Centrality of the Supply Chain Network

Liuren Wu<sup>a</sup>\*

<sup>a</sup>Baruch College, Zicklin School of Business, One Bernard Baruch Way, New York, NY 10010, USA

First draft: May 15, 2015; This version: October 14, 2015

**Abstract** 

With the increasing availability of supply chain information, researchers are paying increasing attention

to information flows and interactions between suppliers and customers. Shocks to a supplier not only impact

its immediate customers, but also generate ripple effects on the whole economy through the supply chain

network. This paper strives to define the relative importance, or centrality, of a supplier in the whole supply

chain network, and understand how the most central suppliers to the economy behave differently, and how

they interact with the aggregate economy and the business cycle. Based on information from the FactSet

Supply Chain Relationships database, the paper builds a supplier-customer network matrix at the beginning

of each year from 2004 to 2014, and computes the supplier centralities of each company based on a list

of centrality definitions. The paper then forms supplier central stock portfolios based on the centrality estimates, and perform historical analysis on their behaviors. Analysis shows that supplier central portfolios

tend to be more volatile than average, and the stock performance of supplier central portfolios tends to

predict the movements of the overall stock market.

JEL Classification: G10, G14.

Keywords: Supply chain, directed network, degree centrality, eigenvector centrality, PageRank, Kleinberg

centrality

I thank Jeremy Zhou of FactSet Revere for making the FactSet Revere supply-chain data available for my re-

search and for many helpful discussions, Manoj Boolani of FactSet Research Systems for many references and helpful

discussions, Yafeng Yin for technical assistance with data processing, Jeremy Bertomeu, Clarence Kwan, Chen Li,

Terrence Martell, Joseph Weintrop, Weina Zhang, Dexin Zhou, and seminar participants at the 5th Annual SWUFE

Baruch Research Symposium for their comments and suggestions.

\*Tel.: +1-646-312-3509. E-mail: liuren.wu@baruch.cuny.edu.

# Contents

1	Intro	oduction	1
2	Data	a Source and Sample Construction	3
3	Supj	ply Chain Centrality Measures	4
	3.1	Degree centrality: The number of companies that the supplier serves	5
	3.2	Eigenvector centrality: The importance of customers as suppliers	6
	3.3	Kleinberg centrality: The importance of customers as economic hubs	7
4	Cent	tral Suppliers of the U.S. Economy	9
	4.1	Distributional behaviors	10
	4.2	The top ten list	11
	4.3	The statistical behavior of central stock portfolios	12
	4.4	Market response propagation to shocks from the top ten companies	13
5	Con	cluding remarks	14

### 1. Introduction

Researchers increasingly appreciate the important role structural relations and connections play in understanding the statistical relations of financial securities from different companies. Such structural relations include, for example, similarities in the underlying business, as often captured by industry classification and peer group identification. Stock returns from the same industry/peer group tend to move more closely together. Similarly, when analyzing the behavior of a particular company, financial analysts and investors o pay close attention to the company's major suppliers and customers, from which they strive to infer the potential risks and opportunities for the company.<sup>2</sup> The closure or production delay of a major supplier can cause significant issues for the company's production, whereas the changing demand of the customer base poses challenges for the company's sales projection. Menzly and Ozbas (2010) argue that fully digesting the implication of the information from structurally connected firms can take time. As evidence, they show that stocks that are in economically related supplier and customer industries cross-predict each other's returns. Chen, Zhang, and Zhang (2014) show that the return predictability across supplier-customer industries can be even stronger for the corporate bond market. Shahrur, Becker, and Rosenfeld (2010) use a sample of equities listed on the exchanges of 22 developed countries to show that equity returns on customer industries lead the returns of supplier industries. At the firm level, Cohen and Frazzini (2008) use a data set of firms' principal customers to identify a set of economically related firms, and show that the stock price of a firm does not fully incorporate news involving its related firms, thus generating predictable subsequent price moves. These studies highlight the importance of understanding the structural connections across companies and the implications of these connections for cross relations.

Understanding the structural connections is important not only for enhancing the identification of pairwise statistical relations (both contemporaneous and across different leads and lags), but also for identifying

<sup>&</sup>lt;sup>1</sup>Largely because of this observation, commonly-used risk models in the industry such as BARRA treat each industry as a stand-alone risk factor.

<sup>&</sup>lt;sup>2</sup>Luo and Nagarajan (2014) examine the antecedents and consequences of analysts choosing to become supply chain analysts, i.e., analysts following both a supplier and its major customer. Guan, Wong, and Zhang (2015) find that the likelihood of an analyst following a supplier-customer firm pair increases with the strength of the economic ties along the supply chain, as measured by the percentage of the supplier's sales to the customer.

the key drivers of the business cycle and aggregate market fluctuations. For this purpose, this paper proposes to examine the supplier-customer relation not in terms of pair-wise connections, but from the perspective of an economic supply chain network, with each relation serving as a directed node of the network. The paper examines the potentials of a list of centrality measures in capturing the major determinants of the supply chain network. Of these measures, the supplier-customer centrality pair defined based on Kleinberg (1999)'s algorithm looks particularly promising. The supplier centrality of a company is defined as the sum of the customer centralities of all its customers and the customer centrality of a company is defined as the sum of the supplier centrality of all its suppliers.

Based on information from the FactSet supply chain relationship database, the paper builds a supplier-customer network matrix at the beginning of each year from 2004 to 2014, computes the supplier and customer centralities of each company, and constructs supplier and customer central stock portfolio based on the centrality estimates. Empirical analysis shows that supplier central portfolios tend to be more volatile than customer central portfolios. Furthermore, the stock performance of supplier central portfolios tends to predict the movements of the overall stock market.

