

$$\textcircled{1} \begin{vmatrix} 3 & -5 \\ 2 & 6 \end{vmatrix}$$

$$3(6) - 2(-5) = 18 + 10 = \boxed{28}^{\textcircled{1}}$$

$$\textcircled{2} \begin{vmatrix} 4 & 1 \\ 0 & -3 \end{vmatrix}$$

$$4(-3) - 0(1) = -12 - 0 = \boxed{-12}^{\textcircled{2}}$$

$$\textcircled{3} \begin{vmatrix} -1 & 0 & 2 \\ 3 & 1 & 4 \\ 2 & 0 & -6 \end{vmatrix} \xrightarrow[e_3 + 2e_1 \rightarrow e_3]{e_2 + 3e_1 \rightarrow e_2} \begin{vmatrix} -1 & 0 & 2 \\ 0 & 1 & 10 \\ 0 & 0 & -2 \end{vmatrix}$$

$$|B| = (-1)(1)(-2) = 2$$

$$|B| = c|A| \quad \textcircled{3}$$

$$|B| = |A|$$

$$\boxed{|A| = 2}$$

$$\textcircled{4} \begin{vmatrix} 2 & 1 & -1 \\ 3 & -2 & 0 \\ 5 & 1 & 6 \end{vmatrix} \rightarrow \begin{vmatrix} 2 & 1 & -1 & 2 & 1 \\ 3 & -2 & 0 & 3 & -2 \\ 5 & 1 & 6 & 5 & 1 \end{vmatrix}$$

$$2(-2)(6) + (1)(0)(5) + (-1)(3)(1) - 5(-2)(-1) + 1(0)(2) + 6(3)(1) = -24 + 0 - 3 - (10 + 0 + 18) = -27 - 28$$

$$\boxed{|A| = -55}^{\textcircled{4}}$$

$$\textcircled{5} \begin{vmatrix} -3 & 2 & 4 \\ 1 & -1 & 2 \\ -1 & 4 & 0 \end{vmatrix} \xrightarrow{\substack{3e_2 + e_1 \\ 3e_3 - e_1}} \begin{vmatrix} -3 & 2 & 4 \\ 0 & -1 & 10 \\ 0 & 10 & -4 \end{vmatrix} \quad \begin{matrix} 3 \times \\ 3 \times \end{matrix}$$

$$\begin{array}{r} 96 \\ \times 3 \\ \hline \end{array}$$

$$\xrightarrow{e_3 + 10e_2 \rightarrow e_3} \begin{vmatrix} -3 & 2 & 4 \\ 0 & -1 & 10 \\ 0 & 0 & 96 \end{vmatrix}$$

$$|B| = 96(-1)(-3)$$

$$|B| = 288$$

$$\begin{array}{r} 32 \\ 9 \overline{) 288} \\ 18 \end{array}$$

$$|B| = c|A| = |B| = 3(3)|A| \quad 288 = 9|A|$$

$$|A| = \frac{288}{9} = 32$$

$$\boxed{|A| = 32} \quad \textcircled{5}$$

$$\textcircled{6} \begin{vmatrix} 0 & -2 & 3 \\ 1 & 2 & -3 \\ 4 & 0 & 5 \end{vmatrix}$$

~~$$\begin{vmatrix} 0 & -2 & 3 \\ 1 & 2 & -3 \\ 4 & 0 & 5 \end{vmatrix}$$~~

$$0(2)(5) + (-2)(-3)(4) + 3(1)(0) - 4(2)(3) + (0)(-3)(0) + 5(1)(-2) = 0 + 24 + 0 - (24 + 0 - 10)$$

$$24 - 14 = 10$$

$$\boxed{|A| = 10} \quad \textcircled{6}$$

$$\textcircled{7} \left| \begin{array}{ccc|c} -2 & 3 & 6 & e_2 + 2e_1 \rightarrow e_2 \\ 4 & 1 & 8 & \\ -2 & 0 & 0 & e_3 - e_1 \rightarrow e_3 \end{array} \right| \rightarrow \left| \begin{array}{ccc|c} -2 & 3 & 6 & \\ 0 & 7 & 20 & \\ 0 & -3 & -6 & \end{array} \right| \rightarrow$$

$$= -2C_1 + 0C_2 + 0C_3$$

$$C_{F1} = \begin{vmatrix} 7 & 20 \\ -3 & -6 \end{vmatrix} = 7(-6) - (-3)(20) = -42 + 60 = 6$$

