

①- Determina la adjunta y la inversa

$$\textcircled{1} \begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \rightarrow \begin{vmatrix} 3 & 0 \\ 0 & 1 \end{vmatrix} \quad |A| = 3 - 0 = 3 \quad |A| = 3$$

$$\begin{bmatrix} 3 & 0 \\ 0 & 1 \end{bmatrix} \quad C = \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix} \quad \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 1 \quad C_{1,2} = 0 \quad C_{2,1} = 0 \quad C_{2,2} = 3$$

$$C^T = \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix}$$

$$A^{-1} = \frac{1}{3} \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix}$$

$$\textcircled{1} \quad A^{-1} = \begin{bmatrix} \frac{1}{3} & 0 \\ 0 & 1 \end{bmatrix} \quad C^T = \begin{bmatrix} 1 & 0 \\ 0 & 3 \end{bmatrix}$$

$$(2) \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 2 \\ 0 & 1 \end{vmatrix} = |A| = 1 - 0 \quad |A| = 1$$

$$\begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -2 & 1 \end{bmatrix} \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{11} = 1 \quad C_{12} = 0 \quad C_{21} = -2 \quad C_{22} = 1$$

$$C^T = \begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix}$$

(2)

$$A^{-1} = \begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix} \quad C^T = \begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix}$$

$$\textcircled{3} \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad |A| = 0 - 1 = -1 \quad |A| = -1$$

$$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix} \quad \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 0 \quad C_{1,2} = -1 \quad C_{2,1} = -1 \quad C_{2,2} =$$

$$C_T = \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$$

$$A^{-1} = -1 \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix} \quad C^T = \begin{bmatrix} 0 & -1 \\ -1 & 0 \end{bmatrix}$$

$$(4) \begin{bmatrix} 1 & 0 \\ -\frac{1}{2} & 1 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 0 \\ -\frac{1}{2} & 1 \end{vmatrix} = 1 - 0 \quad |A| = 1$$

$$\begin{bmatrix} 1 & 0 \\ -\frac{1}{2} & 1 \end{bmatrix} \quad \begin{bmatrix} 1 & \frac{1}{2} \\ 0 & 1 \end{bmatrix} \quad \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 1 \quad C_{1,2} = \frac{1}{2} \quad C_{2,1} = 0 \quad C_{2,2} = 1$$

$$C_T = \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & 1 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & 1 \end{bmatrix} \quad C_T = \begin{bmatrix} 1 & 0 \\ \frac{1}{2} & 1 \end{bmatrix}$$

$$(5) \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{vmatrix}$$

~~$$\begin{vmatrix} 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & -2 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 \end{vmatrix}$$~~

$$|A| = 1 - (0) \quad |A| = 1$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 2 & 1 \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{f,1,1} = 1 \quad C_{f,1,2} = 0 \quad C_{f,1,3} = 0 \quad C_{2,1} = 0 \quad C_{2,2} = 1$$

$$C_{2,3} = 0 \quad C_{f,3,1} = 0 \quad C_{3,2} = +2 \quad C_{3,3} =$$

$$C^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

(5)

$$A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$C^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix}$$

$$(6) \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

~~$$\begin{bmatrix} 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 & 0 \end{bmatrix}$$~~

$$|A| = -1$$

$$\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = 0 \quad C_{1,2} = 0 \quad C_{1,3} = -1 \quad C_{2,1} = 0 \quad C_{2,2} = -1$$

$$C_{2,3} = 0 \quad C_{3,1} = -1 \quad C_{3,2} = 0 \quad C_{3,3} =$$

$$C^T = \begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$$

(6)

$$A^{-1} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$C^T = \begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix}$$

$$(7) \begin{bmatrix} 1 & 0 & 0 \\ 0 & c & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & c & 0 \\ 0 & 0 & 1 \end{vmatrix}$$

~~$$\begin{vmatrix} 1 & 0 & 0 & 1 & 0 \\ 0 & c & 0 & 0 & c \\ 0 & 0 & 1 & 0 & 0 \end{vmatrix}$$~~

$$|A| = c$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & c & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} c & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & c \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = c \quad C_{1,2} = 0 \quad C_{1,3} = 0 \quad C_{2,1} = 0 \quad C_{2,2} = 1$$

$$C_{2,3} = 0 \quad C_{3,1} = 0 \quad C_{3,2} = 0 \quad C_{3,3} = c$$

$$C^T = \begin{bmatrix} c & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & c \end{bmatrix}$$