In related work, Aobdia, Caskey, and Ozel (2014) define centrality of industries based on cross-industry trade flows and find that stock returns on central industries depend more on aggregate risks, and shocks to central industries propagate more strongly than shocks to other industries. Ahern and Harford (2014) represent the economy as a network of industries connected through customer and supplier trade flows and analyze how merger waves propagate through the network. Ahern (2015) show that industries that are more central in the network of intersectoral trade earn higher stock returns than industries that are less central.

The remainder of the paper is organized as follows. The next section describes the FactSet supply chain relationship database. Section 3 discusses different centrality measures and their economic meanings within the context of the supply-chain network. Section 4 analyzes the supplier centralities of the U.S. economy. Section 5 concludes.

## 2. Data Source and Sample Construction

The firm-level supplier-customer relationship information is from FactSet, which maps the historical supplier-customer relationship for each company based on information from the company's regulatory disclosure reports, annual reports, and other primary sources. I confine the analysis to constituents of the S&P Composite 1500 index, which covers about 90% of the U.S. market capitalization and includes three leading indices: the S&P 500 index, the S&P MidCap 400 index, and the S&P SmallCap 600 Index. From January 2004 to January 2014, I take snapshots of the database at the beginning of each year, and merge the information with price and accounting data from Bloomberg. Over the 11 year period, each year I identify from 1214 to 1340 companies, and from 4169 to 6061 supplier-customer pairs, averaging 3-5 suppliers per customer.

The FactSet database indicates the applicable time period for each relationship, from which one can in principle extract the relational mapping at any time; nevertheless, I decide to take the snapshots at a relatively low frequency because of our concern that it may take time for the applicable relationship to become fully known to the average investor. By taking a snapshot once a year, I assume that the structural relation is relatively stable and will hold over the coming year, while avoiding to chase the intra-year variations that one may not be able to capture in practice.

The U.S. Securities and Exchange Commission (SEC) has a mandate (rule SFAS 131) that calls for companies to disclose their customers if their revenue exposure to them is 10% or greater. In addition, some companies choose to disclose more customer and supplier information if they believe the information will help improve their attractiveness and draw more attention from investors. FactSet expands and consolidates such information through cross validation and a reverse linkage methodology. For example, if company A identifies company B as a supplier, company A becomes the customer of company B. In practices, the relationships are not always symmetric due to size differences (among other things). For example, if company A is much smaller than company B, it is possible that although company B is a significant supplier for company A, company A is not a significant customer for B. In this case, the cross validation approach may bring a certain degree of bias to the data. Furthermore, in performing the analysis, I am conscious of the

fact that a company can have supplier/customer relationships, possibly with lesser significance, with many more companies than reported in the database.

Finally, important questions arise on how to define the relative significance of a relationship. When highlighting the significance of a supplier to a company, the company may cite how much it spends on this supplier, maybe in percentage of its total cost of goods sold. On the other hand, when highlighting the significance of a customer to a company, the company can cite how much percentage of its sales come from this customer. While companies sometimes report these numbers and the FactSet database captures them, the information is still far too incomplete for systematic analysis. Absent from more detailed information, I treat each identified supplier as equally significant to its customer, and vice versa. Depending on the specific applications, one can also consider altering the significance of each relationship according to factors such as industry proximity, direction of disclosure, and size of firms. Furthermore, measures that capture the irreplaceability and/or value-added of a supplier can also be used as importance metrics.

# 3. Supply Chain Centrality Measures

Instead of focusing on the pair-wise relationship between a company and its suppliers, this paper examines the relationship from the perspective of the aggregate economy and the economy-wide network of the supply chain. In particular, the paper strives to define appropriate measures that capture the relative importance of each supplier in terms of its contribution to the networked economy.

Formally, the supplier network at a given point in time can be represented by a supplier matrix  $\{A_{i,j}\}_{i,j=1}^N$ , where N denotes the number of companies, and  $A_{i,j} = 1$  if company i is the supplier of company j. Thus, each column j represents an index of the suppliers for company j, and each row i lists the customers that the supplier i has.

In the language of networks, the supply chain network is a directed network, where one can imagine drawing an arrow from each customer to each of its suppliers. The literature on networks, e.g., Newman

(2010), has proposed a long list of centrality measures to represent the relative importance of a vertex in the network. This paper discusses the applicability of these concepts to the supply chain network and explores their economic meaning in capturing the relative importance of a supplier in the supply chain network.

#### 3.1. Degree centrality: The number of companies that the supplier serves

Intuitively, a supplier company is more important to the economy if it is the supplier of many companies instead of just one company. Thus, a simple measure of centrality for a supplier, often referred to as the **degree centrality**, can be defined as the number of companies that this supplier serves. From the perspective of the network topology, if one draws an arrow from a company to each of its suppliers, the degree centrality simply measures the degree of a vertex, or the number of arrows pointed to a particular supplier.

Given the construction of a supplier matrix A, the degree centrality vector,  $\mathbf{c}$ , can be computed as the simple sum of each row,

$$\mathbf{c} = A\mathbf{e} \tag{1}$$

where e denotes a vector of ones.