$$-2(18) = \underline{-36}$$

$$\boxed{|A| = -36} \textcircled{7}$$

$$\textcircled{8} \left| \begin{array}{ccc|c} 2 & -1 & 3 & e_2 - 2e_1 \rightarrow e_2 \\ 4 & 0 & 6 & \\ 5 & -2 & 3 & e_3(2) \rightarrow e_3 \end{array} \right| \begin{array}{ccc|c} 2 & -1 & 3 & \\ 0 & 2 & 0 & \\ 10 & -4 & 6 & \end{array} \quad \begin{array}{l} 2x \\ 2x \end{array}$$

$$e_3 - 5e_1 \rightarrow \left| \begin{array}{ccc|c} 2 & -1 & 3 & \\ 0 & 2 & 0 & 2e_3 - e_2 \\ 0 & 1 & -9 & \end{array} \right| \rightarrow \left| \begin{array}{ccc|c} 2 & -1 & 3 & \\ 0 & 2 & 0 & \\ 0 & 0 & -18 & \end{array} \right| \quad \begin{array}{l} 18 \\ \lambda 2 \\ 136 \\ \lambda 6 \\ 72 \\ -18 \\ -4 \sqrt{72} \\ 32 \end{array}$$

$$|B| = 2(2)(-18) = -72$$

$$|B| = c|A|$$

$$-72 = 2(2)|A|$$

$$-72 = 4|A|$$

$$\frac{-72}{4} = |A|$$

$$\boxed{|A| = -18} \textcircled{8}$$

$$\textcircled{9} \begin{vmatrix} 1 & -1 & 2 & 4 \\ 0 & -3 & 5 & 6 \\ 1 & 4 & 0 & 3 \\ 0 & 5 & -6 & 7 \end{vmatrix} \xrightarrow{e_3 - e_1 \rightarrow e_3} \begin{vmatrix} 1 & -1 & 2 & 4 \\ 0 & -3 & 5 & 6 \\ 0 & -5 & 2 & 1 \\ 0 & 5 & -6 & 7 \end{vmatrix} \begin{matrix} e_2(5) \rightarrow e_2 \\ \times 5 \\ \times 3 \\ \times 3 \end{matrix}$$

$$\begin{vmatrix} 1 & -1 & 2 & 4 \\ 0 & -15 & 25 & 30 \\ 0 & 5 & -2 & -1 \\ 0 & 5 & -6 & 7 \end{vmatrix} \xrightarrow{\begin{matrix} e_3(3) \rightarrow e_3 \\ e_4(3) \rightarrow e_4 \end{matrix}} \begin{vmatrix} 1 & -1 & 2 & 4 \\ 0 & -15 & 25 & 30 \\ 0 & 15 & -6 & -3 \\ 0 & 15 & -18 & 21 \end{vmatrix} \xrightarrow{\begin{matrix} e_3 + e_2 \rightarrow e_3 \\ e_4 + e_2 \rightarrow e_4 \end{matrix}}$$

$$\begin{vmatrix} 1 & -1 & 2 & 4 \\ 0 & -15 & 25 & 30 \\ 0 & 0 & 19 & 27 \\ 0 & 0 & 7 & 51 \end{vmatrix} \quad \begin{array}{r} 51 \\ \times 19 \\ \hline 969 \end{array} \quad \begin{array}{r} 27 \\ \times 7 \\ \hline 189 \end{array} \quad \begin{array}{r} 780 \\ \times 15 \\ \hline 11700 \end{array} \quad \begin{array}{r} 260 \\ 45 \overline{) 11700} \\ \underline{270} \end{array}$$

$$|B| = 1(-15)(19(51) - (27)(7))$$

$$|B| = -15(969 - 189) \quad |B| = -15(780)$$

$$|B| = c|A| \quad -11700 = 5(3)(3)|A|$$

$$-11700 = 5(9)|A|$$

$$-11700 = 45|A|$$

$$|A| = \frac{-11700}{45}$$

$$\boxed{|A| = -260} \quad \textcircled{9}$$

$$(10) \left| \begin{array}{cccc} 2 & -3 & 1 & 4 \\ 0 & -2 & 0 & 0 \\ 3 & 7 & -1 & 2 \\ 4 & 1 & -3 & 8 \end{array} \right| \xrightarrow[e_2 - 2e_1 \rightarrow e_2]{e_3(2) \rightarrow e_3} \left| \begin{array}{cccc} 2 & -3 & 1 & 4 \\ 0 & -2 & 0 & 0 \\ 6 & 14 & -2 & 4 \\ 0 & 7 & -5 & 0 \end{array} \right| \quad \times 2$$

