## Pure Quintile Portfolios

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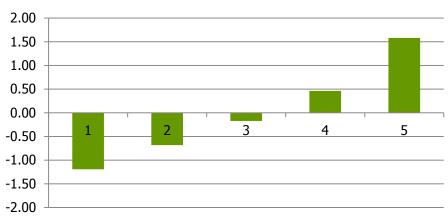
### Summary

- We present a new portfolio construction framework called Pure Quintile Portfolios
- They overcome the drawback of naive quintile portfolios, i.e. not having pure factor exposures
- They have the same exposures to the target factor as naive quintile portfolios, but zero exposures to other factors
  - More accurately reflect pure factor returns
- They create more efficient factor premia for a set of widely used equity factors
  - Pure quintile portfolios have lower risks than naive quintile portfolios
  - Pure Q1-Q5 portfolios have lower risks, higher returns and higher Sharpe ratios than naive Q1-Q5 portfolios

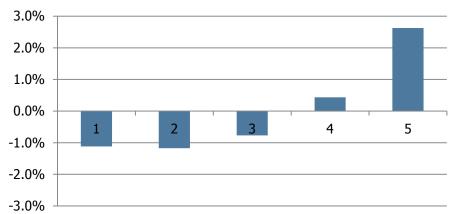
**Ding Liu** 

## Book-to-Price Quintile Portfolios and Their Average Returns





#### **Average Excess Return \*\***

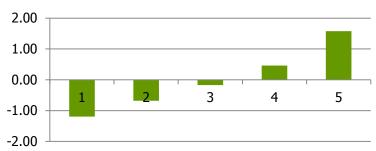


<sup>\*</sup> Average standardized Book-to-Price score from 1979 to 2014; Russell 1000 universe.

<sup>\*\*</sup> Simulated historical average return in excess of equal-weighted market return; quintile portfolios are created monthly; returns are annualized and before transaction costs.

## Book-to-Price Quintile Portfolios and Their Factor Exposures

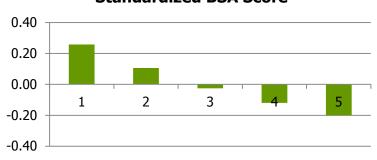




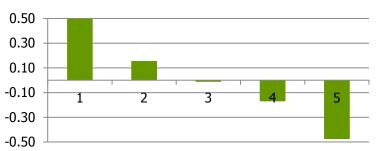
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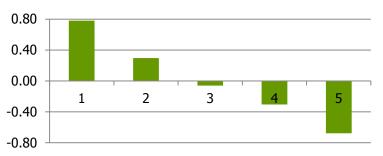
#### Standardized BSA Score



#### **Standardized Momentum Score**



#### **Standardized RoE Score**



#### **Standardized Log Market Cap**



## Creating Pure Quintile Portfolios via Optimization

- Two-way sort
  - Does not generalize to multiple factors: with 5 factors it would create 3125 buckets
  - Does not disentangle factors completely
- Factor-mimicking portfolios / Multivariate regressions
  - Only creates one (typically long-short) portfolio with a unit of standardized exposure
  - But we are interested in evaluating a spectrum of pure factor exposures
  - We adapt and extend the optimization used to create factor-mimicking portfolios

| Minimize w'v    | $\nu$  | (3.1) |
|-----------------|--|-------|
| Subject to:     |  |       |
| $w \ge 0$       |  | (3.2) |
| e'w = 1,        |  | (3.3) |
| $x_i'w = exp$ , | for the target factor i  | (3.4) |
| $x_i'w=0$ ,     | for other non-targeted factors i                                 | (3.5) |
| The number o    | of stocks is the same as in the naïve quintile, i.e. about $n/5$ | (3.6) |

### Focusing on Standard Well-Known Factors

- Value: book-to-price
- Size: natural log of market cap
- Price Momentum: 11 month past price return lagged by 1 month
- Profitability: return on equity
- Earnings Quality: balance sheet accruals
- Use simple factor definitions
- Not trying to fine-tune factors for better economic intuition or performance

#### Notes on Backtest

- Winsorize raw factor values at 5% level
- Standardize factor values (i.e. calculate z-scores) to make them comparable
- "Market" is the equal weighted portfolio of all stocks
- Flip the signs of Size and Earnings Quality exposure so that higher exposures mean higher expected returns for all factors
- Quintile 1 highest exposure; quintile 5 lowest exposure
- Portfolios are created at the beginning of each month; returns are calculated through the end of the month
- US (Russell 1000, 1979-2014), International Developed (MSCI World ex. USA, 1995-2014), and Emerging Markets (MSCI EM, 1999-2014)