Figure 1 plots the top ten suppliers as of January 2014 with the most number of customers. The top two on the list BFAM and BRK/B have more than 50 identified customers and the next five suppliers have 40 or more customers. The top list spans across different industries from child-care provider (BFAM), multinational conglomerate (BRK/B), manufacturers of industrial goods (CR,GE), to large technology companies (IBM, MSFT).

Since the centrality measures are meant to be a relative measure capturing the relative importance of a company within the network economy, one can perform various normalizations to the measures. The definition in (1) uses the raw total number of customers without normalization. Alternatively, one can normalize

the measures so that they sum to N, in which case the measures average to one and the magnitude does not vary with the size of the economy; or one can normalize the measures to sum to one (or 100%) so that the estimate for each company represents the percentage contribution of that company to the overall economy. Henceforth, we take the latter normalization and interpret each estimate as a percentage contribution.

#### 3.2. Eigenvector centrality: The importance of customers as suppliers

Degree centrality treats all customers equally and awards one "centrality point" for each customer; however, not all customers are equivalent. A customer can be a supplier to other companies, and its importance to the economy increases if the customer itself is an important supplier to many other companies. Instead of awarding suppliers just one point for each customer, **eigenvector centrality** gives each supplier a score proportional to the sum of the scores of its customers.

Let  $c_i$  be the eigenvector centrality for company i. The eigenvector centrality of company i is proportional to the sum of the centralities of all its customers,

$$c_i = (1/\lambda) \sum_j A_{i,j} c_j. \tag{2}$$

Equation (2) defines the centrality measure recursively. Given N companies in the network, equation (2) defines N equations, from which one solves for the N centrality measures for the N companies. The proportionality coefficient  $\lambda$  can be determined as a normalization condition by setting, for example,  $\sum_j c_j = 1$ . One can solve the centrality measures recursively by starting at some initial guesses (say, assuming that all companies have equal centrality) and applying equation (2) repeatedly until the solution converges.

Representing equation (2) in matrix notation, we have,

$$\lambda \mathbf{c} = A\mathbf{c}.\tag{3}$$

It can be shown that the thus-defined eigenvector centrality is proportional to the right leading eigenvector of the supplier matrix A (Bonacich (1987)). Furthermore, since all elements of the supplier matrix A are non-negative, the Perron-Frobenius theorem states that the leading eigenvector has strictly positive components.

The eigenvector centrality has the nice property that it can be large either because a supplier has many customers or because it has important customers, or both. The importance of the customer is defined based on its importance as a suppler itself.

#### 3.3. Kleinberg centrality: The importance of customers as economic hubs

Eigenvector centrality treats a customer as important it is an important supplier itself, but suppliers and customers can be important in different ways. A supplier is important if it supplies to many different customers, whereas a customer can be important simply because of its role as a hub for many different types of suppliers.

From the perspective of a directed network, Kleinberg (1999) proposes to construct two types of centralities, labeled as the **authority centrality** and the **hub centrality**, to quantify each vertex's prominence in the two roles, with authorities corresponding to important suppliers and hubs corresponding to important customers in our application. Specifically, each company i has both a supplier authority centrality  $c_i$  and a customer hub centrality  $h_i$ , representing its importance in the two different roles as a supplier and a customer, respectively. The defining characteristic of a supplier with high authority centrality is that it is the supplier to many customers with high hub centrality. The defining characteristic of a customer with high hub centrality is that it is the customer of many suppliers with high authority centrality.

Mathematically, the two centrality measures can be connected as,

$$c_i = \alpha \sum_j A_{i,j} h_j, \quad h_i = \beta \sum_j A_{j,i} c_j. \tag{4}$$

In matrix notation,

$$\mathbf{c} = \alpha A \mathbf{h}, \quad \mathbf{h} = \beta A^{\mathsf{T}} \mathbf{c}.$$
 (5)

Combining the two,

$$AA^{\mathsf{T}}\mathbf{c} = \lambda \mathbf{c}, \quad A^{\mathsf{T}}A\mathbf{h} = \lambda \mathbf{h}. \tag{6}$$

with  $\lambda = (\alpha \beta)^{-1}$ . Therefore, the supplier and customer centralities are respectively given by leading eigenvectors of  $AA^{\top}$  and  $A^{\top}A$  with the same eigenvalue.

A crucial condition for this approach to work, is that  $AA^{\top}$  and  $A^{\top}A$  have the same leading eigenvalue  $\lambda$ ; otherwise, one cannot satisfy both conditions in equation (6). This is indeed the case, and in fact that all eigenvalues are the same for the two matrices. To see this, one can start with  $AA^{\top}\mathbf{c} = \lambda\mathbf{c}$ , and multiply both sides by  $A^{\top}$  to give

$$A^{\top}A(A^{\top}\mathbf{c}) = \lambda(A^{\top}\mathbf{c})$$

and hence  $A^{\top}\mathbf{c}$  is the eigenvector of  $A^{\top}A$  with the same eigenvalue  $\lambda$ . Comparing to (6), this means that

$$A^{\mathsf{T}}\mathbf{c} = \mathbf{h},\tag{7}$$

which gives us a fast way of calculating the customer centrality once we have the supplier centrality.

It is possible that a company is not the supplier to any other company. This will lead to a row of zeros in the supplier matrix. Both the degree centrality and eigenvector centrality for this company will be zero. A zero centrality measure for this company sounds intuitive as a company that supplies to nobody should be ranked low in the supply chain. However, imagine another company, which is a supplier to thousands of such companies. The fact that it is a supplier of many companies should make it "important" and this importance shows up in the degree centrality measure. However, since its customers all have zero eigenvector centrality, this company will also end up having zero eigenvector centrality. Taking this argument further, a company may be pointed to by others that themselves are pointed to by many more, and

so on through many generations, but if the progression ends up at a company or companies that supply to no other companies, it is all for nothing — The final value of the eigenvector centrality will still be zero. Such a chain effect does not sound quite as intuitive.

