

Optimizer Series

Control Leverage in the Optimal Portfolio

Leverage is a popular tool portfolio managers use to potentially enhance the returns on their portfolios. One method to achieve leverage is to create a long/short portfolio; we call this financial leverage. When managing against a benchmark, leverage can also be achieved by holding positions that are riskier than those in the benchmark; we call this instrument leverage.

In this note, we show how both types of leverage can be handled by POINT's Optimizer. In particular, we illustrate how they can be managed alongside other quantitative portfolio objectives.

Changxiu Li
+1 212 526 1745
changxiu.li@barclays.com

Terrence Becker
+1 415 274 5417
terrence.becker@barclays.com

www.barclays.com

Introduction

Leverage is a technique used by investors trying to earn higher returns per unit of investment. A common example of a leverage strategy is the 130:30 equity portfolio, in which 130% of the net market value is owned long while 30% is held short. This example of leverage is referred to as financial leverage. For a portfolio managed against a benchmark, another type of leverage can be developed by holding riskier securities than the benchmark – these extra risks are typically associated with amplified returns (compared with the benchmark). A simple way to achieve this position is by holding securities with higher duration or beta with respect to the benchmark. This technique may be used in conjunction with financial leverage. We refer to this as instrument leverage because we choose instruments of a nature similar to those in the benchmark, but with higher volatility profiles. Both types of leverage are frequently used by asset managers and hedge funds in trading strategies that strive for high returns and are willing to incur the additional risk. Managed leverage could greatly enhance the portfolio's performance; however, excessive leverage could also be disastrous in an adverse tail event. For instance, financial leverage could lead to margin calls and forced liquidation at adverse prices.

POINT's Optimizer handles both types of leverage and is capable of answering questions such as: Given a hard leverage limit, how should long-short positions be allocated? How much long-short leverage is optimal for a given level of risk aversion? How much excess return may one achieve with risk tolerances higher than the one implied by our benchmark index? We provide examples of how to answer to these and other questions by setting optimization problems with leverage considerations in POINT's optimizer.

Leverage in POINT Optimizer

We assume that the readers are familiar with the basic functionalities of the Barclays' POINT Optimizer [for details see Kumar and Lazanas 2009]. The financial leverage ratio can be set as a hard target constraint in the common constraints window. Alternately, it can also be added as a term in the optimization objective function, by setting the leverage target as a soft constraint [see Kumar (2010) for the treatment of soft constraints]. Instrument leverage is implicitly contained in the TEV that can be added as both an objective term and constraint in the optimization. We provide examples of optimization setups for managing both types of leverage and analyze the resulting portfolios.

Financial Leverage

Financial leverage is calculated as the ratio of a portfolio's gross size to its net market value. For cash instruments, such as bonds and stocks, the gross size is simply the sum of the absolute value of the market value across securities. Because market value is not a meaningful measure of size for some derivative instruments, we instead use the duration basis attribute in POINT. Duration basis, based on a derivative's notional exposure, represents a derivative's fully funded market size and is equal to the market value for cash instruments. Portfolio gross size is the sum of the absolute value of the portfolio holdings' duration basis.

Setting the Leverage Target using the Portfolio Gross Size

To introduce leverage into the problem's specification, we start by specifying the maximum gross size (and thereby the leverage) as a common constraint in POINT's optimizer (see Figure 1). Later in the example we illustrate the leverage introduced through a soft constraint instead. Regarding the gross size, the leverage goal can be expressed in base currency units (setting "Measure" = Target) or as a percentage of final portfolio market value (setting "Measure" = % Final Portf MV). For example, to generate a long short 150:50 portfolio with net market value

equal to \$100,000,000, the constraint on gross size should be equal 200,000,000 using the first measure and 200 (%) using the second.

FIGURE 1

Maximum Gross Size Constraint

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change	0
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	% Final Portf MV	200,00
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target	
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio	% Final Portf MV	
<input checked="" type="checkbox"/>	Maximum number of trades		
<input checked="" type="checkbox"/>	Minimum trade size	Target	

Source: Barclays Research

Example 1: Optimization with Financial Leverage Constraint on Cash Bonds

We aim to construct a cash bond portfolio benchmarked to the Global Treasury index (EUR, GBP, USD, and JPY denominated bonds only). We want a portfolio containing bonds from this benchmark only. Therefore, we set the tradable universe to be the benchmark itself. The portfolio is potentially a long/short portfolio. The optimization goal is to deliver a portfolio with the highest expected return possible, where the expected return for each bond is assumed to be its yield to maturity. The initial portfolio is composed by \$100,000,000.

Without any additional constraints, the optimizer fails to deliver a feasible solution. It goes long the security with the highest return and short the one with the lowest return, with infinite leverage amount. To limit the potential solution, we set an additional constraint: an upper bound on the risk of the portfolio, specifically tracking error volatility (TEV) no larger than 40bp per month. The solution is now an optimal portfolio that achieves an expected return of 16.59% per year; has a TEV of 40bp per month; has a gross size exceeding 8.5bn; and contains 819 bonds (Figure 2).

