

2-Day Course – Spatial Modeling with Geostatistics

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"In two days, what a geoscientists needs to know about geostatistics, and workflows to get you started with applying geostatistics to impact your work."

Spatial Modeling with Geostatistics Uncertainty Management



Lecture outline . . .

- What is Uncertainty?
- Calculating Uncertainty
- Types of Uncertainty
- Uncertainty Workflows

Prerequisites

Introduction

Probability Theory

Representative Sampling

Spatial Data Analysis

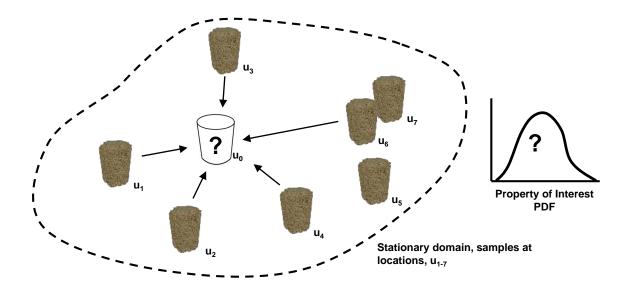
Spatial Estimation

Stochastic Simulation

Uncertainty Management

Machine Learning

- Page The Told Good Rates
- Uncertainty is not an intrinsic property of the subsurface.
- At every location (u_{α}) within the volume of interest the true properties could be measured if we had access (facies, porosity etc.).
- Uncertainty is a function of our ignorance
- This sparsity of sample data combined with heterogeneity results in uncertainty.



- Subsurface uncertainty is a model.
- We should use the term "uncertainty model".
- As with all models, our uncertainty model is imperfect, but useful.
- Our uncertainty assessment is a function of a set of subjective decisions and parameter choices.
- The degree of objectivity is improved by ensuring each of the decisions and parameters are defendable given the available data and judicious use of analogs.

Using Multiple Models:

- We represent uncertainty with multiple models.
- It is convenient to assume that each model is equiprobable, but one could assign variable probability based on available local information and analogs.
- When the input decisions and parameters are changed then these are known as scenarios
- When the input decisions and parameters are held constant and only the random number seed is changed then these are known as realizations

- It is generally not appropriate to analyze a single or few scenarios and realizations.
- For decision making, use all the models all the time applied to the transfer function (e.g. volumetric calculation, contaminant transport, ore grade scale up, flow simulation etc.)(Deutsch, "All the Realizations All the Time, 2018)

- Uncertainty exists because of incomplete data:
 - Cannot be avoided
 - Can be reduced by consideration of all relevant data, and
 - Can be managed / modelled / utilized
 - More data may increase uncertainty!
- The main steps we will propose are:
 - Conceptualize a model for the process
 - Quantify the uncertainty in each of the inputs
 - Transfer the input uncertainty through to output uncertainty
 - Make optimal decision in presence of uncertainty

 \bigcirc 50%

Consider Impact on Uncertainty of:

- 1. Trend Modeling
 - Variance is partitioned between trend, deterministic, known and residual, stochastic, unknown.

Variance
$$\sigma^2 = \sigma_t^2 + \sigma_r^2 + 2C_{t,r}(0)$$
Components

2. Variogram Modeling

Variance is partitioned spatially with variogram features

Nested structures each describe spatial uncertainty components.

$$\sigma_k^2 = \sigma_{nugget}^2 + \sigma_{spherical}^2 + \sigma_{trend}^2$$

3. Scenario / Case Modeling

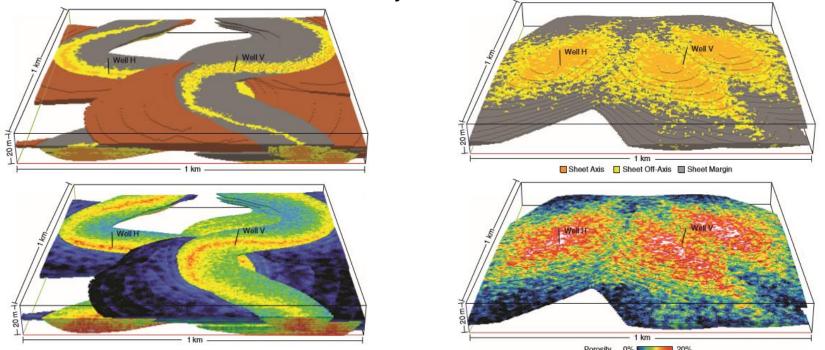
At times it is NOT possible to represent uncertainty as a continuous distribution.