In a strict sense, a company must have customers, even though these customers may not take the form of a company. Furthermore, companies do not report all their customers. By regulation, they only need to report customer companies that generate over 10% of their revenue. Some companies may choose to report more. Even so, it is unlikely the database lists all possible customers. For many retail companies, their customers are simply the consumers. Thus, one common solution to this issue is to give each company a small amount of centrality "for free," regardless of its position in the network. This modification was first proposed by Katz (1953). The addition can also be different for different companies if one thinks of it as a "prior" centrality measure estimated from information outside of the network matrix.

The customer and supplier hub and authority centralities circumvent this problem from an alternative angle. Companies not cited by any others as a supplier (that is, companies with no customers) have supplier centrality zero, which is reasonable, but they can still have non-zero customer centrality. Thus, their suppliers can have non-zero supplier centrality by virtue of being a supplier. This is perhaps a more elegant solution to the problems of eigenvector centrality in directed networks than the more ad hoc method of introducing an additive constant term in Katz (1953). Defining the importance of a supplier based on the importance of its customers as a customer also sounds more economically intuitive than based on the importance of its customers as a supplier.

# 4. Central Suppliers of the U.S. Economy

To analyze the historical behaviors of the different centrality measures constructed on the U.S. economy, I map the FactSet supply-chain data to the universe of the S&P composite 1500 companies and construct the supply-chain matrix *A* at the beginning of each year from 2004 to 2014. From the supply chain matrix,

I construct the four centrality measures: Degree centrality, Eigenvector centrality, Supplier centrality, and Customer centrality. For the analysis, all centrality measures are normalized to sum to 100% so that the estimate for each company represents its percentage contribution to the total economy.

#### 4.1. Distributional behaviors

To understand how the distribution of the centrality estimates across different companies, for each centrality measure at a certain date, we first sort the estimates from large to small, and then compute the cumulative sum of these estimates. By normalization, the total sum is equal to 100%. The speed to which the cumulative sum increases reveals the distributional behavior of the centrality measure: A straight line would suggest that all companies are equally central to the economy, whereas a highly concave plot would indicate that a small number of companies contribute to a large proportion to the aggregate economy. Figure 2 plots the cumulative centrality at the beginning of four selected years. The plots look similar across different time periods. All the plots are concave, highlighting the fact that different companies have different centrality estimates. The least concave and hence the most uniform measure comes from the simple degree centrality measure. The most concave, on the other hand, comes from the eigenvector centrality measure, in which case the recursive definition magnifies the contribution of a few companies while diminishing the contribution of the rest. The Kleinberg authority and hub centrality measures fall in between. It is interesting to observe that over the whole sample period, the hub centrality estimates show a steeper curvature than the authority centrality estimates, suggesting that the important customer hubs are more concentrated than important supplier authorities.

### [Fig. 2 about here.]

To gauge their similarities and differences of these measures, Table 1 estimates the Spearman rank correlation of the four centrality measures each year and reports the historical average of the cross correlation estimates. The first three centrality measures are all about the relative importance as a supplier. They show

highly positive correlations. The customer centrality measure, on the other hand, measures the relative importance of a company as a customer and shows negative correlations with all four supplier centrality measures. The most negative correlation is between the customer centrality and its counterpart suppler centrality at –0.111.

#### 4.2. The top ten list

I rank the companies based on each centrality measure and analyze the behavior of the top ten companies with the highest centrality estimates. Panel A of Table 2 provides the ticker of the top ten suppliers with the most customers (and hence the highest degree centrality) at the beginning of each year. Technology companies are the most prominent top suppliers during the earlier period of the sample, but the list becomes more diverse in the more recent years with some companies from the industrial goods and services sectors.

Panel B of Table 2 provides the top ten suppliers with the highest eigenvector centrality. Once we consider the feedback effect of the network, technology companies dominate the top ten lists for most years. In particular, Atmel, which designs, develops, and manufactures semiconductor integrated circuit products, becomes the top supplier from 2006 to 2012.

Table 3 provides the top ten list of Kleinberg supplier authority centrality in panel A. By changing the definition of customer importance, the top ten supplier list has a completely new makeover in recent years. In particular, the 2014 top ten list includes six REIT companies, but none from the technology sector. The reasoning behind this shift needs further exploration.

Panel B of Table 3 provides the top ten list of Kleinberg customer hub centrality. The list is quite distinctive and includes many large retail stores. In 2014, this list includes BestBuy, Costco, Home Depot, Lowe's, Sears, Target, and Walmart.

### 4.3. The statistical behavior of central stock portfolios

While the paper defines several centrality measures to identify the central suppliers and customers of an economy, it is unclear how the central vertices of the network behave and how their behaviors impact the aggregate economy. To explore the historical behavior of "central" companies, I form equal-weighted stock portfolios using the top ten companies<sup>3</sup> defined by each centrality measure and analyze their statistical behaviors in terms of their relations with the aggregate market, proxyed by the S&P 500 index. The compositions of the portfolios are updated at the beginning of each year based on the renewed centrality measure estimates. Table 4 summarizes these statistical behaviors.

