

Improving the Performance of Distributed Data Parallelism Over Low Communication Bandwidths

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Abstract

There is no doubt that networking is a bottleneck when training neural networks across multiple GPUs and computers. Having a low bandwidth or a high latency can drastically increase training time of a neural network. In this paper we look at a variety of methods to reduce the effect of a low bandwidth including gradient sparsification, gradient quantization and a using a large batch size. We find ... COULDN'T FIND COMPUTER

1 Introduction

Distributed data parallelism is a widely used technique for training Artificial Intelligence (AI) models, especially when working with large datasets. It involves dividing the data across multiple nodes and training multiple copies of the model in parallel, which can significantly reduce the time required for training. However, the efficiency of this technique can be affected by several factors, including the bandwidth of the communication channels between the nodes.

Low communication bandwidths can have a significant impact on the training time of AI who are training using distributed data parallelism. When the communication channels between nodes have low bandwidth, this can lead to slower data transfer and synchronization between the nodes, which can in turn result in slower training times. In addition, low communication bandwidths may also lead to increased latency in the communication between nodes, further diminishing the efficiency of the training process.

In this paper, we aim to explore the relationship between low communication bandwidths and the training time of AI models using distributed data parallelism. We will discuss the various ways in which low communication bandwidths can impact the communication between nodes and the over-

all efficiency of the training process. We will also present potential solutions for mitigating the negative effects of low communication bandwidths on model training time.

To provide a better understanding of the role that communication bandwidths play in the training of AI models using distributed data parallelism, we will conduct experiments using a variety of datasets and model architectures. We will compare the training time of models trained using distributed data parallelism in high and low communication bandwidth environments to evaluate the impact of low communication bandwidths on the training process.

Overall, our goal is to shed light on the importance of the communication bandwidth in the training of AI models using distributed data parallelism and to identify strategies for optimizing the training process in low bandwidth environments. We hope that the findings of this research will be useful for practitioners seeking to improve the efficiency of their model training process and for researchers studying the optimization of distributed data parallelism for AI model training.

2 Methodology

2.1 Distributed Data Parallelism

The goal of distributed data parallelism is to split the data across the GPUs and computers in the cluster, so that the training process can be completed faster by leveraging the additional computational resources.

Here is an overview of the process:

1. First, the data and model are partitioned or "split" across the GPUs and computers in the cluster. This is typically done by dividing the data into smaller chunks and assigning each

chunk to a GPU or computer in the cluster.

2. Next, the training process begins. On each GPU or computer in the cluster, the model processes the data assigned to it and computes the gradients of the loss function with respect to the model parameters.
3. The gradients computed on each GPU or computer are then averaged together, and the model parameters are updated using this average gradient. This process is known as "gradient averaging" or "gradient synchronization."
4. The process is then repeated, with each GPU or computer processing its assigned data and computing gradients, until the model has been trained.

By training the model in this way, the computation is distributed across multiple GPUs and computers, which can significantly reduce the time it takes to train the model. However, it also adds complexity to the training process, as the gradients must be averaged across the GPUs and computers and the model parameters must be kept consistent across the cluster. There are multiple ways of performing this gradient averaging depending on the architecture of your GPUs and computers. In this paper we work with a synchronous architecture for simplicity, as all of our GPUs have roughly the same compute power. There is also the argument of a centralised versus a decentralised topology.

In a centralized topology, the process of gradient averaging or gradient synchronization in step 3 of the distributed data parallelism process is typically performed on a central server or "parameter server." This is done by sending the gradients computed on each GPU or computer in the cluster to the central server, where they are averaged together and the model parameters are updated.

In a decentralized topology, the process of gradient averaging or gradient synchronization is performed in a decentralized manner, without the use of a central server or parameter server. This can be done using a number of different techniques, such as peer-to-peer communication or gossip protocols.

We find in this paper (Lian, 2017)[10] that decentralized topology's are effected less by low bandwidths, and that is why we implement a decentralized architecture in our paper. To be more specific, we use our own implementation of the Ring AllReduce algorithm [4] to average our gradients.

All of our code will be written using the JAX [1] machine learning framework with MPI being used for peer-to-peer communication via the mpi4jax [7] library.

2.2 SGD

The training data is denoted as $\{x_i\}_{i=1}^n \subset \mathbb{R}^d$, and the model parameter vector is denoted as $w \in \mathbb{R}^d$. The goal of training is to solve the following optimization problem

$$\min_w f(w) = \frac{1}{n} \sum_{i=1}^n L(w, x_i)$$

Where L is the loss function. We typically use an algorithm such as Stochastic Gradient Descent (SGD) to solve the equation above. In which we need to calculate the unbiased stochastic gradients of f at time step t which satisfies $\mathbb{E}[g_t(w_{t-1})] = \nabla L(w_{t-1})$. SGD can be written as:

$$w_t = w_{t-1} - \eta g_t(w_{t-1})$$

Where $g_t(w_{t-1})$ is an estimate for the actual gradient $\nabla L_t(w_t)$ and η is the learning rate. For simplicity we'll let g represent $g_t(w_t)$. The convergence of SGD is largely influenced by the variance of g . In most implementations of distributed parallelism it is g which is averaged between all of the replicas.