Assign nested case probabilities.

$$P(NTG,DS) = P(NTG \mid DS) \times P(DS)$$

Discrete Scenarios

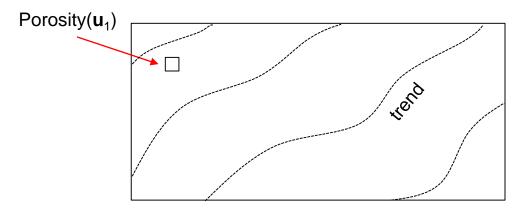
- At times it is NOT possible to represent uncertainty as a continuous distribution.
- Discrete scenarios are required
 - » Porosity compaction trend yes or no.
 - » Channelized or lobe uncertainty



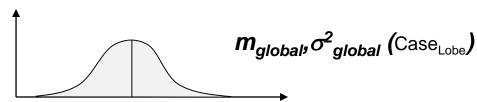
Avoid low, med and high only modeling if possible.



- Simple example:
 - Uncertainty in porosity estimate at location u₁.



1. Global Uncertainty from Scenario: Depositional Setting Deepwater Lobe



2. Local Uncertainty given Trend Model

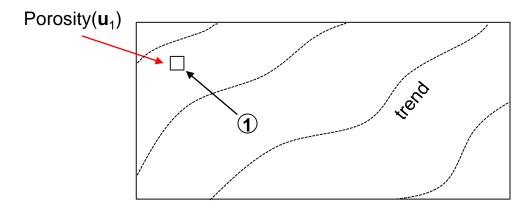
ty given Trend Model
$$\sigma_{residual}^2(\mathbf{u}_1) = \sigma_{global}^2(\mathbf{u}_1) - \sigma_{trend}^2(\mathbf{u}_1)$$

$$m_{trend}(\mathbf{u}_1), \ \sigma_{residual}^2(\mathbf{u}_1)$$

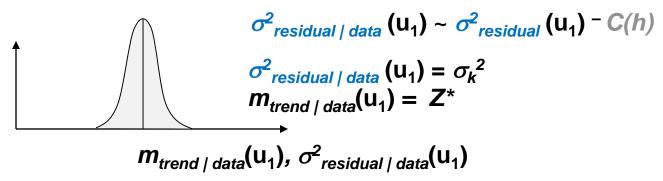


Simple example:

Uncertainty in porosity estimate at location u₁.



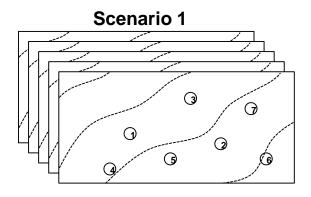
3. Local Uncertainty given Trend Model and Conditioning Data



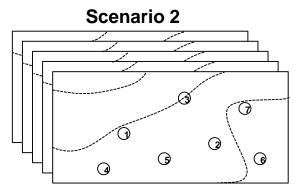
Uncertainty at u₁ for porosity given Case_{Lobe}, trend model and conditioning data.



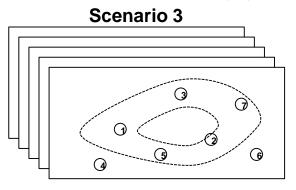
- We have sampled through modeling scenarios and realizations:
 - We can ask any question of the model by considering all scenarios and realizations jointly.



1,...,L realizations (all inputs the same)



1,...,L realizations (all inputs the same)



1,...,L realizations (all inputs the same)

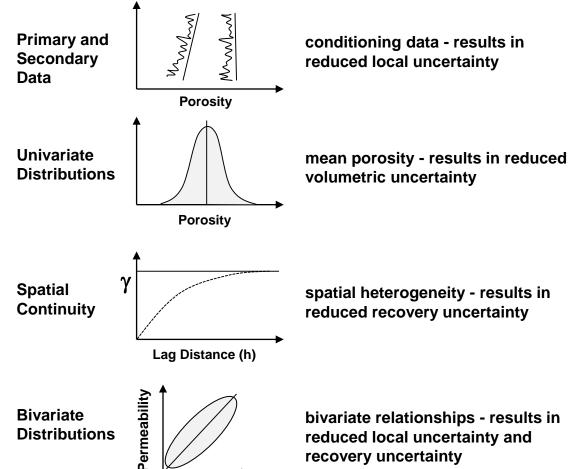


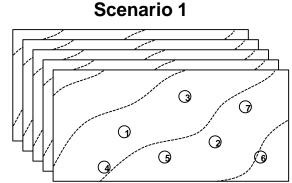
Modeling Subsurface Uncertainty Without Scenarios?

