

Feature extraction

Robert Haase

With material from

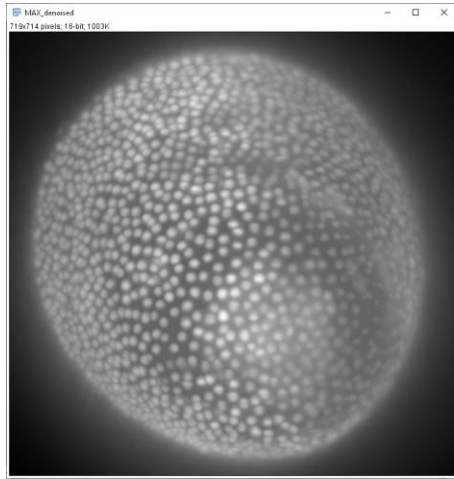
Johannes Müller, PoL TU Dresden

Marcelo Zoccoler, PoL, TU Dresden

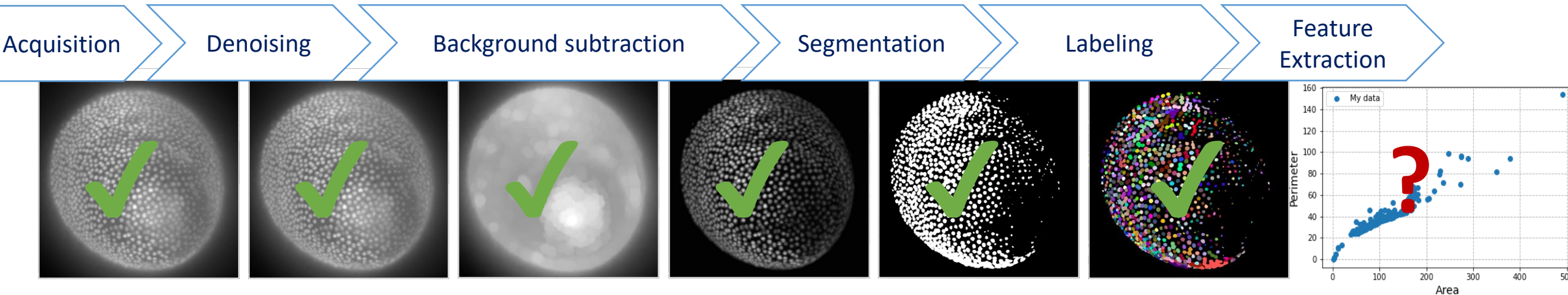
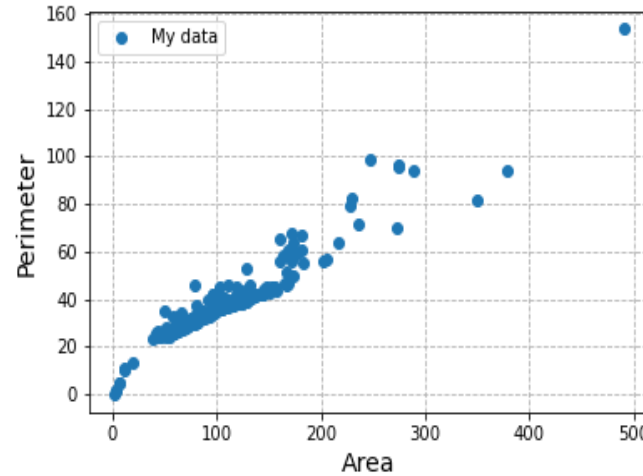
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- Feature extraction is a *late* processing step in image analysis.
- It can be used for images, or segmented/labelled images

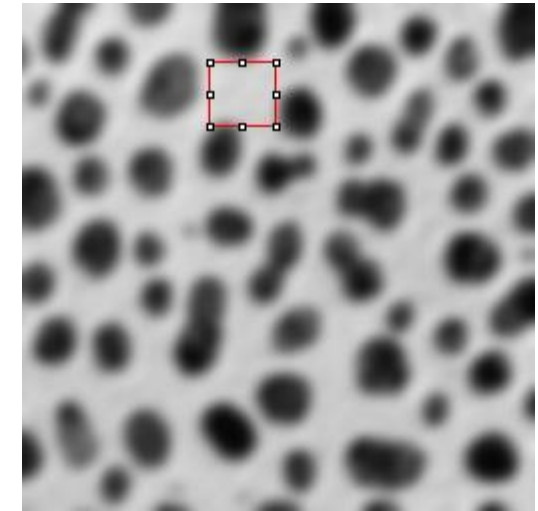
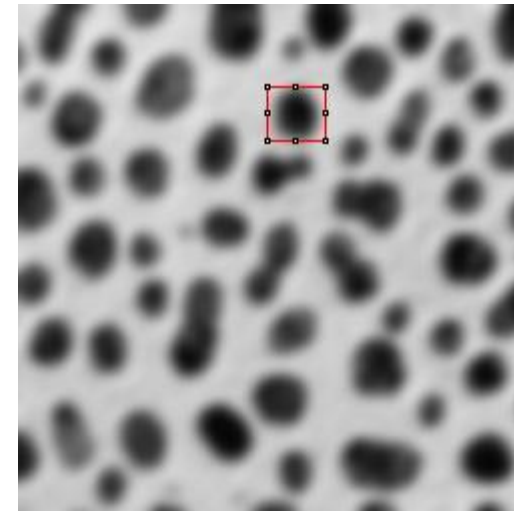
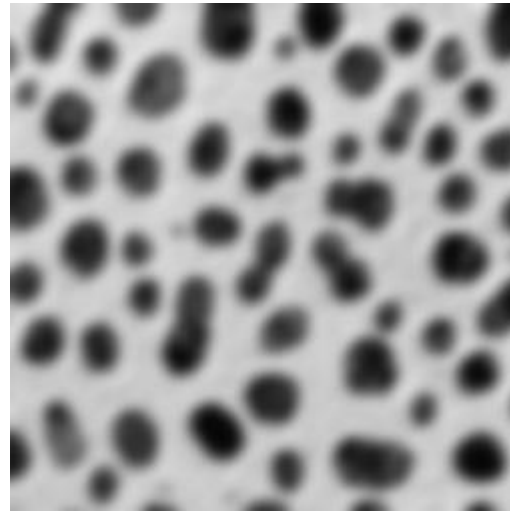