## Naive and Pure Quintile Portfolio Factor Exposures

|    | Val  | ue Naiv | ve Quin               | tiles             |                     |  | Value Pure Quintiles |       |       |                       |                   |                     |
|----|--|---------|-----------------------|-------------------|---------------------|--|----------------------|-------|-------|-----------------------|-------------------|---------------------|
|    | Value                                      | Size    | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |  |                      | Value | Size  | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |
| Q1 | 1.58                                       | 0.21    | -0.48                 | -0.68             | 0.20                |  | Q1                   | 1.58  | 0.00  | 0.00                  | 0.00              | 0.00                |
| 2  | 0.46                                       | 0.07    | -0.17                 | -0.31             | 0.12                |  | 2                    | 0.46  | 0.00  | 0.00                  | 0.00              | 0.00                |
| 3  | -0.17                                      | -0.03   | -0.01                 | -0.06             | 0.03                |  | 3                    | -0.17 | 0.00  | 0.00                  | 0.00              | 0.00                |
| 4  | -0.68                                      | -0.13   | 0.16                  | 0.30              | -0.11               |  | 4                    | -0.68 | 0.00  | 0.00                  | 0.00              | 0.00                |
| Q5 | -1.19                                      | -0.18   | 0.50                  | 0.78              | -0.26               |  | Q5                   | -1.19 | 0.00  | 0.00                  | 0.00              | 0.00                |
|    |  |         |                       |                   |                     |  |                      |       |       |                       |                   |                     |
|    | Siz  | e Naiv  | e Quint               | iles              |                     |  | Size Pure Quintiles  |       |       |                       |                   |                     |
|    | Value                                      | Size    | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |  |                      | Value | Size  | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |
| Q1 | 0.21                                       | 1.17    | -0.30                 | -0.21             | -0.04               |  | Q1                   | 0.00  | 1.17  | 0.00                  | 0.00              | 0.00                |
| 2  | 0.06                                       | 0.70    | 0.02                  | -0.08             | -0.03               |  | 2                    | 0.00  | 0.70  | 0.00                  | 0.00              | 0.00                |
| 3  | -0.03                                      | 0.20    | 0.10                  | -0.03             | -0.03               |  | 3                    | 0.00  | 0.20  | 0.00                  | 0.00              | 0.00                |
| 4  | -0.03                                      | -0.47   | 0.08                  | 0.05              | 0.05                |  | 4                    | 0.00  | -0.47 | 0.00                  | 0.00              | 0.00                |
| Q5 | Q5 -0.21 <mark>-1.59</mark> 0.09 0.26 0.05 |         |                       |                   |                     |  | Q5                   | 0.00  | -1.59 | 0.00                  | 0.00              | 0.00                |

| Pr | ice Mo  | mentu    | m Naiv                | e Quint           | iles                | Pı | rice Mo | mentu    | m Pure                | Quint             | iles                |
|----|---------|----------|-----------------------|-------------------|---------------------|----|---------|----------|-----------------------|-------------------|---------------------|
|    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |
| Q1 | -0.50   | -0.05    | 1.53                  | 0.19              | -0.10               | Q1 | 0.00    | 0.00     | 1.53                  | 0.00              | 0.00                |
| 2  | -0.16   | -0.15    | 0.42                  | 0.13              | 0.04                | 2  | 0.00    | 0.00     | 0.42                  | 0.00              | 0.00                |
| 3  | 0.04    | -0.11    | -0.11                 | 0.05              | 0.08                | 3  | 0.00    | 0.00     | -0.11                 | 0.00              | 0.00                |
| 4  | 0.20    | -0.01    | -0.58                 | -0.04             | 0.05                | 4  | 0.00    | 0.00     | -0.58                 | 0.00              | 0.00                |
| Q5 | 0.43    | 0.27     | -1.27                 | -0.30             | -0.06               | Q5 | 0.00    | 0.00     | -1.27                 | 0.00              | 0.00                |
|    |         |          |                       |                   |                     |    |         |          |                       |                   |                     |
|    | Profita | bility I | Naive C               | uintile           | S                   |    | Profit  | ability  | Pure Q                | uintiles          | 5                   |
|    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |
| Q1 | -0.86   | -0.26    | 0.22                  | 1.40              | -0.15               | Q1 | 0.00    | 0.00     | 0.00                  | 1.40              | 0.00                |
| 2  | -0.37   | -0.15    | 0.10                  | 0.43              | -0.10               | 2  | 0.00    | 0.00     | 0.00                  | 0.43              | 0.00                |
| 3  | 0.12    | 0.01     | 0.02                  | -0.01             | -0.01               | 3  | 0.00    | 0.00     | 0.00                  | -0.01             | 0.00                |
| 4  | 0.59    | 0.07     | -0.12                 | -0.42             | 0.07                | 4  | 0.00    | 0.00     | 0.00                  | -0.42             | 0.00                |
| Q5 | 0.58    | 0.26     | -0.24                 | -1.41             | 0.18                | Q5 | 0.00    | 0.00     | 0.00                  | -1.41             | 0.00                |
|    |         |          |                       |                   |                     |    |         |          |                       |                   |                     |
| Ea | arnings | Qualit   | y Naive               | Quint             | iles                | Е  | arnings | s Qualit | ty Pure               | Quinti            | les                 |
|    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |    | Value   | Size     | Price<br>Momentu<br>m | Profitabili<br>ty | Earnings<br>Quality |
| Q1 | 0.14    | 0.06     | 0.00                  | -0.34             | 1.16                | Q1 | 0.00    | 0.00     | 0.00                  | 0.00              | 1.16                |
| 2  | 0.21    | -0.10    | -0.03                 | -0.04             | 0.55                | 2  | 0.00    | 0.00     | 0.00                  | 0.00              | 0.55                |
| 3  | 0.08    | -0.12    | -0.03                 | 0.08              | 0.19                | 3  | 0.00    | 0.00     | 0.00                  | 0.00              | 0.19                |
| 4  | -0.11   | -0.06    | -0.03                 | 0.17              | -0.29               | 4  | 0.00    | 0.00     | 0.00                  | 0.00              | -0.29               |
| Q5 | -0.29   | 0.11     | 0.05                  | 0.12              | -1.60               | Q5 | 0.00    | 0.00     | 0.00                  | 0.00              | -1.60               |

Russell 1000 universe; 1979 to 2014.