First, I regress the daily returns on the central stock portfolios against the S&P 500 index return to estimate the beta of each central portfolio. The beta estimates on reported in Table 4 under the column titled "β." The customer central portfolio has a beta estimate slightly less than one at 0.984, whereas the supplier centrality portfolios all have beta estimates around 1.2 or higher, except the portfolio defined on degree centrality. Thus, top suppliers companies show larger market exposure than top customer companies. When I measure the correlation between the daily central portfolio returns and the S&P 500 index returns, the estimates are very high, all around 0.8 or higher, as reported in Table 4 under the column "ρ."

To examine whether the stock performance of top suppliers and customers provide any precursor for the overall market movements, I compute quarterly returns on the central portfolios, and measures their forecasting correlations with the S&P 500 index returns over three- and six-month horizons. When using total return on the central portfolios as the predictor, the forecasting correlations are all positive for all central portfolios at both horizons. The predictions are the most positive for the Kleinberg supplier authority central portfolio at both three- and six-month horizons.

Part of the positive correlation prediction is due to the momentum effect identified by, for example, Jegadeesh and Titman (2001). To control for this, I regress each stock return against the S&P 500 index

<sup>&</sup>lt;sup>3</sup>An alternative is to form stock portfolios with weights proportional to the centrality estimates. The results are qualitatively similar whether we use equal weighting or set weighting proportional to the centrality estimates. Varying the number of companies included in the portfolio does not alter the qualitative conclusion, either.

return to generate excess stock returns, and then compute the excess returns on the central portfolios. Using the excess returns as a predictor of future index returns, I find that the forecasting correlation is virtually zero for the customer central portfolio, but remain positive for all supplier central portfolios. Again, excess return on the Kleinberg supplier authority central portfolio generates the strongest predictive correlation at both three and six month horizons. Thus, the evidence seems to suggest that the stock performance of central suppliers predict the following performance of the overall market, but the stock performance of central customers do not lead the market performance.

Comparing the relative forecasting power of the different centrality measures, we can also gain some basic understanding on the effectiveness of different measures. The quarterly forecasting correlation is 8.8% for the simple degree centrality portfolio. By contrast, the eigenvector centrality portfolio generates stronger forecasting correlations at 11.5%, highlighting the importance of the feedback effect. Finally, defining the importance of the supplier based on the importance of the customer as a hub using Kleinberg (1999)'s algorithm generates the strongest and most persistent forecasting power for the supplier central portfolio. By contrast, excess returns on the customer hub central portfolio do not show any predictive power on the index return. Thus, stock performance of suppliers seem to precursors of the aggregate economy and the customer hubs.

#### 4.4. Market response propagation to shocks from the top ten companies

To better appreciate how these different central portfolios work through the supply-chain network, we generate simultaneous shocks to the top ten companies under each measure, and propagate the shocks step by step, and compute the market's aggregate response to these stocks at each stage. For convergence, we normalize the first-stage response to unity. Specifically, let  $\tau$  denote the shock vector, with elements of one for the top ten companies and zeros for others. The first-stage raw response is computed as  $RR_1 = \mathbf{e}^{\top}(A\tau)$ .

Then, the normalized responses for each step h is computed as

$$R_h = \mathbf{e}^{\top} (A^h \mathbf{\tau}), \tag{8}$$

with  $R_1 = 1$  by normalization. If the shocks are on ten stand-alone companies, the response will be zero to begin with because these shocks will not impact any others. If the shocks are on companies, either with one unconnected customer. The response of their customers is normalized to be one in the first stage, but the responses will stop there and will not propagate further simply because their customers are disconnected from the economy and hence cannot propagate the shocks further. Only when the customers are suppliers of others and/or connected with other firms, can the shocks propagate multiple steps.

Figure 3 plots the responses to shocks from different top ten portfolios at selected sampling points. The response function looks different at different time periods. Most shocks dissipate quickly and have little list after the first round, but there are exception. In a few years such as 2008 and 2014, shocks to the authority portfolio show visibly stronger long-lasting propagation effects. These long-lasting propagation effects are potentially responsible for the authority portfolio's predictive power on the aggregate stock market

[Fig. 3 about here.]

### 5. Concluding remarks

With the increasing availability of supply chain information, researchers are paying increasing attention to information flows and interactions between suppliers and customers. In this paper, I examine the interactions from the perspective of an economy-wide supply-chain network, and propose a list of network centrality measures to capture the relative importance of each company within this network. Based on information from the FactSet Supply Chain Relationships database, I build a supplier network matrix at the beginning of each year from 2004 to 2014, and compute the supplier centralities of each company. I then construct

supplier central stock portfolio based on the top ten companies with the highest centrality estimates and find that supplier central portfolios tend to be more volatile than customer central portfolios. Furthermore, the stock performance of supplier central portfolios tends to predict the movements of the overall stock market.

The idea of analyzing the centrality of the supply-chain network is relatively new. While my analysis shows some promising results, there is much to do for future research. First, this paper has explored several centrality definitions. A lot more research, both theoretical and empirical, is needed to fully understand which measure is the most relevant for what purpose. Furthermore, many more variations can be constructed both from the perspective of building the supplier network matrix and from the perspective of constructing new centrality measures. For the network matrix, one can explore different firm characteristics and data sources to enrich the network and differentiate the relative importance of each supplier to a customer. The importance metrics can be based on how much it supplies to the customer and/or how unique and irreplaceable the supply is. One can also explore different clustering of the network matrix to understand flows from a more aggregate level, for example, for one industry to another industry or from one economic or geographic region to another region. For centrality measures, much theoretical work can be done one the shock and response dynamics, from which one can motivate the definition of an appropriate centrality measure and better understand the flow of the shocks within the supply chain. Second, given the construction of the network matrix and centrality measures, much research can be done in understanding the statistical behavior of financial security prices and trading behaviors across different centrality levels and how they interact. Shocks to the supply chain can generate ripple effects, which can show up potentially as lead-lag predictive relations in security returns, earning surprises, default probabilities, and/or distinctive term structure patterns in realized and option implied volatilities and credit default swaps.