Feature
Extraction

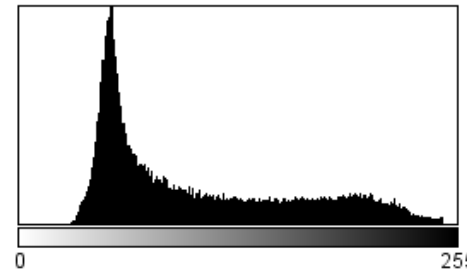


- A *feature* is a countable or measurable property of an image or object.
- Goal of feature extraction is finding a minimal set of features to describe an object well enough to differentiate it from other objects.
- **Intensity based**
 - Mean intensity
 - Standard deviation
 - Total intensity
 - Textures
- **Shape based /spatial**
 - Area / Volume
 - Roundness
 - Solidity
 - Circularity / Sphericity
 - Elongation
 - Centroid
 - Bounding box
- **Spatio-temporal**
 - Displacement,
 - Speed,
 - Acceleration
- **Others**
 - Overlap
 - Colocalization
 - Neighborhood
- **Mixed features**
 - Center of mass
 - Local minima / maxima

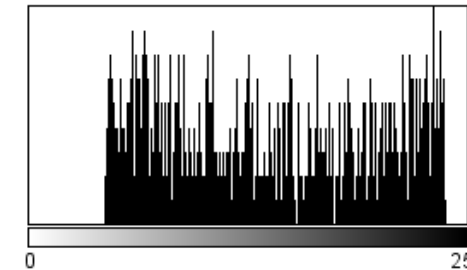
- Min / max
- Median
- Mean
- Mode
- Variance
- Standard deviation



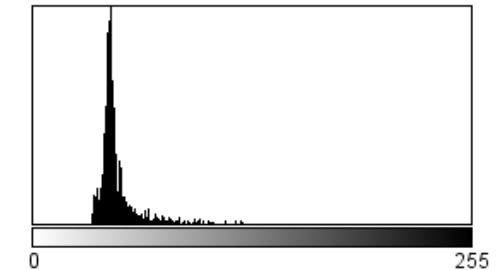
- Can be derived from pixel values
- Don't take spatial relationship of pixels into account
- See also:
 - descriptive statistics
 - histogram



Count: 65024
Mean: 103.301
StdDev: 57.991
Min: 29
Max: 248
Mode: 53 (1663)



Count: 783
Mean: 141.308
StdDev: 61.876
Min: 44
Max: 243
Mode: 236 (9)



Count: 1056
Mean: 49.016
StdDev: 12.685
Min: 34
Max: 122
Mode: 45 (120)

- Relative position in an image weighted by pixel intensities

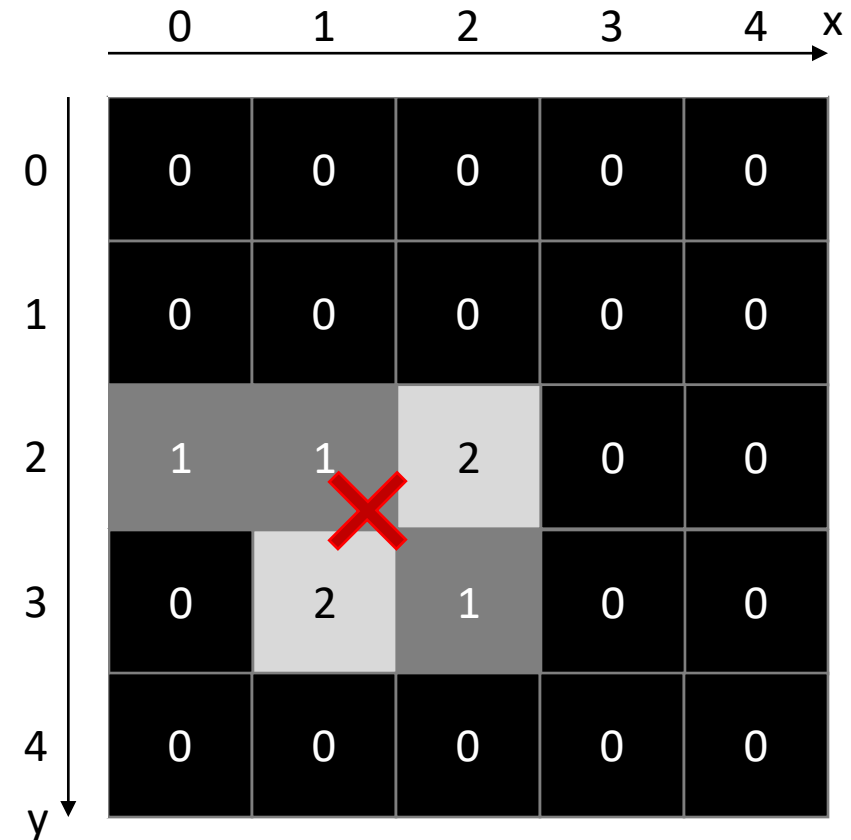
- x, y ... pixel coordinates
- w ... image width
- h ... image height
- μ ... mean intensity
- $g_{x,y}$... pixel grey value
- x_m, y_m ... center of mass coordinates

$$\mu = \frac{1}{wh} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} g_{x,y}$$

$$x_m = \frac{1}{wh\mu} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} x g_{x,y}$$

$$y_m = \frac{1}{wh\mu} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} y g_{x,y}$$

“sum intensity”
“total intensity”



$$x_m = 1/7 (1 \cdot 0 + 1 \cdot 1 + 2 \cdot 2 + 2 \cdot 1 + 1 \cdot 2) = 1.3$$

$$y_m = 1/7 (1 \cdot 2 + 1 \cdot 2 + 2 \cdot 3 + 2 \cdot 2 + 1 \cdot 3) = 2.4$$

- Relative position in an image weighted by pixel intensities
- Special case of center of mass for binary images
 - x, y ... pixel coordinates
 - w ... image width
 - h ... image height
 - μ ... mean intensity
 - $g_{x,y}$... pixel grey value, integer in range [0;1]
 - x_m, y_m ... center of mass coordinates

$$\mu = \frac{1}{wh} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} g_{x,y}$$

$$x_m = \frac{1}{wh\mu} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} x g_{x,y}$$