#### Value Naive and Pure Quintile Portfolio Performance

| \     | /alue N                  | aive Qı             | uintiles                    |                               | Value Pure Quintiles |                          |                     |                             |                               |  |
|-------|--------------------------|---------------------|-----------------------------|-------------------------------|----------------------|--------------------------|---------------------|-----------------------------|-------------------------------|--|
|       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |                      | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |  |
| Q1    | 2.6%                     | 8.7%                | 0.30                        | 153%                          | Q1                   | 3.0%                     | 7.7%                | 0.39                        | 319%                          |  |
| 2     | 0.4%                     | 4.4%                | 0.10                        | 248%                          | 2                    | 2.2%                     | 3.9%                | 0.56                        | 612%                          |  |
| 3     | -0.8%                    | 3.1%                | -0.25                       | 255%                          | 3                    | 0.0%                     | 2.9%                | 0.01                        | 670%                          |  |
| 4     | -1.2%                    | 4.0%                | -0.29                       | 220%                          | 4                    | -2.0%                    | 3.9%                | -0.52                       | 582%                          |  |
| Q5    | -1.1%                    | 8.2%                | -0.14                       | 130%                          | Q5                   | -2.7%                    | 7.2%                | -0.37                       | 211%                          |  |
| Q1-Q5 | 3.7%                     | 15.7%               | 0.24                        | 282%                          | Q1-Q5                | 5.7%                     | 12.3%               | 0.46                        | 530%                          |  |

### Size Naive and Pure Quintile Portfolio Performance

|       | Size Na                  | aive Qu             | intiles                     |                               | Size Pure Quintiles |                          |                     |                             |                               |  |
|-------|--------------------------|---------------------|-----------------------------|-------------------------------|---------------------|--------------------------|---------------------|-----------------------------|-------------------------------|--|
|       | Avy.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |                     | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |  |
| Q1    | 2.8%                     | 9.0%                | 0.31                        | 195%                          | Q1                  | 3.6%                     | 6.1%                | 0.59                        | 264%                          |  |
| 2     | 0.2%                     | 3.1%                | 0.06                        | 225%                          | 2                   | 0.4%                     | 3.7%                | 0.11                        | 746%                          |  |
| 3     | -0.6%                    | 2.8%                | -0.22                       | 185%                          | 3                   | -0.5%                    | 2.4%                | -0.19                       | 566%                          |  |
| 4     | -0.4%                    | 3.3%                | -0.11                       | 135%                          | 4                   | -1.2%                    | 3.3%                | -0.38                       | 652%                          |  |
| Q5    | -2.0%                    | 5.8%                | -0.35                       | 69%                           | Q5                  | -2.2%                    | 5.0%                | -0.44                       | 98%                           |  |
| Q1-Q5 | 4.8%                     | 14.1%               | 0.34                        | 265%                          | Q1-Q5               | 5.8%                     | 10.3%               | 0.56                        | 362%                          |  |

#### Momentum Naive and Pure Quintile Portfolio Performance

| Price M | lomen                    | tum Na              | ive Qu                      | intiles                       | Price I | Momen                    | tum Pı              | ıre Qui                     | ntiles                        |
|---------|--------------------------|---------------------|-----------------------------|-------------------------------|---------|--------------------------|---------------------|-----------------------------|-------------------------------|
|         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |
| Q1      | 3.7%                     | 10.9%               | 0.34                        | 328%                          | Q1      | 4.2%                     | 10.0%               | 0.43                        | 398%                          |
| 2       | 0.7%                     | 5.4%                | 0.13                        | 604%                          | 2       | 0.2%                     | 4.6%                | 0.04                        | 736%                          |
| 3       | -0.3%                    | 4.3%                | -0.08                       | 664%                          | 3       | -0.5%                    | 3.3%                | -0.15                       | 865%                          |
| 4       | -1.3%                    | 4.6%                | -0.27                       | 606%                          | 4       | -1.5%                    | 4.5%                | -0.34                       | 818%                          |
| Q5      | -2.8%                    | 13.2%               | -0.21                       | 335%                          | Q5      | -3.2%                    | 11.4%               | -0.28                       | 378%                          |
| Q1-Q5   | 6.5%                     | 22.3%               | 0.29                        | 664%                          | Q1-Q5   | 7.4%                     | 19.4%               | 0.38                        | 776%                          |

### Profitability Naive and Pure Quintile Portfolio Performance

| Prof  | fitabilit                | y Naive             | <b>Quint</b>                | iles                          | Pro   | fitabilit                | ty Pure             | Quinti                      | les                           |
|-------|--------------------------|---------------------|-----------------------------|-------------------------------|-------|--------------------------|---------------------|-----------------------------|-------------------------------|
|       | Avy.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |       | Avy.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |
| Q1    | 1.4%                     | 4.7%                | 0.31                        | 103%                          | Q1    | 3.3%                     | 5.6%                | 0.60                        | 245%                          |
| 2     | 1.0%                     | 4.0%                | 0.24                        | 150%                          | 2     | 2.2%                     | 3.7%                | 0.58                        | 576%                          |
| 3     | 0.2%                     | 4.0%                | 0.06                        | 173%                          | 3     | -0.7%                    | 3.3%                | -0.21                       | 743%                          |
| 4     | -0.4%                    | 3.5%                | -0.11                       | 168%                          | 4     | -1.5%                    | 2.9%                | -0.52                       | 527%                          |
| Q5    | -2.3%                    | 9.9%                | -0.23                       | 132%                          | Q5    | -3.0%                    | 6.7%                | -0.44                       | 188%                          |
| Q1-Q5 | 3.7%                     | 13.4%               | 0.28                        | 235%                          | Q1-Q5 | 6.3%                     | 9.3%                | 0.68                        | 433%                          |