(7)

$$A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \frac{1}{c} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$C^T = \begin{bmatrix} c & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & c \end{bmatrix}$$

$$(8) \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & c \\ 0 & 0 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & c \\ 0 & 0 & 1 \end{vmatrix}$$

~~$$\begin{vmatrix} 1 & 0 & 0 & 1 & 0 \\ 0 & 1 & c & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 \end{vmatrix}$$~~

$$|A| = 1$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & c \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & -c & 1 \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = 1 \quad C_{1,2} = 0 \quad C_{1,3} = 0 \quad C_{2,1} = 0 \quad C_{2,2} = 1$$

$$C_{2,3} = 0 \quad C_{3,1} = 0 \quad C_{3,2} = -c$$

$$C^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -c \\ 0 & 0 & 1 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -c \\ 0 & 0 & 1 \end{bmatrix}$$

$$C^T = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & -c \\ 0 & 0 & 1 \end{bmatrix}$$

$$(9) \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 2 \\ 3 & 4 \end{vmatrix} = 4 - 6 = -2 \quad |A| = -2$$

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \quad \begin{bmatrix} 4 & -3 \\ -2 & 1 \end{bmatrix} \quad \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 4 \quad C_{1,2} = -3 \quad C_{2,1} = -2 \quad C_{2,2} = 1$$

$$C^T = \begin{bmatrix} 4 & -2 \\ -3 & 1 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \frac{4}{-2} & \frac{-2}{-2} \\ \frac{-3}{-2} & \frac{1}{-2} \end{bmatrix} = \begin{bmatrix} -2 & 1 \\ \frac{3}{2} & -\frac{1}{2} \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} -2 & 1 \\ \frac{3}{2} & -\frac{1}{2} \end{bmatrix} \quad C^T = \begin{bmatrix} 4 & -2 \\ -3 & 1 \end{bmatrix}$$

$$(10) \begin{bmatrix} -2 & 4 \\ 3 & -1 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} -2 & 4 \\ 3 & -1 \end{vmatrix} \quad |A| = 2 - 12 \quad |A| = -10$$

$$\begin{bmatrix} -2 & 4 \\ 3 & -1 \end{bmatrix} \quad \begin{bmatrix} -1 & -3 \\ -4 & -2 \end{bmatrix} \quad \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = -1 \quad C_{1,2} = -3 \quad C_{2,1} = -4 \quad C_{2,2} = -2$$

$$C^T = \begin{bmatrix} -1 & -4 \\ -3 & -2 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \frac{-1}{-10} & \frac{-4}{-10} \\ \frac{-3}{-10} & \frac{-2}{-10} \end{bmatrix} = \begin{bmatrix} \frac{1}{10} & \frac{2}{5} \\ \frac{3}{10} & \frac{1}{5} \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \frac{1}{10} & \frac{2}{5} \\ \frac{3}{10} & \frac{1}{5} \end{bmatrix} \quad C^T = \begin{bmatrix} -1 & -4 \\ -3 & -2 \end{bmatrix}$$

$$(11) \begin{bmatrix} 3 & -4 \\ -6 & 8 \end{bmatrix} \quad A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 3 & -4 \\ -6 & 8 \end{vmatrix} \quad |A| = 24 - 24 = 0 \quad \therefore \text{la inversa no existe}$$

$$\begin{bmatrix} 3 & -4 \\ -6 & 8 \end{bmatrix} \begin{bmatrix} 8 & 6 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 8 \quad C_{1,2} = 6 \quad C_{2,1} = 4 \quad C_{2,2} = 3$$

$$C^T = \begin{bmatrix} 8 & 4 \\ 6 & 3 \end{bmatrix} \quad A^{-1} = \text{No existe}$$

$$(12) \begin{bmatrix} 1 & a \\ -a & 1 \end{bmatrix} A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & a \\ -a & 1 \end{vmatrix} \quad |A| = 1 - (-a^2) \quad |A| = 1 + a^2$$

$$\begin{bmatrix} 1 & a \\ -a & 1 \end{bmatrix} \begin{bmatrix} 1 & a \\ -a & 1 \end{bmatrix} \begin{bmatrix} + & - \\ - & + \end{bmatrix}$$

$$C_{1,1} = 1 \quad C_{1,2} = a \quad C_{2,1} = -a \quad C_{2,2} = 1$$

$$C_T = \begin{bmatrix} 1 & -a \\ a & 1 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \frac{1}{1+a^2} & \frac{-a}{1+a^2} \\ \frac{a}{1+a^2} & \frac{1}{1+a^2} \end{bmatrix}$$