Michael Pyrcz (@GeostatsGuy, Univ. of Texas at Austin)

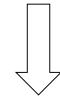
Implicitly assume perfect knowledge of:

Porosity





1,...,L realizations (all the same inputs)

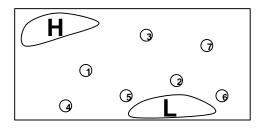


Relying on ergodic fluctuations to characterize uncertainty in the input statistics.



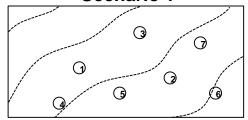
- **Working without realizations?:**
 - Implicitly assume perfect knowledge:

Spatial Uncertainty



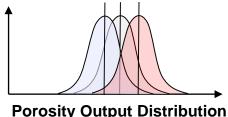
Spatially, away from data. Freeze stochastic islands away from data!





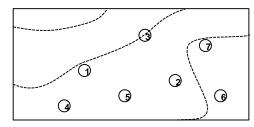
Porosity Realization

Input Statistic Fluctuations



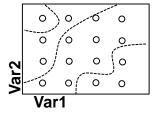
Ergodic fluctuations from target statistics.

Scenario 2



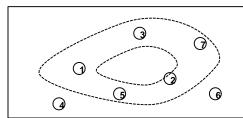
Scenario 3

Response **Surface**



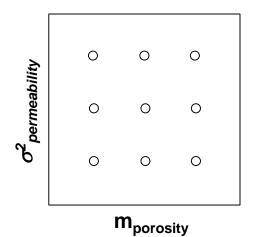
Response Surface

Ergodic fluctuations transfer to response surface creating additional undulations.



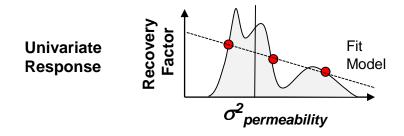


- Uncertainty Space is Vast!
 - Consider typical design



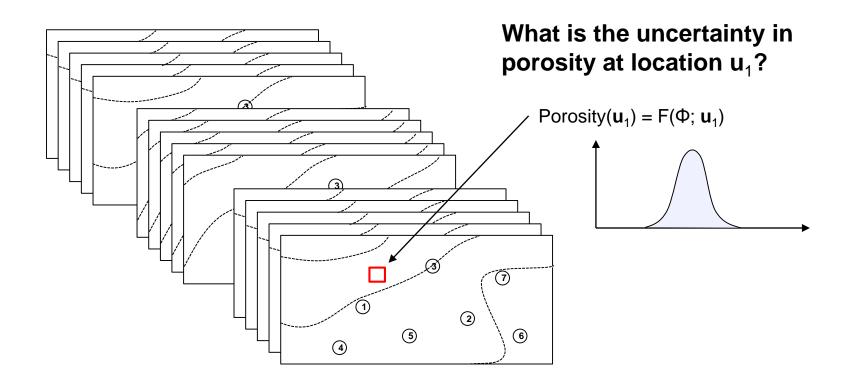
3 level design, 2 variables level^{var} = 9 scenarios

- Consider there are typically are around 10 or more uncertain variables.
 - $^{310} = 59,049$ scenarios x 10 realizations of each scenario = 590,490 models
 - » Variable screening is important!
 - » 3 level may still poor sampling



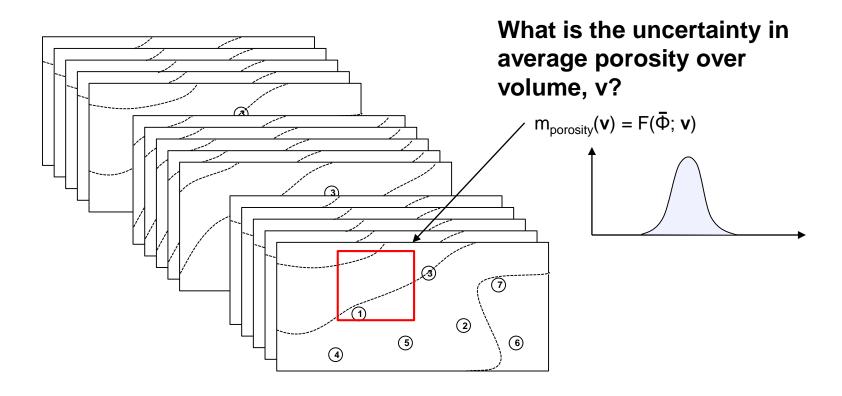


- We have represented the "uncertainty model" through scenarios and realizations:
 - We can ask any question of the model by considering all scenarios and realizations jointly.