$$\xrightarrow{e_3 - 3e_1} \left| \begin{array}{cccc} 2 & -3 & 1 & 4 \\ 0 & -2 & 0 & 0 \\ 0 & 23 & -5 & -8 \\ 0 & 7 & -5 & 0 \end{array} \right|$$

$$|B| = 2C_{f1}$$

$$C_{f1} = \left| \begin{array}{ccc} -2 & 0 & 0 \\ 23 & -5 & -8 \\ 7 & -5 & 0 \end{array} \right| \rightarrow \begin{array}{ccccc} -2 & 0 & 0 & -2 & 0 \\ 23 & -5 & -8 & 23 & -5 \\ 7 & -5 & 0 & 7 & -5 \end{array}$$

$$7(-5)(0) + (-5)(-8)(-2) + 0(23)(0) - (-2)(-5)(0) + (0)(-8)(7) - 0(23)(-5) = -80$$

$$|B| = -2(-80) = -160$$

$$|B| = c|A| \quad -160 = -2|A|$$

$$|A| = \frac{-160}{-2} = +80$$

$$(10) \quad |A| = 80$$

$$(11) \begin{vmatrix} 1 & 1 & -1 & 0 \\ -3 & 4 & 6 & 0 \\ 2 & 5 & -1 & 3 \\ 4 & 0 & 3 & 0 \end{vmatrix} \begin{vmatrix} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{vmatrix}$$

$$|A| = -0C_{f1} + 0C_{f2} - 3C_{f3} + 0C_{f4}$$

$$|A| = -3C_{f3}$$

$$C_{f3} = \begin{vmatrix} 1 & 1 & -1 \\ -3 & 4 & 6 \\ 4 & 0 & 3 \end{vmatrix} \rightarrow \begin{vmatrix} 1 & 1 & -1 & 1 & 1 \\ -3 & 4 & 6 & -3 & 4 \\ 4 & 0 & 3 & 4 & 0 \end{vmatrix}$$

$$1(4)(3) + 1(6)(4) + (-1)(-3)(0) - 4(9)(-1) + (0)(6)(1) + 3(-3)(1)$$

$$12 + 24 - (-16 - 9) = 36 - (-25) = 36 + 25 = 61$$

$$|A| = -3(61) \quad (11)$$

$$|A| = -183$$

$$(12) \begin{vmatrix} 3 & -1 & 2 & 1 \\ 4 & 3 & 1 & -2 \\ -1 & 0 & 2 & 3 \\ 6 & 2 & 5 & 2 \end{vmatrix} \xrightarrow[e_3(3) \rightarrow e_3]{e_2(3) \rightarrow e_2} \begin{vmatrix} 3 & -1 & 2 & 1 \\ 12 & 9 & 3 & -6 \\ -3 & 0 & 6 & 9 \\ 6 & 2 & 5 & 2 \end{vmatrix} \begin{matrix} \times 3 \\ \times 3 \end{matrix}$$

$$\begin{vmatrix} 3 & -1 & 2 & 1 \\ 0 & 13 & -5 & -10 \\ 0 & -1 & 8 & 10 \\ 0 & 4 & 1 & 0 \end{vmatrix} \begin{vmatrix} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{vmatrix}$$

$$|B| = 3C_{f1} - 0C_{f2} + 0C_{f3} - 0C_{f4}$$

$$C_{f1} = \begin{vmatrix} 13 & -5 & -10 \\ -1 & 8 & 10 \\ 4 & 1 & 0 \end{vmatrix}$$

$$\begin{vmatrix} 13 & -5 & -10 & 13 \\ -1 & 8 & 10 & -5 \\ 4 & 1 & 0 & 8 \\ & & & 130 \end{vmatrix}$$

$$C_{f1} = 13(8)(10) + (-5)(10)(4) + (-10)(-1)(1) - 4(8)(-10) + 1(10)(13) + 0(-1)(-5)$$

