

Assignment 2: Implementing Sorting Algorithms in C and Creating a Shared Library for Python with Case Study

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1 Introduction

In this assignment, I implemented 4 sorting algorithms in C: Insertion, Merge, Heap, and Counting Sort. The assignment file came with an implementation of the Bubble Sort algorithm, which I did not modify. In this report, I will aim to discuss how each algorithm works, the time complexity of each algorithm, and the results of running the algorithms on a set of random integers.

2 Sorting Algorithms

2.1 Bubble Sort

Bubble Sort iterates through a list of elements and compares adjacent elements, swapping them if they are in the wrong order. This process is repeated until the list is sorted. Typically, this is implemented with two nested loops, where the outer loop iterates through the list and the inner loop iterates through the list - 1 elements checking and swapping adjacent elements. The following graphic demonstrates the process of Bubble Sort:

Initial Array:

5	3	8	2	1	4
---	---	---	---	---	---

Step 1: Compare 5 and 3 (swap)

3	5	8	2	1	4
---	---	---	---	---	---

Step 2: Compare 5 and 8 (no swap)

3	5	8	2	1	4
---	---	---	---	---	---

Step 3: Compare 8 and 2 (swap)

3	5	2	1	4	8
---	---	---	---	---	---

Step 4: Compare 8 and 1 (swap)

3	5	2	1	8	4
---	---	---	---	---	---

Step 5: Compare 8 and 4 (swap)

3	5	2	1	4	8
---	---	---	---	---	---

Array after 1 iteration:

3	5	2	1	4	8
---	---	---	---	---	---

You can see above that the largest integer bubbles to the top of the list. This process illustrates a single iteration of Bubble Sort, but it is repeated until the list is sorted.

2.2 Insertion Sort

Insertion Sort is an algorithm that, similar to Bubble Sort, iterates through a list of elements. It finds the smallest element in the list and places it at the beginning. It then finds the

second smallest element and places it in the second position, and so on. The following graphic demonstrates the process of Insertion Sort:

Initial Array:

4	-2	3	7	1	5
---	----	---	---	---	---

Step 1: Insert -2

-2	4	3	7	1	5
----	---	---	---	---	---

Step 2: Insert 1

-2	1	4	3	7	5
----	---	---	---	---	---

Step 3: Insert 3

-2	1	3	4	7	5
----	---	---	---	---	---

Step 4: Insert 5

-2	1	3	4	5	7
----	---	---	---	---	---

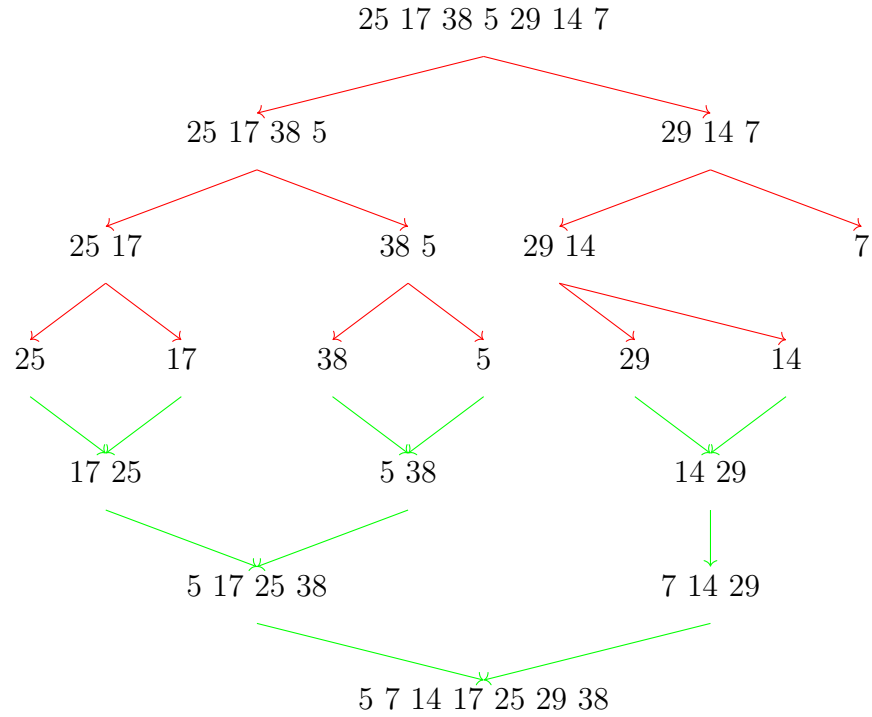
Step 5: Insert 7

-2	1	3	4	5	7
----	---	---	---	---	---

You can see above that the smallest integer is selected and placed at the beginning of the list each iteration. This results in a sorted list at the end of the process.