$$y_m = \frac{1}{wh\mu} \sum_{y=0}^{h-1} \sum_{x=0}^{w-1} y g_{x,y}$$

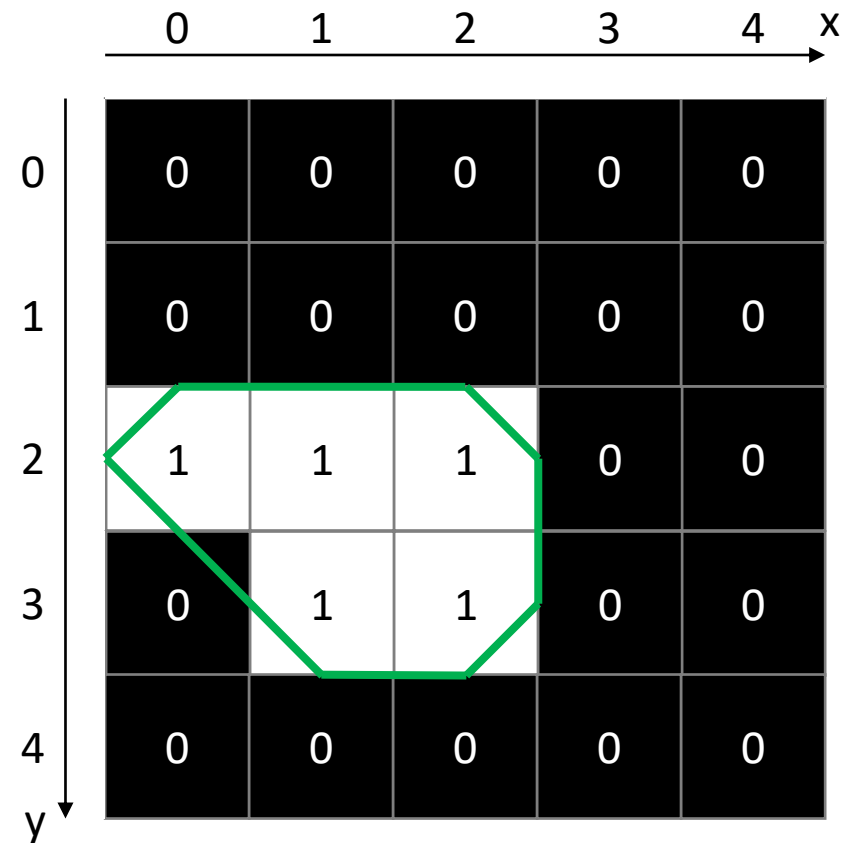
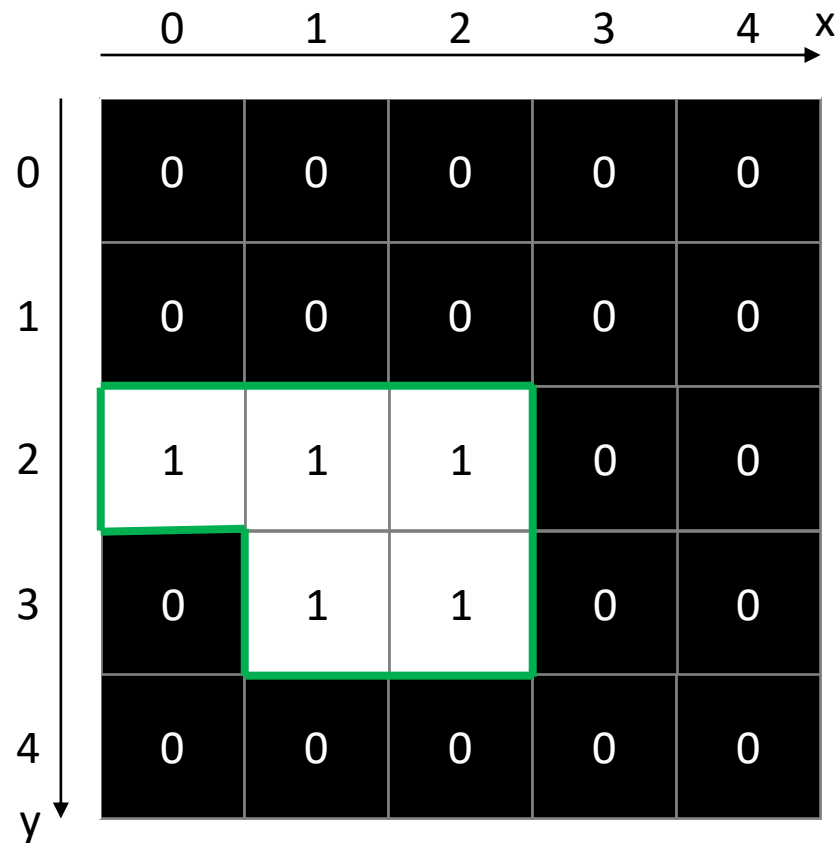
Number of white pixels

	0	1	2	3	4	x
0	0	0	0	0	0	
1	0	0	0	0	0	
2	1	1	1	0	0	
3	0	1	1	0	0	
4	0	0	0	0	0	
y						

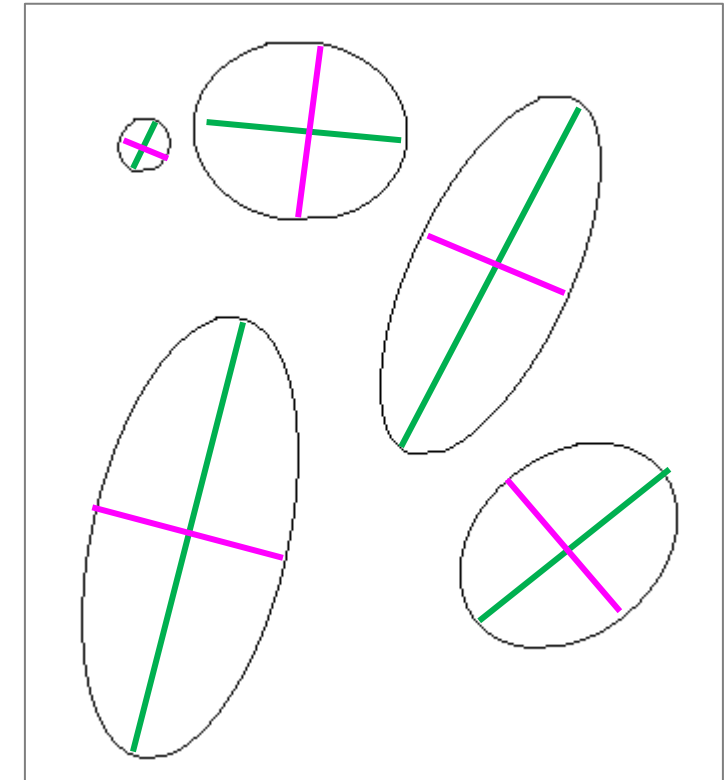
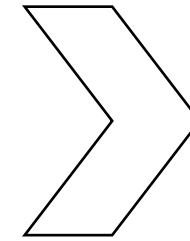
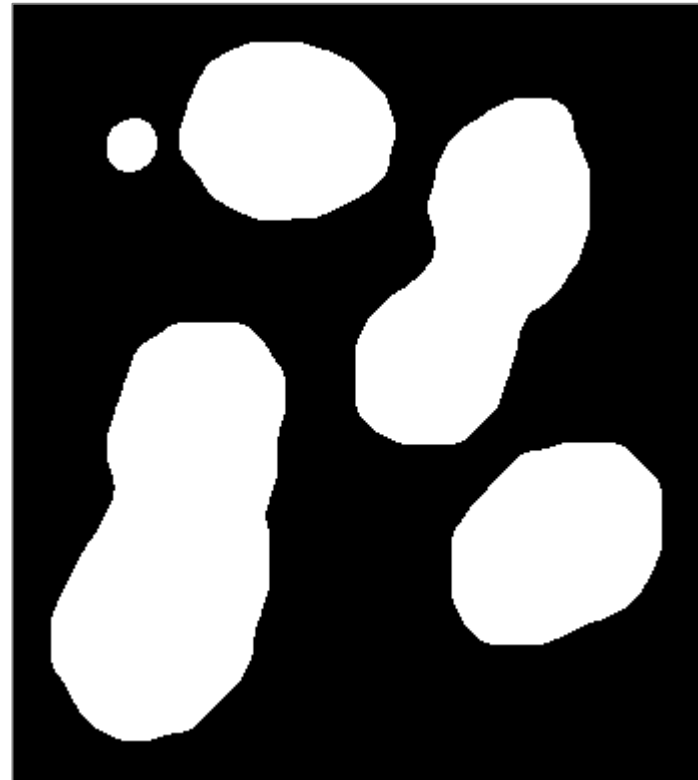
$$x_m = 1/5 (1 \cdot 0 + 1 \cdot 1 + 1 \cdot 2 + 1 \cdot 1 + 1 \cdot 2) = 1.2$$

