Unsupervised Machine Learning: Clustering

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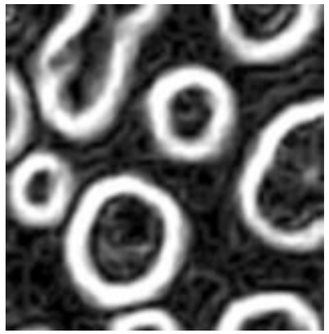
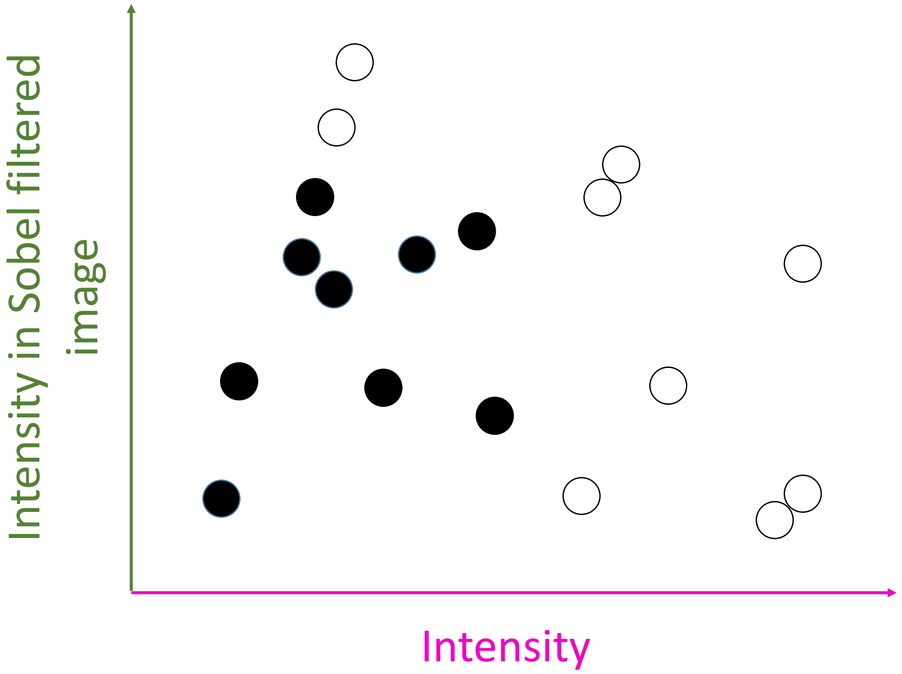
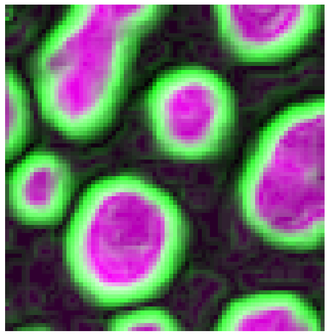
Recap: Object classification

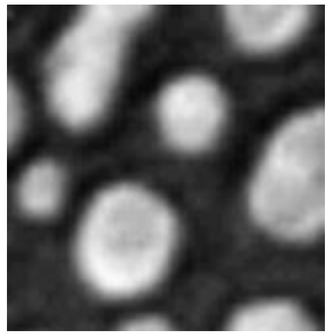
- What if we exchange pixel features with object features?