### Quality Naive and Pure Quintile Portfolio Performance

| Earnin | gs Qua                   | lity Na             | ive Qui                     | ntiles                        | Earnir | ngs Qua                  | ality Pu            | re Quir                     | ntiles                        |
|--------|--------------------------|---------------------|-----------------------------|-------------------------------|--------|--------------------------|---------------------|-----------------------------|-------------------------------|
|        | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |        | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Return-to-<br>Risk<br>Ratio | Annual<br>One-Way<br>Turnover |
| Q1     | 3.4%                     | 4.5%                | 0.76                        | 183%                          | Q1     | 3.6%                     | 3.3%                | 1.09                        | 208%                          |
| 2      | 2.5%                     | 4.3%                | 0.58                        | 253%                          | 2      | 1.4%                     | 3.2%                | 0.43                        | 610%                          |
| 3      | 1.0%                     | 3.4%                | 0.28                        | 267%                          | 3      | 0.9%                     | 3.0%                | 0.30                        | 619%                          |
| 4      | -1.1%                    | 2.9%                | -0.39                       | 241%                          | 4      | -1.3%                    | 2.6%                | -0.52                       | 606%                          |
| Q5     | -5.8%                    | 8.1%                | -0.71                       | 169%                          | Q5     | -5.0%                    | 5.4%                | -0.92                       | 202%                          |
| Q1-Q5  | 9.2%                     | 11.0%               | 0.84                        | 352%                          | Q1-Q5  | 8.6%                     | 7.8%                | 1.11                        | 411%                          |

## Pure Quintile Portfolios Have Better Performance Net of T-Costs . . .

| Naive Q1-Q5<br>Portfolios | Gross of<br>T-Cost<br>Excess<br>Return | Net of T-<br>Cost<br>Excess<br>Return | Annualize<br>d Risk | Net of T-<br>Cost IR | Pure Q1-Q5<br>Portfolios | Gross of<br>T-Cost<br>Excess<br>Return | Net of T-<br>Cost<br>Excess<br>Return | Annualize<br>d Risk | Net of T-<br>Cost IR |
|---------------------------|--|---------------------------------------|---------------------|----------------------|--------------------------|--|---------------------------------------|---------------------|----------------------|
| Value                     | 3.7%                                   | 2.0%                                  | 15.7%               | 0.13                 | Value                    | 5.7%                                   | 2.5%                                  | 12.3%               | 0.21                 |
| Size                      | 4.8%                                   | 3.2%                                  | 14.1%               | 0.23                 | Size                     | 5.8%                                   | 3.6%                                  | 10.3%               | 0.35                 |
| Momentum                  | 6.5%                                   | 2.5%                                  | 22.3%               | 0.11                 | Momentum                 | 7.4%                                   | 2.8%                                  | 19.4%               | 0.14                 |
| Profitability             | 3.7%                                   | 2.3%                                  | 13.4%               | 0.17                 | Profitability            | 6.3%                                   | 3.7%                                  | 9.3%                | 0.40                 |
| Quality                   | 9.2%                                   | 7.1%                                  | 11.0%               | 0.65                 | Quality                  | 8.6%                                   | 6.1%                                  | 7.8%                | 0.79                 |

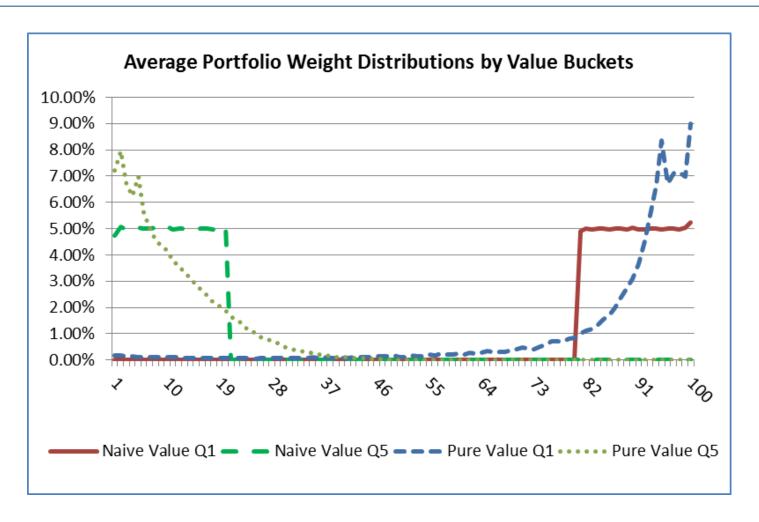
Transaction costs are assumed to be 30bps per trade one-way; returns and risks are annualized.

