

Resposta dos exercícios da Lista 2

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Exercício 2 [7.2] Efetue:

$$(a) (x+1)(2x-1)4x^2 = (2x^2+x-1) \cdot 4x^2 = 8x^4+4x^3-4x^2$$

$$(b) (2x-3y)4xy = 8x^2y-12xy^2$$

$$(c) (3x^2-4x+5)(x^2-6x+4) = 3x^4-18x^3+12x^2-4x^3+24x^2-16x+5x^2-30x+20$$

$$(d) (x^2-6x+4+2x^3)(2-3x^2) = 2x^2-3x^4-12x+18x^3+8-12x^2+4x^3-6x^5$$

$$(e) (3u-6v)(u^2-v^2) = 3u^2-3uv^2-6vu^2+6v^3$$

$$(f) (x^4+x^3+x^2+x+1)(x-1) = x^5-\cancel{x^4}+\cancel{x^4}-\cancel{x^3}+\cancel{x^3}-\cancel{x^2}+\cancel{x^2}-\cancel{x}+x-1 = x^5-1$$

Exercício 3 [7.4] Verifique se são igualdades:

$$(a) x^2-1 = (x-1)(x+1) \quad \checkmark$$

$$(b) (x-4)(x+4) = x^2-16 \quad \checkmark$$

$$(c) (2x-1)(2x+1) = 4x^2-1 \quad \checkmark$$

$$(d) 9x^2-25 = (3x-5)(3x+5) \quad \checkmark$$

$$(e) (x+1)^2 = x^2+2x+1 \quad \checkmark$$

$$(f) (x-2)^2 = x^2-4x+4 \quad \checkmark$$

$$(g) (x+5)^2 = x^2+x+25 \quad \text{F}$$

$$(h) (x+3)^2 = x^2+3^2 \quad \text{F}$$

$$(i) (x+1)^3 = x^3+3x^2+3x+1 \quad \checkmark$$

$$(j) (x-1)^3 = x^3-3x^2+3x-1 \quad \checkmark$$

$$(l) (x+4)^3 = x^3+12x^2+48x+64 \quad \checkmark$$

$$(m) (x-2)^3 = x^3-6x^2+12x-8 \quad \checkmark$$

$$(n) (x+3)^3 = x^3+3^3 \quad \text{F}$$

$$(o) (x-5)^3 = x^3-5^3 \quad \text{F}$$

$$(p) (3x-1)^2 = 9x^2-6x+1 \quad \checkmark$$

$$(q) (4x^2+5)^2 = 16x^4+40x^2+25 \quad \checkmark$$

Exercício 4 [7.5] Resolva a equação em cada

$$(o) (x-5)^3 = x^3 - 5^3 \quad F$$

$$(p) (3x-1)^2 = 9x^2 - 6x + 1 \quad \checkmark$$

$$(q) (4x^2+5)^2 = 16x^4 + 40x^2 + 25 \quad \checkmark$$

Exercício 4 [7.5] Resolva a equação em cada caso:

$$\begin{array}{l|l} (a) (x+2)^2 = x^2 + 2^2 & (b) (2x+3)^2 = (2x)^2 + 3^2 \\ \hline \rightarrow \cancel{x^2} + 4x + \cancel{4} = \cancel{x^2} + \cancel{4} & \cancel{4x^2} + 12x + \cancel{9} = \cancel{4x^2} + \cancel{9} \\ 4x = 0 \Rightarrow x = 0 & 12x = 0 \Rightarrow x = 0 \\ S = \{0\} & S = \{0\} \end{array}$$

Exercício 7 [7.10] Fatore:

(a) $9x^2 + 12x + 4$	(b) $16x^2 - 40x + 25$	a) $(3x+2)^2$	b) $(4x-5)^2$
(c) $4 + 28x + 49x^2$	(d) $1 - 2x^2 + x^4$	c) $(7x+2)^2$	d) $(x^2-1)^2$
(e) $9x^2 - 6x + 1$	(f) $x^2 - x + \frac{1}{4}$	e) $(3x-1)^2$	f) $(x - \frac{1}{2})^2$

Exercício 8 [7.11] Fatore:

(a) $x^2 + 3x + 2$	(b) $x^2 + 4x + 3$	a) $(x+1)(x+2)$	b) $(x+3)(x+1)$
(c) $x^2 + x - 2$	(d) $x^2 - 3x + 2$	c) $(x+2)(x-1)$	d) $(x-2)(x-1)$

Exercício 10 [7.13] Fatore:

(a) $x^4 - 16$	(b) $1 - 81x^4$
(c) $t^8 - 256$	(d) $x^4 - 1$

$$a) (x^2)^2 - 4^2 = (x^2 - 4)(x^2 + 4) = (x+2)(x-2)(x^2+4)$$

$$b) 1 - (9x^2)^2 = (1 - 9x^2)(1 + 9x^2)$$

$$c) (t^4)^2 - (2^4)^2 = (t^4 - 2^4)(t^4 + 16) = (t^2 - 2^2)(t^2 + 2^2) \cdot (t^4 + 16)$$

$$d) (x^2)^2 - 1^2 = (x^2 - 1)(x^2 + 1) = (x+1) \cdot (x-1) \cdot (x^2 + 1)$$