(12)

$$A^{-1} = \begin{bmatrix} \frac{1}{1+a^2} & \frac{-a}{1+a^2} \\ \frac{a}{1+a^2} & \frac{1}{1+a^2} \end{bmatrix} \quad C_T = \begin{bmatrix} 1 & -a \\ a & 1 \end{bmatrix}$$

(13)
$$\begin{bmatrix} 2 & 0 & -1 \\ 1 & 5 & 1 \\ 2 & 3 & 0 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 2 & 0 & -1 \\ 1 & 5 & 1 \\ 2 & 3 & 0 \end{vmatrix}$$

~~$$\begin{vmatrix} 2 & 0 & -1 \\ 1 & 5 & 1 \\ 2 & 3 & 0 \end{vmatrix}$$~~

$$|A| = -3 - (-10 + 6) \quad |A| = -3 - (-4)$$

$$|A| = -3 + 4 \quad |A| = 1$$

$$\begin{bmatrix} 2 & 0 & -1 \\ 1 & 5 & 1 \\ 2 & 3 & 0 \end{bmatrix} \quad \begin{bmatrix} -3 & 2 & -7 \\ -3 & 2 & -6 \\ 5 & -3 & 10 \end{bmatrix} \quad \begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = -3 \quad C_{1,2} = 2 \quad C_{1,3} = 3 - 10 = -7$$

$$C_{2,1} = -3 \quad C_{2,2} = 2 \quad C_{2,3} = -6 \quad C_{3,1} = 5 \quad C_{3,2} = -3$$

$$C_{3,3} = 10$$

$$C^T = \begin{bmatrix} -3 & -3 & 5 \\ 2 & 2 & -3 \\ -7 & -6 & 10 \end{bmatrix}$$

(13)

$$A^{-1} = \begin{bmatrix} -3 & -3 & 5 \\ 2 & 2 & -3 \\ -7 & -6 & 10 \end{bmatrix}$$

$$C^T = \begin{bmatrix} -3 & -3 & 5 \\ 2 & 2 & -3 \\ -7 & -6 & 10 \end{bmatrix}$$

(14) $\begin{bmatrix} 1 & -1 & 2 \\ 3 & 1 & 2 \\ 2 & 3 & -1 \end{bmatrix}$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & -1 & 2 \\ 3 & 1 & 2 \\ 2 & 3 & -1 \end{vmatrix}$$

~~$$\begin{vmatrix} 1 & -1 & 2 \\ 3 & 1 & 2 \\ 2 & 3 & -1 \end{vmatrix}$$~~

$$|A| = -1 - 4 + 18 - (4 + 6 + 3)$$

$$|A| = 13 - 13$$

$$|A| = 0$$

La inversa no existe

$$\begin{bmatrix} 1 & -1 & 2 \\ 3 & 1 & 2 \\ 2 & 3 & -1 \end{bmatrix} \begin{bmatrix} -7 & 7 & 7 \\ 5 & -5 & -5 \\ -4 & 4 & 4 \end{bmatrix} \begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{f1,1} = -1 - 6 = -7 \quad C_{f1,2} = (-3 - 4) = +7 \quad C_{f1,3} = 9 - 2 = 7$$

$$C_{f2,1} = 1 - 6 = -(-5) \quad C_{f2,2} = -1 - 4 = -5 \quad C_{f2,3} = 3 + 2 = -5$$

$$C_{f3,1} = -2 - 2 = -4 \quad C_{f3,2} = 2 - 6 = +4 \quad C_{f3,3} = 1 + 3 = 4$$

$$C^T = \begin{bmatrix} -7 & 5 & -4 \\ 7 & -5 & 4 \\ 7 & -5 & 4 \end{bmatrix}$$

(14)

$$A^{-1} = \text{No existe}$$

$$C^T = \begin{bmatrix} -7 & 5 & -4 \\ 7 & -5 & 4 \\ 7 & -5 & 4 \end{bmatrix}$$

(IS)

$$\begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{vmatrix}$$

~~$$\begin{vmatrix} 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 & 1 \end{vmatrix}$$~~

$$|A| = 1 - (1+1) \quad |A| = 1 - 2 \quad |A| = -1$$

$$\begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 1 \\ 0 & 1 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 0 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 0 \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1}=0 \quad C_{1,2}=1 \quad C_{1,3}=1 \quad C_{2,1}=-1 \quad C_{2,2}=1$$

$$C_{2,3}=-1 \quad C_{3,1}=1 \quad C_{3,2}=1 \quad C_{3,3}=0$$

$$C^T = \begin{bmatrix} 0 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 0 \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} 0 & \frac{-1}{-1} & \frac{1}{-1} \\ \frac{-1}{-1} & \frac{1}{-1} & \frac{-1}{-1} \\ \frac{1}{-1} & \frac{-1}{-1} & 0 \end{bmatrix}$$

