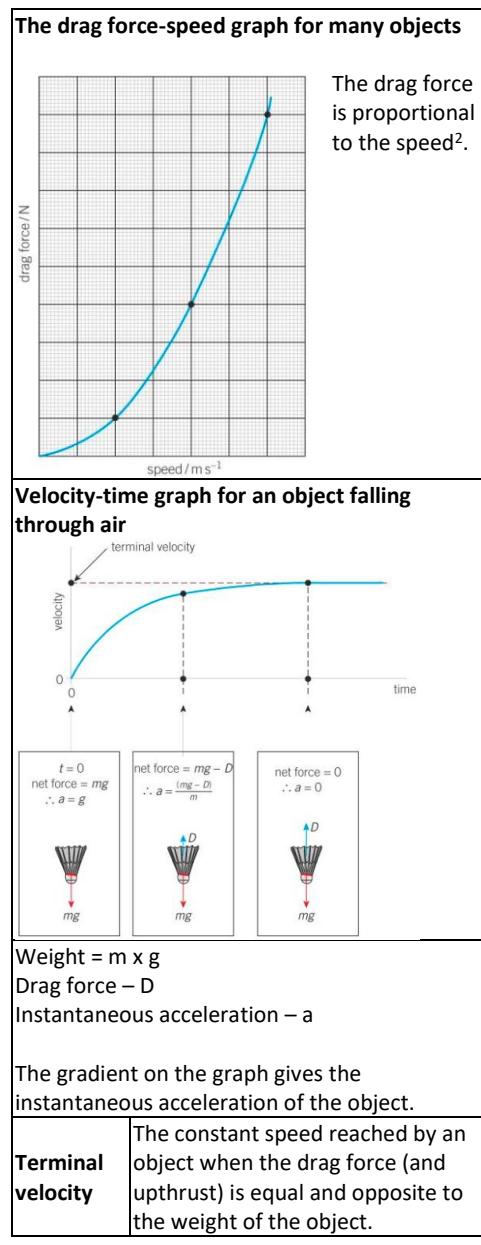


| 1. Force, mass, and weight | |
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| Mass | Amount of matter, a base quantity measured in kilograms, kg. |
| Relativistic mass | Relativistic mass, in the special theory of relativity, the mass that is assigned to a body in motion. Your mass will not alter much at the speeds at which we move around. The relativistic mass m becomes infinite as the velocity of the body approaches the speed of light. $m = \frac{m_0}{\sqrt{1 - \left(\frac{v}{c}\right)^2}}$ |
| Net (resultant) force | The net force is the vector sum of all the forces that act upon an object. |
| Force | A push or pull on an object, measured in newtons, N. |
| Acceleration | The rate of change of velocity, a vector quantity, measured in metres per second squared, m/s ² . |
| Newton's second law - equation | $F = m \times a$ F – force (N) m – mass (kg) a – acceleration (m s ⁻²) - When m is constant, F is proportional to a . - When F is constant, a is inversely proportional to m . |
| Newton (unit definition) | One newton is equal to the force needed to accelerate a mass of one kilogram one meter per second per second. |
| Newton meter | A Newton meter is a device that measures Newtons. |

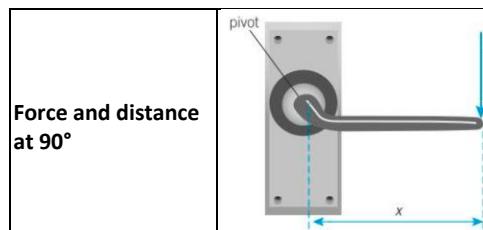
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| Weight | <p>The gravitational force on an object, measured in newtons, N.</p> $W = m \times g$ <p>W – weight (N) m – mass (kg) g – gravitational field strength (m s⁻²)</p> |
| Calibration | <p>Calibration is a comparison between a known measurement (the standard) and the measurement using your instrument. The goal of calibration is to minimise any measurement uncertainty by ensuring the accuracy of test equipment.</p> |
| Are the centre of mass and centre of gravity at the same point? | <p>If the acceleration due to gravity on all the particles of a rigid body is a constant (same), then the centre of mass coincides with the centre of gravity.</p> <p>Figure 2 The centre of gravity, through which the object's weight acts, coincides with its centre of mass</p> |
| Centre of mass | <p>A point through which any externally applied force produces straight-line motion but no rotation.</p> |
| Centre of gravity | <p>An imaginary point at which the entire weight of an object appears to act.</p> |
| Rigid body | <p>A rigid body (also known as a rigid object) is a solid body in which deformation is zero or so small it can be neglected. The distance between any two given points on a rigid body remains constant in time regardless of external forces exerted on it.</p> |
| Point mass | <p>In calculations, it is possible to consider that all of the mass in an object is concentrated into one small point.</p> |
| Plumb-line | <ul style="list-style-type: none"> - A string with a weight used to provide a vertical reference line. - A heavy object, the plumb-bob, is suspended from a piece of string. |
| Finding the centre of gravity | <ul style="list-style-type: none"> - Make small holes along the edges of the object made from card. - Insert a pin through one of the holes and hold the pin firmly in a clamp. - A freely suspended object will come to rest with its centre of gravity vertically below the point of suspension. - Hang a plumb-line from the pin and draw a line along the vertical string of the plumb-line. - Repeat the process for other holes. - The centre of gravity will be the point of intersection of the lines. |
| 3. Free-body diagrams | |
| Free body diagram | A diagram that represents the forces acting on a single object. |
| Some important forces | |
| Weight | <p>The gravitational force acting on an object through its centre of mass.</p> |
| Friction | <p>The force that arises when two surfaces rub against each other.</p> |