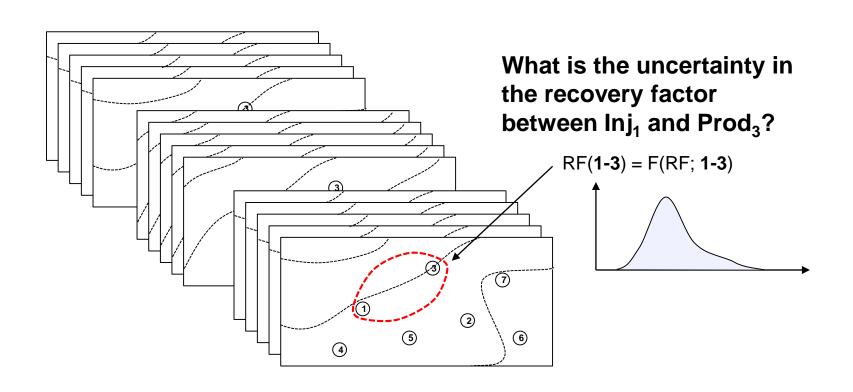


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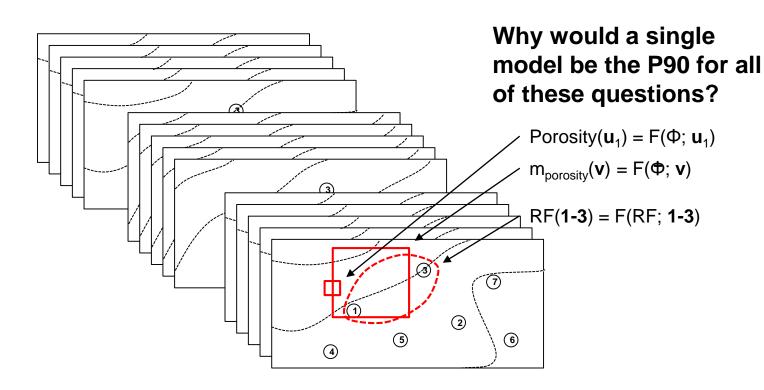


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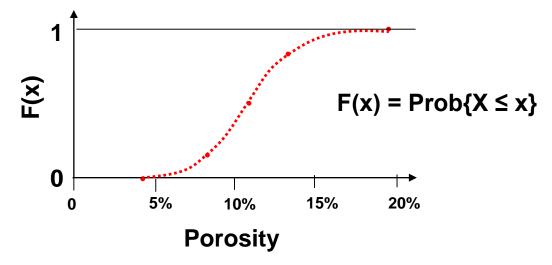


- We have represented the "uncertainty model" through scenarios and realizations:
 - Models could be ranked as Pxx for a specific question.
 - But for every new question, the calculation of rank must be RERUN!





- Frequentist Approach (recall from Lecture 2)
 - Sample and pool data samples and formulate a CDF (assumption of stationarity)
 - Local data, analog data, calibrated data etc.



- Calculate all required marginal, joint and conditional probabilities density functions and their associated variances or conditional variances
 - $F(x) = Prob\{X \le x\}$
 - $F(x,y) = Prob\{X \le x, Y \le y\}$



- Bayesian Approach (recall from Lecture 2)
 - Formulate prior belief
 - Calibrate new data, information into a likelihood
 - Update to calculate a posterior

Prob
$$\{A \mid B\} = \frac{\text{Prob } \{B \mid A\} \times \text{Prob } \{A\}}{\text{Prob } \{B\}}$$

- Induction would be very difficult without Bayesian methods or a lot of data!
- E.g. probability of reservoir NTG > 0.5, given < 50 ft. net pay average over wells.

Guidance:

- 1. Formulate a prior model / marginal probability of event A alone.
 - Prior must be fair, Caers (Stanford) re-iterates that the prior should be quite naïve.
- 2. Calculate a likelihood that models the impact of event A on B
 - Likelihood must fairly account for this relationship
- 3. Calculate the evidence term.
 - Often just normalization constant. May be difficult to infer.

Model Parameter Uncertainty

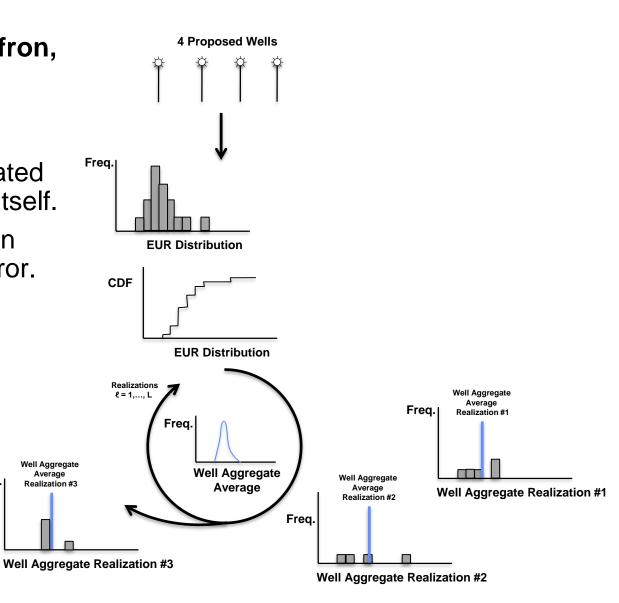


Bootstrap Approach (Efron, 1982)