### ... or Rebalanced Quarterly

| Naive Q1-Q5<br>Portfolios | Gross of<br>T-Cost<br>Excess<br>Return | Net of T-<br>Cost<br>Excess<br>Return | Annualize<br>d Risk | Net of T-<br>Cost IR | Pure Q1-Q5<br>Portfolios | Gross of<br>T-Cost<br>Excess<br>Return | Net of T-<br>Cost<br>Excess<br>Return | Annualize<br>d Risk | Net of T-<br>Cost IR |
|---------------------------|--|---------------------------------------|---------------------|----------------------|--------------------------|--|---------------------------------------|---------------------|----------------------|
| Value                     | 2.1%                                   | 1.1%                                  | 17.7%               | 0.06                 | Value                    | 3.3%                                   | 1.7%                                  | 13.8%               | 0.12                 |
| Size                      | 3.7%                                   | 2.8%                                  | 14.8%               | 0.19                 | Size                     | 4.7%                                   | 3.5%                                  | 10.8%               | 0.32                 |
| Momentum                  | 6.3%                                   | 4.1%                                  | 23.2%               | 0.17                 | Momentum                 | 7.4%                                   | 4.9%                                  | 19.1%               | 0.26                 |
| Profitability             | 3.1%                                   | 2.0%                                  | 14.4%               | 0.14                 | Profitability            | 4.4%                                   | 2.8%                                  | 10.4%               | 0.27                 |
| Quality                   | 9.0%                                   | 7.3%                                  | 11.1%               | 0.66                 | Quality                  | 7.9%                                   | 6.1%                                  | 7.6%                | 0.81                 |

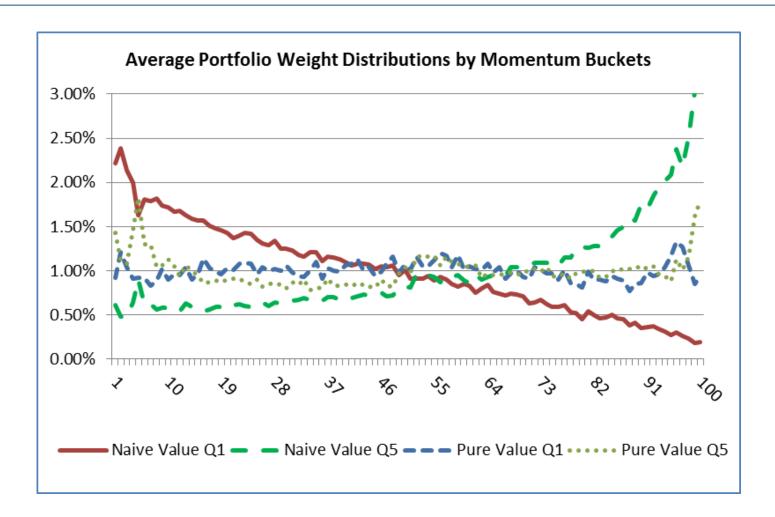
Transaction costs are assumed to be 30bps per trade one-way; returns and risks are annualized. Each quintile portfolio return is calculated as the average of 3 sub-portfolios created at the beginning of January, February and March of 1979 respectively. Each sub-portfolio is recreated every 3 months, and its return is calculated through the end of the 3-month period.

#### Pure and Naive Value Q1 & Q5 Portfolio Bucket Weights



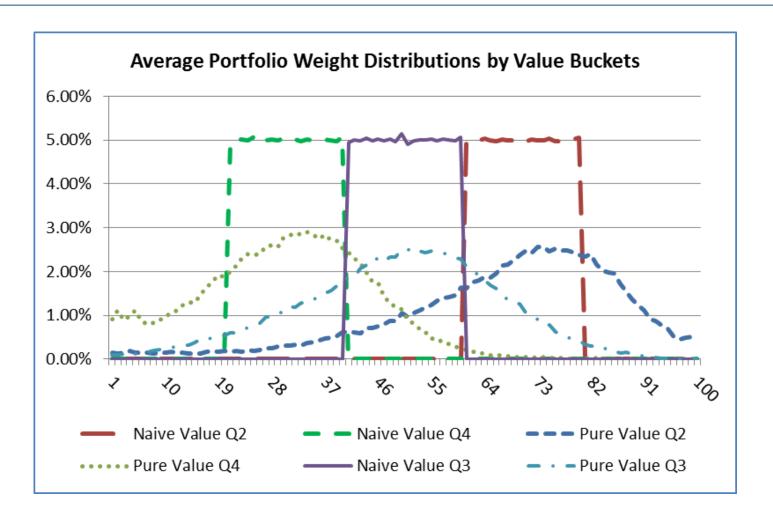
This chart shows average weight distributions of naive and pure Value Q1 & Q5 in buckets sorted by Value. Every month we sort by each factor and create 100 buckets, with bucket 1 having the lowest exposure and bucket 100 having the highest exposure. For each quintile portfolio we calculate the total percentage of its weights from each bucket in each month, and average over all months.

#### Pure Value Q1 & Q5 Portfolios Have Little Momentum Exposures



This chart shows average weight distributions of naive and pure Value Q1 & Q5 in buckets sorted by Price Momentum.

## Pure and Naive Value Q2/Q3/Q4 Portfolio Bucket Weights



This chart shows average weight distributions of naive and pure Value Q2, Q3 & Q4 in buckets sorted by Value.