Pixel classification

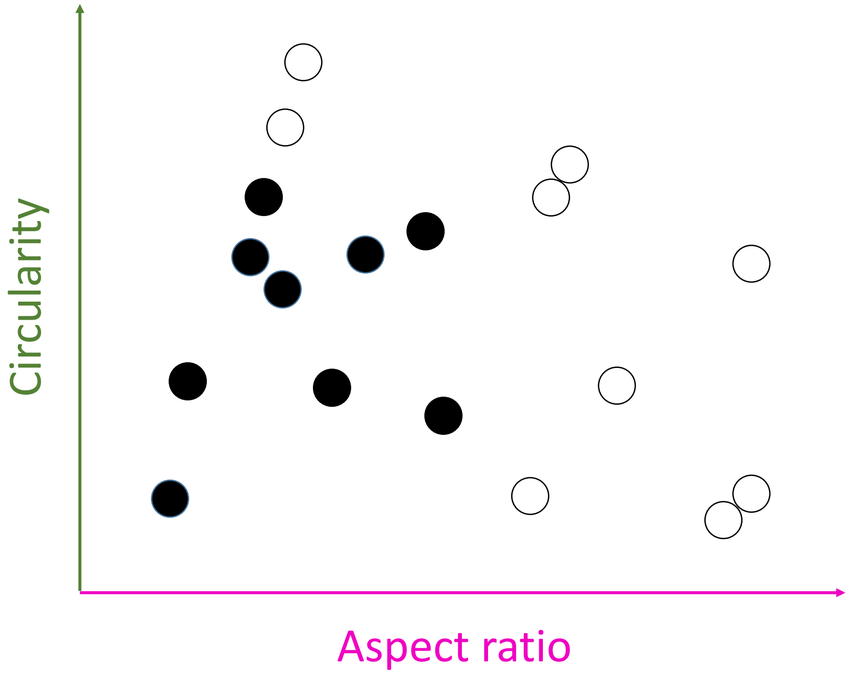








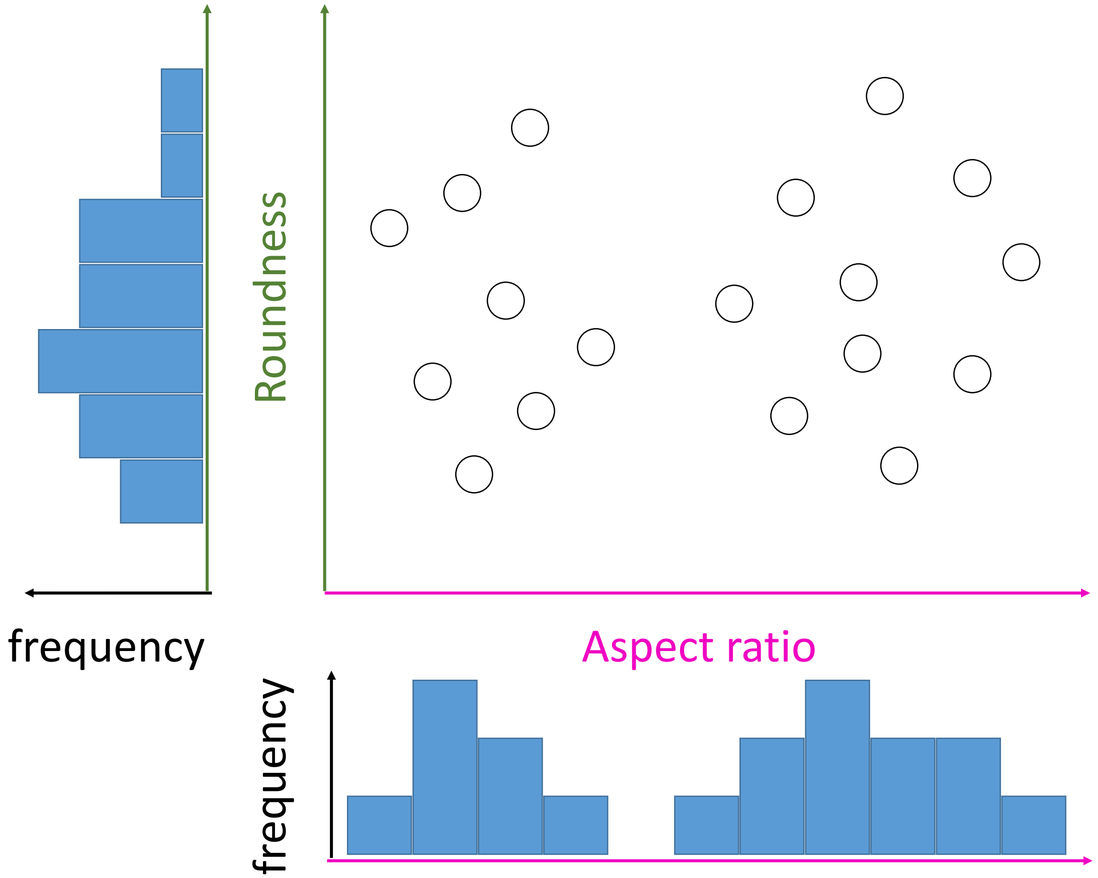
Object classification



- The algorithms work the same but with different
  - Features
  - Number of features
  - Tree / forest parameters
  - Selection criteria