### References

- Ahern, K. R., 2015. Network centrality and the cross section of stock returns. Journal of Finance forthcoming.
- Ahern, K. R., Harford, J., 2014. The importance of industry links in merger waves. Journal of Finance 69, 527–576.
- Aobdia, D., Caskey, J., Ozel, N. B., 2014. Inter-industry network structure and the cross-predictability of earnings and stock returns. Review of Accounting Studies 19, 1191–1224.
- Bonacich, P., 1987. Power and centrality: A family of measures. American Journal of Sociology 92, 1170–1182.
- Brin, S., Page, L., 1998. The anatomy of a large-scale hypertextual web search engine. Computer Networks and ISDN Systems 30, 107–117.
- Chen, L., Zhang, G., Zhang, W., 2014. Return predictability in corporate bond market along the supply chain. Working paper. Cheung Kong Graduate School of Business, University of Missouri-St. Louis, and National University of Singapore.
- Cohen, L., Frazzini, A., 2008. Economic links and predictable returns. Journal of Finance 63, 1977–2011.
- Guan, Y., Wong, F., Zhang, Y., 2015. Analyst following along the supply chain. Review of Accounting Studies 210, 210–241.
- Jegadeesh, N., Titman, S., 2001. Profitability of momentum strategies: An evaluation of alternative explanations. Journal of Finance 56, 699–720.
- Katz, L., 1953. A new status index derived from sociometric analysis. Psychometrika 18, 39–43.
- Kleinberg, J. M., 1999. Authoritative sources in a hyperlinked environment. Journal of the ACM 46, 604–632.
- Luo, S., Nagarajan, N. J., 2014. Information complementarities and supply chain analysts. The Accounting Review forthcoming.

Menzly, L., Ozbas, O., 2010. Market segmentation and cross-predictability of returns. Journal of Finance 65, 1555–1580.

Newman, M. E. J., 2010. Networks: An Introduction. Oxford University Press.

O'Connor, N. G., Wu, A., Anderson, S. W., 2014. Relative performance evaluation in supply chain management. Working paper. Hong Kong Baptist University, National Chengchi University, and University of California, Davis.

Shahrur, H., Becker, Y. L., Rosenfeld, D., 2010. Return predictability along the supply chain: The international evidence. Financial Analysts Journal 66, 60–77.

Table 1
Average rank correlation between different centrality measures
Entries report the historical average of the Spearman rank correlation estimates between the different centrality measures estimated at the beginning of each year from 2004 to 2014 on U.S. S&P 1500 companies.

	Degree	Eigenvector	Supplier	Customer
Degree	1.000	0.776	0.891	-0.086
Eigenvector	0.776	1.000	0.805	-0.045
Supplier	0.891	0.805	1.000	-0.111
Customer	-0.086	-0.045	-0.111	1.000

Table 2
Top ten suppliers with the most number of customers and eigenvector centrality
Entries list the tickers of the top ten companies with the most customers and hence the highest degree centrality estimates in panel A ad with the highest eigenevector centrality in panel B, at the beginning of each year from 2004 to 2014.