FIGURE 2

Optimization Setup – Cash Bonds

Currency: USD - United States Dollar **As of:** ☐ Previous Close ☒ 12/31/2012 **Run** **Cancel** **Faq** **Help** **View Response Log** **View Request XML**

Benchmark: Global Treasury (EUR, GBP, US... **Profile:** DefaultProfile ☐ Commit Trades after Run

Tradable Universe Options

No.	Name	Type	Trade/Buy/Sell	Long/Short
1	Initial Portfolio	Initial Portfolio	Buy and Sell	Long Only
2	Global Treasury (EUR, GBP, USD, JPY... Index		Buy and Sell	Long/Short

Risk Model Options Sys Wgt, Idio Wgt, Def Wgt, Basis Points

Normalization

☒ Returns (bps) ☐ P&L (currency) **Benchmark MV** ☒ Do not scale ☐ Scale (Amount) ☐ Scale (Percent) **Scale To:**

Objectives (Robust Optimization available)

☐ Minimize ☒ Maximize

No.	Attribute	Measure	Weight	Unit	Initial Value	Realized Value
1	Expected Return [%]			% / yr	0.17	16.59
2	Total TEV	Net vs Bmark		bps / mo	158.93	40.00
3	Systematic TEV	Net vs Bmark		bps / mo	158.92	4.55
4	Idiosyncratic TEV	Net vs Bmark		bps / mo	1.00	39.74

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound	Unit	Realized Value
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change		0 USD	0
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	Target		USD	8,500,952,493
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target		USD	8,490,985,795
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio				819
<input checked="" type="checkbox"/>	Maximum number of trades				819
<input checked="" type="checkbox"/>	Minimum trade size	% Final Portfolio MV		USD	0

Constraints on values aggregated by Buckets

No.	Soft	Penalty	Attribute	Universe	Measure	Lower Bound	Upper Bound	Unit	Initial Value	Realized Value	Aggregation Rule
1	<input type="checkbox"/>		Total TEV	Final Portfolio	Net vs Bmark		40.00 bps ...		158.93	40.00	TOTAL_VARIANCE

Source: Barclays Research

Though theoretically feasible, this portfolio is uninvestable in three ways: first, it has 85x leverage, which is excessive for a typical portfolio; second, it has a large number of bonds, potentially incurring unreasonable transaction costs; and third, it sells bonds short in unrealistic amounts. Shorting bonds is not the most practical way to achieve leverage. Similar results can be achieved in more efficient ways by using derivatives such as futures and swaps.

Example 2: Optimization with Financial Leverage Constraint on Futures

To explore the use of derivatives, we change the tradable universe of the previous example to include instead a set of Treasury futures only. Specifically, the tradable universe contains 18 future contracts on Treasury bonds from the US, euro area, the UK, and Japan. Cash from each of the currencies is also included in the tradable universe, to facilitate matching FX exposure. For each futures contract, the expected return was proxied by the annualized total return of the corresponding cheapest-to-deliver bond over a 3-month unchanged curve scenario (Figure 3) ¹. The expected return of cash is set to be the short-term rate in each currency. Exchange rates are assumed to hold constant during this period.

¹ User can specify expected return through the field USER_EXPECTED_RETURN in the import User Defined Data Fields paste wizard.

FIGURE 3

Tradable Universe – Treasury Futures and Cash

Identifier	Description	Expected Return (%)
TYH13:CBT	10 year Treasury Notes	2.472
3YH13:CBT	3 year Treasury Notes	0.836
FWH13:CBT	5 year Treasury Notes	1.400
TUH13:CBT	2 year Treasury Notes	0.556
FBTPH13:UDE	Euro-BTP	1.483
FOATH13:UDE	Euro-OAT	3.364
FGBXH13:UDE	Euro-BUXL	2.348
FGBLH13:UDE	Euro-BUND	2.804
FGBMH13:UDE	Euro-BOBL	1.592
FGBSH13:UDE	Euro-SCHATZ	0.060
JGB1H13:TKS	10 year JGB	1.288
JMBH13:TKS	5yr JGB	0.384
USH13:CBT	30 year US Treasury Bonds	3.036
WNH13:CBT	US Ultra Long Term Treasury B...	3.120
GH13:LIF	Short Gilt	0.368
HH13:LIF	Medium Gilt	1.900
RH13:LIF	Long Gilt	2.976
FBTSH13:UDE	Short Euro-BTP	2.912
EUR	CASH - European Monetary Unit	0.014
GBP	CASH - Pounds Sterling	0.501
JPY	CASH - Japanese Yen	0.105
USD	CASH - U.S. Dollar	0.154

Source: Barclays Research.

Apart from the change in the tradable universe, all other parameters of the optimization problem are maintained: the optimizer select futures to maximize the expected return while keeping the total TEV against the G4 Treasury index less than 40bp per month. As before, the constraint on the total TEV rules out the unbounded solution that concentrates on extreme positions.