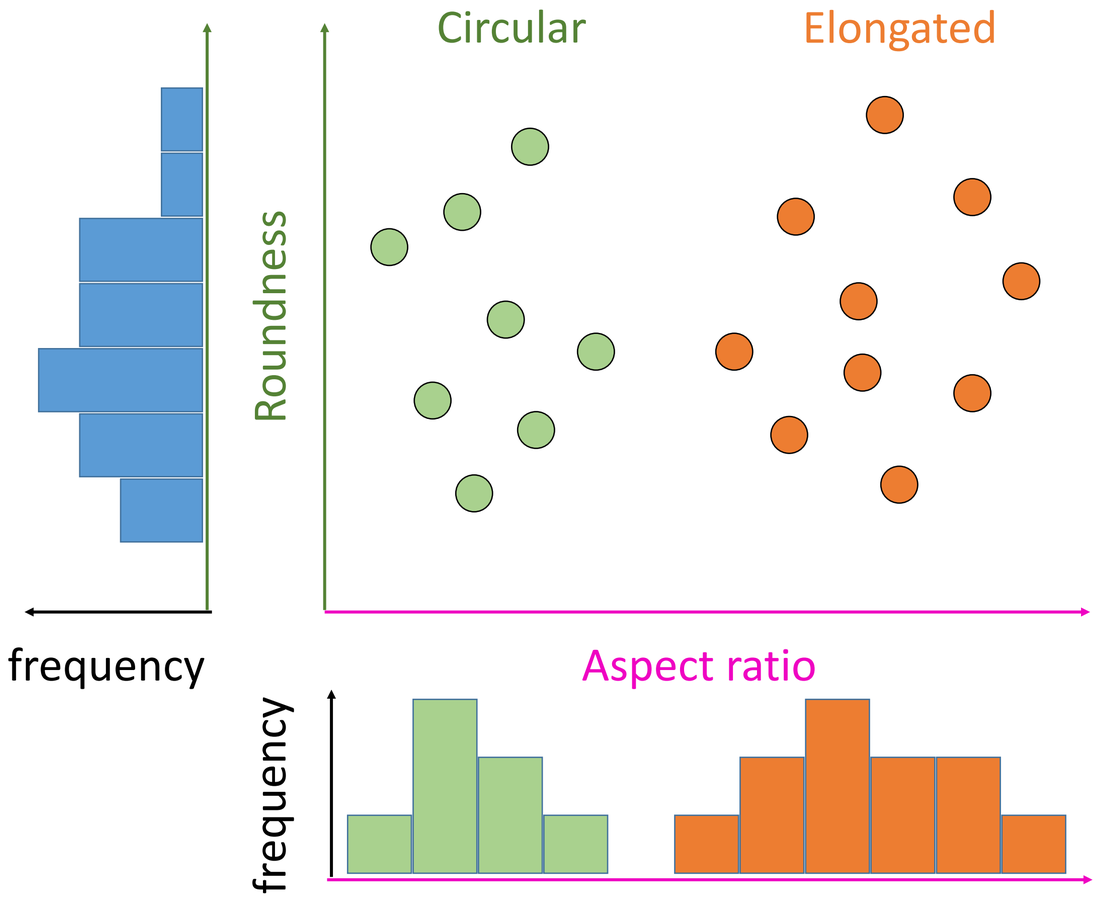
Unsupervised machine learning

- If you don’t provide ground truth, the algorithm is *unsupervised*.



Unsupervised machine learning

- If you don’t provide ground truth, the algorithm is unsupervised.
- Nevertheless, algorithms can tell us something about the data



K-means clustering

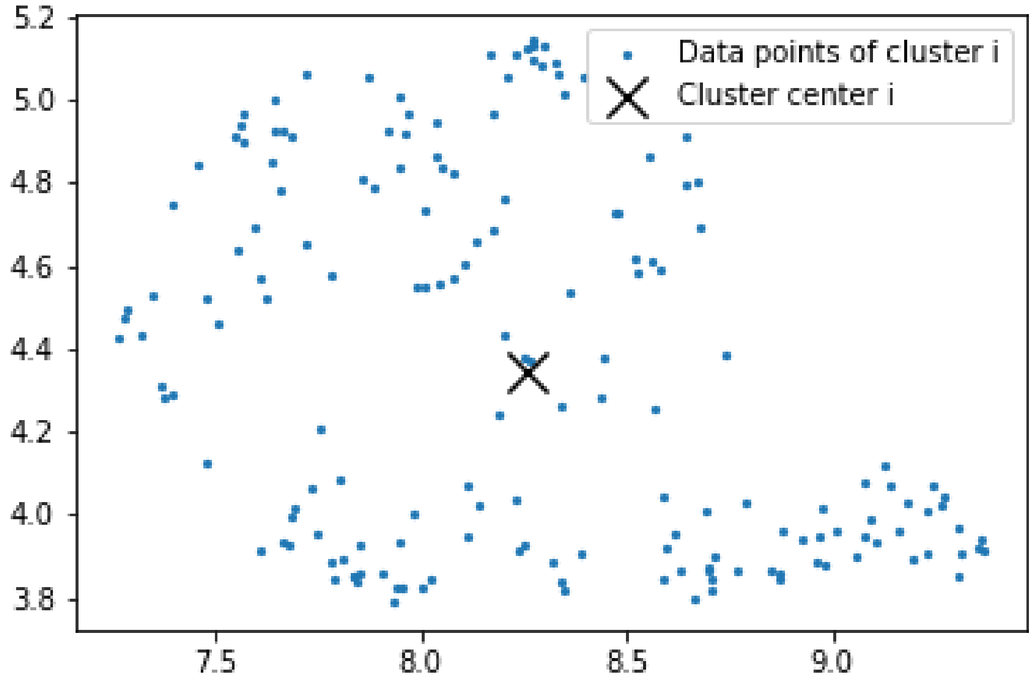
Strategy: Group data points into n groups so that variance within group is minimal

$$\sum_{i=1}^{k} \underbrace{\sum_{x_j \in S_i} \left\| x_j - \mu_i \right\|^2}_{\text{Variance within cluster i}}$$

μ_i: Center of cluster i

S_i: Cluster i

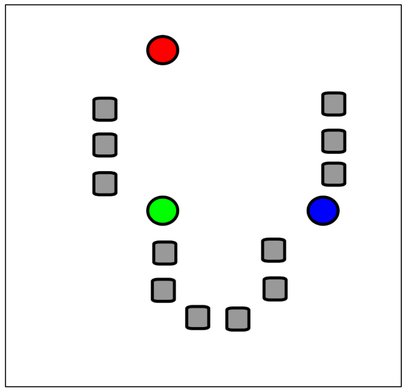
x_j: Datapoint j



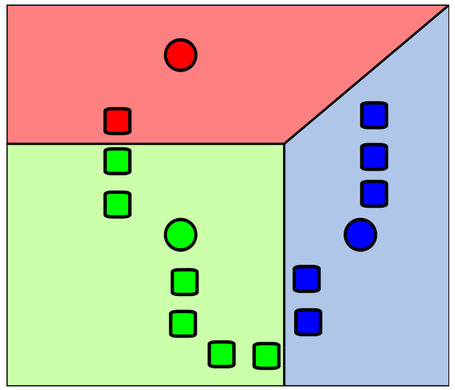
K-means clustering

Strategy: Group data points into n groups so that variance within group is minimal

