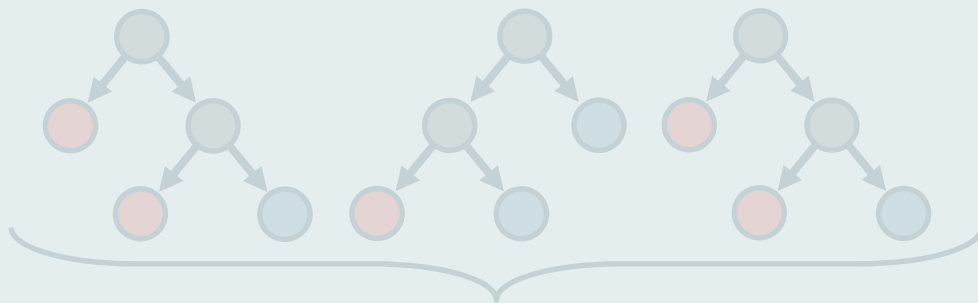


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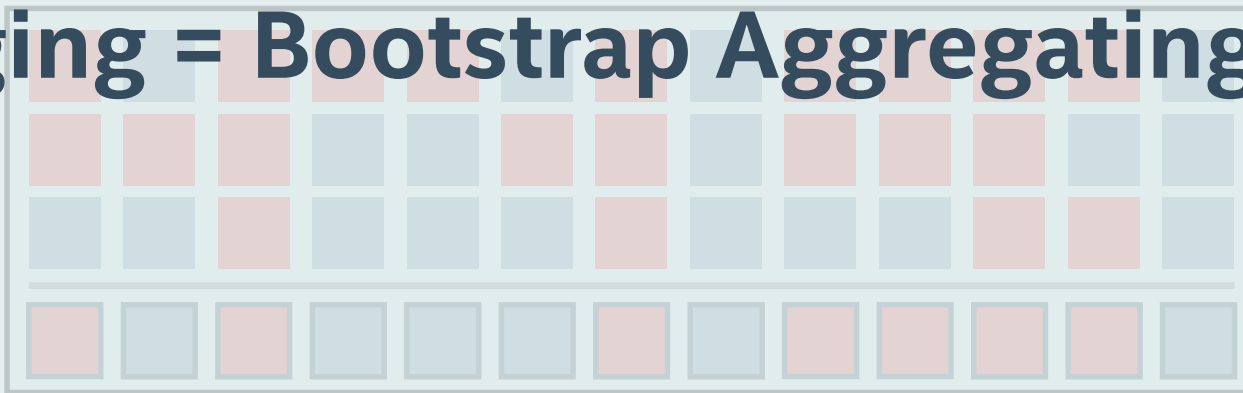
AGGREGATE RESULTS

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Bagging = Bootstrap Aggregating

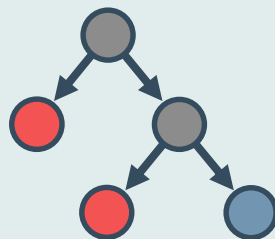
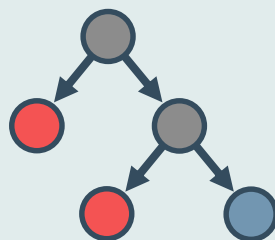
Vote to Form
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BAGGING ERROR CALCULATIONS

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
0	2013-11-22 The Hunger Games: Catching Fire	130000000	424668047	Francis Lawrence	PG-13	146
1	2013-05-03 Iron Man 3	200000000	409013994	Shane Black	PG-13	129
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6	2013-06-21 Monsters University	NaN	268492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	NaN	258366855	Peter Jackson	PG-13	161
8	2013-05-24 Fast & Furious 6	160000000	238679850	Justin Lin	PG-13	130
9	2013-03-08 Oz The Great and Powerful	215000000	234911825	Sam Raimi	PG	127
10	2013-05-16 Star Trek Into Darkness	190000000	228778861	J.J. Abrams	PG-13	123
11	2013-11-08 Thor: The Dark World	170000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	190000000	202359711	Marc Forster	PG-13	116
13	2013-03-22 The Croods	135000000	187168425	Kirk De MiccoChris Sanders	PG	98
14	2013-06-28 The Heat	43000000	159582188	Paul Feig	R	117
15	2013-08-07 We're the Millers	37000000	150394119	Rawson Marshall Thurber	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
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1	2013-05-03 Iron Man 3	200000000	409013994	Shane Black	PG-13	129
2	2013-11-22 Frozen	150000000	400738009	Chris BuckJennifer Lee	PG	108
3	2013-07-03 Despicable Me 2	76000000	368061265	Pierre CoffinChris Renaud	PG	98
4	2013-06-14 Man of Steel	225000000	291045518	Zack Snyder	PG-13	143
5	2013-10-04 Gravity	100000000	274092705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	NaN	268492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	NaN	258366855	Peter Jackson	PG-13	161
8	2013-05-24 Fast & Furious 6	160000000	238679850	Justin Lin	PG-13	130
9	2013-03-08 Oz The Great and Powerful	215000000	234911825	Sam Raimi	PG	127
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17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