$$y_m = 1/5 (1 \cdot 2 + 1 \cdot 2 + 1 \cdot 3 + 1 \cdot 2 + 1 \cdot 3) = 2.4$$

- Length of the outline around an object
- Depends on the actual implementation

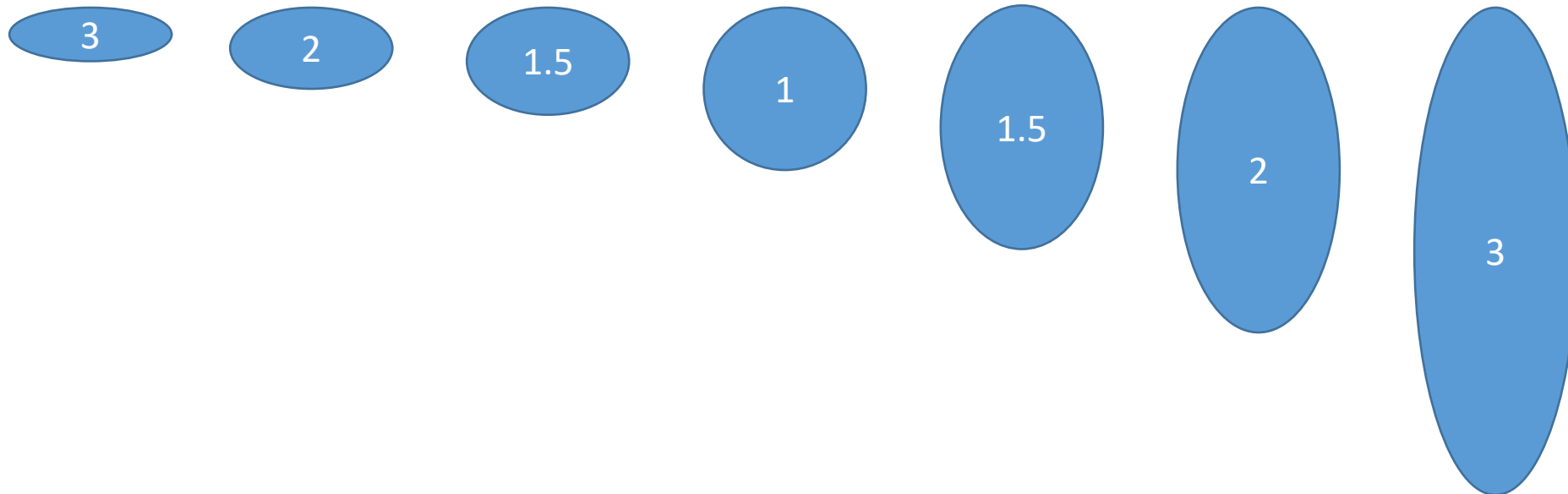


- For every object, find the optimal ellipse simplifying the object.
- Major axis ... long diameter
- Minor axis ... short diameter
- Major and minor axis are perpendicular to each other

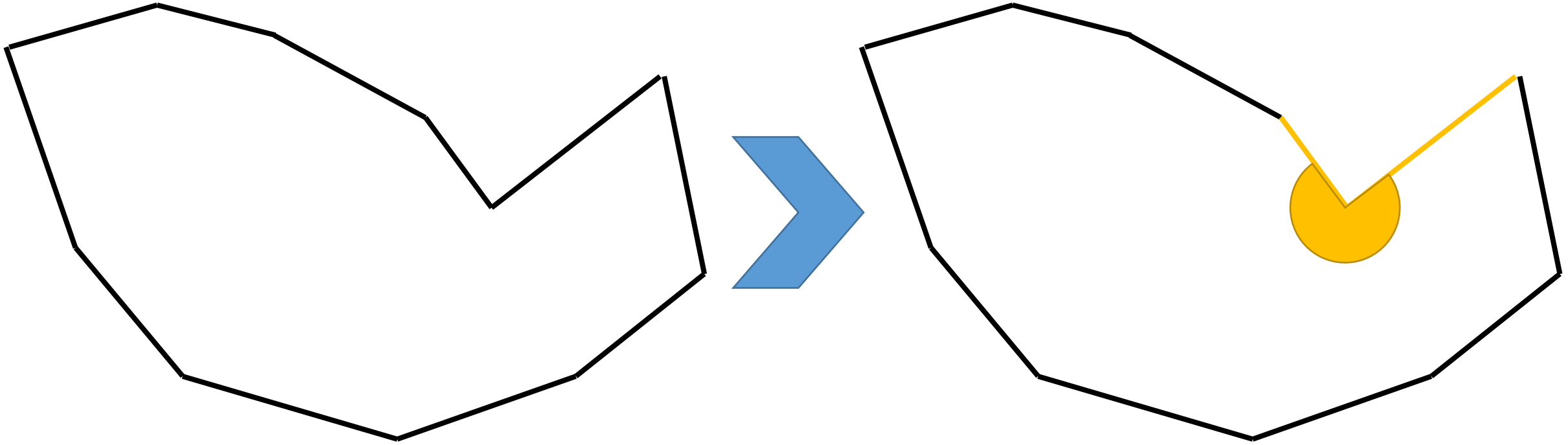


- The aspect ratio describes the elongation of an object.