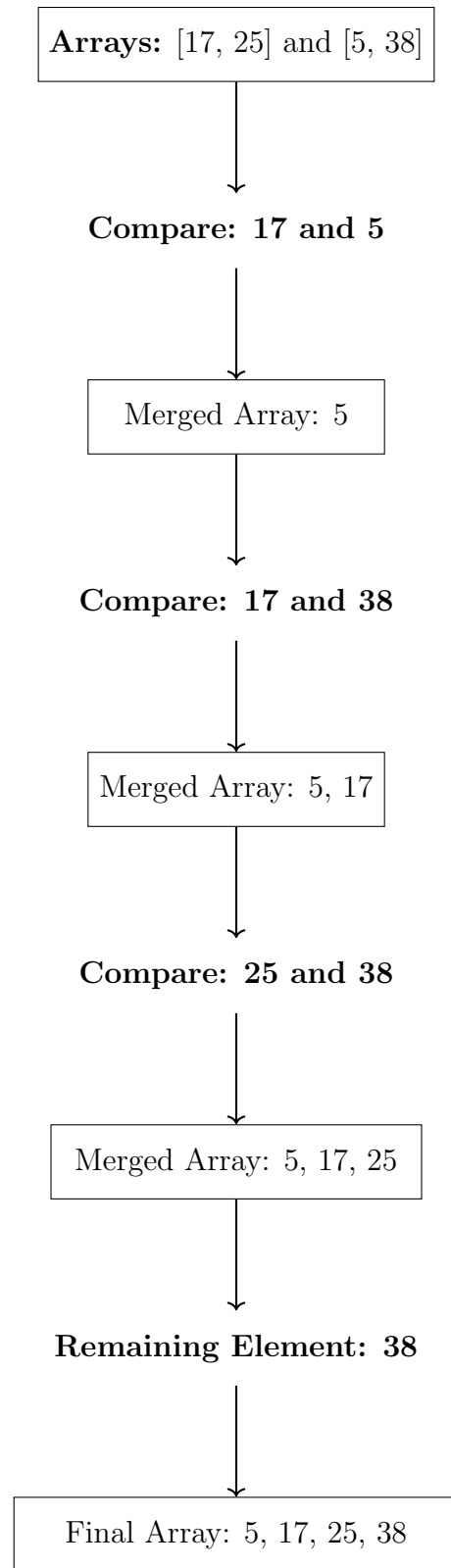
2.3 Merge Sort

Merge Sort is a recursive algorithm that divides the list into two halves, sorts each half, and then merges the two halves together. The first step is to recursively divide the list until the base case is reached (a list of size 1). A list of size 1 is considered sorted. This means that we can begin merging the lists back together in sorted order. The following graphic demonstrates the process of Merge Sort:



To elaborate on the process, the list is divided into two halves until the base case is reached (a list of size 1). When the list's are added back together, the elements are compared and merged in a sorted order. This process is repeated until the entire list is sorted.

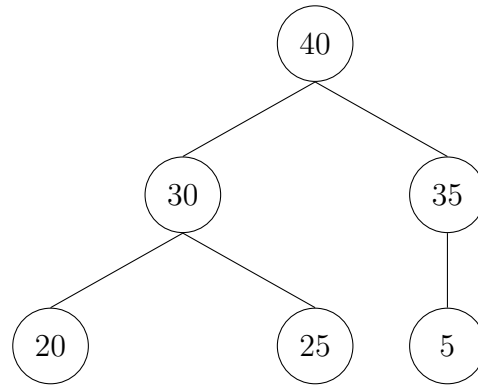
The following graphic represents the comparison of elements in a merge operation:



The process of merging two sorted lists involves comparing the first elements of each list and adding the smaller element to the merged list. When this process is repeated, the merged list is sorted.

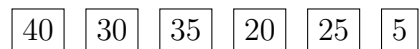
2.4 Heap Sort

Heap Sort consists of two main steps: building a heap and sorting the heap. The first step involves building a heap from the list of elements. A heap is a structure where the parent node is greater than or equal to its children. The following graphic represents a heap structure:



You can see that in the heap shown above, the parent nodes are all greater than or equal to their children nodes. When this structure is made, the root node (the largest element) is swapped with the last element in the list. Then another heap making process is done on the remaining elements while excluding the last node (since it is already sorted). This process is repeated until the entire list is sorted.

In array form, the heap structure is represented as follows:



The left node is $2 * (\text{parent node}) + 1$ and the right node is $2 * (\text{parent node}) + 2$.

The heap making process is a recursive, bottom-up process. It consists of comparing the parent node with its children and swapping them if the parent node is smaller. When a swap is performed, the process is repeated on the child node that was swapped to ensure the heap property is maintained. This process starts from the last node and works its way up to the root node.