# Pure Quintile Portfolios also Have Better Performance on International Developed Stocks . . .

| \     | /alue N                  | laive Qı            | uintiles              |                               | ,     | Value F                  | ure Qu              | intiles               |                               |
|-------|--------------------------|---------------------|-----------------------|-------------------------------|-------|--------------------------|---------------------|-----------------------|-------------------------------|
|       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |
| Q1    | 3.9%                     | 8.4%                | 0.47                  | 156%                          | Q1    | 6.4%                     | 8.6%                | 0.75                  | 323%                          |
| 2     | 0.7%                     | 3.6%                | 0.21                  | 261%                          | 2     | 2.1%                     | 3.4%                | 0.60                  | 590%                          |
| 3     | -1.3%                    | 2.8%                | -0.48                 | 265%                          | 3     | -0.8%                    | 2.7%                | -0.32                 | 665%                          |
| 4     | -2.0%                    | 3.6%                | -0.57                 | 212%                          | 4     | -2.9%                    | 3.6%                | -0.80                 | 491%                          |
| Q5    | -1.2%                    | 7.0%                | -0.17                 | 115%                          | Q5    | -3.9%                    | 7.1%                | -0.56                 | 195%                          |
| Q1-Q5 | 5.1%                     | 14.4%               | 0.35                  | 271%                          | Q1-Q5 | 10.4%                    | 12.8%               | 0.81                  | 518%                          |
|       |                          |                     |                       |                               |       |                          |                     |                       |                               |
|       | Size Na                  | aive Qu             | intiles               |                               |       | Size P                   | ure Qui             | ntiles                |                               |
|       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |
| Q1    | 1.4%                     | 6.0%                | 0.23                  | 128%                          | Q1    | 0.4%                     | 4.7%                | 0.09                  | 156%                          |
| 2     | -0.1%                    | 3.1%                | -0.03                 | 178%                          | 2     | 0.4%                     | 3.6%                | 0.12                  | 663%                          |
| 3     | -0.4%                    | 2.5%                | -0.17                 | 166%                          | 3     | 0.4%                     | 3.4%                | 0.13                  | 681%                          |
| 4     | -0.5%                    | 2.5%                | -0.20                 | 127%                          | 4     | 0.0%                     | 2.8%                | -0.01                 | 640%                          |
| Q5    | -0.4%                    | 4.8%                | -0.09                 | 67%                           | Q5    | 0.0%                     | 4.6%                | -0.01                 | 99%                           |
| Q1-Q5 | 1.8%                     | 9.9%                | 0.18                  | 195%                          | Q1-Q5 | 0.4%                     | 7.8%                | 0.06                  | 255%                          |

| Price N | /lomen                   | tum Na              | ive Qu                | intiles                       | Price N | Momen                    | ıtum Pı             | ıre Qui               | ntiles                        |
|---------|--------------------------|---------------------|-----------------------|-------------------------------|---------|--------------------------|---------------------|-----------------------|-------------------------------|
|         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |
| Q1      | 2.3%                     | 8.4%                | 0.27                  | 324%                          | Q1      | 2.9%                     | 7.9%                | 0.36                  | 385%                          |
| 2       | 1.4%                     | 4.8%                | 0.29                  | 612%                          | 2       | 2.1%                     | 4.4%                | 0.48                  | 780%                          |
| 3       | 0.7%                     | 3.4%                | 0.20                  | 665%                          | 3       | 0.7%                     | 2.8%                | 0.23                  | 895%                          |
| 4       | -0.8%                    | 3.7%                | -0.21                 | 606%                          | 4       | -1.9%                    | 3.8%                | -0.49                 | 825%                          |
| Q5      | -3.6%                    | 11.7%               | -0.30                 | 324%                          | Q5      | -4.1%                    | 10.9%               | -0.37                 | 383%                          |
| Q1-Q5   | 5.8%                     | 19.1%               | 0.30                  | 648%                          | Q1-Q5   | 6.9%                     | 17.6%               | 0.39                  | 767%                          |
| Prof    | fitabilit                | y Naive             | e Quint               | iles                          | Pro     | fitabili                 | ty Pure             | Quinti                | les                           |
|         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |
| Q1      | 1.9%                     | 5.4%                | 0.35                  | 93%                           | Q1      | 4.5%                     | 6.7%                | 0.68                  | 240%                          |
| 2       | 1.8%                     | 4.3%                | 0.41                  | 140%                          | 2       | 2.4%                     | 3.2%                | 0.76                  | 611%                          |
| 3       | 0.6%                     | 3.0%                | 0.19                  | 157%                          | 3       | -1.2%                    | 4.0%                | -0.29                 | 765%                          |
| 4       | -1.5%                    | 4.2%                | -0.35                 | 151%                          | 4       | -2.2%                    | 4.0%                | -0.55                 | 602%                          |
| Q5      | -2.6%                    | 7.7%                | -0.34                 | 120%                          | Q5      | -5.0%                    | 5.5%                | -0.92                 | 179%                          |
| Q1-Q5   | 4.5%                     | 12.3%               | 0.37                  | 213%                          | Q1-Q5   | 9.6%                     | 10.6%               | 0.90                  | 419%                          |
| Earnin  | igs Qua                  | lity Na             | ive Qui               | ntiles                        | Earnir  | ngs Qua                  | ality Pu            | re Quir               | ntiles                        |
|         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |
| Q1      | 1.6%                     | 3.6%                | 0.43                  | 134%                          | Q1      | 1.4%                     | 3.1%                | 0.46                  | 159%                          |
| 2       | 1.4%                     | 3.5%                | 0.39                  | 149%                          | 2       | 1.2%                     | 3.1%                | 0.38                  | 634%                          |
| 3       | 0.2%                     | 3.1%                | 0.08                  | 156%                          | 3       | 1.4%                     | 2.6%                | 0.52                  | 530%                          |
| 4       | -0.3%                    | 2.6%                | -0.11                 | 149%                          | 4       | -0.5%                    | 2.2%                | -0.24                 | 566%                          |
| Q5      | -2.9%                    | 5.4%                | -0.54                 | 127%                          | Q5      | -3.1%                    | 4.4%                | -0.69                 | 164%                          |
| Q1-Q5   | 4.5%                     | 7.5%                | 0.60                  | 261%                          | Q1-Q5   | 4.5%                     | 5.9%                | 0.76                  | 323%                          |