When we impose no leverage, the optimal portfolio contains only cash on each of the four currencies, with weights very similar to the benchmark and an expected return of 10bp. The Treasury bonds in the benchmark are exposed to both curve and FX risk factors. On a relative basis, the latter is riskier than the former. Therefore, the optimizer selects cash because it is the only instrument available in the tradable universe that provides FX exposure. Treasury futures, having no market value, hedge only the less important rate risk and are less useful than cash to hedge the benchmark total risk. When we relax the leverage constraint, allowing for unlimited leverage, the optimizer constructs a \$487,119,556 (notional) portfolio with an expected return of 5.56%, as shown in Figure 4.

FIGURE 4

Optimization Setup – Unlimited Leverage with Futures

Currency: USD - United States Dollar **As of:** ☐ Previous Close ☒ 12/31/2012 **Run** **Cancel** **FAQ** **Help** [View Response Log](#) [View Request XML](#)

Benchmark: Global Treasury (EUR, GBP, US... **Profile:** [DefaultProfile](#) ☐ Commit Trades after Run

Tradable Universe Options

No.	Name	Type	Trade/Buy/Sell	Long/Short
1	Initial Portfolio	Initial Portfolio	Buy and Sell	Long/Short
2	OPT Series: Leverage - Bond Futures	Portfolio	Buy and Sell	Long/Short

Risk Model Options [Sys Wgt](#), [Idio Wgt](#), [Def Wgt](#), [Basis Points](#)

Normalization

☒ Returns (bps) ☐ P&L (currency) **Benchmark MV** ☒ Do not scale ☐ Scale (Amount) ☐ Scale (Percent) **ScaleTo:**

Objectives (Robust Optimization available)

☐ Minimize ☒ Maximize

No.	Attribute	Measure	Weight	Unit	Initial Value	Realized Value
1	Expected Return [%]			1.00 % / yr	0.17	5.56
2	Total TEV	Net vs Bmark		0.00 bps / mo	158.93	40.00
3	Systematic TEV	Net vs Bmark		0.00 bps / mo	158.92	26.60
4	Idiosyncratic TEV	Net vs Bmark		0.00 bps / mo	1.00	29.70

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound	Unit	Realized Value
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change		0 USD	0
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	Target		USD	487,119,556
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target		USD	455,040,294
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio				22
<input checked="" type="checkbox"/>	Maximum number of trades				22
<input checked="" type="checkbox"/>	Minimum trade size	% Final Portfolio MV		USD	1

Constraints on values aggregated by Buckets

No.	Soft	Penalty	Attribute	Universe	Measure	Lower Bound	Upper Bound	Unit	Initial Value	Realized Value	Aggregation Rule
1	<input type="checkbox"/>		Total TEV	Final Portfolio	Net vs Bmark		40.00 bps ...		158.93	40.00	TOTAL_VARIANCE

Source: Barclays Research.

Although much more intuitive, the solution above, with almost 5x leverage in our example may still exceed the leverage appetite of most portfolio managers. One may therefore want to impose a direct limit on the maximum leverage. One way to do that using the POINT's Optimizer is by setting the gross size of the final portfolio, as shown before (see Figure 1). Recall that throughout this exercise we have imposed the market value of the final portfolio to be \$100mn. By setting its gross size to \$200mn, we establish a maximum leverage of 2x.

Figure 5 shows the problem setup and some characteristics of its solution – the final optimal portfolio – under the new leverage constraint. Comparing the solution with the one from the unconstrained case, we can see that the expected return reduces to 3.20% (from 5.56%). Note also that in this case, the leverage constraint reduces the portfolio concentrations on individual instruments. In our example, this leads to the reduction of the idiosyncratic TEV (from 29.7bp to 13.3bp), indicating an improved portfolio diversification.

FIGURE 5
Optimization Setup – 2x Leverage with Futures

Currency: USD - United States Dollar **As of:** ☐ Previous Close ☒ 12/31/2012 **Run** **Cancel** **Results available**

Benchmark: Global Treasury (EUR, GBP, US... **Faq** **Help** **View Response Log** **View Request XML**

Profile: DefaultProfile ☐ Commit Trades after Run

Tradable Universe Options

No.	Name	Type	Trade/Buy/Sell	Long/Short
1	Initial Portfolio	Initial Portfolio	Buy and Sell	Long/Short
2	OPT Series: Leverage - Bond Futures	Portfolio	Buy and Sell	Long/Short

Risk Model Options Sys Wgt, Idio Wgt, Def Wgt, Basis Points

Normalization

☒ Returns (bps) ☐ P&L (currency) **Benchmark MV** ☐ Do not scale ☐ Scale (Amount) ☒ Scale (Percent) **ScaleTo:** 100.00 %

Objectives (Robust Optimization available)