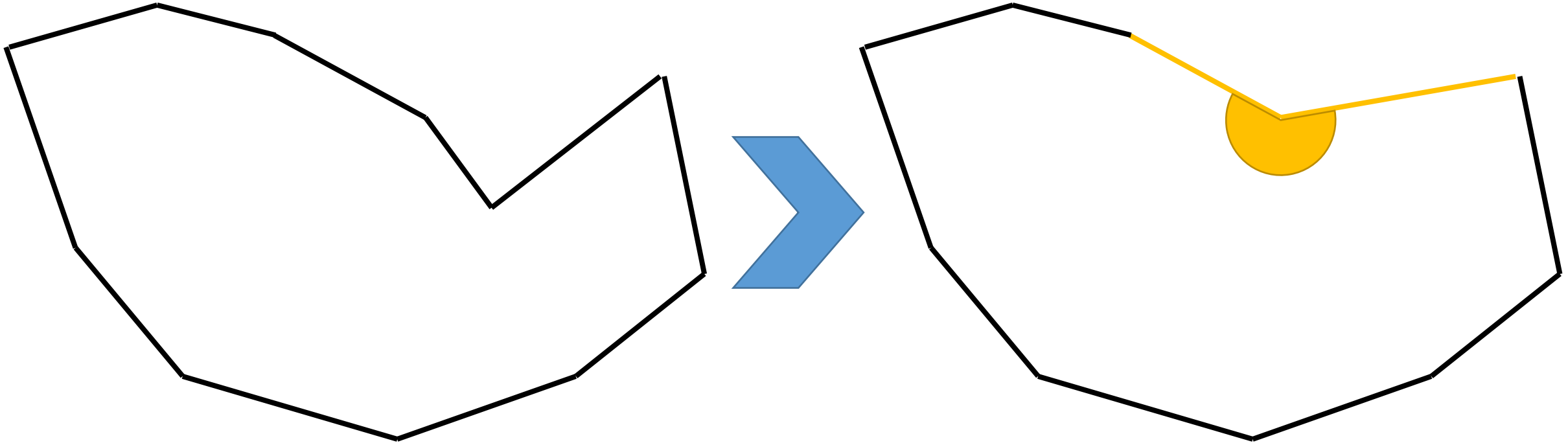
$$AR = \text{major} / \text{minor}$$



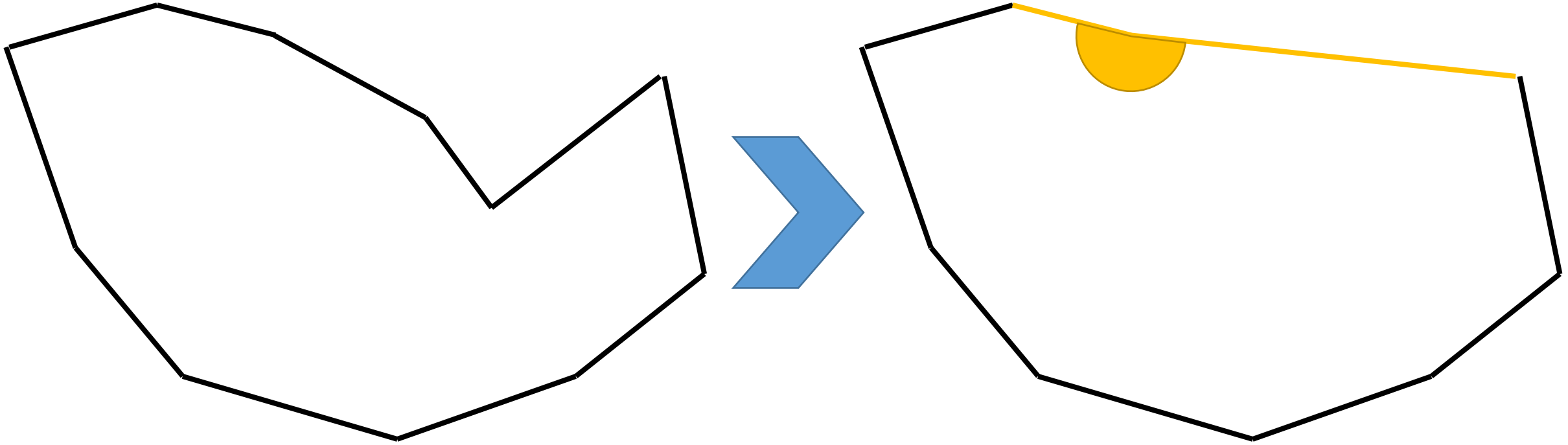
- By removing all concave corners of an object, we retrieve its **convex hull**.



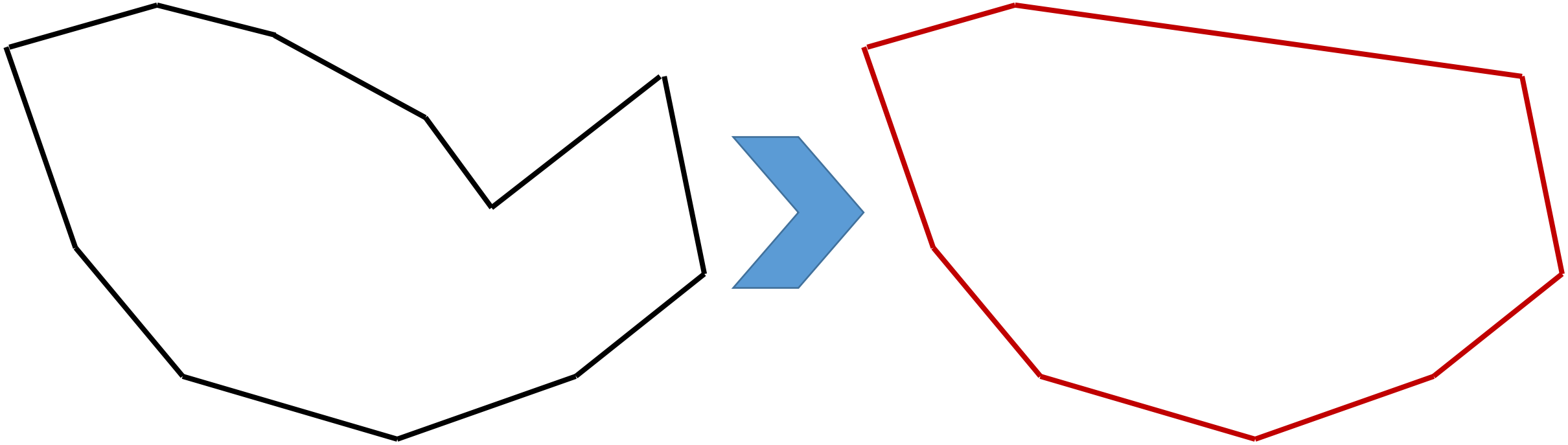
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$$solidity = \frac{A}{A_{convexHull}}$$

Roundness and circularity

- The definition of a circle leads us to measurements of circularity and roundness.
- In case you use these measures, define them correctly. They are not standardized!