(IS)

$$A^{-1} = \begin{bmatrix} 0 & 1 & -1 \\ 1 & -1 & 1 \\ -1 & 1 & 0 \end{bmatrix}$$

$$C^T = \begin{bmatrix} 0 & -1 & 1 \\ -1 & 1 & -1 \\ 1 & -1 & 0 \end{bmatrix}$$

(16)
$$\begin{bmatrix} a & 0 & 0 \\ 1 & a & 0 \\ 0 & 1 & a \end{bmatrix}$$

$$\begin{vmatrix} a & 0 & 0 \\ 1 & a & 0 \\ 0 & 1 & a \end{vmatrix}$$

$$|A| = a^3$$

$$\begin{bmatrix} a & 0 & 0 \\ 1 & a & 0 \\ 0 & 1 & a \end{bmatrix} \begin{bmatrix} a^2 & -a & 1 \\ 0 & a^2 & -a \\ 0 & 0 & a^2 \end{bmatrix} \begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = a^2 \quad C_{1,2} = -a \quad C_{1,3} = 1 \quad C_{2,1} = 0 \quad C_{2,2} = a^2$$

$$C_{2,3} = a \quad C_{3,1} = 0 \quad C_{3,2} = 0 \quad C_{3,3} = a^2$$

$$C^T = \begin{bmatrix} a^2 & 0 & 0 \\ -a & a^2 & 0 \\ 1 & -a & a^2 \end{bmatrix} \quad A^{-1} = \begin{bmatrix} \frac{a^2}{a^3} & 0 & 0 \\ -\frac{a}{a^3} & \frac{a^2}{a^3} & 0 \\ \frac{1}{a^3} & -\frac{a}{a^3} & \frac{a^2}{a^3} \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} \frac{1}{a} & 0 & 0 \\ -\frac{1}{a^2} & \frac{1}{a} & 0 \\ \frac{1}{a^3} & -\frac{1}{a^2} & \frac{1}{a} \end{bmatrix} \quad C^T = \begin{bmatrix} a^2 & 0 & 0 \\ -a & a^2 & 0 \\ 1 & -a & a^2 \end{bmatrix}$$

(16)

$$(17) \begin{bmatrix} 0 & a & 0 \\ b & 0 & c \\ 0 & d & 0 \end{bmatrix}$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\begin{vmatrix} 0 & a & 0 \\ b & 0 & c \\ 0 & d & 0 \end{vmatrix}$$

~~$$\begin{vmatrix} 0 & a & 0 \\ b & 0 & c \\ 0 & d & 0 \end{vmatrix}$$~~

$$|A| = 0$$

No existe la inversa

$$\begin{bmatrix} 0 & a & 0 \\ b & 0 & c \\ 0 & d & 0 \end{bmatrix}$$

$$\begin{bmatrix} -cd & 0 & bd \\ 0 & 0 & 0 \\ ac & 0 & -ab \end{bmatrix}$$

$$\begin{bmatrix} + & - & + \\ - & + & - \\ + & - & + \end{bmatrix}$$

$$C_{1,1} = -cd \quad C_{1,2} = 0 \quad C_{1,3} = bd \quad C_{2,1} = 0 \quad C_{2,2} = 0$$

$$C_{2,3} = 0 \quad C_{3,1} = ac \quad C_{3,2} = 0 \quad C_{3,3} = -ab$$

$$C^T = \begin{bmatrix} -cd & 0 & ac \\ 0 & 0 & 0 \\ bd & 0 & -ab \end{bmatrix}$$

(17)