☐ Minimize ☒ Maximize

No.	Attribute	Measure	Weight	Unit	Initial Value	Realized Value
1	Expected Return [%]			1.00 % / yr	0.17	3.20
2	Total TEV	Net vs Bmark		0.00 bps / mo	158.93	40.00
3	Systematic TEV	Net vs Bmark		0.00 bps / mo	158.92	37.71
4	Idiosyncratic TEV	Net vs Bmark		0.00 bps / mo	1.00	13.33

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound	Unit	Realized Value
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change		0 USD	0
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	Target		200,000,000 USD	200,000,000
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target		USD	177,081,498
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio				19
<input checked="" type="checkbox"/>	Maximum number of trades				19
<input checked="" type="checkbox"/>	Minimum trade size	% Final Portfolio MV		USD	0

Constraints on values aggregated by Buckets

No.	Soft	Penalty	Attribute	Universe	Measure	Lower Bound	Upper Bound	Unit	Initial Value	Realized Value	Aggregation Rule
1	<input type="checkbox"/>		Total TEV	Final Portfolio	Net vs Bmark		40.00	bps ...	158.93	40.00	TOTAL_VARIANCE

Source: Barclays Research

Setting the Leverage Target as a Soft Constraint

Up to this point, we have been setting leverage by controlling the gross size of the portfolio explicitly. POINT offers another way to attain this goal. Leverage can be incorporated by augmenting the mean-variance optimization objective function with a leverage aversion penalty. In POINT's optimizer, this can be achieved by adding a soft constraint on the absolute duration basis of the final portfolio. Soft constraints are appended into the optimization objective function, with a particular penalty term. This term manages how costly it is for the final solution to violate the constraint [see Kumar (2009)].

When setting this constraint, the user should “right-click” and select the absolute sum option under aggregation rule (Figure 6). The user can enter a lower bound and an upper bound for his desired leverage amount. The soft constraint penalty factor expresses the leverage aversion. The higher the penalty value, the higher is the cost given to a leverage constraint violation. In an extreme, a soft constraint with a very large penalty is equivalent to a hard constraint. For illustration, we set the penalty weight to one (its default value).

FIGURE 6

Soft Constraint on Financial Leverage

Setup Generic Constraints Round Lots No Trade List Trade List Final Portfolio Warnings/Exclusions									
Constraints on values aggregated by Buckets									
No.	Soft	Penalty	Attribute	Universe	Measure	Lower Bound	Upper Bound	Unit	Aggregation Rule
1	<input checked="" type="checkbox"/>		Duration Basis	Final Portfolio	Absolute		200,000,000 USD		Absolute Sum
2	<input type="checkbox"/>		Total TEV	Final Portfolio	Net vs Bmark		40.00 bps / mo		TOTAL_VARIANCE

Source: Barclays Research

Example 3: Optimization with Financial Leverage Soft Constraint

To illustrate the soft constraint feature, we modify the setup of Example 2. Specifically, we do not impose any constraint on the gross size on the portfolio. Instead, we use the exact soft constraint as is displayed in Figure 6. The results from this new optimization problem are displayed in Figure 7. The optimal solution breaches the soft target of \$200mn gross size by almost 50% (the gross size is \$296mn, for a leverage ratio of 3x). The expected return is higher, at 5% (from 3.2% previously) and the idiosyncratic risk also increased. Note that the optimal leverage level is solved together with the optimal portfolio holdings, when using the soft constraint. The POINT optimizer easily incorporates this type of functionality, which is discussed in Jacobs & Levy (2011). An iterative use of this framework – namely by using different values for the penalty violation – allows the user to find the right trade-off between expected return, gross size, and risk.

FIGURE 7

Optimization Setup – 2x Leverage Soft Constraints

Currency: USD - United States Dollar As of: Previous Close 12/31/2012 Run Cancel Results available

Benchmark: Global Treasury (EUR, GBP, US...)

Profile: DefaultProfile ☐ Commit Trades after Run

Tradable Universe Options

No.	Name	Type	Trade/Buy/Sell	Long/Short
1	Initial Portfolio	Initial Portfolio	Buy and Sell	Long/Short
2	OPT Series: Leverage - Bond Futures	Portfolio	Buy and Sell	Long/Short

Risk Model Options Sys Wgt, Idio Wgt, Def Wgt, Basis Points

Normalization

☒ Returns (bps) ☐ P&L (currency) Benchmark MV ☐ Do not scale ☐ Scale (Amount) ☒ Scale (Percent) ScaleTo: 100.00 %

Objectives (Robust Optimization available)

☐ Minimize ☒ Maximize

No.	Attribute	Measure	Weight	Unit	Initial Value	Realized Value
1	Expected Return [%]		1.00	% / yr	0.17	5.00
2	Total TEV	Net vs Bmark		0.00 bps / mo	158.93	40.00
3	Systematic TEV	Net vs Bmark		0.00 bps / mo	158.92	31.47
4	Idiosyncratic TEV	Net vs Bmark		0.00 bps / mo	1.00	24.69

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound	Unit	Realized Value
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change		0 USD	-11
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	Target		USD	295,928,745
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target		USD	266,676,905
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio				22
<input checked="" type="checkbox"/>	Maximum number of trades				22
<input checked="" type="checkbox"/>	Minimum trade size	% Final Portfolio MV		USD	0