Diameter

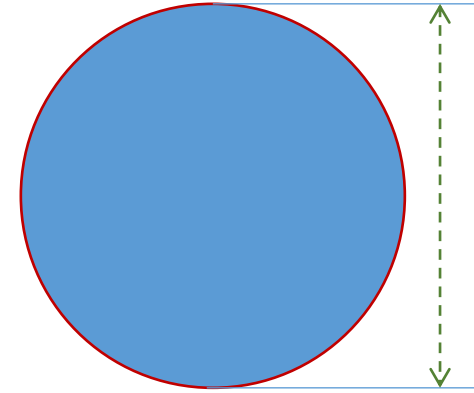
d

Circumference

$$C = \pi d$$

Area

$$A = \frac{\pi d^2}{4}$$



$$roundness = \frac{4 * A}{\pi major^2}$$

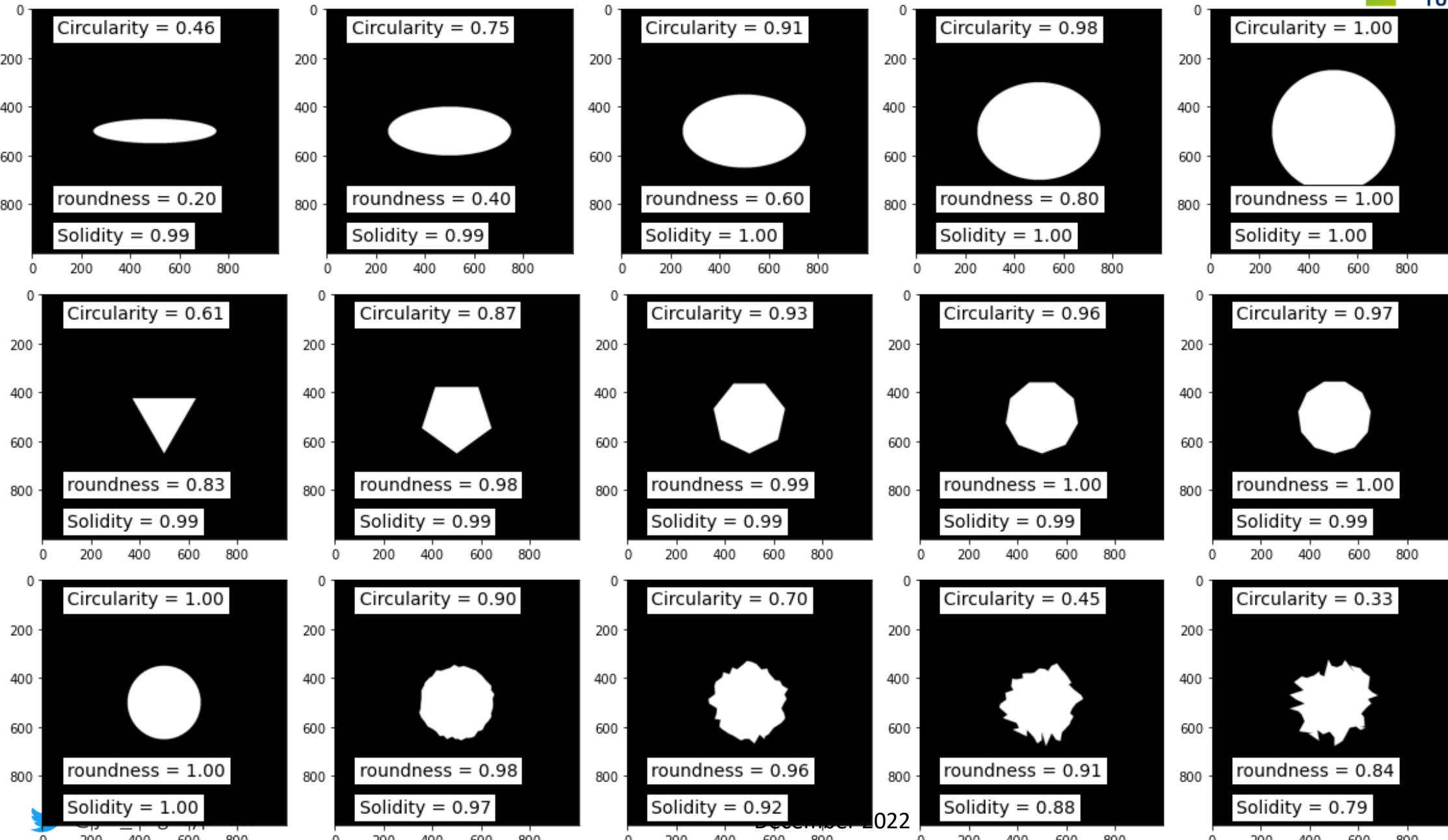
$$circularity = \frac{4\pi * A}{perimeter^2}$$

Roundness = 1
Circularity = 1

Roundness \approx 1
Circularity \approx 1

Roundness < 1
Circularity < 1

Roundness and circularity



$$\text{roundness} = \frac{4 * A}{\pi \text{major}^2}$$

$$\text{circularity} = \frac{4\pi * A}{\text{perimeter}^2}$$

$$\text{solidity} = \frac{A}{A_{\text{convexHull}}}$$

- In Python: `from skimage import measure`

<https://scikit-image.org/docs/stable/api/skimimage.measure.html>

`skimage.measure.blur_effect` (image[, h_size, ...]) Compute a metric that indicates the strength of blur in an image (0 for no blur, 1 for maximal blur).

`skimage.measure.euler_number` (image[, ...]) Calculate the Euler characteristic in binary image.

`skimage.measure.find_contours` (image[, ...]) Find iso-valued contours in a 2D array for a given level value.

`skimage.measure.grid_points_in_poly` (shape, verts) Test whether points on a specified grid are inside a polygon.

`skimage.measure.inertia_tensor` (image[, mu]) Compute the inertia tensor of the input image.

`skimage.measure.inertia_tensor_eigvals` (image) Compute the eigenvalues of the inertia tensor of the image.

`skimage.measure.label` (label_image[, ...]) Label connected regions of an integer array.

`skimage.measure.regionprops` (label_image[, ...]) Measure properties of labeled image regions.