2.3 Gradient Quantization

Gradient quantization is a technique used in distributed data parallelism to reduce the amount of data that needs to be transmitted over channels during training. It works by reducing the precision of the gradients that are transmitted between worker nodes.

A model parameter is usually stored in memory as a 32bit floating point. There are $7.8e39$ (38 zeros) unique 32bit floating points, but that said 32bit floating points like 0.000100, 0.000101 and 0.000102 are very close. We can approximate these numbers to be equal, this is the core concept of quantization.

If you have a vector $a \in \mathbb{R}^d$ where $a \sim \mathcal{N}(0.1, 0.55)$ where we know the max a and min a . We can split a into equal size bins and represent each bin with either a 8bit or 16bit integer. For example, suppose we have a set of 100 bins, each representing a range

of gradient values. If the gradient of a particular parameter falls within the range of the first bin, it will be represented as a 0; if it falls within the range of the second bin, it will be represented as a 1; and so on. Then once the quantized a has been sent to another node that node can look up what values the bin represents and replaces all the gradients in the bin with that value. This allows us to represent each gradient value using a single integer, rather than a floating-point value, which can significantly reduce the amount of bandwidth required to when sending gradients. The difference between using 8bit or 16bit integer is the number of bins, which effects not only the accuracy of the data but how much data is sent over the network. If we use 16 bit integers there can be 65,536 bins where as with 8bit there is only 256 which is a significant reduction.

2.3.1 Non-Linear Quantization

Our implementation of non-Linear quantization is a dumbed down version of [2]. As mentioned above $a \sim \mathcal{N}(0.1, 0.55)$ this tells us that that most of the values will be located around 0.1 which means it may be more representative of a if the there are more bins located around the mean than max a and min a . This means bins closer to the mean cover a lower range of values, but occur at a higher frequency. Bins closer to the min and the max cover a larger range of values. Instead of all the bins covering an equal range of values at a common interval each bin will contain an equal range of values(if you have 200 gradients and 10 bins each bin will contain 20 gradients). This value assigned to the the bin is the mean of the values in the bin.

2.3.2 Block-Wise Quantization

Modern models can contain billions of trainable parameters, which translates to billions of gradients. If we represent all of those gradient as 256 different integers we loose a lot of accuracy and make it alot harder for the model to converge, so what we do is we split gradients into chunks of around 2000 or 4000 items(depending on the size of the model) and quantize each chunk separately this means that the first bin in the first chunk might cover a different ranges of values to the first bin in the second chunk. There are a few reasons for this, the first being that it allows us to use 8bit integers without a significant loss in accuracy, the second being that we can allocate each chunk to a specific GPU core making the quantization step a lot faster. If one of the values in a was 7 it is a clear outlier, this will ef-

fect one of the bins it to be wasted because of single outlier. By splitting up the data into chunks only a one chunk would be effected by this outliers.

2.4 Gradient Sparsification

Gradient sparsification is a technique that involves identifying and removing "zero" or nearly zero gradients [13] from the gradients being transmitted between GPUs or computers in a distributed data parallelism setting. The goal is to reduce the size of the gradients without significantly affecting their quality, so that they can be transmitted more efficiently over the network.

In order to perform gradient sparsification we have to decide on a threshold to determine whether or not a gradient is a zero gradient or not, if the gradient is less than the threshold then it is deemed a zero gradient. In our implementation of gradient sparsification we accumulate zero gradients locally and sum them with gradients from the next iteration.

2.4.1 Formula

We denote sparsified gradients as $S(g, Z_t)$. We have to remember that $g \in \mathbb{R}^d$ so we let g_i be the i -th component of the vector ($g = [g_1, \dots, g_d]$). $Z \in \mathbb{R}^d$ is a vector with the same shape as g , when the w is initialized at the start of the training process $Z_{0,i} = 0$. The function S has 2 outputs the first being v the new representation of the gradient of the weights at iteration t , and the second being the accumulated gradients Z_{t+1}

Sparsification of the gradients is shown as follows:

$$v_{t,i} = \begin{cases} 0 & |g_i + Z_{t-1,i}| < \alpha \\ g_i + Z_{t-1,i} & |g_i + Z_{t-1,i}| \geq \alpha \end{cases}$$

$$Z_{t,i} = \begin{cases} Z_{t-1,i} + g_i & |g_i + Z_{t-1,i}| < \alpha \\ 0 & |g_i + Z_{t-1,i}| \geq \alpha \end{cases}$$

where α is the the threshold.