$$\begin{matrix} 320 \\ -130 \\ \hline 190 \end{matrix}$$

$$C_{f1} = -200 + 10 - (-320 + 130) = -190 - (-190)$$

$$C_{f1} = -190 + 190 = 0$$

$$|B| = 3(0) = 0$$

$$|B| = c|A| \quad 0 = 9|A|$$

$$|A| = \frac{0}{9} = 0$$

$$|A| = 0 \quad (12)$$

$$(13) \begin{vmatrix} 2 & 0 & 0 & 0 \\ 0 & 0 & 3 & 0 \\ 0 & -1 & 0 & 0 \\ 0 & 0 & 0 & 4 \end{vmatrix}$$

$$|A| = 2 C_{f1} - \cancel{0 C_{f2}} + \cancel{0 C_{f3}} - \cancel{0 C_{f4}}$$

$$|A| = 2 C_{f1}$$

$$C_{f1} = \begin{vmatrix} 0 & 3 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 4 \end{vmatrix} \quad \begin{vmatrix} 0 & 3 & 0 & 0 & 3 \\ -1 & 0 & 0 & -1 & 0 \\ 0 & 0 & 4 & 0 & 0 \end{vmatrix}$$

$$C_{f1} = 0 + 0 + 0 - (0 + 0 + 4(-1)(3))$$

$$C_{f1} = -(-12)$$

$$C_{f1} = 12$$

$$|A| = 2(12)$$

$$\boxed{|A| = 24}$$

(13)

$$(14) \begin{vmatrix} 0 & a & 0 & 0 \\ b & 0 & 0 & 0 \\ 0 & 0 & 0 & c \\ 0 & 0 & d & 0 \end{vmatrix} \quad \begin{vmatrix} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{vmatrix}$$

$$|A| = 0C_{f1} - aC_{f2} + 0C_{f3} - 0C_{f4}$$

$$|A| = -aC_{f2}$$

$$C_{f2} \begin{vmatrix} b & 0 & 0 \\ 0 & 0 & c \\ 0 & d & 0 \end{vmatrix} \quad \begin{vmatrix} b & 0 & 0 & b & 0 \\ 0 & 0 & c & 0 & 0 \\ 0 & d & 0 & 0 & d \end{vmatrix}$$

$$C_{f2} = 0 - dcb \quad |A| = -a(-dcb)$$

$$C_{f2} = -dcb$$

$$|A| = abcd$$

$$(15) \left| \begin{array}{cccc} 1 & 2 & 0 & 0 \\ 3 & -2 & 0 & 0 \\ 0 & 0 & 1 & -5 \\ 0 & 0 & 7 & 2 \end{array} \right| \begin{array}{l} e_2 - 3e_1 \rightarrow e_2 \\ e_4 - 7e_1 \rightarrow e_4 \end{array}$$

$$\left| \begin{array}{cccc} 1 & 2 & 0 & 0 \\ 0 & -8 & 0 & 0 \\ 0 & 0 & 1 & -5 \\ 0 & 0 & 0 & 37 \end{array} \right|$$

$$|A| = 1(-8)(1)(37) \quad \begin{array}{r} 5 \\ 37 \\ \times 8 \\ \hline 296 \end{array}$$

$$|A| = -296$$

$$(15) \quad |A| = -296$$

$$(16) \left| \begin{array}{cccc} a & b & 0 & 0 \\ c & d & 0 & 0 \\ 0 & 0 & a & -b \\ 0 & 0 & c & d \end{array} \right| \quad \begin{array}{cccc} + & - & + & - \\ - & + & - & + \\ + & - & + & - \\ - & + & - & + \end{array}$$

$$|A| = aC_{f1} - bC_{f2} + 0C_{f3} - 0C_{f4} \quad |A| = aC_{f1} - bC_{f2}$$

$$C_{f1} = \left| \begin{array}{cc} d & 0 \\ 0 & a \\ 0 & c \end{array} \right| \quad \begin{array}{cccc} d & 0 & 0 & d \\ 0 & a & -b & 0 \\ 0 & c & d & 0 \end{array}$$

$$C_{f1} = d \cdot a \cdot d - (-b \cdot d \cdot c) = d^2 a + b d c$$

$$C_{f2} = \left| \begin{array}{cc} c & 0 \\ 0 & a \\ 0 & c \end{array} \right| \quad \begin{array}{cccc} c & 0 & 0 & c \\ 0 & a & -b & 0 \\ 0 & c & d & 0 \end{array}$$