## ... and Emerging Markets Stocks

| Value Naive Quintiles |                          |                     |                       |                               | Value Pure Quintiles |                     |                          |                     |                       |                               |  |
|-----------------------|--------------------------|---------------------|-----------------------|-------------------------------|----------------------|---------------------|--------------------------|---------------------|-----------------------|-------------------------------|--|
|                       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |                      |                     | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |  |
| Q1                    | 5.9%                     | 10.1%               | 0.59                  | 175%                          |                      | Q1                  | 9.6%                     | 8.5%                | 1.14                  | 287%                          |  |
| 2                     | 1.9%                     | 4.2%                | 0.46                  | 286%                          |                      | 2                   | 1.3%                     | 4.2%                | 0.32                  | 685%                          |  |
| 3                     | -1.4%                    | 3.0%                | -0.48                 | 299%                          |                      | 3                   | -1.7%                    | 4.2%                | -0.41                 | 714%                          |  |
| 4                     | -2.5%                    | 4.9%                | -0.52                 | 251%                          |                      | 4                   | -4.5%                    | 5.6%                | -0.80                 | 551%                          |  |
| Q5                    | -3.7%                    | 7.9%                | -0.46                 | 140%                          |                      | Q5                  | -9.2%                    | 9.4%                | -0.98                 | 231%                          |  |
| Q1-Q5                 | 9.6%                     | 16.9%               | 0.57                  | 316%                          |                      | Q1-Q5               | 18.8%                    | 14.7%               | 1.27                  | 518%                          |  |
|                       |                          |                     |                       |                               |                      |                     |                          |                     |                       |                               |  |
| Size Naive Quintiles  |                          |                     |                       |                               |                      | Size Pure Quintiles |                          |                     |                       |                               |  |
|                       | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |                      |                     | Avg.<br>Annual<br>Excess | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |  |
| Q1                    | 1.9%                     | 10.9%               | 0.17                  | 155%                          |                      | Q1                  | 0.9%                     | 9.0%                | 0.11                  | 187%                          |  |
| 2                     | 0.5%                     | 3.8%                | 0.12                  | 229%                          |                      | 2                   | -0.6%                    | 4.7%                | -0.13                 | 554%                          |  |
| 3                     | 0.1%                     | 3.7%                | 0.02                  | 218%                          |                      | 3                   | -1.1%                    | 3.3%                | -0.33                 | 579%                          |  |
| 4                     | -0.2%                    | 4.4%                | -0.04                 | 172%                          |                      | 4                   | 1.2%                     | 4.3%                | 0.28                  | 716%                          |  |
| Q5                    | -1.8%                    | 5.3%                | -0.33                 | 93%                           |                      | Q5                  | -0.3%                    | 5.3%                | -0.05                 | 98%                           |  |
| Q1-Q5                 | 3.7%                     | 15.0%               | 0.24                  | 248%                          |                      | Q1-Q5               | 1.2%                     | 12.3%               | 0.10                  | 286%                          |  |

