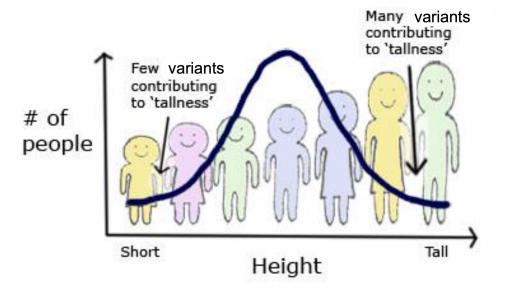
### Complex Phenotypes

## What is a complex phenotype

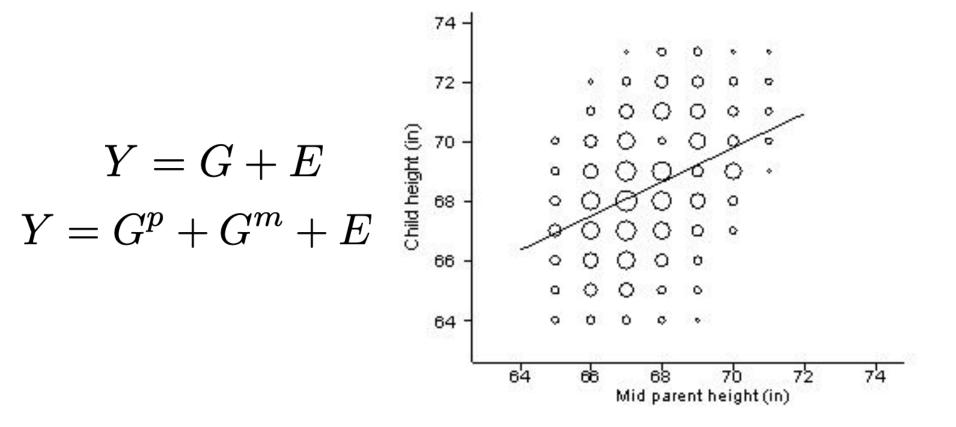
- Height
- BMI
- hair color
- diabetes
- autism
- annual salary
- favorite color
- blood sugar level
- RELN protein level

$$Y = Genetics + Environment$$
  
 $Y = G + E$ 

Complex phenotypes have many genetic variants contributing to their genetic component.



#### Complex phenotypes are "heritable"



Galton, Francis. "Regression towards mediocrity in hereditary stature." *The Journal of the Anthropological Institute of Great Britain and Ireland* 15 (1886): 246-263.

```
...A...T...T...C...
...G...C...T...C...
- \( \psi \) - \( \psi \)
```





...G...T...A...G... ...G...C...A...G... ↑ ↓ ↑ -





```
...A...T...T...C...
...G...C...T...C...
- ↓ - ↓
↑ - - ↓
```



# Y = G + E

#### **Environmental Effects**

- Exercise
- Diet/nutrition
- Race/ethnicity
- sex/gender
- Socio-economic status
- Parental Education
- Kindergarten Attendance
- Access to medical care
- Access to opportunity
- Distance to major cities

...A...T...T...C...
...G...C...T...C...
- \( \psi \) - \( \psi \)



$$y = \mu + \beta_1 g_1 + \beta_2 g_2 + \overline{\beta_3} g_3 + \dots + \beta_M g_M + e$$
  

$$y = \mu + 0.2g_1 + (-0.1)g_2 + 0.3g_3 + \dots + (-0.2)g_M + e$$

DeVito

$$y = \mu + 0.2(1) + (-0.1)(1) + 0.3(0) + \dots + (-0.2)(2) + e = \mu + (-0.3) + e$$

Schwarzenegger  $y = \mu + 0.2(2) + (-0.1)(1) + 0.3(2) + \ldots + (-0.2)(0) + e = \mu + 0.9 + e$ 

...A...T...C...
...G...C...T...C...
$$- \quad \lor \quad - \quad \lor$$

$$\uparrow \quad - \quad - \quad \lor$$

$$y_D = \sum \beta_i g_{Di} + e_D$$



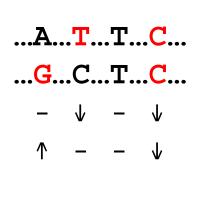
...G...T...A...G...  $\uparrow \quad \downarrow \quad \uparrow \quad \uparrow \quad - \quad \uparrow \quad y_S = \sum_i \beta_i g_{Si} + e_S$ 

$$y_j = \sum_i \beta_i g_{ji} + e_j$$

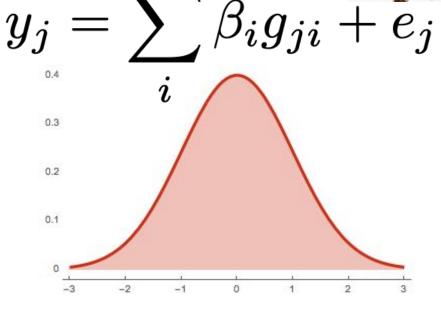
$$y = \mu + 0.2(1) + (-0.1)(1) + 0.3(0) + \dots + (-0.2)(2) + e = \mu + (-0.3) + e$$

Schwarzenegger

$$y = \mu + 0.2(2) + (-0.1)(1) + 0.3(2) + \dots + (-0.2)(0) + e = \mu + 0.9 + e$$







...G...T...A...G... ...G...C...A...G... ↑ ↓ ↑ – ↑ – ↑ –

#### **Environmental Effects**

- Exercise
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$$e_j \sim \mathcal{N}(0, \sigma_e^2)$$

https://brilliant.org/wiki/normal-distribution/

#### Linear Algebra Version

$$y_j = \sum_i \beta_i g_{ji} + e_j$$

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix} = \begin{bmatrix} g_{11} & g_{12} & \dots & g_{1M} \\ g_{21} & g_{22} & \dots & g_{2M} \\ \vdots & \vdots & \vdots & \vdots \\ g_{N1} & g_{1N} & \dots & g_{NM} \end{bmatrix} \begin{bmatrix} \beta_1 \\ \beta_2 \\ \vdots \\ \beta_M \end{bmatrix} + \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_N \end{bmatrix}$$

$$Y = G\beta + E$$

#### Linear Algebra Version

$$y_j = \sum_i \beta_i g_{ji} + e_j$$

$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_N \end{bmatrix} = \begin{bmatrix} g_{11} & g_{12} & \dots & g_{1M} \\ g_{21} & g_{22} & \dots & g_{2M} \\ \vdots & \vdots & \vdots & \vdots \\ g_{N1} & g_{1N} & \dots & g_{NM} \end{bmatrix} \begin{bmatrix} 0.2 \\ 0 \\ \vdots \\ -0.05 \end{bmatrix} + \begin{bmatrix} e_1 \\ e_2 \\ \vdots \\ e_N \end{bmatrix}$$

$$Y = G\beta + E$$

### Types of Models

$$Y=G+E$$
 Additive Genetics + Environment  $Y=G+E+GE$  Additive Genetics + Environment + Gene by Environment Interaction  $Y=G+E+GG$  Additive Genetics + Environment + Gene by Environment Interaction + Gene by Gene Interaction

$$y = \mu + \sum_{i} \beta_{i}g_{i} + e$$

$$y = \mu + \sum_{i} \beta_{i}^{g}g_{i} + \sum_{i} \beta_{i}^{gd}e^{d}g_{i} + \sum_{i} \beta_{i}^{gs}e^{s}g_{i} + \sum_{i} \sum_{j} \beta_{ij}^{gg}g_{i}g_{j} + e$$