$$C_{f2} = c \cdot a \cdot d - (-b \cdot c^2) = cad + bc^2$$

$$|A| = a(d^2 a + b d c) - b(cad + bc^2)$$

$$|A| = a^2 d^2 + a b c d - a b c d + b^2 c^2$$

$$(16) \quad |A| = a^2 d^2 - b^2 c^2$$

$$(17) \left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 3 & 1 & -1 & 2 & 0 & \\ 3 & 2 & -2 & 5 & 1 & \\ 0 & 0 & 4 & -1 & 6 & \\ 3 & 2 & 1 & -1 & 1 & \end{array} \right| \begin{array}{l} e_2 \times 2 \rightarrow e_2 \\ \hline e_3 \times 2 \rightarrow e_3 \\ e_5 \times 2 \rightarrow e_5 \end{array} \left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 6 & 2 & -2 & 4 & 0 & \\ 6 & 4 & -4 & 10 & 2 & \\ 0 & 0 & 4 & -1 & 6 & \\ 6 & 4 & 2 & -2 & 2 & \end{array} \right| \begin{array}{l} \times 2 \\ \times 2 \\ \times 2 \\ \hline \times 8 \\ \times 5 \\ \hline \times 40 \end{array}$$

$$\begin{array}{l} e_2 - 3e_1 \rightarrow e_2 \\ e_3 - 3e_1 \rightarrow e_3 \\ e_5 - 3e_1 \rightarrow e_5 \end{array} \left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 0 & 5 & -2 & -8 & -3 & \\ 0 & 7 & -4 & -2 & -1 & \\ 0 & 0 & 4 & -1 & 6 & \\ 0 & 7 & 2 & -14 & -1 & \end{array} \right| \begin{array}{l} e_5 - e_3 \rightarrow e_5 \\ \hline \end{array}$$

$$\left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 0 & 5 & -2 & -8 & -3 & \\ 0 & 7 & -4 & -2 & -1 & \\ 0 & 0 & 4 & -1 & 6 & \\ 0 & 0 & 6 & -12 & 0 & \end{array} \right| e_3 \times 5 \rightarrow e_3 \rightarrow \left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 0 & 5 & -2 & -8 & -3 & \\ 0 & 35 & -20 & -10 & -5 & \\ 0 & 0 & 4 & -1 & 6 & \\ 0 & 0 & 6 & -12 & 0 & \end{array} \right| \begin{array}{l} e_3 - 7e_2 \rightarrow \\ e_3 \end{array}$$

$$\left| \begin{array}{ccccc|c} 2 & -1 & 0 & 4 & 1 & \\ 0 & 5 & -2 & -8 & -3 & \\ 0 & 0 & -6 & 46 & 16 & \\ 0 & 0 & 4 & -1 & 6 & \\ 0 & 0 & 6 & -12 & 0 & \end{array} \right| \quad |C| = \left| \begin{array}{ccc} -6 & 46 & 16 \\ 4 & -1 & 6 \\ 6 & -12 & 0 \end{array} \right|$$

$$|B| = 2(5)(|C|)$$

~~$$\begin{array}{ccc} -6 & 46 & 16 \\ 4 & -1 & 6 \\ 6 & -12 & 0 \end{array}$$~~

$$|C| = 1656 - 768 - (-96 + 432) \quad |B| = 10(552)$$

$$|6| = 888 - 336$$

$$|B| = 5520$$

$$|C| = 552$$

$$|B| = c|A|$$

$$5520 = 40|A|$$

$$|A| = \frac{5520}{40} = 138$$

$$|A| = 138$$

(17)

$$(18) \left| \begin{array}{ccccc} 1 & -1 & 2 & 0 & 0 \\ 3 & 1 & 4 & 0 & 0 \\ 2 & -1 & 5 & 0 & 0 \\ 0 & 0 & 0 & 2 & 3 \\ 0 & 0 & 0 & -1 & 4 \end{array} \right| \xrightarrow{\substack{e_2 - 3e_1 \rightarrow e_2 \\ e_3 - 2e_1 \rightarrow e_3}} \left| \begin{array}{ccccc} 1 & -1 & 2 & 0 & 0 \\ 0 & 4 & -2 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 2 & 3 \\ 0 & 0 & 0 & -1 & 4 \end{array} \right|$$