| Price Momentum Naive Quintiles   |                               |                     |                       |                               | Price I | Price Momentum Pure Quintiles   |                     |                       |                               |  |  |
|----------------------------------|-------------------------------|---------------------|-----------------------|-------------------------------|---------|---------------------------------|---------------------|-----------------------|-------------------------------|--|--|
|                                  | Avg.<br>Annual<br>Excess      | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess        | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |  |  |
| Q1                               | 5.2%                          | 9.2%                | 0.56                  | 319%                          | Q1      | 6.6%                            | 9.3%                | 0.71                  | 356%                          |  |  |
| 2                                | 1.6%                          | 5.9%                | 0.26                  | 601%                          | 2       | 1.7%                            | 5.0%                | 0.33                  | 812%                          |  |  |
| 3                                | -0.3%                         | 4.8%                | -0.07                 | 661%                          | 3       | -1.2%                           | 4.1%                | -0.29                 | 824%                          |  |  |
| 4                                | -3.2%                         | 4.5%                | -0.71                 | 610%                          | 4       | -3.9%                           | 5.0%                | -0.79                 | 780%                          |  |  |
| Q5                               | -3.2%                         | 12.5%               | -0.26                 | 340%                          | Q5      | -6.9%                           | 11.4%               | -0.60                 | 396%                          |  |  |
| Q1-Q5                            | 8.4%                          | 19.5%               | 0.43                  | 659%                          | Q1-Q5   | 13.5%                           | 18.5%               | 0.73                  | 752%                          |  |  |
|                                  |                               |                     |                       |                               |         |                                 |                     |                       |                               |  |  |
| Prof                             | Profitability Naive Quintiles |                     |                       |                               | Pro     | Profitability Pure Quintiles    |                     |                       |                               |  |  |
|                                  | Avg.<br>Annual<br>Excess      | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess        | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |  |  |
| Q1                               | 1.9%                          | 6.0%                | 0.32                  | 119%                          | Q1      | 2.9%                            | 7.2%                | 0.40                  | 236%                          |  |  |
| 2                                | 0.2%                          | 4.1%                | 0.05                  | 175%                          | 2       | 2.9%                            | 4.7%                | 0.62                  | 601%                          |  |  |
| 3                                | 1.0%                          | 4.0%                | 0.24                  | 189%                          | 3       | 1.6%                            | 4.2%                | 0.38                  | 694%                          |  |  |
| 4                                | 0.4%                          | 3.1%                | 0.12                  | 180%                          | 4       | -1.8%                           | 3.8%                | -0.46                 | 565%                          |  |  |
| Q5                               | -3.4%                         | 9.3%                | -0.37                 | 140%                          | Q5      | -7.1%                           | 7.9%                | -0.90                 | 182%                          |  |  |
| Q1-Q5                            | 5.3%                          | 14.0%               | 0.38                  | 259%                          | Q1-Q5   | 10.0%                           | 12.0%               | 0.83                  | 418%                          |  |  |
| Earnings Quality Naive Quintiles |                               |                     |                       |                               | Earnii  | Earnings Quality Pure Quintiles |                     |                       |                               |  |  |
|                                  | Avg.<br>Annual<br>Excess      | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |         | Avg.<br>Annual<br>Excess        | Annualize<br>d Risk | Informati<br>on Ratio | Annual<br>One-Way<br>Turnover |  |  |
| Q1                               | 0.3%                          | 5.2%                | 0.05                  | 140%                          | Q1      | 0.0%                            | 4.0%                | 0.00                  | 164%                          |  |  |
| 2                                | 1.5%                          | 3.9%                | 0.38                  | 154%                          | 2       | -0.3%                           | 4.3%                | -0.07                 | 709%                          |  |  |
| 3                                | 1.4%                          | 3.4%                | 0.41                  | 162%                          | 3       | 0.7%                            | 3.2%                | 0.21                  | 571%                          |  |  |
| 4                                | -0.5%                         | 3.5%                | -0.15                 | 159%                          | 4       | -0.8%                           | 4.0%                | -0.19                 | 660%                          |  |  |
| Q5                               | -2.6%                         | 6.3%                | -0.41                 | 142%                          | Q5      | -2.3%                           | 5.7%                | -0.41                 | 178%                          |  |  |
| Q1-Q5                            | 2.8%                          | 10.0%               | 0.28                  | 281%                          | Q1-Q5   | 2.3%                            | 8.4%                | 0.28                  | 342%                          |  |  |

#### Conclusion

- A common way to evaluate factors is to sort and create quintile portfolios
  - Does not control for exposures to other factors; does not reflect the efficacy of pure factor exposures
  - Existing techniques to disentangle factors either do not generalize to multiple factors, or do not extend to a spectrum of pure factor exposures
- We propose a new framework "Pure Quintile Portfolios" to address these issues
  - Adapt and extend the optimization used to create factor-mimicking portfolios
  - Each pure quintile portfolio has the same exposure to the target factor and the same number of stocks as the naive quintile portfolio, but has zero exposures to other factors
  - Strong evidence in the US that pure quintile portfolios have lower risks, and pure Q1-Q5 portfolios have lower risks, higher returns and higher Sharpe ratios than their naïve counterparts
  - The results hold after transaction costs
  - Similar but somewhat weaker results with International Developed and Emerging Market stocks

**Ding Liu** 

# Thank You!

### Are the Sharpe Ratio Differences Statistically Significant?

|               | G                                      | ross of T-Co                             | ost                           | Net of T-Cost                          |                                       |      |
|---------------|--|--|-------------------------------|--|---------------------------------------|------|
|               | Pure<br>minus<br>Naive SR<br>(Monthly) | Standard<br>Error of<br>SR<br>Difference | T-Stat of<br>SR<br>Difference | Pure<br>minus<br>Naive SR<br>(Monthly) | Standard<br>Error of SR<br>Difference |      |
| Value         | 6.5%                                   | 3.8%                                     | 1.69                          | 2.2%                                   | 3.9%                                  | 0.56 |
| Size          | 6.4%                                   | 2.5%                                     | 2.50                          | 3.5%                                   | 2.5%                                  | 1.38 |
| Profitability | 11.5%                                  | 4.1%                                     | 2.82                          | 6.5%                                   | 4.0%                                  | 1.64 |
| Momentum      | 2.6%                                   | 1.4%                                     | 1.95                          | 0.9%                                   | 1.3%                                  | 0.66 |
| Quality       | 7.8%                                   | 2.4%                                     | 3.32                          | 4.3%                                   | 2.2%                                  | 1.96 |

- "Comparing Sharpe Ratios: So where are the p-values?" by J.D. Opdyke, *Journal of Asset Management*, 8(5), Dec. 2007
- "The Statistics of Sharpe Ratios" by Andrew Lo, *Financial Analyst Journal, Vol. 58, No. 4, July/August 2002*