- Statistical resampling procedure to calculate uncertainty in a calculated statistic from the data itself.
- For uncertainty in mean solution is standard error.

$$\sigma_{x}^{2} = \sigma_{s}^{2}$$

Freq.



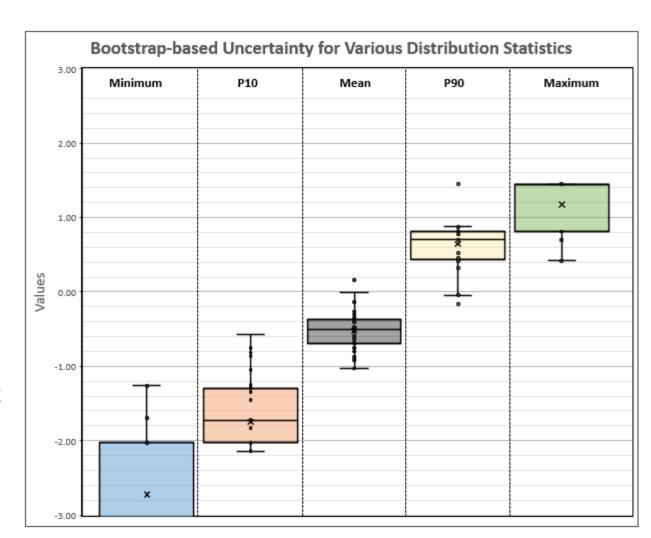
Bootstrap Hands-on In Excel



Observed the bootstrap method for estimating uncertainty in a variety of statistics

What happens if you decrease the number of samples form 20 to 10?

File is Bootstrap_Demo.xlsx



Model Parameter Uncertainty

(3) Spatial Bootstrap Realizations

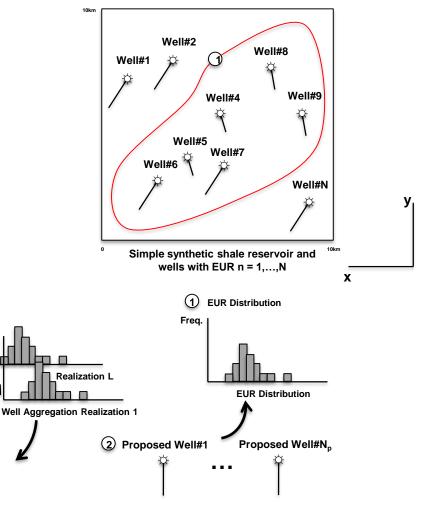
Uncertainty in Average N_n Well EUR

L = 1,...,L



Spatial Bootstrap Approach (Journel, 1994)

- Spatial bootstrap is a variant of bootstrap that accounts for spatial correlations when resampling
- method accounts for:
 - Proposed and previous well locations
 - Spatial Continuity
 - Local trends and secondary data
- Based on sequential simulation from EUR distribution

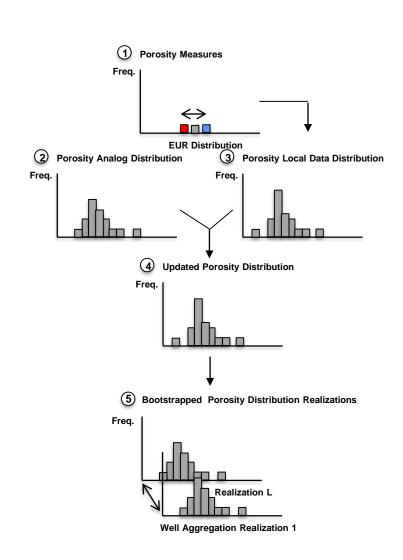


Model Parameter Uncertainty



Example Workflow

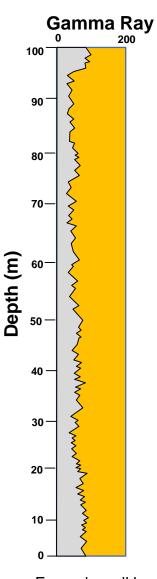
- Calculate measurement error for all data and calculate data realizations. Insignificant.
- Frequentist approach to build porosity global CDF from available analogs
- 3. Frequentist approach to build declustered local data CDF.
- 4. Bayesian updating of analog prior porosity global CDF
- Spatial bootstrap to calculate multiple realizations of porosity distribution.