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| Drag | The resistive force on an object travelling through a fluid (e.g., air or water); the same as friction. |
| Tension | The force within a stretched cable or rope. |
| Upthrust | An upward buoyancy force acting on an object when it is in a fluid. |
| Normal contact force | A force arising when one object rests against another object. |
| Representing forces | - Each force vector is represented by an arrow labelled with the force it represents. - Each arrow is drawn to the same scale (the longer the arrow, the greater the force). |
| Inclined slope | A plane surface inclined to the horizon, or forming with a horizontal plane any angle but a right angle. |
| Object on a slope | |

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| Assumptions | - No friction - The only force acting on the object is its weight |
| Weight components | Parallel component $F_x = W \times \sin \theta = mxg \sin \theta$ Perpendicular component $F_y = W \times \cos \theta = mxg \cos \theta$ |
| Perpendicular forces to the slope | There is no acceleration of the object perpendicular to the slope. The normal contact force N is equal to the perpendicular component of the weight. $F_y = N = mxg \cos \theta$ |
| 4. Drag and terminal velocity | |



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| Investigating motion in a fluid | You can easily investigate the motion of an object falling affected by a drag force by using a motion sensor connected to a data-logger or a laptop. |
| 5. Moments and equilibrium | |
| Moment of force | The product of force and perpendicular distance from a pivot or stated point. moment = force × perpendicular distance of the line of action of force from the axis or point of rotation moment = Fx |
| F – force (N) X – perpendicular distance (m) Moment (Nm) | |
| Pivot | A point about which a body can rotate. |
| Equilibrium | A body is in equilibrium when the net force and net moment acting on it are zero. |
| Principle of moments | For a body in rotational equilibrium, the sum of the anticlockwise moments about a point is equal to the sum of the clockwise moments about the same point. |


Force and distance at an angle different than 90°

You can calculate the perpendicular distance x from the pivot using trigonometry.

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| 1st method | Example: $x = 0.20 \times \cos \theta$ The clockwise moment of the force must therefore be $\text{Moment} = F \times 0.20 \times \cos \theta$ |
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| 2nd method | Example: Resolve the force F into two perpendicular directions. - Component, $F \sin \theta$, has zero perpendicular distance from the pivot. - Component, $F \cos \theta$, has a perpendicular distance of 0.20 m from the pivot. The clockwise moment about the pivot is $\text{Moment} = F \times 0.20 \times \cos \theta$ |
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| 6. Couples and torques | |
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| Couple | A pair of equal and opposite forces acting on a body but not in the same straight line. |
| Torque (of a couple) | The product of one of the forces of a couple and the perpendicular distance between the forces. The moment of a couple is known as a torque. The torque of a couple is defined as $\text{torque of a couple} = \text{one of the forces} \times \text{perpendicular separation between the forces} = Fd$ F – force (N) d – perpendicular distance between two forces (m) |

| 7. Triangles of forces | |
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| Tension | The pulling force exerted by a string, cable, or chain on an object. |
| Coplanar forces | Coplanar forces are the forces lie in the same plane. The resultant of these three coplanar forces must be zero. |
| Triangle of forces | Three forces acting at a point in equilibrium, represented by the sides of a triangle. |
| Equilibrium interpretation | 1. The resultant of forces F and T must be equal in magnitude to the third force W but in the opposite direction. 2. The resultant force vertically must be zero and the resultant horizontal force must also be zero. - The force T can be resolved into its vertical and horizontal components. |

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| $T \cos \theta = F$ (vertical forces are equal, opposite direction) |
| $T \sin \theta = W$ (horizontal forces are equal, opposite direction) |

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| Objects that have shape and form |
| Example: This is a free-body diagram of a section of a bridge platform. All three coplanar forces pass through a point P in space, so you can draw a triangle of forces for the forces passing through P. |

| 8. Density and pressure | |
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| Density | The mass per unit volume of a substance. $\rho = \frac{m}{V}$ ρ – density (kg m^{-3}) m – mass (kg) V – volume (m^{-3}) $1 \text{ g m}^{-3} = 1000 \text{ kg m}^{-3}$ |
| Volume | Volume is the quantity of three-dimensional space occupied by a liquid, solid, or gas. The SI unit of volume is m^3 . |
| Atmospheric pressure | $1.0 \times 10^5 \text{ Pa}$ |