2.5 Larger Batch Sizes

In machine learning, we have the concept of batch sizes this can be thought of as the number of samples that will be processed before the model's weights are updated. The batch size is a hyper parameter that can be chosen when training a model. When using a batch size the SGD algorithm becomes mini-batch SGD it looks something like this:

$$g_{t-1} = \frac{1}{B_k} \sum_{i=1}^{B_k} \nabla L(w_{t-1})$$

$$w_t = w_{t-1} - \eta g_t$$

Where B_k is the batch size. Increasing the batch size in a distributed training setup can also improve training efficiency by reducing the frequency of the gradient averaging step. This is because each device will process a larger amount of data before the gradients are averaged and applied to the model weights. This can reduce the overhead associated with performing the gradient averaging step, and can allow the model to make more efficient use of the available computation resources.

One negative effect of large batch sizes is that they can lead to a decrease in generalization performance [8]. This occurs because large batch sizes can result in an increase in the variance of the stochastic gradient descent (SGD) updates.

Another negative effect of large batch sizes is that they can lead to a decrease in the convergence rate of the model [5]. This occurs because large batch sizes can result in a reduction in the magnitude of the SGD updates, which can slow down the convergence of the model. In some cases, this can result in the model failing to converge at all.

Furthermore, using large batch sizes can lead to an increase in the amount of memory required to store and process the data. This can be a problem for systems with limited memory or for models with a large number of parameters, as the large batch sizes may not fit in memory.

One way to counteract the the decrease in convergence is to increase the learning rate η [5] so that the magnitude of the SGD updates are increased this usually works for a few of epochs but after a while has a limited effect. We plan to use a adaptive batch size [3]. At the start of training an initial batch size is determined, and the primary test error is calculated from the models initial untrained parameters w_0 . After each epoch the test error is checked, once the test error is half of the primary test error the batch size gets doubled, once the test error is a quarter of the primary test error the batch size is doubled again batch.

Another way which we can reduce the negative effect of a large batch size is to use a different optimizer algorithm to SGD, a common alternative is Adam (Adaptive Moment Estimation) [9] the problem with ADAM is that Adam has been found to

scale poorly with large batch sizes. There are 2 optimizers that scale well with large batch sizes, LARS (Layer-wise Adaptive Rate Scaling) [14] & LAMB (Layer-wise Adaptive Moments for Batch Training) [15]. We have chosen to use LAMB as our optimiser.

LAMB is pretty similar to Adam. We start by computing the gradients g_t at time step t , then much like Adam we calculate the first m and second v moment of each layer l using the following equations:

$$m_t^l = \beta_1 m_{t-1}^l + (1 - \beta_1) g_t^l$$

$$v_t^l = \beta_2 v_{t-1}^l + (1 - \beta_2) g_t^l \odot g_t^l$$

Then we bias correct for both of the moments:

$$\hat{m}_t^l = m_t^l / (1 - \beta_1^t)$$

$$\hat{v}_t^l = v_t^l / (1 - \beta_2^t)$$

In these equations $\beta_{1/2}$ are the coefficient of the first/second moment. After we bias correct the moments we calculate the trust ratio:

$$r_t^l = 1.0$$

$$r_1 = \phi(\|w_{t-1}^l\|)$$

$$r_2 = \left\| \frac{\hat{m}_t^l}{\sqrt{\hat{v}_t^l + \epsilon}} + \lambda w_{t-1}^l \right\|$$

$$r_t^l = \begin{cases} r_1/r_2 & r_1 > 0 \text{ and } r_2 > 0 \\ 1 & r_1 < 0 \text{ or } r_2 < 0 \end{cases}$$

r_1 is the norm of the gradients and r_2 is the element-wise weight decay. r_t^l has to be greater than zero. ϵ in equation 2.5 is to prevent a division by 0 error.

our final step is to upgrade the parameters:

$$w_t^l = w_{t-1}^l - \eta r_t^l \left(\frac{\hat{m}_t^l}{\sqrt{\hat{v}_t^l + \epsilon}} + \lambda w_{t-1}^l \right)$$

2.5.1 Formula for the Adaptive Batch Size

Let E_e be the test error function at epoch e which takes the parameters w_t which is the model parameters at the time step t at the start of epoch e . Let b be the initial batch size and where β is the maximum batch size.

$$\varepsilon = \max \left(1, 2^{(\lfloor E_0(w_0, x_R) / E_e(w_t, x_R) \rfloor - 1)} \right)$$

$$B_k = \min(\beta, b\varepsilon)$$

These equations explain adaptive batch sizing. First the scaling factor ε where $E_0(w_0, x_R)$ is the primary test error, we make sure that value of ε is greater than 1 as if for some reason $E_0(w_0, x_R) < E_e(w_t, x_R)$ the batch size would decrease which is not what we want. Then its just a case of multiplying b by your scaling factor ε and checking to see if its greater than β . Please note that using the output of a loss function instead of the test error is sufficient.