`skimage.measure.regionprops_table` (label_image) Compute image properties and return them as a pandas-compatible table.

area : int

Number of pixels of the region.

area_bbox : int

Number of pixels of bounding box.

area_convex : int

Number of pixels of convex hull image, which is the smallest convex polygon that e

area_filled : int

Number of pixels of the region will all the holes filled in. Describes the area of the i

axis_major_length : float

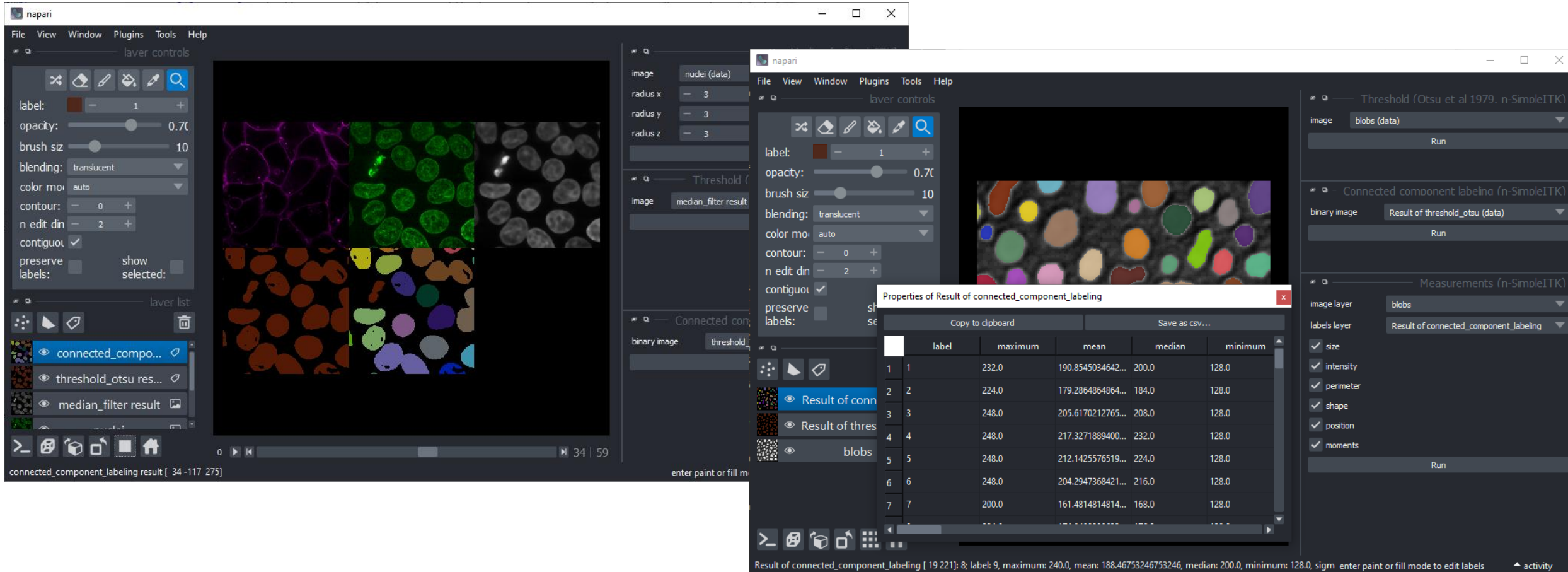
The length of the major axis of the ellipse that has the same normalized second ce
the region.

axis_minor_length : float

The length of the minor axis of the ellipse that has the same normalized second ce
the region.