$$e_3 \times 4 \rightarrow e_3 \rightarrow \left| \begin{array}{ccccc} 1 & -1 & 2 & 0 & 0 \\ 0 & 4 & -2 & 0 & 0 \\ 0 & 4 & 4 & 0 & 0 \\ 0 & 0 & 0 & 2 & 3 \\ 0 & 0 & 0 & -1 & 4 \end{array} \right| \xrightarrow{e_3 - e_2} \left| \begin{array}{ccccc} 1 & -1 & 2 & 0 & 0 \\ 0 & 4 & -2 & 0 & 0 \\ 0 & 0 & 6 & 0 & 0 \\ 0 & 0 & 0 & 2 & 3 \\ 0 & 0 & 0 & -1 & 4 \end{array} \right| \times 4$$

$$|B| = 1(4)(6)(2(4) - 3(-1))$$

$$|B| = 24(8 + 3) = 24(11) = 264$$

$$|B| = c|A|$$

$$264 = 4|A|$$

$$|A| = \frac{264}{4} = 66$$

(18)

$$|A| = 66$$

$$(19) \begin{vmatrix} a & 0 & 0 & 0 & 0 \\ 0 & 0 & b & 0 & 0 \\ 0 & 0 & 0 & 0 & c \\ 0 & 0 & 0 & d & 0 \\ 0 & e & 0 & 0 & 0 \end{vmatrix} \begin{vmatrix} + & - & + & - & + \\ - & + & - & + & - \\ + & - & + & - & + \\ - & + & - & + & - \\ + & - & + & - & + \end{vmatrix}$$

$$|A| = a C_{f1} - 0 C_{f2} + 0 C_{f3} - 0 C_{f4} + 0 C_{f5}$$

$$C_{f1} = \begin{vmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & c \\ 0 & 0 & d & 0 \\ c & 0 & 0 & 0 \end{vmatrix}$$

$$C_{f1} = -b K_{f2}$$

$$K_{f2} = \begin{vmatrix} 0 & 0 & c \\ 0 & d & 0 \\ c & 0 & 0 \end{vmatrix} \begin{vmatrix} 0 & 0 & c & 0 & 0 \\ 0 & d & 0 & 0 & d \\ c & 0 & 0 & c & 0 \end{vmatrix}$$

$$K_{f2} = -(cde)$$

$$-b(-cde) = bcde$$

$$a(bcde) = abcde$$

$$(29) \boxed{|A| = abcde}$$

$$(20) \left| \begin{array}{ccccc} 2 & 5 & -6 & 8 & 0 \\ 0 & 1 & -7 & 6 & 0 \\ 0 & 0 & 0 & 4 & 0 \\ 0 & 2 & 1 & 5 & 1 \\ 4 & -1 & 5 & 3 & 0 \end{array} \right| \xrightarrow[e_5 - 2e_1]{e_5 \rightarrow e_5} \left| \begin{array}{ccccc} 2 & 5 & -6 & 8 & 0 \\ 0 & 1 & -7 & 6 & 0 \\ 0 & 0 & 0 & 4 & 0 \\ 0 & 2 & 1 & 5 & 1 \\ 0 & -11 & 17 & -13 & 0 \end{array} \right|$$

$$\begin{array}{l} e_4 - 2e_2 \rightarrow e_4 \\ e_5 + 11e_1 \rightarrow e_5 \end{array} \left| \begin{array}{ccccc} 2 & 5 & -6 & 8 & 0 \\ 0 & 1 & -7 & 6 & 0 \\ 0 & 0 & 0 & 4 & 0 \\ 0 & 0 & 15 & -7 & 1 \\ 0 & 0 & -60 & 53 & 0 \end{array} \right|$$

$$|A| = 2(1)(|B|)$$

$$|B| = \begin{vmatrix} 0 & 4 & 0 \\ 15 & -7 & 1 \\ -60 & 53 & 0 \end{vmatrix} \quad \begin{vmatrix} 0 & 4 & 0 & 0 & 4 \\ 15 & -7 & 1 & 15 & -7 \\ -60 & 53 & 0 & -60 & 53 \end{vmatrix}$$

$$|B| = -240 + 0 - (0)$$

$$|B| = -240$$

$$|A| = 2(-240)$$

$$(20) \boxed{|A| = -480}$$

(21) a) $2x - y - 3z = 5$
 $3x - 2y + 2z = 5$
 $5x - 3y - z = 16$

$$\left[\begin{array}{ccc|c} 2 & -1 & -3 & 5 \\ 3 & -2 & 2 & 5 \\ 5 & -3 & -1 & 16 \end{array} \right]$$

$$\Delta_s = \begin{vmatrix} 2 & -1 & -3 \\ 3 & -2 & 2 \\ 5 & -3 & -1 \end{vmatrix}$$