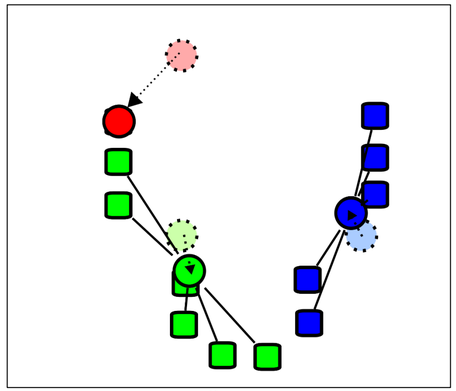
Step1: Random initialization of cluster centers

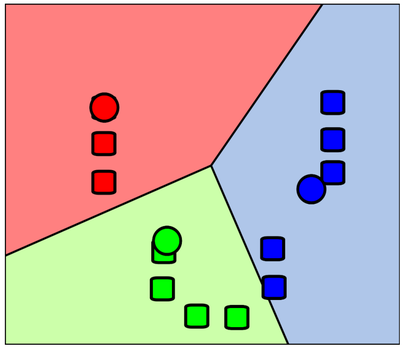


Step2: Tessellation of space into cluster regions



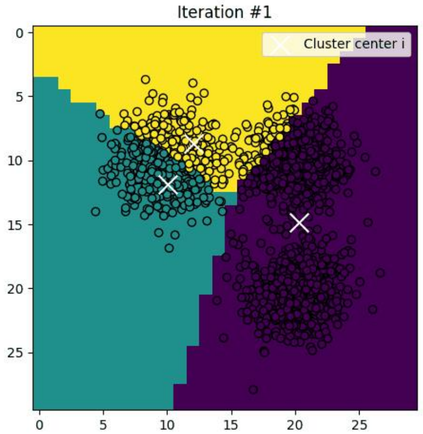
Step3: Replace cluster center with centrois





Step4: Repeat 2&3 until convergence

→ Fast convergence



In Python:

```
from sklearn import cluster
```

Create

```
clusterer = cluster.KMeans(n_clusters=3)
clusterer.fit(X)
```

Predict

```
predicted_class = clusterer.predict(X)
```

Source: https://de.wikipedia.org/wiki/K-Means-Algorithmus
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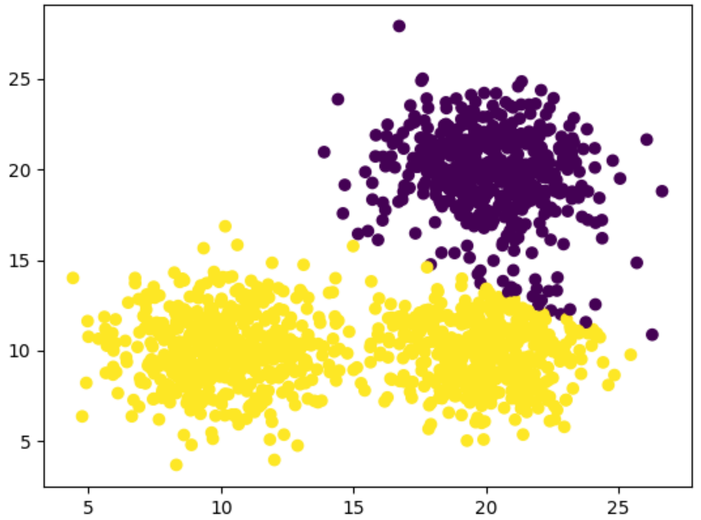
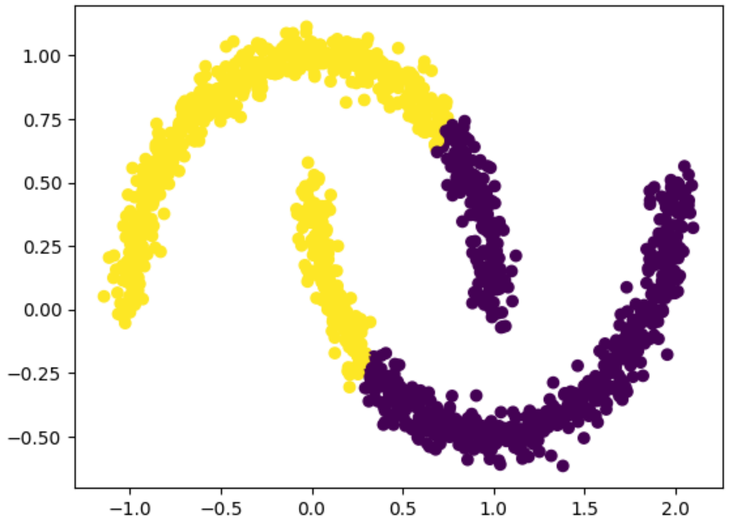
K-means clustering

Strength and weaknesses

- Very fast
- Based on Euclidian metrics → every new point can be assigned to a cluster