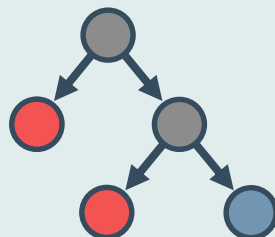
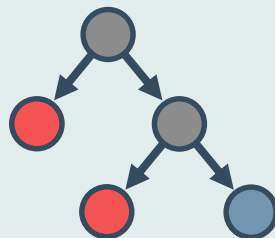


- Bootstrapped samples provide built-in error estimate for each tree

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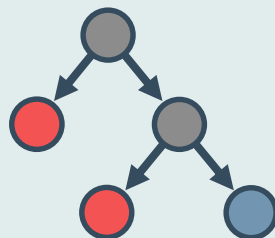
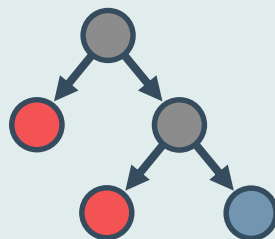


- Bootstrapped samples provide built-in error estimate for each tree
- Create tree based on subset of data

BAGGING ERROR CALCULATIONS

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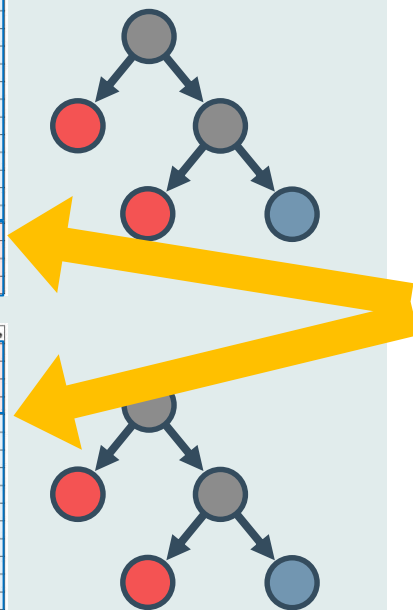


- Bootstrapped samples provide built-in error estimate for each tree
- Create tree based on subset of data
- Measure error for that tree on unused samples

BAGGING ERROR CALCULATIONS

Date	Title	Budget	DomesticTotalGross	Director	Rating	Runtime
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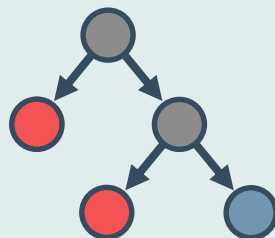
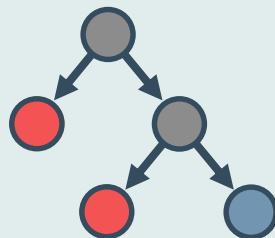


- Bootstrapped samples provide built-in error estimate for each tree
- Create tree based on subset of data
- Measure error for that tree on unused samples

BAGGING ERROR CALCULATIONS

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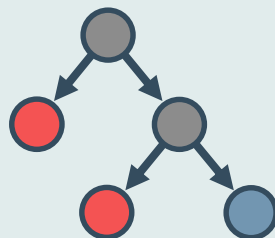
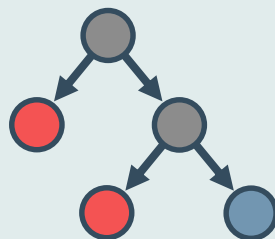