Types of Uncertainty



- Measurement / Interpretation Error.
 - Formation evaluation tool tolerance, calibration error, approximations / assumptions
 - Interpreter experience and prior model / assumptions
 - How to integrate it?
 - » Indicator method code as soft inputs
 - » Multiple data realizations in design of experiments

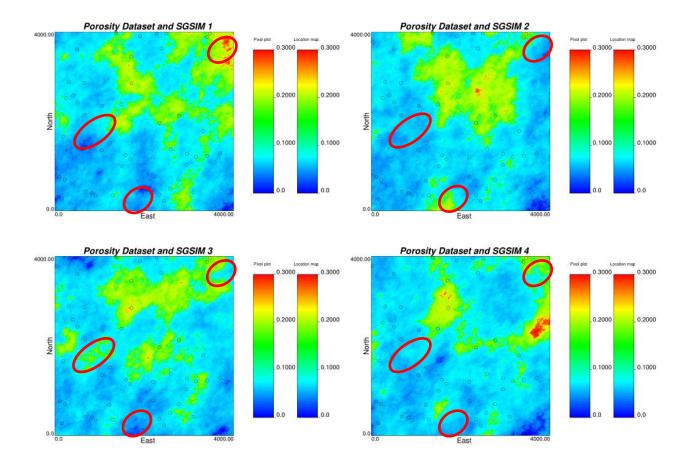


Example well log.

Types of Uncertainty



- Spatial Uncertainty
 - Uncertainty due to spatial offset from sampled locations
 - Integrate through multiple local realizations and scenarios

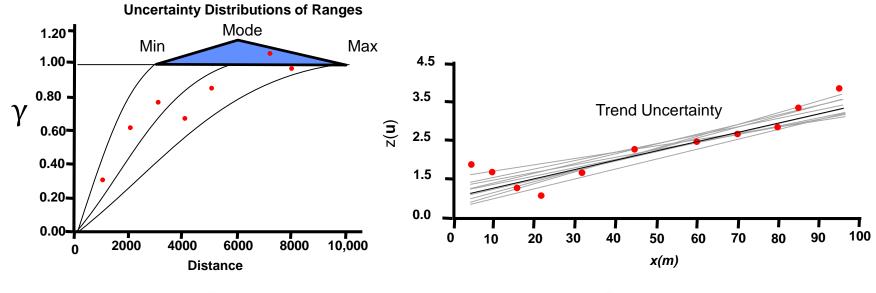


Types of Uncertainty



Parameter Uncertainty

- Uncertainty in the input statistics
- E.g. global reference porosity distribution for simulation
- Formulate distribution scenarios (could bootstrap for parameter realizations)



Uncertainty in Porosity Variogram

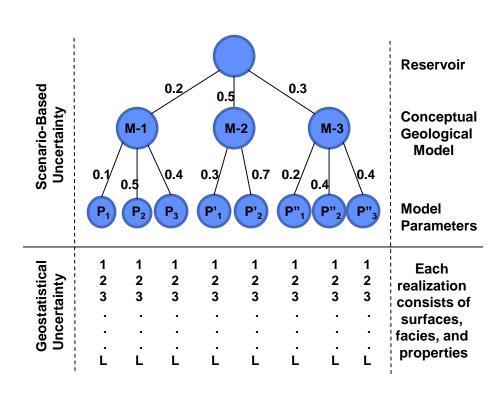
Trend Uncertainty

Uncertainty



Best Practice

- 1. Seek out all significant uncertainty sources
- Assign scenarios when needed with associated debiased probabilities
- 3. Include data realizations if needed.
- 4. Also include stochastic realizations to account for spatial uncertainty.
- 5. Need enough models the uncertainty space is vast.
- 6. Document / defend choices.
- 7. Make decision with the entire suite of models