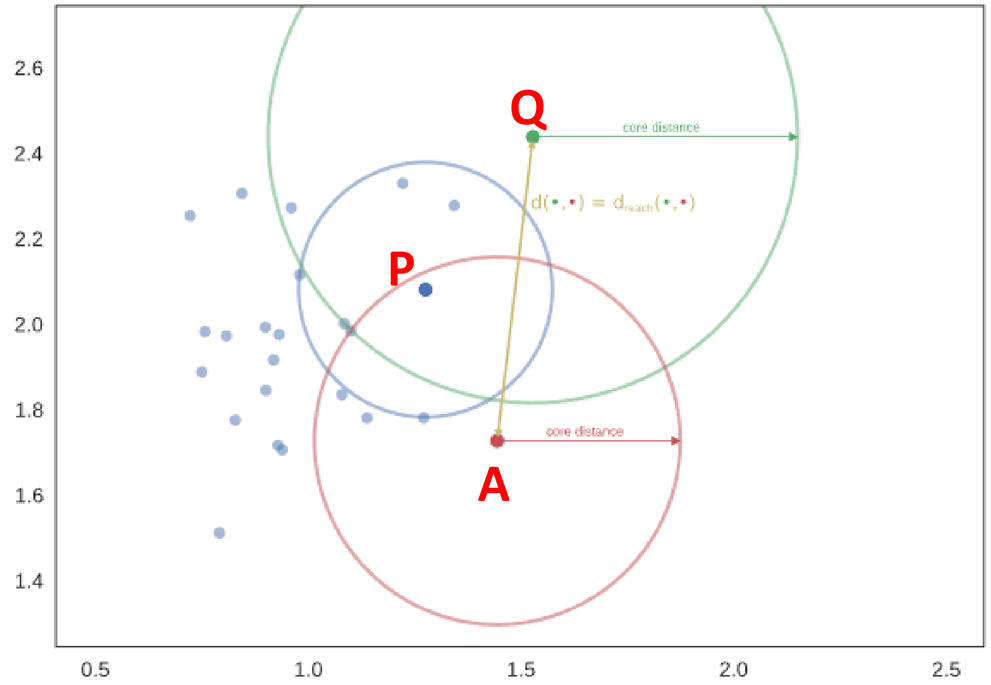
- Number of clusters needs to be known
- Clusters can not capture more complex topologies



HDBSCAN

Hierarchical Density-Based Spatial Clustering of Applications with Noise

Strategy: Build neighborhood graph and identify strongly connected groups



Core distance: Distance to n-th nearest neighbor

Distance metric: Mutual reachability

Core distance of Q > d(P, Q) ➔ $d_{new}(P,Q)$ = core distance

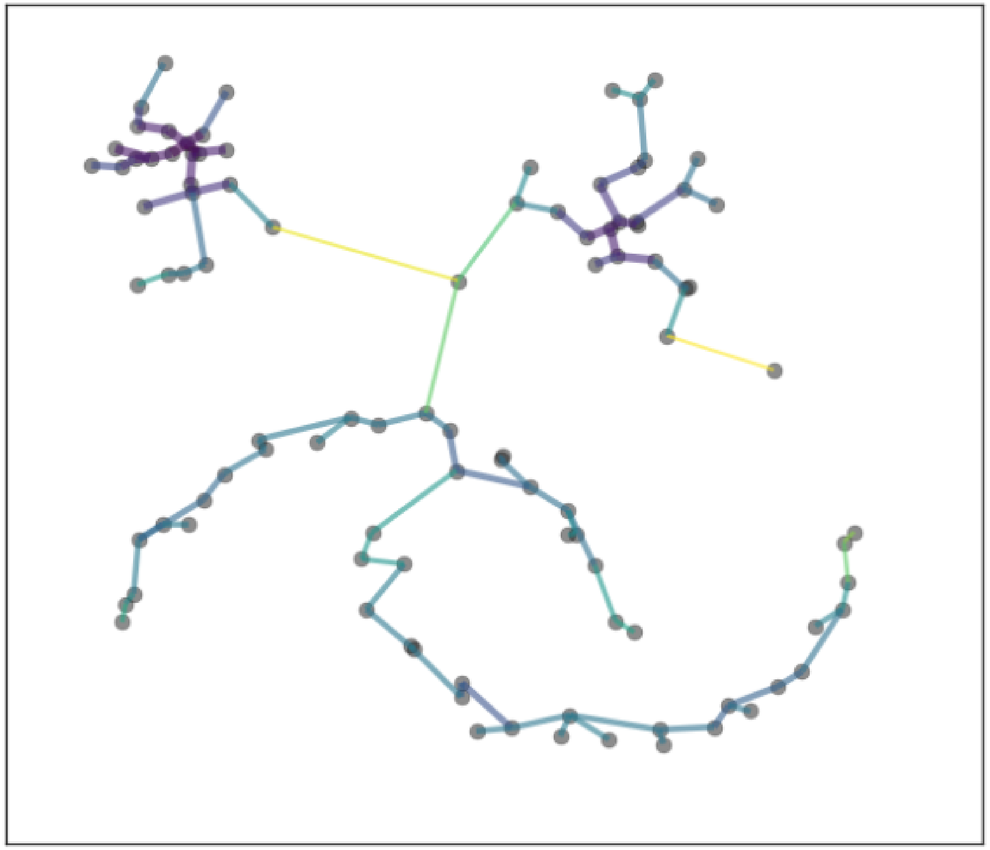
Core distance of Q < d(A, Q) ➔ $d_{new}(A,Q)$ = d(A,Q)

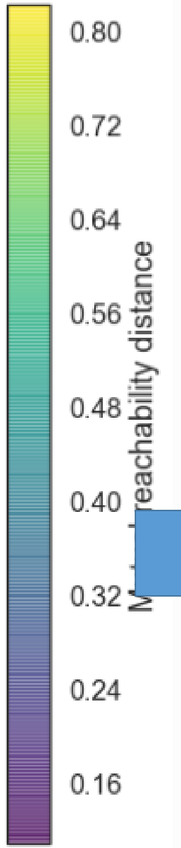
→ Isolated points are pushed further away from clusters

"To find clusters we want to find the islands of higher density amid a sea of sparser noise […] For practical purposes that means making 'sea' points more distant from each other and from the 'land'."