- Bootstrapped samples provide built-in error estimate for each tree
- Create tree based on subset of data
- Measure error for that tree on unused samples
- Called “Out-of-Bag” error

CALCULATION OF FEATURE IMPORTANCE

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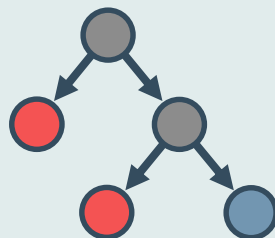
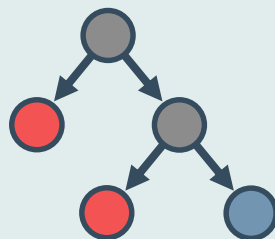


- Fitting a bagged model doesn't produce coefficients like logistic regression

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5	2013-10-04 Gravity	100000000	274092705	Alfonso Cuaron	PG-13	91
6	2013-06-21 Monsters University	NaN	268492764	Dan Scanlon	G	107
7	2013-12-13 The Hobbit: The Desolation of Smaug	NaN	258366855	Peter Jackson	PG-13	161
8	2013-05-24 Fast & Furious 6	160000000	238679850	Justin Lin	PG-13	130
9	2013-03-08 Oz The Great and Powerful	215000000	234911825	Sam Raimi	PG	127
10	2013-05-16 Star Trek Into Darkness	190000000	228778861	J.J. Abrams	PG-13	123
11	2013-11-08 Thor: The Dark World	170000000	206362140	Alan Taylor	PG-13	120
12	2013-06-21 World War Z	190000000	202359711	Marc Forster	PG-13	116
13	2013-03-22 The Croods	135000000	187168425	Kirk De MiccoChris Sanders	PG	98
14	2013-06-28 The Heat	43000000	159582188	Paul Feig	R	117
15	2013-08-07 We're the Millers	37000000	150394119	Rawson Marshall Thurber	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143

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2	2013-11-22 Frozen	150000000	400738009	Chris BuckJennifer Lee	PG	108
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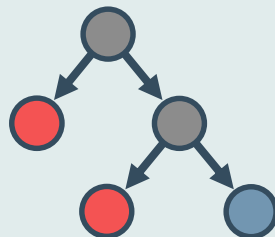
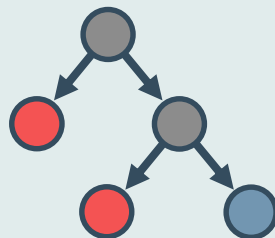


- Fitting a bagged model doesn't produce coefficients like logistic regression
- Instead, feature importances are estimated using oob error

CALCULATION OF FEATURE IMPORTANCE

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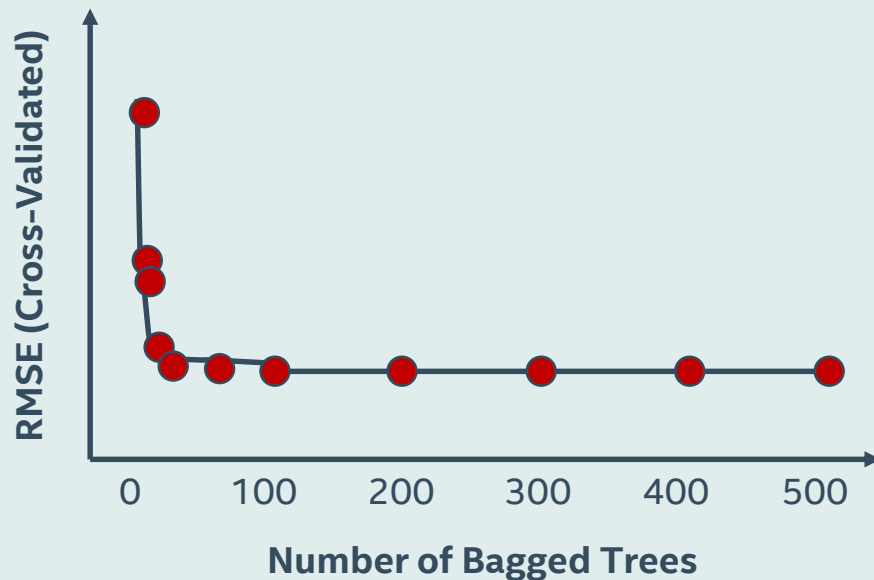
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- Fitting a bagged model doesn't produce coefficients like logistic regression
- Instead, feature importances are estimated using oob error
- Randomly permute data for particular feature and measure change in accuracy