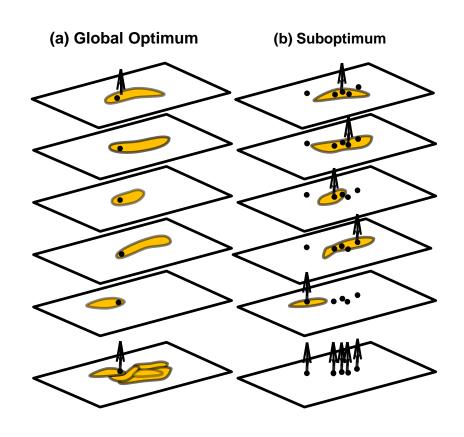


Uncertainty exploration scheme

Working with Multiple Realizations



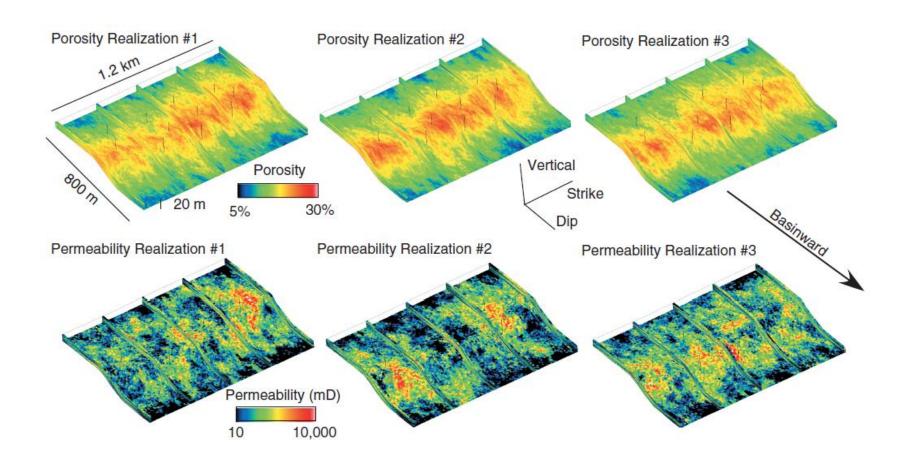
- Making Decisions with Multiple Realizations
- One Realizations at a Time
 - For each model you could make a suboptimal decision.
 - For L models, you would have L suboptimal decisions
- All Realizations Jointly
 - A single decision taken with all the realizations
 - 1. Place well, for each model calculate the resulting production, and calculate the expected production
 - 2. Repeat for multiple locations
 - 3. Select the location that maximizes production



Working with Multiple Realizations



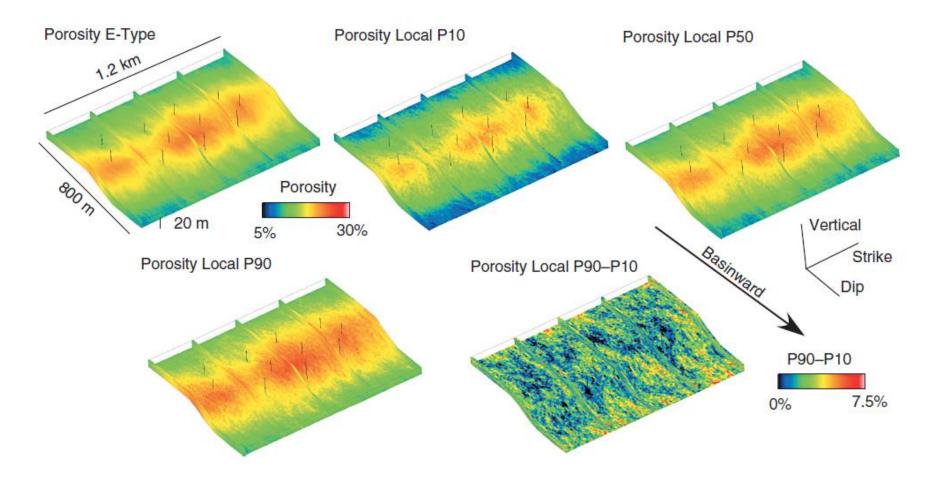
- Summarizing over Multiple Realizations
 - Multiple reservoir model realizations.



Working with Multiple Realizations



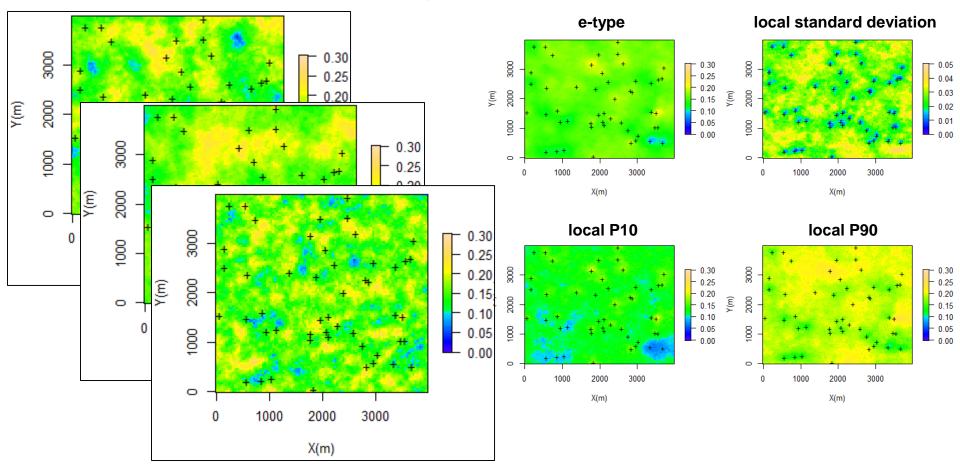
- Summarizing over Multiple Realizations
 - E-type, Local P-value, Local Range, Local Standard Deviation