2004	GE	HPQ	IBM	INFA	INTC	<b>IWOV</b>	MSFT	ORCL	ROK	WBSN
2005	A	ACN	CNQR	GE	HPQ	IBM	INTC	<b>IWOV</b>	MSFT	ORCL
2006	ACN	GE	HPQ	IBM	INFA	<b>IWOV</b>	MANH	<b>MSFT</b>	ORCL	ROVI
2007	<b>EMC</b>	GE	HPQ	IBM	<b>IWOV</b>	MSFT	ORCL	PRGS	QTM	ROVI
2008	DDR	<b>EMC</b>	HPQ	IBM	<b>IWOV</b>	<b>JDAS</b>	MSFT	ORCL	PRGS	ROVI
2009	DDR	<b>EMC</b>	HPQ	IBM	<b>JDAS</b>	LXP	MSFT	ORCL	PRGS	ROVI
2010	DDR	<b>EMC</b>	HPQ	IBM	<b>JDAS</b>	LXP	MSFT	ORCL	PRGS	ROVI
2011	ACN	DIS	FRT	HPQ	IBM	INTC	JDSU	LXP	MSFT	PTC
2012	ADC	BFS	EP	FRT	HPQ	IBM	INTC	LFUS	MSFT	PWR
2013	BRK/B	CR	HON	HPQ	IBM	IRC	LFUS	MSFT	NPO	ORCL
2014	<b>BFAM</b>	BRK/B	CR	GE	IBM	MSCC	MSFT	NPO	ORCL	SXI
		uppliers wit								9711
Panel I	B. Top ten s	uppliers wit	h the highe	est eigenved	ctor centra	lity				
Panel 1	B. Top ten s	uppliers wit	h the highe	st eigenved KEM	ctor centra	lity ORCL	PSEM	SMTC	TTMI	XLNX
Panel 1 2004 2005	B. Top ten s.  CYMI A	uppliers wit  IBM  AMCC	h the highe INTC CYMI	kEM IBM	otor centra NTAP IRF	ORCL KEM	PSEM NTAP	SMTC PSEM	TTMI SMTC	XLNX TTMI
Panel I 2004 2005 2006	CYMI A	IBM AMCC ATML	h the highe INTC CYMI IBM	KEM IBM IRF	NTAP IRF MSFT	ORCL KEM ORCL	PSEM NTAP PSEM	SMTC PSEM ROVI	TTMI SMTC TTMI	XLNX TTMI XLNX
2004 2005 2006 2007	CYMI A A ATML	IBM AMCC ATML BRKS	h the highe INTC CYMI IBM CA	KEM IBM IRF	NTAP IRF MSFT JBL	ORCL KEM ORCL JDSU	PSEM NTAP PSEM KEM	SMTC PSEM ROVI PSEM	TTMI SMTC TTMI QTM	XLNX TTMI XLNX SNIC
2004 2005 2006 2007 2008	CYMI A A ATML ATML	IBM AMCC ATML BRKS AVT	h the highe INTC CYMI IBM CA COGT	KEM IBM IRF IBM CYMI	NTAP IRF MSFT JBL IBM	ORCL KEM ORCL JDSU KEM	PSEM NTAP PSEM KEM ORCL	SMTC PSEM ROVI PSEM PSEM	TTMI SMTC TTMI QTM ROVI	XLNX TTMI XLNX SNIC SNIC
2004 2005 2006 2007 2008 2009	CYMI A A ATML ATML ATML	IBM AMCC ATML BRKS AVT CYMI	INTC CYMI IBM CA COGT EMC	KEM IBM IRF IBM CYMI HPQ	NTAP IRF MSFT JBL IBM IBM	ORCL KEM ORCL JDSU KEM JAVA	PSEM NTAP PSEM KEM ORCL MSFT	SMTC PSEM ROVI PSEM PSEM QLGC	TTMI SMTC TTMI QTM ROVI ROVI	XLNX TTMI XLNX SNIC SNIC SNIC
2004 2005 2006 2007 2008 2009 2010	CYMI A A ATML ATML	IBM AMCC ATML BRKS AVT	h the highe INTC CYMI IBM CA COGT	KEM IBM IRF IBM CYMI	NTAP IRF MSFT JBL IBM	ORCL KEM ORCL JDSU KEM	PSEM NTAP PSEM KEM ORCL	SMTC PSEM ROVI PSEM PSEM	TTMI SMTC TTMI QTM ROVI ROVI ROVI	XLNX TTMI XLNX SNIC SNIC
2004 2005 2006 2007 2008 2009 2010 2011	CYMI A A ATML ATML ATML ATML	IBM AMCC ATML BRKS AVT CYMI EMC	INTC CYMI IBM CA COGT EMC HPQ	KEM IBM IRF IBM CYMI HPQ IBM	NTAP IRF MSFT JBL IBM IBM JAVA	ORCL KEM ORCL JDSU KEM JAVA MSFT	PSEM NTAP PSEM KEM ORCL MSFT QLGC	SMTC PSEM ROVI PSEM PSEM QLGC QTM	TTMI SMTC TTMI QTM ROVI ROVI	XLNX TTMI XLNX SNIC SNIC SNIC SNIC SNIC
2004 2005 2006 2007 2008	CYMI A A ATML ATML ATML ATML ATML ATML ADBE	IBM AMCC ATML BRKS AVT CYMI EMC ATML	INTC CYMI IBM CA COGT EMC HPQ CDNS	KEM IBM IRF IBM CYMI HPQ IBM HPQ	NTAP IRF MSFT JBL IBM IBM JAVA IBM	ORCL KEM ORCL JDSU KEM JAVA MSFT INTC	PSEM NTAP PSEM KEM ORCL MSFT QLGC KEM	SMTC PSEM ROVI PSEM PSEM QLGC QTM MSFT	TTMI SMTC TTMI QTM ROVI ROVI ROVI QTM	XLNX TTMI XLNX SNIC SNIC SNIC SNIC

Table 3
Top ten companies with the highest Kleinberg supplier authority centralities and customer hub centralities
Entries list the tickers of the top ten companies with the highest Kleinberg supplier authority centrality
(panel A) and customer hub centrality (panel B) at the beginning of each year from 2004 to 2014.