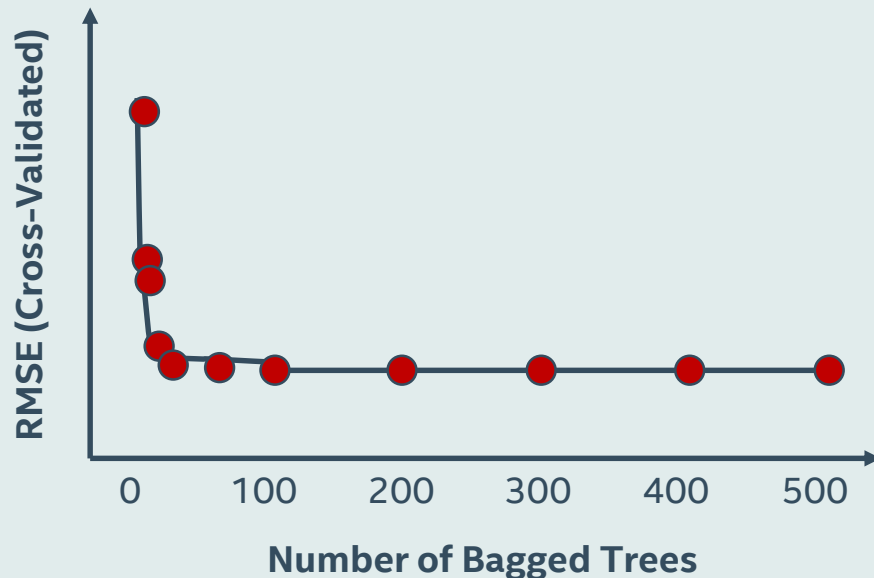
HOW MANY TREES TO FIT?

- Bagging performance improvements increase with more trees



HOW MANY TREES TO FIT?

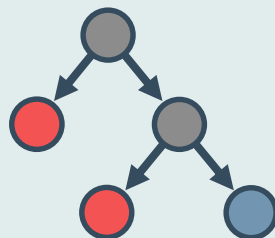
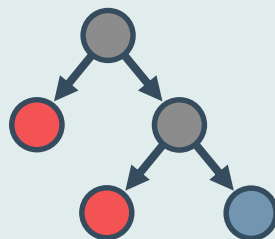
- Bagging performance improvements increase with more trees
- Maximum improvement generally reached ~50 trees



STRENGTHS OF BAGGING

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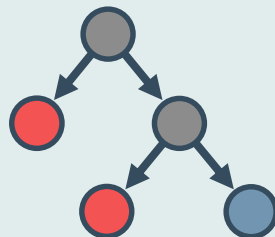
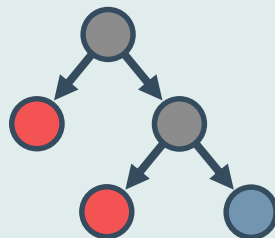
Same as decision trees:

- Easy to interpret and implement

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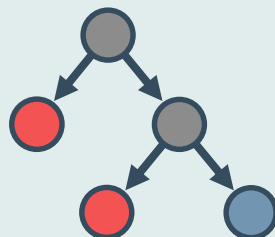
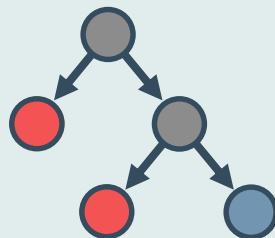
Same as decision trees:

- Easy to interpret and implement
- Heterogeneous input data allowed, no preprocessing required

STRENGTHS OF BAGGING

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Same as decision trees:

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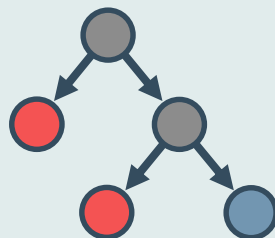
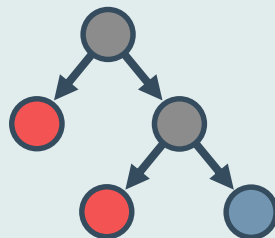
Specific to bagging:

- Less variability than decision trees

STRENGTHS OF BAGGING

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15	2013-08-07 We're the Millers	37000000	150394119	Rawson Marshall Thurber	R	110
16	2013-12-13 American Hustle	40000000	150117807	David O. Russell	R	138
17	2013-05-10 The Great Gatsby	105000000	144840419	Baz Luhrmann	PG-13	143



Same as decision trees:

- Easy to interpret and implement
- Heterogeneous input data allowed, no preprocessing required

Specific to bagging:

- Less variability than decision trees
- Can grow trees in parallel

BAGGINGCLASSIFIER: THE SYNTAX

Import the class containing the classification method.

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Fit the instance on the data and then predict the expected value.

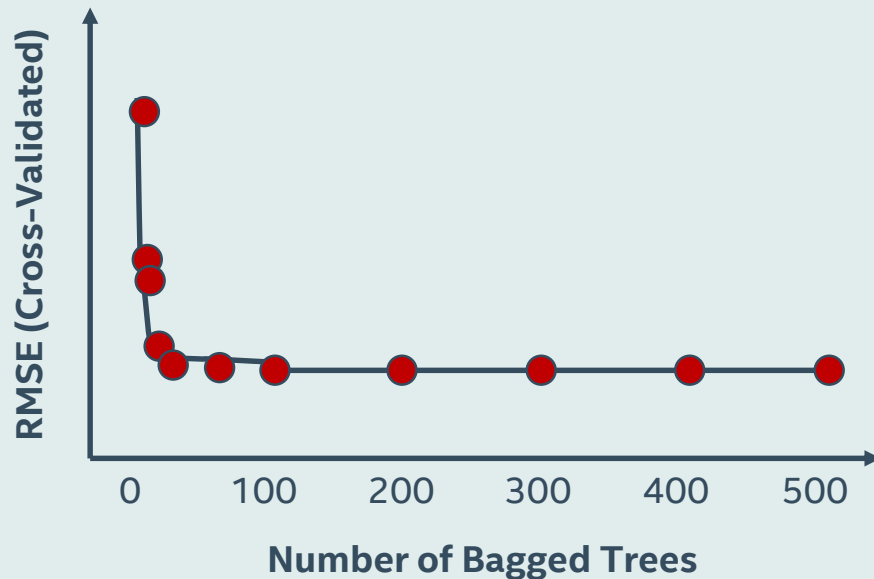
```
BC = BC.fit(X_train, y_train)  
y_predict = BC.predict(X_test)
```

Tune parameters with cross-validation. Use **BaggingRegressor** for regression.

REDUCTION IN VARIANCE DUE TO BAGGING

- For n independent trees, each with variance σ^2 , the bagged variance is:

$$\frac{\sigma^2}{n}$$



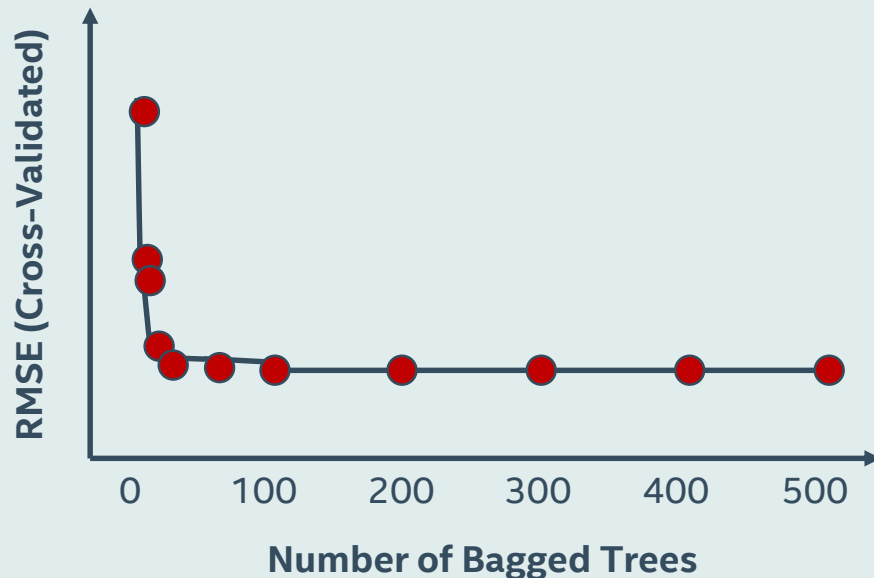
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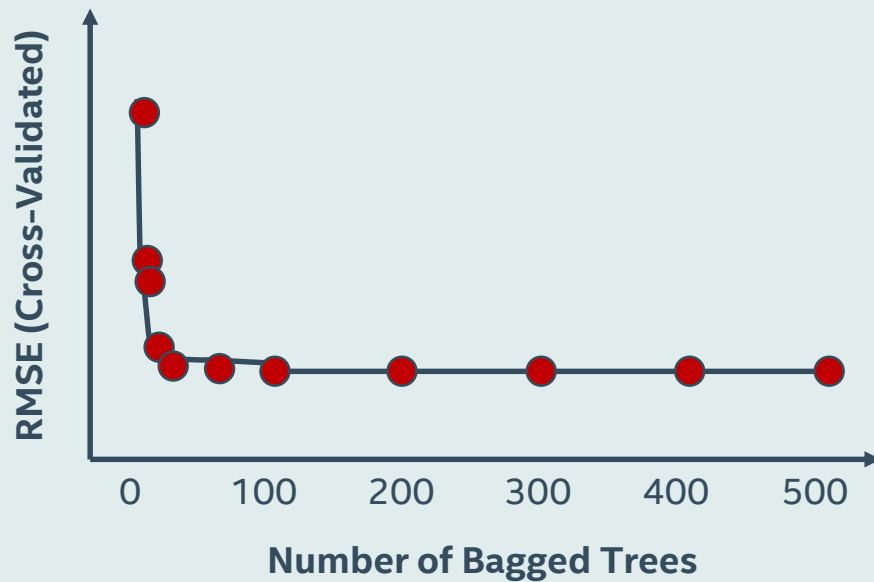
- However, bootstrap samples are correlated (ρ):