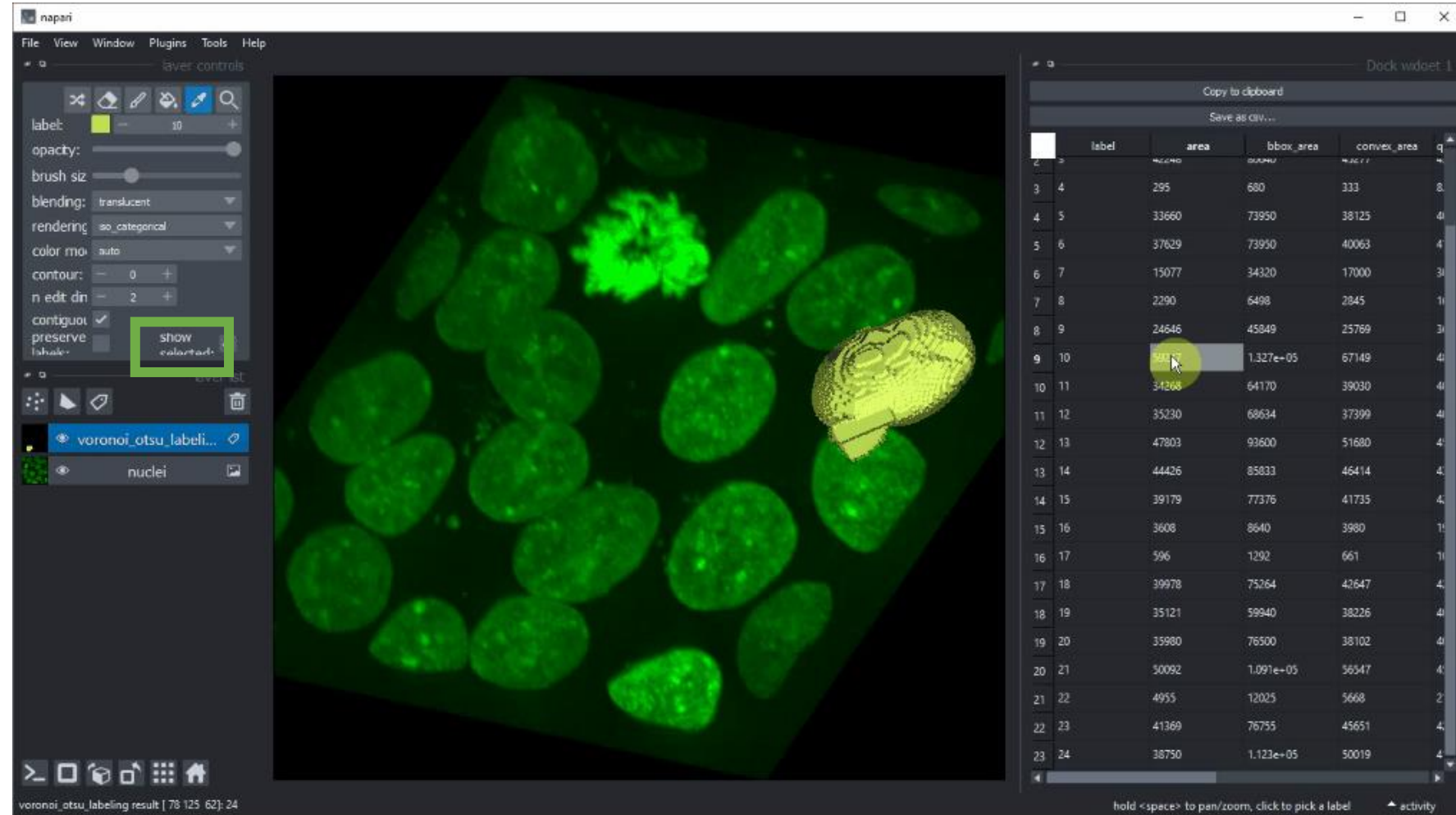
SimpleITK

- Recommended for 3D-measurements, based on the SimpleITK-project



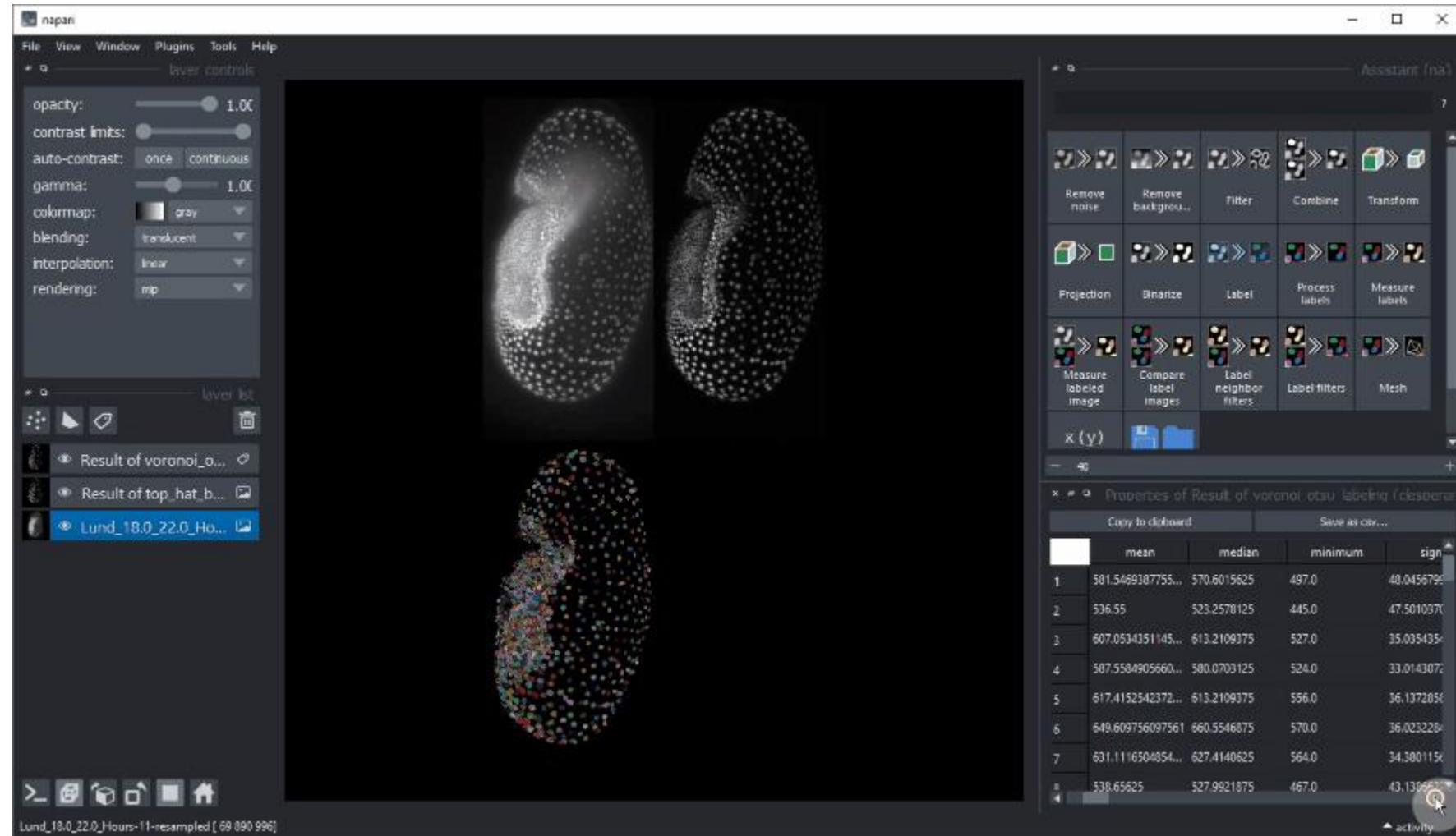
Exploring features in Napari

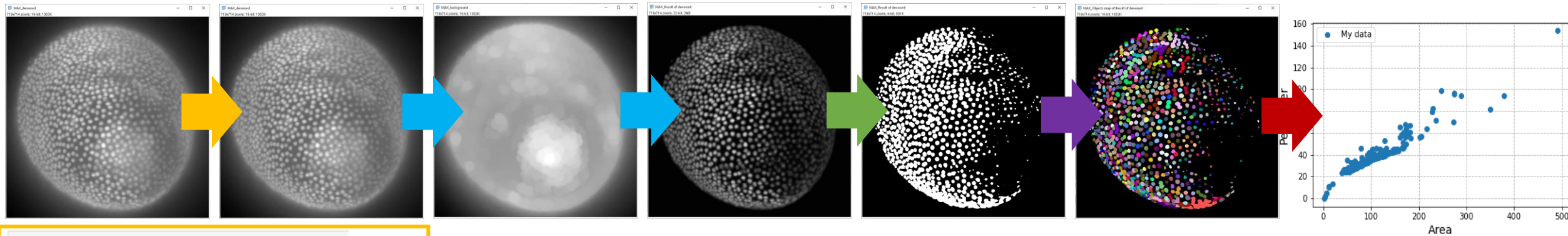
- Select table rows and view corresponding object in 2D/3D space



Exploring features in Napari

- Double-click on table column to retrieve a parametric map image





```
filtered = filters.median(image)  
  
filtered = filters.gaussian(image, sigma=5)
```

Filtering the image reduces pixel noise

```
bg_subtracted = morphology.white_tophat(image, footprint=footprint)
```

Top-hat filtering removes the background

Thresholding binarizes the image

```
threshold = filters.threshold_otsu(image)
```

Connected-components analysis groups pixels to objects

```
labels = measure.label(binary)
```

Feature extraction allows descriptive statistics

```
measurements = measure.regionprops_table(labels, properties=properties)
```