HDBSCAN

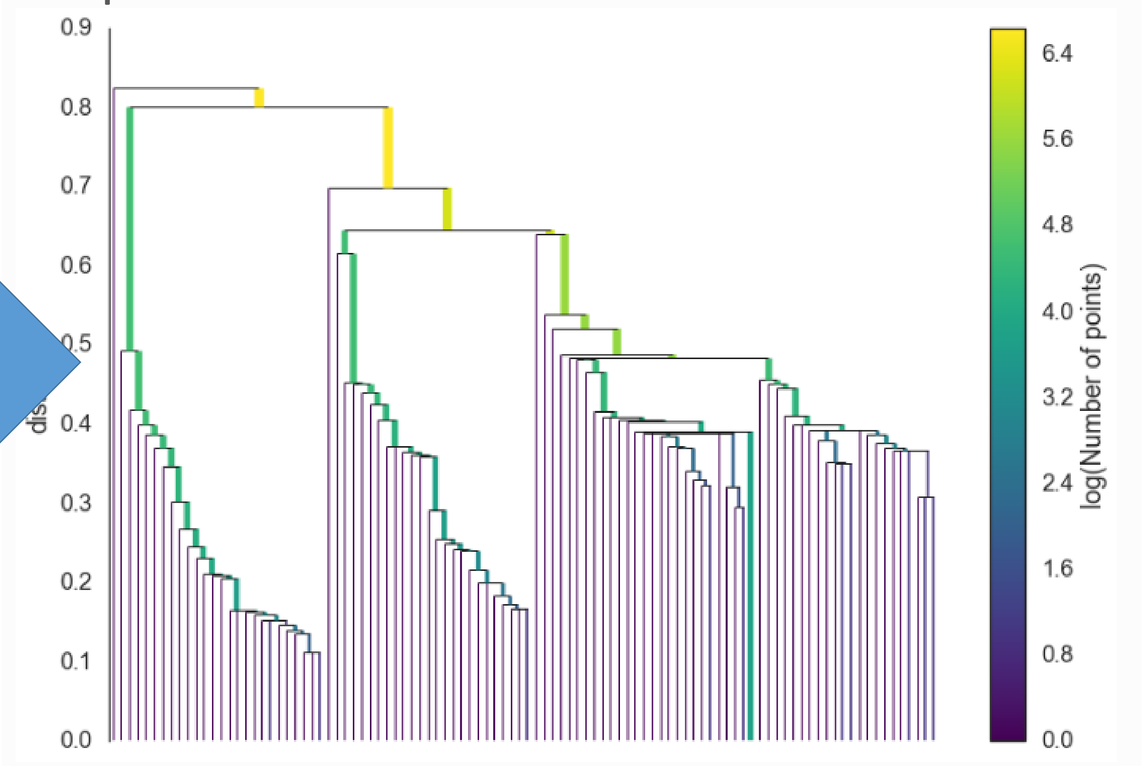
Strategy: Build neighborhood graph and identify strongly connected groups





Minimum spanning tree: Neighborhood graph with minimal total distances (=mutual reachability) between points

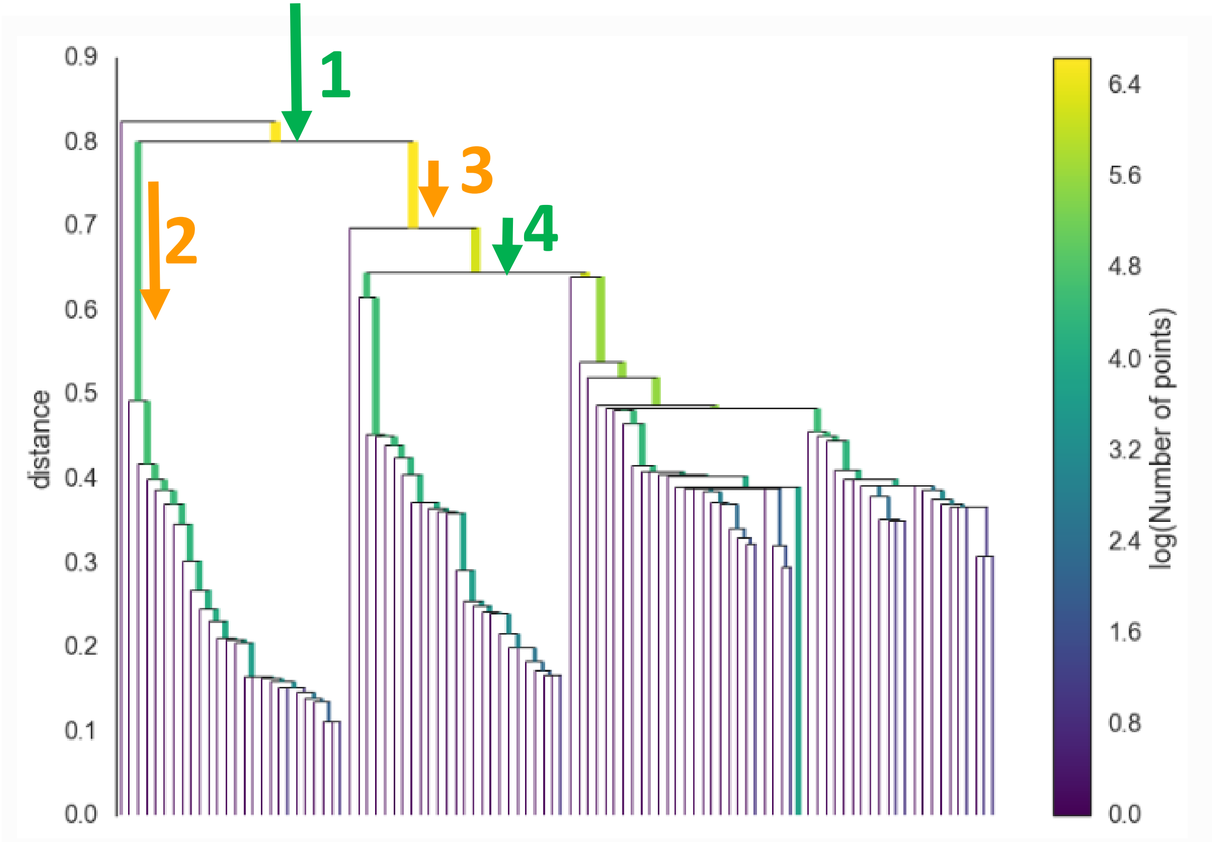
Sort edges by distances & Merge close points