$A^{-1} = \text{No existe}$

$$C^T = \begin{bmatrix} -cd & 0 & ac \\ 0 & 0 & 0 \\ bd & 0 & -ab \end{bmatrix}$$

$$(18) \begin{bmatrix} 0 & -1 & 1 & 0 \\ 2 & 1 & 0 & 2 \\ 1 & -1 & 3 & 0 \\ 0 & 1 & 1 & -1 \end{bmatrix} e_1 +$$

$$A^{-1} = \frac{C^T}{|A|}$$

$$\left| \begin{array}{cccc|l} 0 & -1 & 1 & 0 & e_1 + e_3 \Rightarrow e_1 \\ 2 & 1 & 0 & 2 & \\ 1 & -1 & 3 & 0 & \\ 0 & 1 & 1 & -1 & \end{array} \right| \xrightarrow{\quad} \left| \begin{array}{cccc|l} 1 & -2 & 4 & 0 & e_2 - 2e_1 \Rightarrow e_2 \\ 2 & 1 & 0 & 2 & \\ 1 & -1 & 3 & 0 & e_3 - e_1 \Rightarrow e_3 \\ 0 & 1 & 1 & -1 & \end{array} \right|$$

$$\left| \begin{array}{cccc} 1 & -2 & 4 & 0 \\ 0 & 5 & -8 & 2 \\ 0 & 1 & -1 & 0 \\ 0 & 1 & 1 & -1 \end{array} \right|$$

$$\left| \begin{array}{ccc} 5 & -8 & 2 \\ 1 & -1 & 0 \\ 1 & 1 & -1 \end{array} \right|$$

$$\begin{array}{cccccc} 5 & -8 & 2 & 5 & -8 \\ 1 & -1 & 0 & 1 & -1 \\ 1 & 1 & -1 & 1 & 1 \end{array}$$

$$|A| = 1(5 + 2 - (-2 + 8))$$

$$|A| = 7 - 6$$

$$|A| = 1$$

$$\begin{bmatrix} 0 & -1 & 1 & 0 \\ 2 & 1 & 0 & 2 \\ 1 & -1 & 3 & 0 \\ 0 & 1 & 1 & -1 \end{bmatrix} \begin{bmatrix} -11 & +4 & 5 & 9 \\ -2 & 1 & 1 & 2 \\ 5 & -2 & -2 & -4 \\ -4 & 2 & 2 & 3 \end{bmatrix}$$

$$\begin{bmatrix} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{bmatrix}$$

$$C_{1,1} = \begin{bmatrix} 1 & 0 & 2 \\ -1 & 3 & 0 \\ 1 & 1 & -1 \end{bmatrix} \begin{array}{cccccc} 1 & 0 & 2 & 1 & 0 \\ -1 & 3 & 0 & -1 & 3 \\ 1 & 1 & -1 & 1 & 1 \end{array}$$

$$C_{1,1} = -3 - 2 - (6) = -3 - 2 - 6 = -11$$

$$C_{1,2} = \begin{bmatrix} 2 & 0 & 2 \\ 1 & 3 & 0 \\ 0 & 1 & -1 \end{bmatrix} \begin{array}{cccccc} 2 & 0 & 2 & 2 & 0 \\ 1 & 3 & 0 & 1 & 3 \\ 0 & 1 & -1 & 0 & 1 \end{array}$$

$$C_{1,2} = -6 + 2 - (0) = -6 + 2 = -4$$

$$C_{4,3} = \begin{bmatrix} 0 & -1 & 0 \\ 2 & 1 & 2 \\ 1 & -1 & 0 \end{bmatrix}$$

~~$$\begin{bmatrix} 0 & -1 & 0 & 0 & -1 \\ 2 & 1 & 2 & 2 & 1 \\ 1 & -1 & 0 & 1 & -1 \end{bmatrix}$$~~

$$C_{4,3} = -2$$

$$C_{4,4} = \begin{bmatrix} 0 & -1 & 1 \\ 2 & 1 & 0 \\ 1 & -1 & 3 \end{bmatrix}$$

~~$$\begin{bmatrix} 0 & -1 & 1 & 0 & -1 \\ 2 & 1 & 0 & 2 & 1 \\ 1 & -1 & 3 & 1 & -1 \end{bmatrix}$$~~

$$C_{4,4} = -2 - (1 - 6) = -2 - (-5) = -2 + 5 = 3$$

$$C^T = \begin{bmatrix} -11 & -2 & 5 & -4 \\ 4 & 1 & -2 & 2 \\ 5 & 1 & -2 & 2 \\ 9 & 2 & -4 & 3 \end{bmatrix}$$

(18)

$$A^{-1} = \begin{bmatrix} -11 & -2 & 5 & -4 \\ 4 & 1 & -2 & 2 \\ 5 & 1 & -2 & 2 \\ 9 & 2 & -4 & 3 \end{bmatrix}$$

$$C^T = \begin{bmatrix} -11 & -2 & 5 & -4 \\ 4 & 1 & -2 & 2 \\ 5 & 1 & -2 & 2 \\ 9 & 2 & -4 & 3 \end{bmatrix}$$