$$\rho\sigma^2 + \frac{1-\rho}{n}\sigma^2$$



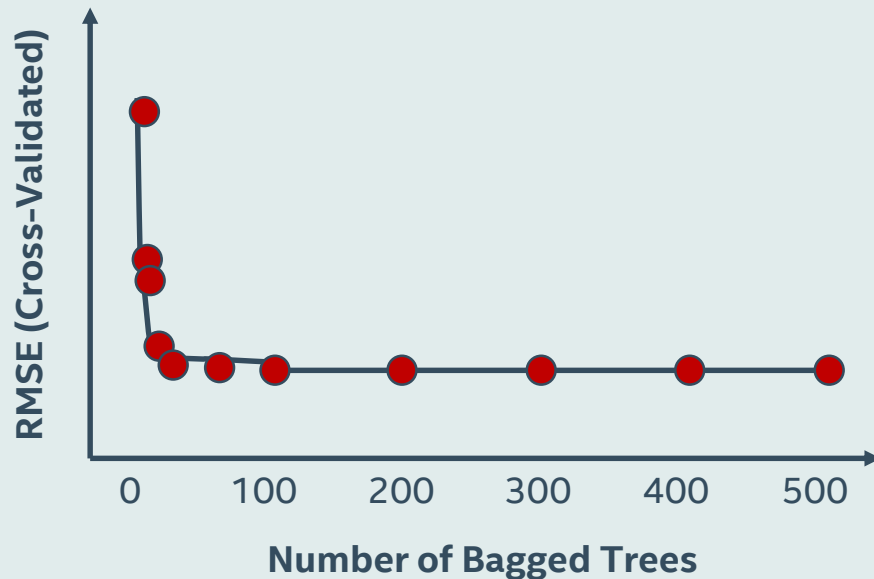
INTRODUCING MORE RANDOMNESS

- **Solution: further de-correlate trees**



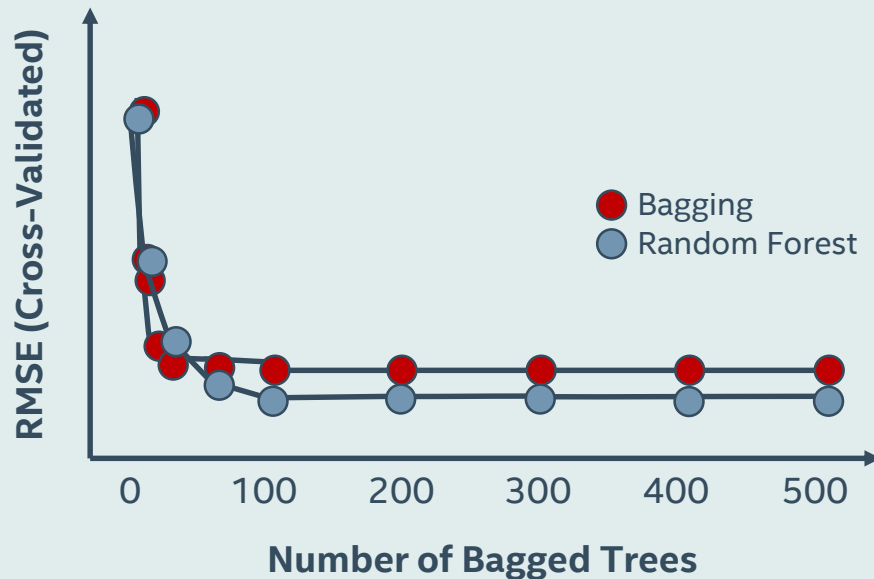
INTRODUCING MORE RANDOMNESS

- **Solution: further de-correlate trees**
- **Use random subset of features for each tree**
 - Classification: \sqrt{m}
 - Regression: $m/3$



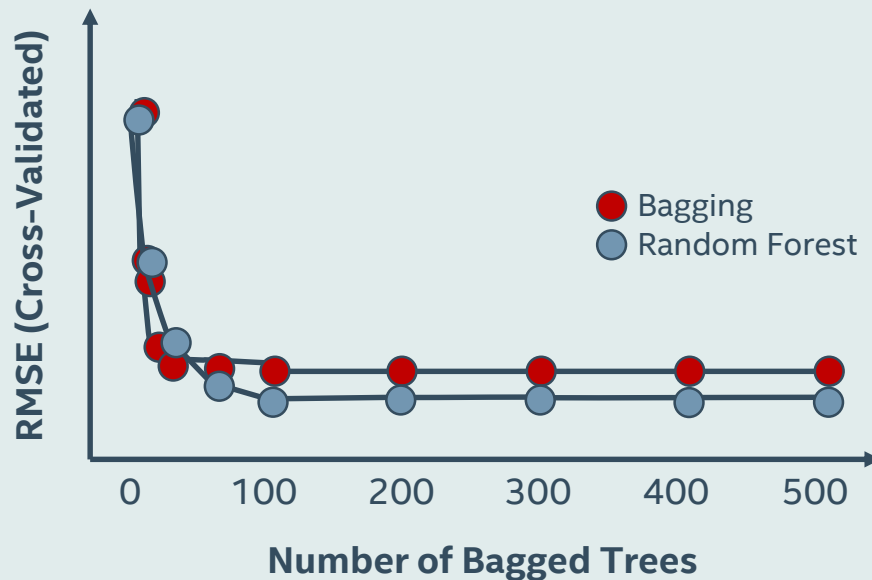
INTRODUCING MORE RANDOMNESS

- **Solution:**
further de-correlate trees
- **Use random subset of features for each tree**
 - Classification: \sqrt{m}
 - Regression: $m/3$
- **Called “Random Forest”**



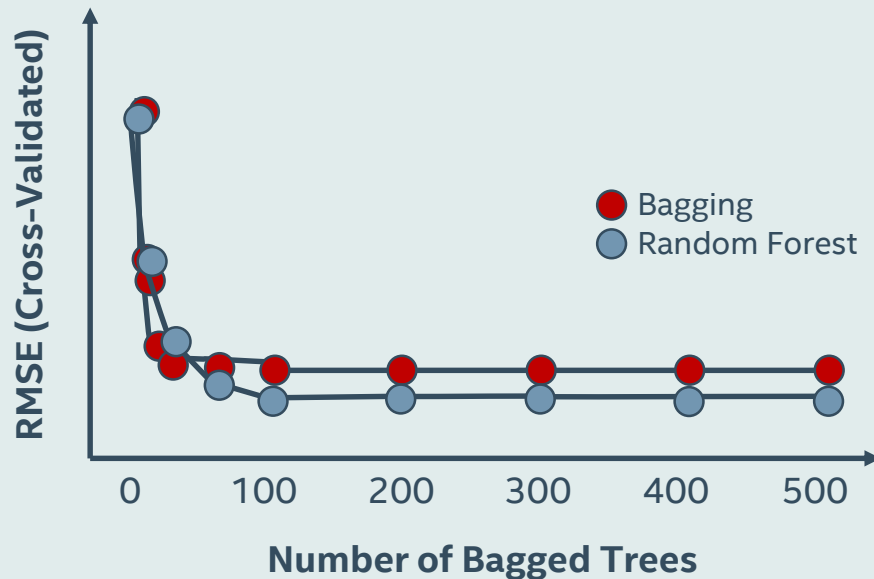
HOW MANY RANDOM FOREST TREES?