Constraints on values aggregated by Buckets

No.	Soft	Penalty	Attribute	Universe	Measure	Lower Bound	Upper Bound	Unit	Initial Value	Realized Value	Aggregation Rule
1	<input checked="" type="checkbox"/>		Duration Basis	Final Portfolio	Absolute		200,000,000 USD		100,000,000	295,928,745	Absolute Sum
2	<input type="checkbox"/>		Total TEV	Final Portfolio	Net vs Bmark		40.00 bps / mo		158.93	40.00	TOTAL_VARIANCE

Source: Barclays Research

Instrument Leverage

A portfolio consisting of riskier assets than a benchmark (such as stocks with higher beta or bonds with longer durations or higher spreads) can be constructed so that its portfolio forecasted volatility is a specified multiple of the benchmark. This feature is especially useful when the portfolio manager does not have a specific return forecast on the security level, but rather seeks a broad tilt to the portfolio. For instance, an equity manager may forecast positive market returns, and therefore want to increase the beta of its portfolio versus a benchmark. The following example shows how to select riskier assets out of an index in exchange for the potential higher return. The instrument leverage can be applied on its own, or in combination with financial leverage.

Example 4: Optimization with Instrument Leverage

Consider the case of a portfolio manager who is comfortable with the systematic exposures of a particular index. However, given her return targets or risk tolerance, she needs to leverage those exposures. Specifically, suppose that her goal requires twice the volatility of the current benchmark. In what follows we show how to construct this kind of portfolio using POINT's Optimizer.

There is one straightforward way to construct a portfolio with the required characteristics: Start by leveraging the required benchmark by shorting cash on that benchmark. For instance, for a 2x levered version of the benchmark, a user can short 50% of the benchmark market value. Then use the optimizer to construct a portfolio tracking the leveraged benchmark. Though simple, this technique involves two steps and needs adjustments as the market value of the benchmark changes. Fortunately, the Optimizer allows a simpler way of performing this exercise.

The Optimizer provides easy manipulation of the treatment of benchmarks along the dimensions required for this exercise. The default optimization set-up is to work with relative market weights (on the return space). This makes the comparison of large market value benchmarks with smaller portfolios meaningful. However, for some exercises, like hedging or liability matching, the absolute size of the benchmark (e.g., liabilities) is the relevant variable. In this case, the optimization can be performed instead with nominal exposures (i.e., in P&L terms). We can use this flexibility to solve the problem at hand.

The P&L normalization option includes a scaling factor for the benchmark market value. The default scale is 100%, meaning the P&L exposures of the benchmark are scaled so to match (on duration basis terms) those of the initial portfolio (\$100mn as in the example). By adjusting this factor, the user can target any multiple of the benchmark exposure. In our case, we do that through a minimization of the scaled TEV in P&L space. To construct a portfolio with volatility target leverage of twice the benchmark, P&L normalization should be selected with the scaling set to 200%, so that the \$100mn portfolio replicates the risk exposure of a \$200mn benchmark, as highlighted in Figure 8.

FIGURE 8

Optimization Setup – 2x Volatility Target

Currency: USD - United States Dollar **As of:** ☐ Previous Close ☒ 12/31/2012 **Run** **Cancel** **Results available**

Benchmark: Global Treasury (EUR, GBP, US... **Faq** **Help** **View Response Log** **View Request XML**

Profile: DefaultProfile ☐ Commit Trades after Run

Tradable Universe Options

No.	Name	Type	Trade/Buy/Sell	Long/Short
1	Initial Portfolio	Initial Portfolio	Buy and Sell	Long/Short
2	OPT Series: Leverage - Bond Futures	Portfolio	Buy and Sell	Long/Short

Risk Model Options: Sys Wgt, Idio Wgt, Def Wgt, PL, Benchmark Custom-Scaled to 200% of Portfolio MV

Normalization

☐ Returns (bps) ☒ P&L (currency) ☐ Benchmark MV ☐ Do not scale ☐ Scale (Amount) ☒ Scale (Percent) **ScaleTo:** 200.00 %

Objectives (Robust Optimization available)

☒ Minimize ☐ Maximize

No.	Attribute	Measure	Weight	Unit	Initial Value	Realized Value
1	Total TEV	Net vs Bmark	1.00	USD / mo	3,178,500.00	264,426.18
2	Systematic TEV	Net vs Bmark	0.00	USD / mo	3,178,440.00	222,257.02
3	Idiosyncratic TEV	Net vs Bmark	0.00	USD / mo	20,008.30	143,258.59

Common Constraints

Final Portfolio Cash (base currency): ☒ Long/Short ☐ Long Only ☐ Short Only ☐ No Cash

E...	Description	Measure	Bound	Unit	Realized Value
<input checked="" type="checkbox"/>	Budget: Final Portfolio Market Value	Change		0 USD	0
<input checked="" type="checkbox"/>	Final portfolio maximum gross size	Target		USD	440,386,463
<input checked="" type="checkbox"/>	Turnover: Maximum gross size of trades	Target		USD	395,695,190
<input checked="" type="checkbox"/>	Maximum number of securities in final portfolio				22
<input checked="" type="checkbox"/>	Maximum number of trades				22
<input checked="" type="checkbox"/>	Minimum trade size	Target		USD	717,144

Source: Barclays Research

In this example we use the same \$100mn initial portfolio and tradable universe of government bond futures and cash. The objective is set to minimize the Total TEV versus a benchmark that doubles the risk exposures of the G4 Treasury index.