Source: https://hdbscan.readthedocs.io/en/latest/how_hdbscan_works.html

HDBSCAN

Strategy: Build neighborhood graph and identify strongly connected groups



Source: https://hdbscan.readthedocs.io/en/latest/how_hdbscan_works.html

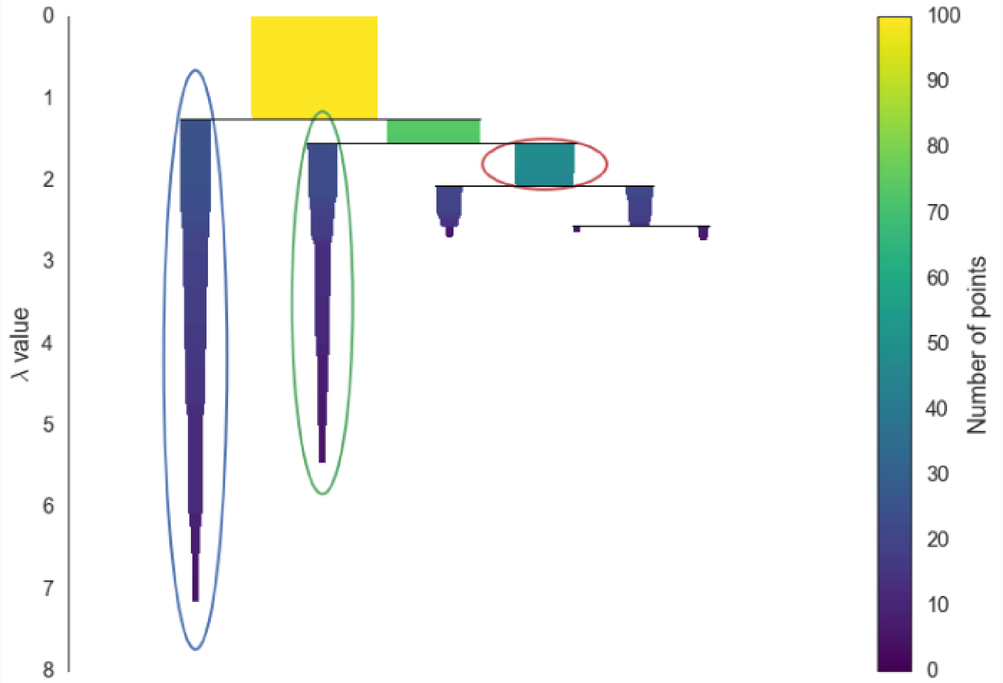
Condense the tree: Traverse graph from top to bottom and decide whether a new cluster is formed at every crossroads