~~$$\begin{vmatrix} 2 & -1 & -3 & 2 & -1 \\ 3 & -2 & 2 & 3 & -2 \\ 5 & -3 & -1 & 5 & -3 \end{vmatrix}$$~~

$$\Delta_s = 4 - 10 + 27 - (30 - 12 + 3)$$

$$\Delta_s = 21 - (21)$$

$$\Delta_s = 0$$

(21)

Infinidad de soluciones o no hay solución al sistema

(22) $2x + 3y - 2z = 5$
 $x - 2y + 3z = 2$
 $4x - y + 4z = 1$

$$\left[\begin{array}{ccc|c} 2 & 3 & -2 & 5 \\ 1 & -2 & 3 & 2 \\ 4 & -1 & 4 & 1 \end{array} \right]$$

$$\Delta_s = \begin{vmatrix} 2 & 3 & -2 \\ 1 & -2 & 3 \\ 4 & -1 & 4 \end{vmatrix}$$

~~$$\begin{vmatrix} 2 & 3 & -2 & 2 & 3 \\ 1 & -2 & 3 & 1 & -2 \\ 4 & -1 & 4 & 4 & -1 \end{vmatrix}$$~~

$$\begin{array}{r} 12 \\ \times 3 \\ \hline 36 \end{array}$$

$$\Delta_s = -16 + 36 + 2 - (16 - 6 + 12)$$

$$\Delta_s = 22 - 22$$

$$\Delta_s = 0$$

(22)

Infinidad de soluciones o no hay solución al sistema

(23) $x + 2y + 3z = 3$

c) $2x + 3y + 8z = 4$

$3x + 2y + 17z = 1$

$$\begin{bmatrix} 1 & 2 & 3 & | & 3 \\ 2 & 3 & 8 & | & 4 \\ 3 & 2 & 17 & | & 1 \end{bmatrix}$$

$$\begin{array}{rrrrrr} 1 & 2 & 3 & 1 & 2 & \\ 2 & 3 & 8 & 2 & 3 & \\ 3 & 2 & 17 & 3 & 2 & \end{array}$$

$$\begin{array}{r} 2 \times 17 \\ \hline 34 \\ \hline 51 \end{array}$$

$$\begin{array}{r} 1 \times 17 \\ \hline 17 \\ \hline 34 \end{array}$$

3

$$\begin{array}{r} 168 \\ + 16 \\ \hline 184 \\ + 27 \\ \hline 211 \end{array}$$

(23)

$$\Delta_s = 51 + 48 + 12 - (27 + 16 + 68)$$

$$\Delta_s = 111 - 111$$

$$\Delta_s = 0$$

Infinidad de soluciones o no hay solución al sistema

(24) $A = \begin{pmatrix} 1 & 3 & -1 & 2 \\ 0 & 11 & -5 & 3 \\ 2 & -5 & 3 & 1 \\ 4 & 1 & 1 & 5 \end{pmatrix} \longrightarrow \begin{vmatrix} 1 & 3 & -1 & 2 \\ 0 & 11 & -5 & 3 \\ 2 & -5 & 3 & 1 \\ 4 & 1 & 1 & 5 \end{vmatrix}$

$e_3 - 2e_1 \rightarrow e_3$
 \longrightarrow
 $e_4 - 4e_1 \rightarrow e_4$

$$\begin{vmatrix} 1 & 3 & -1 & 2 \\ 0 & 11 & -5 & 3 \\ 0 & -11 & 5 & -3 \\ 0 & -11 & 5 & -3 \end{vmatrix}$$

$e_4 + e_2 \rightarrow e_4$
 $e_3 + e_2 \rightarrow e_3$

(24)

$$\begin{vmatrix} 1 & 3 & -1 & 2 \\ 0 & 11 & -5 & 3 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{vmatrix}$$

$\Delta_s = 0$

(25) $A = \begin{pmatrix} 0 & 1 & 3 & -2 \\ 0 & 4 & -1 & 3 \\ 0 & 0 & 1 & 1 \\ 0 & 5 & -3 & 4 \end{pmatrix}$

(25)

Como una fila es de ceros
la determinante del sistema
es 0