FIGURE 9

Risk and Analytics

	G4 Treasury	1x Vol Target Portfolio	2x Vol Target Portfolio
Risk Metrics			
total Volatility	158.9	158.4	316.7
Systematic Vol	158.9	158.2	316.4
Idiosyncratic Vol	1	7.1	14.2
OAD	7	6	11.9
OASD	6.8	5.9	11.8
OAS	36.5	39	53
FX Exposure			
EUR	29.4	30.6	61.1
JPY	32.9	34.1	68.2
GBP	8.6	7.7	15.4
Expected Return			
	1.2	2.3	4.5
Gross Size			
	1x	2.3x	4.4x

Source: Barclays Research

Figure 9 summarizes the risk metrics and key analytics between the benchmark, the optimized portfolio that replicates 100% of the G4 Treasury index and the optimized portfolio with double risk exposure to that index. The portfolio with 1x target leverage matches well the benchmark across major risk metrics: OAD, OASD and the FX exposures. As expected, the portfolio with 2x target leverage has twice the exposures seen in the benchmark. Consequently the total volatility of the 2x portfolio, at 316.7bp per month, is twice that of the benchmark.

References

Kumar, A. and Lazanas, A. (2009), *Barclays Capital Portfolio Optimizer: User Guide, Portfolio Modelling*, Barclays Research

Kumar, A. (2010), *Barclays Capital Portfolio Optimizer: Soft Constraints, Portfolio Modelling*, Barclays Research.

Jacobs, B. and Levey, K. (2011), "Leverage Aversion and Portfolio Optimality," *Financial Analysts Journal*, Volume 68, No 5.

Analyst Certification

We, Terrence Becker and Changxiu Li, hereby certify (1) that the views expressed in this research report accurately reflect our personal views about any or all of the subject securities or issuers referred to in this research report and (2) no part of our compensation was, is or will be directly or indirectly related to the specific recommendations or views expressed in this research report.

Important Disclosures:

Barclays Research is a part of the Corporate and Investment Banking division of Barclays Bank PLC and its affiliates (collectively and each individually, "Barclays"). For current important disclosures regarding companies that are the subject of this research report, please send a written request to: Barclays Research Compliance, 745 Seventh Avenue, 17th Floor, New York, NY 10019 or refer to <http://publicresearch.barcap.com> or call 212-526-1072.

Barclays Capital Inc. and/or one of its affiliates does and seeks to do business with companies covered in its research reports. As a result, investors should be aware that Barclays may have a conflict of interest that could affect the objectivity of this report. Barclays Capital Inc. and/or one of its affiliates regularly trades, generally deals as principal and generally provides liquidity (as market maker or otherwise) in the debt securities that are the subject of this research report (and related derivatives thereof). Barclays trading desks may have either a long and / or short position in such securities and / or derivative instruments, which may pose a conflict with the interests of investing customers. Where permitted and subject to appropriate information barrier restrictions, Barclays fixed income research analyst(s) regularly interact with its trading desk personnel to determine current prices of fixed income securities. Barclays fixed income research analyst(s) receive compensation based on various factors including, but not limited to, the quality of their work, the overall performance of the firm (including the profitability of the investment banking department), the profitability and revenues of the Fixed Income, Currencies and Commodities Division ("FICC") and the outstanding principal amount and trading value of, the profitability of, and the potential interest of the firms investing clients in research with respect to, the asset class covered by the analyst. To the extent that any historical pricing information was obtained from Barclays trading desks, the firm makes no representation that it is accurate or complete. All levels, prices and spreads are historical and do not represent current market levels, prices or spreads, some or all of which may have changed since the publication of this document. The Corporate and Investment Banking division of Barclays produces a variety of research products including, but not limited to, fundamental analysis, equity-linked analysis, quantitative analysis, and trade ideas. Recommendations contained in one type of research product may differ from recommendations contained in other types of research products, whether as a result of differing time horizons, methodologies, or otherwise. In order to access Barclays Statement regarding Research Dissemination Policies and Procedures, please refer to <https://live.barcap.com/publiccp/RSR/nyfipubs/disclaimer/disclaimer-research-dissemination.html>.