- Errors are further reduced for Random Forest relative to Bagging



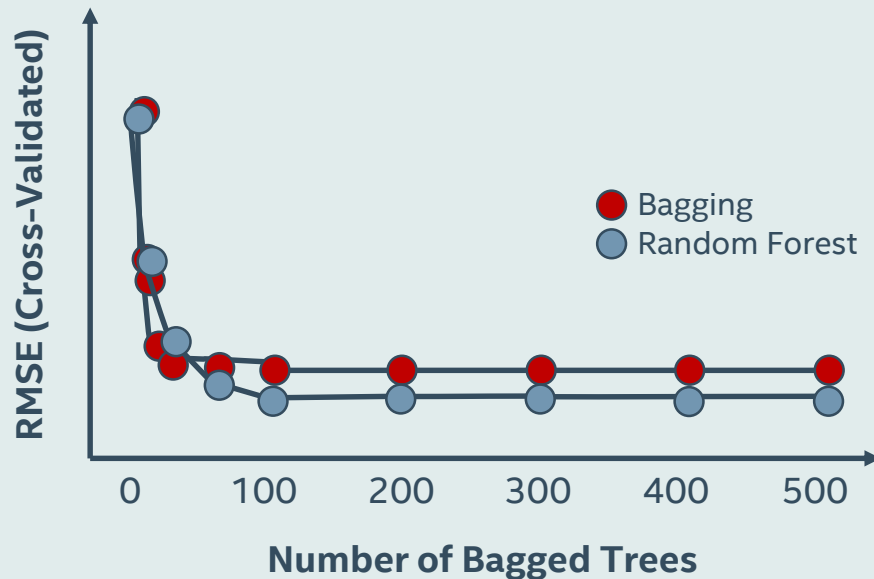
HOW MANY RANDOM FOREST TREES?

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- Grow enough trees until error settles down



HOW MANY RANDOM FOREST TREES?

- Errors are further reduced for Random Forest relative to Bagging
- Grow enough trees until error settles down
- Additional trees won't improve results



RANDOMFOREST: THE SYNTAX

Import the class containing the classification method.

```
from sklearn.ensemble import RandomForestClassifier
```

Create an instance of the class.

```
RC = RandomForestClassifier(n_estimators=100, max_features=10)
```

Fit the instance on the data and then predict the expected value.

```
RC = RC.fit(X_train, y_train)
y_predict = RC.predict(X_test)
```

Tune parameters with cross-validation. Use **RandomForestRegressor** for regression.

INTRODUCING EVEN MORE RANDOMNESS

- Sometimes additional randomness is desired beyond Random Forest

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- Solution: select features randomly and create splits randomly—don't choose greedily

INTRODUCING EVEN MORE RANDOMNESS

- Sometimes additional randomness is desired beyond Random Forest
- Solution: select features randomly and create splits randomly—don't choose greedily
- Called “Extra Random Trees”

EXTRATREESCLASSIFIER: THE SYNTAX

Import the class containing the classification method.

```
from sklearn.ensemble import ExtraTreesClassifier
```

Create an instance of the class.

```
EC = ExtraTreesClassifier(n_estimators=100, max_features=10)
```

Fit the instance on the data and then predict the expected value.

```
EC = EC.fit(X_train, y_train)
y_predict = EC.predict(X_test)
```

Tune parameters with cross-validation. Use **ExtraTreesRegressor** for regression.