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| Pressure | The force exerted per unit cross-sectional area, measured in pascals, (Pa). |
| | $p = \frac{F}{A}$ p - pressure (Pa) F - force (N) A - surface area (m^2) $1 \text{ Pa} = 1 \text{ N m}^{-2}$ |
| Determining density | You need to know mass and volume to determine the density of a substance. |
| Measuring mass | The mass can be measured directly using a digital balance. |
| Measuring volume – irregular solids | The volume of irregular solids can be determined by displacement of a liquid. The volume is the difference between the two water levels. |
| Measuring volume – regular shaped solids | The volume of regular-shaped solids can be calculated from measurements taken with a ruler, digital callipers, or a micrometer. |

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| Measuring volume - liquids | For liquids, you can use a measuring cylinder to determine the volume. |
| | 9. $p = h\rho g$ and Archimedes' principle |
| Fluids | A substance that can flow, including liquids and gases. |
| Pressure exerted by a vertical column | $p = h \times \rho \times g$ p – pressure (Pa) h – height of the fluid column (m) g – gravitational field strength (m s^{-2}) ρ – density of a liquid (kg m^{-3}) |
| How is this equation derived? | The pressure at the base is equal to the weight W of the column divided by A . $W = \text{mass of column} \times g$ The mass of the column is the density ρ times the volume. $W = (\rho V) \times g$ The volume V of the column is Ah . $W = \rho \times Ah \times g$ The pressure p is given by $p = \frac{\rho \times A \times h \times g}{A} = h\rho g$ |

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| Pressure property | The pressure in a fluid at any particular depth is the same in all directions. |
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| Equation | Total pressure $p = p_0 + \rho \cdot g \cdot h + p$ p_0 – atmospheric pressure ($1.0 \times 10^5 \text{ Pa}$) |
| How does pressure depend on depth? | Pressure increases with depth, so the speed of water leaking from the bottom hole is larger than that from the higher ones. |
| Upthrust | The upward buoyant force exerted on a body immersed in a fluid. |
| Equation | $\text{Upthrust} = A \times \rho \times g$ A – cross sectional area (m^2) x – height (m) ρ – fluid density (kg m^{-3}) g – gravitational field strength (m s^{-2}) |

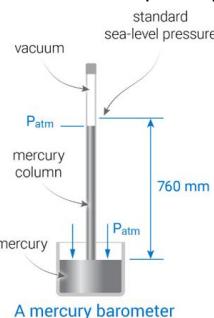
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| How is this equation derived? | This is submerged rectangular block. This block will displace the fluid. |
| | force at the top surface = $h\rho gA$ force at the bottom surface = $(h+x)\rho gA$ resultant upward force = $(h+x)\rho gA - h\rho gA = x\rho gA$ This resultant force is upthrust $\text{upthrust} = Ax\rho g$ |
| | The upthrust is equal to the weight of the fluid displaced by the block. |
| Archimedes' principle | The upthrust exerted on a body immersed in a fluid, whether fully or partially submerged, is equal to the weight of the fluid that the body displaces. |
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| Icebergs | Nine-tenths of an iceberg lie hidden underwater. |
| Water anomaly | The behaviour of liquid water is entirely different from what is found with other liquids. |

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| Density at 0°C | Water (maximum) 1000 kg m^{-3} Ice 900 kg m^{-3} |
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| Density at 4°C | Water less than 1000 kg m^{-3} |
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| Density above 4°C | Water less than 1000 kg m^{-3} |
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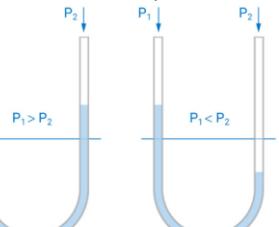
- The original mercury barometers were simply a glass tube filled with the mercury and part-vacuum.
 - The height of the mercury column would rise and fall in tandem with differing atmospheric pressure.
 - This was calibrated against a scale allowing the measurement of actual atmospheric pressure.



If both ends of the U-tube are left open to the atmosphere then the pressure on each side will be equal. As a consequence the level of the liquid on the left-hand side will be the same as the level of the liquid on the right-hand side – equilibrium.

- If one end of the U-tube is left open to the atmosphere and the other connected to an additional gas/liquid supply this will create different pressures.

- As a consequence, the liquid will be pushed down on one side with the greater pressure causing the liquid to rise on the side with the lesser pressure.



U tube manometer $p_1 > p_2$ or $p_1 < p_2$

- By measuring the different heights of liquid on the left and the right hand side of the U-tube it is possible to calculate the pressure from the outside source in relation to atmospheric pressure.

$$p = \rho g h$$

p – pressure (Pa)

h – height of the liquid column (m)

g – gravitational field strength (m s^{-2})

ρ – density of a liquid (kg m^{-3})