Disclaimer

This publication has been prepared by the Corporate and Investment Banking division of Barclays Bank PLC and/or one or more of its affiliates (collectively and each individually, "Barclays"). It has been issued by one or more Barclays legal entities within its Corporate and Investment Banking division as provided below. It is provided to our clients for information purposes only, and Barclays makes no express or implied warranties, and expressly disclaims all warranties of merchantability or fitness for a particular purpose or use with respect to any data included in this publication. Barclays will not treat unauthorized recipients of this report as its clients. Prices shown are indicative and Barclays is not offering to buy or sell or soliciting offers to buy or sell any financial instrument.

Without limiting any of the foregoing and to the extent permitted by law, in no event shall Barclays, nor any affiliate, nor any of their respective officers, directors, partners, or employees have any liability for (a) any special, punitive, indirect, or consequential damages; or (b) any lost profits, lost revenue, loss of anticipated savings or loss of opportunity or other financial loss, even if notified of the possibility of such damages, arising from any use of this publication or its contents.

Other than disclosures relating to Barclays, the information contained in this publication has been obtained from sources that Barclays Research believes to be reliable, but Barclays does not represent or warrant that it is accurate or complete. Barclays is not responsible for, and makes no warranties whatsoever as to, the content of any third-party web site accessed via a hyperlink in this publication and such information is not incorporated by reference.

The views in this publication are those of the author(s) and are subject to change, and Barclays has no obligation to update its opinions or the information in this publication. The analyst recommendations in this publication reflect solely and exclusively those of the author(s), and such opinions were prepared independently of any other interests, including those of Barclays and/or its affiliates. This publication does not constitute personal investment advice or take into account the individual financial circumstances or objectives of the clients who receive it. The securities discussed herein may not be suitable for all investors. Barclays recommends that investors independently evaluate each issuer, security or instrument discussed herein and consult any independent advisors they believe necessary. The value of and income from any investment may fluctuate from day to day as a result of changes in relevant economic markets (including changes in market liquidity). The information herein is not intended to predict actual results, which may differ substantially from those reflected. Past performance is not necessarily indicative of future results.

This communication is being made available in the UK and Europe primarily to persons who are investment professionals as that term is defined in Article 19 of the Financial Services and Markets Act 2000 (Financial Promotion Order) 2005. It is directed at, and therefore should only be relied upon by, persons who have professional experience in matters relating to investments. The investments to which it relates are available only to such persons and will be entered into only with such persons. Barclays Bank PLC is authorised and regulated by the Financial Services Authority ("FSA") and a member of the London Stock Exchange.

The Corporate and Investment Banking division of Barclays undertakes U.S. securities business in the name of its wholly owned subsidiary Barclays Capital Inc., a FINRA and SIPC member. Barclays Capital Inc., a U.S. registered broker/dealer, is distributing this material in the United States and, in connection therewith accepts responsibility for its contents. Any U.S. person wishing to effect a transaction in any security discussed herein should do so only by contacting a representative of Barclays Capital Inc. in the U.S. at 745 Seventh Avenue, New York, New York 10019.

Non-U.S. persons should contact and execute transactions through a Barclays Bank PLC branch or affiliate in their home jurisdiction unless local regulations permit otherwise.

Barclays Bank PLC, Paris Branch (registered in France under Paris RCS number 381 066 281) is regulated by the Autorité des marchés financiers and the Autorité de contrôle prudentiel. Registered office 34/36 Avenue de Friedland 75008 Paris.

This material is distributed in Canada by Barclays Capital Canada Inc., a registered investment dealer and member of IIROC (www.iroc.ca).

Subject to the conditions of this publication as set out above, Absa Capital, the Investment Banking Division of Absa Bank Limited, an authorised financial services provider (Registration No.: 1986/004794/06. Registered Credit Provider Reg No NCRCP7), is distributing this material in South Africa. Absa Bank

Limited is regulated by the South African Reserve Bank. This publication is not, nor is it intended to be, advice as defined and/or contemplated in the (South African) Financial Advisory and Intermediary Services Act, 37 of 2002, or any other financial, investment, trading, tax, legal, accounting, retirement, actuarial or other professional advice or service whatsoever. Any South African person or entity wishing to effect a transaction in any security discussed herein should do so only by contacting a representative of Absa Capital in South Africa, 15 Alice Lane, Sandton, Johannesburg, Gauteng 2196. Absa Capital is an affiliate of Barclays.

In Japan, foreign exchange research reports are prepared and distributed by Barclays Bank PLC Tokyo Branch. Other research reports are distributed to institutional investors in Japan by Barclays Securities Japan Limited. Barclays Securities Japan Limited is a joint-stock company incorporated in Japan with registered office of 6-10-1 Roppongi, Minato-ku, Tokyo 106-6131, Japan. It is a subsidiary of Barclays Bank PLC and a registered financial instruments firm regulated by the Financial Services Agency of Japan. Registered Number: Kanto Zaimukyokuchō (kinsho) No. 143.

Barclays Bank PLC, Hong Kong Branch is distributing this material in Hong Kong as an authorised institution regulated by the Hong Kong Monetary Authority. Registered Office: 41/F, Cheung Kong Center, 2 Queen's Road Central, Hong Kong.