		5 FF	ишногиу (	centrality						
2004	IBM	INFA	INTC	IRF	KEM	MSFT	ORCL	SANM	WBSN	XLNX
2005	A	<b>EMC</b>	GE	HPQ	IBM	IRF	KEM	<b>MSFT</b>	ORCL	SANM
2006	A	HPQ	IBM	INFA	IRF	<b>IWOV</b>	<b>MSFT</b>	ORCL	PRGS	ROVI
2007	ATML	<b>EQIX</b>	IBM	IRF	<b>IWOV</b>	JCI	MSFT	PRGS	QTM	ROVI
2008	BCSI	DDR	EQY	FICO	FRT	<b>IWOV</b>	MAC	PEI	PRGS	ROVI
2009	DDR	<b>EMC</b>	EQY	HPQ	IBM	MAC	MSFT	PEI	PTC	PRGS
2010	DDR	<b>EMC</b>	EQY	HPQ	IBM	KRG	MAC	MSFT	PEI	PRGS
2011	DDR	FRT	HPQ	IBM	JAH	KRG	MAC	MSFT	PEI	SPG
2012	ADC	AKR	DDR	EQY	FRT	KIM	KRG	MAC	PEI	SPG
2013	ADC	CR	DDR	FRT	HON	IRC	KIM	KRG	LEG	MAC
2014	ADC	CR	DDR	FRT	IRC	KRG	LEG	MAC	MMM	SXI
Tunei D.	Kieinber	g customer	hub centr							
2004	AVT	BA	CSCO	DELL	GE	HPQ	IBM	INTC	LMT	WMT
2005	BA	CSCO	DELL	F	GE	HPQ	IBM	INTC	LMT	WMT
2006	BA	CSCO	F	GE	HPQ	IBM	INTC	LMT	MSFT	WMT
2007	BA	CSCO	F	GE	HPQ	IBM	LMT	SHLD	T	WMT
2008	BA	CSCO	HD	HPQ	IBM	LMT	SHLD	T	TGT	WMT
	BA	HD	HPQ	IBM	KSS	MSFT	SHLD	T	TGT	WMT
	BA	BBY	HD	HPQ	IBM	KSS	SHLD	T	TGT	WMT
	BBY	HD	HPQ	IBM	JCP	KSS	M	SHLD	TGT	WMT
	BBY	COST	HD	JCP	KSS	LOW	M	SHLD	TGT	WMT
	BA	GE	HD	KSS	LMT	LOW	NOC	SHLD	TGT	WMT
2014	BA	BBY	COST	HD	LMT	LOW	NOC	SHLD	TGT	WMT

Table 4
Statistical behaviors of central company stock portfolios

I form equal weighted stock portfolios using the top ten companies with the highest centrality measures. The compositions of the portfolios are updated at the beginning of each year based on the renewed centrality measure estimates. Entries report the relations between these portfolios and the S&P 500 index.  $\beta$  measures the contemporaneous daily return regression slope against the index,  $\rho$  measures the contemporaneous daily return correlation with the S&P 500 index. The remaining columns reports the predictive correlation of quarterly total portfolio returns and quarterly excess portfolio returns on future index returns over three and six month horizons.

			Quarterly	total return	Quarterly e	xcess return
Year	β	ρ	3-month	6-month	3-month	6-month
Degree	1.075	0.879	0.177	0.043	0.088	0.015
Eigenvector	1.245	0.795	0.185	0.079	0.115	0.093
Authority	1.208	0.840	0.232	0.103	0.232	0.177
Hub	0.984	0.872	0.122	0.016	0.010	-0.002

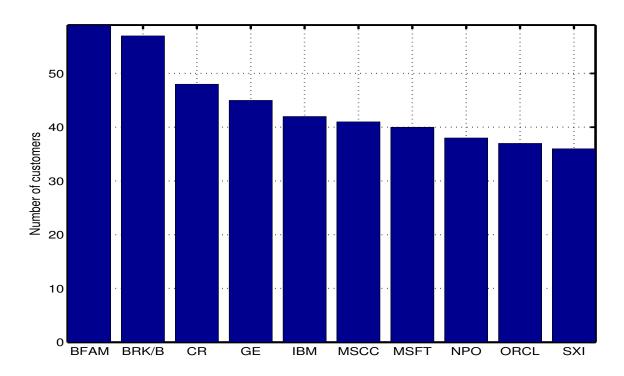


Fig. 1. Top ten suppliers with the most number of customers.

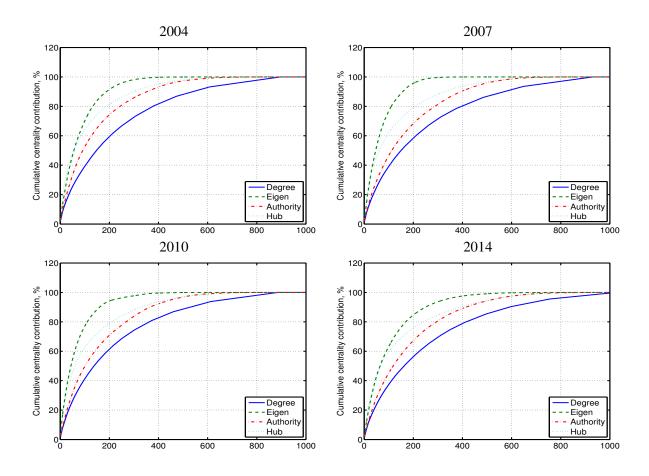


Fig. 2. Cumulative centrality plots Top ten suppliers with the most number of customers.

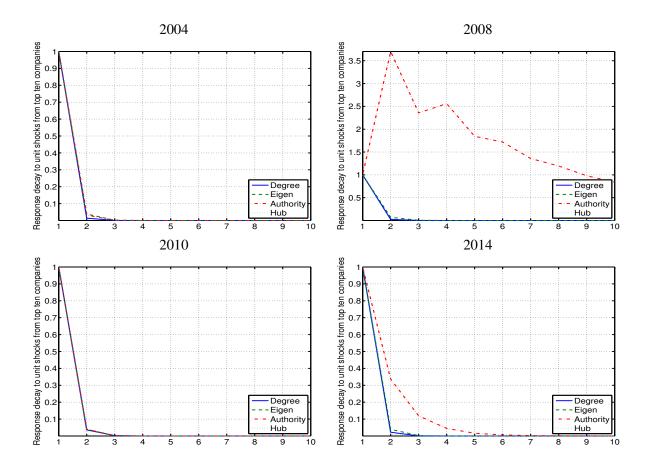


Fig. 3. Aggregate normalized responses to simultaneous shocks to top ten companies