2.6 Models

Within our test we use a range of different models. The most important factor when choosing a model is to make sure we get a good range of sizes between our models. These are the models [6, 11, 12] we train to get results:

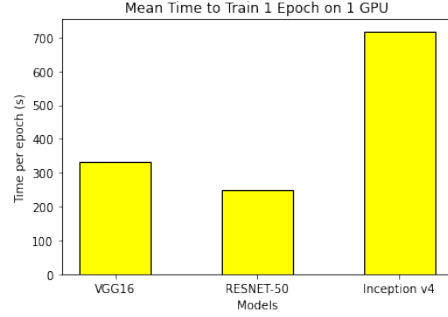
Model	No. Parameters	Gradient Physical Size (MB)
RESNET-50	25,583,592	94.1
VGG16	138,357,544	428.2
Inception v4	42,608,450	170.2

3 Results

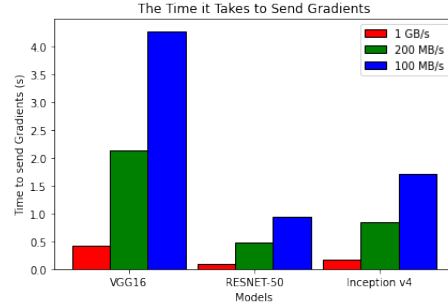
In an ideal world training speed would increase linearly with the number of GPUs you have training the model. In our test to determine the results of Figure 1 (a) we train each model with a B_k (batch size) of 32 and on the cifar 100 dataset of which we use 50000 images for training, this means that there are just under 1600 iterations in a single epoch. Figure 1(b) is determined by the size of the model divided by the speed of the network.

3.1 Baseline

In our result we plan to compare the theoretical with the applied. In this case 8 GPUs were each node has 1 GPU, the data is evenly split between each node translating to each node training with a sample of 6250 images. By increasing the number of nodes from 1 to 8 we reduces the number of communication steps per epoch to around 200 but there is also more data sent in each communication step as each node is sending its own gradients to 8 other nodes.



(a) Training 1 Epoch on 1 P100 GPU



(b) The Theoretical Time to Send Gradients

Figure 1: a & b

If each node was to individually send its gradients to all the other node, there would be $N(N-1)$ messages being sent between nodes, where N is the number of nodes, in the case of 8 nodes that is 56 messages. If we were dealing with our worst case scenario where you are training VGG16 on 100MBps you could take multiple hours ($4 \times 200 \times 56$ seconds) per epoch. This is caused by only 1 node sending data at a time while the rest of the nodes are idle caused by the networks constraints. As we are using a more efficient ring all reduce algorithm, we should have a much lower communication time than multiple hours.

We plan to use 8bit quantization using both non-linear and block-wise techniques. non-linear quantization doesn't effect bandwidth it just helps to reduce variance. Block-wise allows us to decrease the gradients size by a factor of 4 but adds $\frac{p}{k} \times 256$ float16 numbers on top of the quantized gradients in order to undo the quantization where p is the number of parameters and k is the value that determines the number of block usually 2048 or 4096. For the example of vgg16 you decrease the gradients to around 110 MB in size but add the additional size of an extra size of 8,000,000 32 bit float-ing points.

When using sparsification with quantization, sparsification occurs before quantization and quantization only occurs on the non zero grads.



Figure 2: Percentage of Zeros Grads in the First Epoch

We see that as the model gets closer to converging the number of zero grads increases, the graph also shows us that when we have a threshold of 0.00001 we drop over 80% of our gradients this seems like it would have a large effect on the training process this is something we will address in our Benchmarks. If we drop 80%, you are only sending 20% of gradients to other nodes.

By doubling the batch size you should half the communication time as there half as many communication step taking place in an epoch. Whilst using a adaptive batch size it can take quite a long time before the batch size doubles as the it takes multiple epoch before the train error halves.

3.2 Benchmarks

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4 Conclusion

We were not able to access a computer cluster, so we were not able to validate whether the techniques we implemented had a beneficial effect on the training performance. We believe AI and Machine learning is getting to a point where it is completely inaccessible for the majority of researchers. Models are beginning to reach the 1 trillion parameter mark, making it impossible for a researcher that doesn't work for a company like Microsoft or Google to work on the cutting edge. We believe that by implementing techniques like the ones presented in this paper, machine learning at larger scale can become more accessible to everyone.

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