This material is issued in Taiwan by Barclays Capital Securities Taiwan Limited. This material on securities not traded in Taiwan is not to be construed as 'recommendation' in Taiwan. Barclays Capital Securities Taiwan Limited does not accept orders from clients to trade in such securities. This material may not be distributed to the public media or used by the public media without prior written consent of Barclays.

This material is distributed in South Korea by Barclays Capital Securities Limited, Seoul Branch.

All equity research material is distributed in India by Barclays Securities (India) Private Limited (SEBI Registration No: INB/INF 231292732 (NSE), INB/INF 011292738 (BSE), Registered Office: 208 | Ceejay House | Dr. Annie Besant Road | Shivsagar Estate | Worli | Mumbai - 400 018 | India, Phone: + 91 22 67196363). Other research reports are distributed in India by Barclays Bank PLC, India Branch.

Barclays Bank PLC Frankfurt Branch distributes this material in Germany under the supervision of Bundesanstalt für Finanzdienstleistungsaufsicht (BaFin).

This material is distributed in Malaysia by Barclays Capital Markets Malaysia Sdn Bhd.

This material is distributed in Brazil by Banco Barclays S.A.

This material is distributed in Mexico by Barclays Bank Mexico, S.A.

Barclays Bank PLC in the Dubai International Financial Centre (Registered No. 0060) is regulated by the Dubai Financial Services Authority (DFSA). Principal place of business in the Dubai International Financial Centre: The Gate Village, Building 4, Level 4, PO Box 506504, Dubai, United Arab Emirates. Barclays Bank PLC-DIFC Branch, may only undertake the financial services activities that fall within the scope of its existing DFSA licence. Related financial products or services are only available to Professional Clients, as defined by the Dubai Financial Services Authority.

Barclays Bank PLC in the UAE is regulated by the Central Bank of the UAE and is licensed to conduct business activities as a branch of a commercial bank incorporated outside the UAE in Dubai (Licence No.: 13/1844/2008, Registered Office: Building No. 6, Burj Dubai Business Hub, Sheikh Zayed Road, Dubai City) and Abu Dhabi (Licence No.: 13/952/2008, Registered Office: Al Jazira Towers, Hamdan Street, PO Box 2734, Abu Dhabi).

Barclays Bank PLC in the Qatar Financial Centre (Registered No. 00018) is authorised by the Qatar Financial Centre Regulatory Authority (QFCRA). Barclays Bank PLC-QFC Branch may only undertake the regulated activities that fall within the scope of its existing QFCRA licence. Principal place of business in Qatar: Qatar Financial Centre, Office 1002, 10th Floor, QFC Tower, Diplomatic Area, West Bay, PO Box 15891, Doha, Qatar. Related financial products or services are only available to Business Customers as defined by the Qatar Financial Centre Regulatory Authority.

This material is distributed in the UAE (including the Dubai International Financial Centre) and Qatar by Barclays Bank PLC.

This material is distributed in Saudi Arabia by Barclays Saudi Arabia ('BSA'). It is not the intention of the publication to be used or deemed as recommendation, option or advice for any action (s) that may take place in future. Barclays Saudi Arabia is a Closed Joint Stock Company, (CMA License No. 09141-37). Registered office Al Faisaliah Tower, Level 18, Riyadh 11311, Kingdom of Saudi Arabia. Authorised and regulated by the Capital Market Authority, Commercial Registration Number: 1010283024.

This material is distributed in Russia by OOO Barclays Capital, affiliated company of Barclays Bank PLC, registered and regulated in Russia by the FSFM. Broker License #177-11850-100000; Dealer License #177-11855-010000. Registered address in Russia: 125047 Moscow, 1st Tverskaya-Yamskaya str. 21.

This material is distributed in Singapore by the Singapore branch of Barclays Bank PLC, a bank licensed in Singapore by the Monetary Authority of Singapore. For matters in connection with this report, recipients in Singapore may contact the Singapore branch of Barclays Bank PLC, whose registered address is One Raffles Quay Level 28, South Tower, Singapore 048583.

Barclays Bank PLC, Australia Branch (ARBN 062 449 585, AFSL 246617) is distributing this material in Australia. It is directed at 'wholesale clients' as defined by Australian Corporations Act 2001.

IRS Circular 230 Prepared Materials Disclaimer: Barclays does not provide tax advice and nothing contained herein should be construed to be tax advice. Please be advised that any discussion of U.S. tax matters contained herein (including any attachments) (i) is not intended or written to be used, and cannot be used, by you for the purpose of avoiding U.S. tax-related penalties; and (ii) was written to support the promotion or marketing of the transactions or other matters addressed herein. Accordingly, you should seek advice based on your particular circumstances from an independent tax advisor.

© Copyright Barclays Bank PLC (2013). All rights reserved. No part of this publication may be reproduced in any manner without the prior written permission of Barclays. Barclays Bank PLC is registered in England No. 1026167. Registered office 1 Churchill Place, London, E14 5HP. Additional information regarding this publication will be furnished upon request.