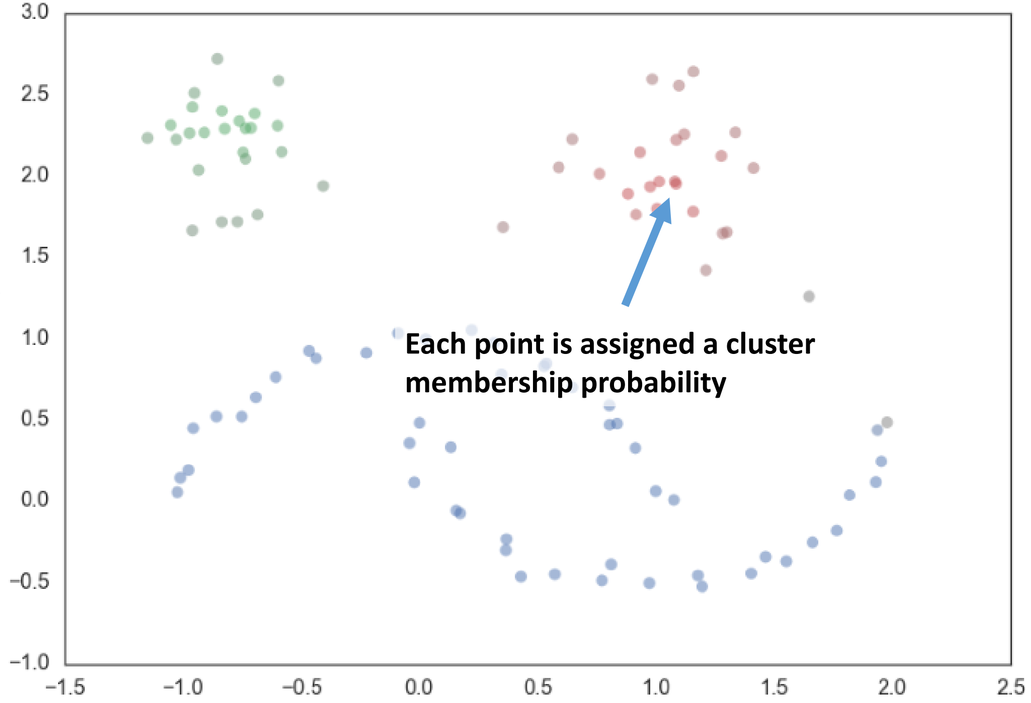
1. If points are split into clusters here – are both clusters larger than min_size? Yes
2. No – this part of the tree remains a single cluster
3. No – this part of the tree remains a single cluster
4. Yes – remaining points are split into new clusters here

HDBSCAN

Strategy: Build neighborhood graph and identify strongly connected groups

Extracting the clusters with ‘largest total ink area’ leads to the final selection of clusters





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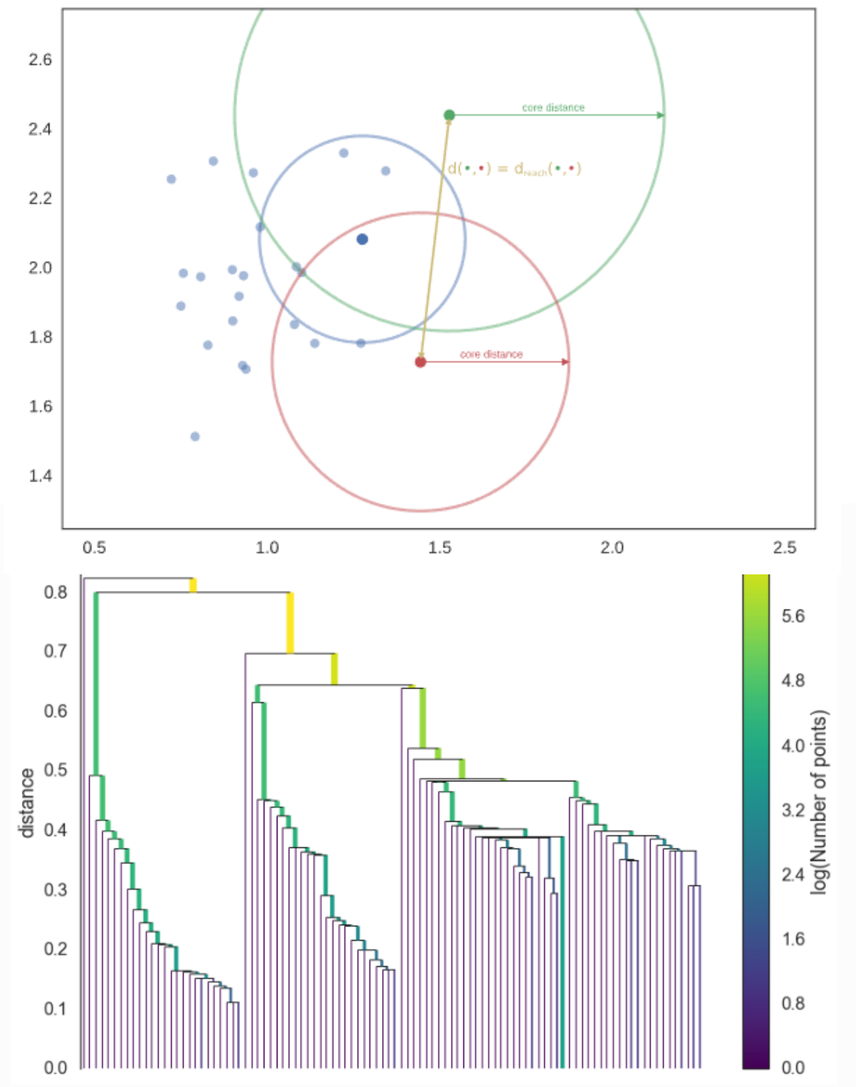
Variants of linkage-clustering



There are multiple ways to reconstruct the neighborhood graph and the clusters in the hierarchy schematic:

- Setting a maximum distance between two points to be considered neighbors → DBSCAN
  https://scikit-learn.org/stable/modules/generated/sklearn.cluster.DBSCAN.html

- Aggregate points into clusters bottom-up → Agglomerative clustering
  https://scikit-learn.org/stable/modules/generated/sklearn.cluster.AgglomerativeClustering.html

Exercise: Clustering in practice

… in combination with dimensionality reduction