Working with Multiple Realizations Demo in R



- Summarizing over Multiple Realizations
 - 3 scenarios, 10 realizations of each
 - E-type, Local P-value, Local Range, Local Standard Deviation



Working with Multiple Realizations Hands-on in R



 At the very end of the demo, these lines modify the variogram model, rerun the ordinary kriging and plot the estimate and estimation variance.

```
# Three variogram scenarios
vm1 <- vgm(psill = 1.0*sill, "Sph", 600, anis = c(000, 1.0),nugget=0.0*sill)
vm1
vm2 <- vgm(psill = 1.0*sill, "Sph", 1200, anis = c(000, 1.0),nugget=0.0*sill)
vm2
vm3 <- vgm(psill = 0.99*sill, "Sph", 300, anis = c(000, 1.0),nugget=0.01*sill)
vm3</pre>
```

Some ideas to explore:

- 1. Set the nugget high (use nugget parameter and set psill to 1-nugget).
- 2. Set the range lower and higher (currently 300, 600, 1200) in the function call.

3. Increase and decrease the anisotropy ratio (currently 1.0, isotropic) in the function call.

Working with Multiple Realizations Hands-on in R

e-type



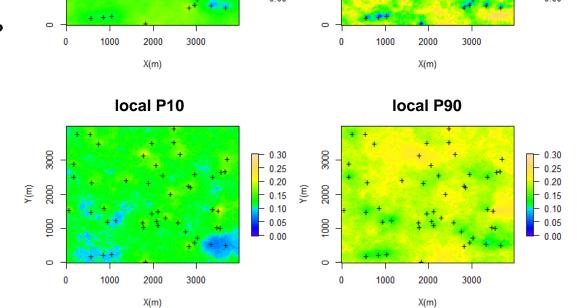
0.02

local standard deviation

- Where would you drill?
 - 1. To maximize production?

2. To minimize risk of a bad well?

3. To gather information?



Summary on Uncertainty



Calculating Uncertainty in a Modeling Parameter:

 Use Bayesian methods, spatial bootstrap etc. You must account for the volume of interest, sample data quantity and locations, and spatial continuity.

If You Know It, Put It In.

 Use expert geologic knowledge and data to model trends. Any variability captured in a trend model is known and is removed from the unknown, uncertain component of the model. Over fit trend will result in unrealistic certainty.

Types of Uncertainty:

• (1) data measurement, calibration uncertainty, (2) decisions and parameters uncertainty, and (3) spatial uncertainty in estimating away from data. Your job is to hunt for and include all significant sources of uncertainty.

Summary on Uncertainty



What about Uncertainty in the Uncertainty?

 Don't go there. Use defendable choices in your uncertainty model, be conservative about what you known, document and move on. Matheron taught us to strip all away all defenseless assumptions. Journel warned us to avoid the circular quest of uncertainty in uncertainty in...

Uncertainty Depends on Scale.

• It is much harder to predict a property of tea spoon vs. a house-sized volume at a location (u_{α}) in the subsurface. Ensure that scale and heterogeneity are integrated.

You Cannot Hide From It.

 Ignoring uncertainty assumes certainty and is often a very extreme and dangerous assumption.

Decision Making with Uncertainty.

 Apply all the models to the transfer function to calculate uncertainty in subsurface outcome to support decision making in the presence of uncertainty.



Uncertainty New Tools

Topic	Application to Subsurface Modeling
Partition Variance / Uncertainty Spatial	Modeling a trend Use additivity of variance to communicate decomposition of variance into known trend and unknown residual.
Integrate Scenarios	Build multiple scenarios Capture the uncertainty in model choices, parameters
Integrate Realizations	Build multiple realizations Capture spatial uncertainty away from sampled locations in the subsurface.
Parameter Uncertainty	Calculate subsurface parameter uncertainty Utilize bootstrap to assess the uncertainty in an model parameter given sparse sampling. Consider spatial bootstrap if data is spatially correlated.