2.5 Counting Sort

Counting Sort is different from the other sorting algorithms in that it requires knowledge of the range of elements in the list. Moreover, it doesn't require comparisons between elements unlike the other sorting algorithms. The algorithm works by counting the number of occurrences of each element in the list and then placing them in sorted order. After knowing that fact, you can create a count array that stores the number of occurrences of each element in order of their size.

To demonstrate the process, consider the following list of elements: [4, 2, 2, 8, 3, 3, 1]. The count array would look like this: [1, 2, 2, 2, 1, 0, 0, 1]. That is, there is one 1, two 2's, two 3's, one 4, no 5's, no 6's, and one 8. The sorted list would then be the number of occurrences of each element in order: [1, 2, 2, 3, 3, 4, 8].

While this process is simple, it requires knowledge of the range of elements in the list. This makes it less flexible than the other sorting algorithms, but it is very efficient when the range of elements is known.

To incorporate negatives into the Counting Sort algorithm, you can add the absolute minimum value to each element in the list. This will make all elements positive and allow the algorithm to work as intended. In this case, the minimum value (if it's a negative) should occupy the first index in the count array, which would be 0 (negative + abs(negative) = 0).

3 Compiling and Running the Algorithms

To compile the sorting algorithms, you can use the following commands:

```
1 gcc main.c mySort.c -o mySort
2 ./mySort
```

The `main.c` file contains the main function that tests the different sorting algorithms. The `mySort.c` file contains the implementation of the sorting algorithms. When you run the compiled program, it will output the results of each sorting algorithm on a set of random integers.

To create the shared library for Python, you can use the makefile provided in the assignment. The makefile as well as the `mySort.c` and `main.c` files can be found in the appendix section of this report.

4 Space and Time Complexity

Each algorithm was timed using the `time` module in Python. The following table shows the time complexity of each algorithm in comparison with the built in Python `sorted` function and the `numpy.sort()` function:

Algorithm	Time Complexity	Space Complexity	CPU Time (sec)
Bubble Sort	$O(n^2)$	$O(1)$	588.41
Insertion Sort	$O(n^2)$	$O(1)$	612.63
Merge Sort	$O(n \log n)$	$O(n)$	0.08
Heap Sort	$O(n \log n)$	$O(1)$	0.11
Counting Sort	$O(n + k)$	$O(k)$	0.02
Python <code>sorted</code>	$O(n \log n)$	$O(n)$	0.40
<code>numpy.sort()</code>	$O(n \log n)$	$O(n)$	0.06

4.1 Explanation of Time and Space Complexity

- **Bubble Sort:** Bubble Sort has a time complexity of $O(n^2)$ because it requires two nested loops to compare and swap elements. The space complexity is $O(1)$ because it doesn't require any additional space.

- **Insertion Sort:** Insertion Sort also has a time complexity of $O(n^2)$ because it requires nested loops to compare and insert elements. The space complexity is $O(1)$ because it doesn't require any additional space.
- **Merge Sort:** Merge Sort has a time complexity of $O(n \log n)$ because it divides the list into two halves and merges them in sorted order. We have n elements and the height of the tree is $\log n$, hence the reason why this algorithm is $O(n \log n)$. The space complexity is $O(n)$ because it requires additional space to store the merged list. Since at most we'll have n sublists, the space complexity is $O(n)$.
- **Heap Sort:** Heap Sort has a time complexity of $O(n \log n)$ because it builds a heap from the list and sorts it. The heap has n elements and a height of $\log n$, hence the time complexity is $O(n \log n)$. The space complexity is $O(1)$ because it doesn't require any additional space: We can just perform operations on the original list instead of making sublists like in Merge Sort.
- **Counting Sort:** Counting Sort has a time complexity of $O(n + k)$ where n is the number of elements and k is the range of elements. This is because we need to count the occurrences of each element in the list. The space complexity is $O(k)$ because we need to store the count of each element in the list. The CPU time for Counting Sort is the lowest because it doesn't require any comparisons between elements.
- **Python sorted and numpy.sort():** Both the Python `sorted` function and the `numpy.sort()` function have a time complexity of $O(n \log n)$ because they use efficient sorting algorithms. The space complexity is $O(n)$ because they require additional space to store the sorted list.

4.2 Comparison of Algorithms

From the table above, we can see that Merge Sort, Heap Sort, and Counting Sort are more efficient than Bubble Sort and Insertion Sort. This makes sense because Merge Sort, Heap Sort, and Counting Sort have better time complexity than Bubble Sort and Insertion Sort. Merge Sort and Heap Sort have a time complexity of $O(n \log n)$, which is better than the $O(n^2)$ time complexity of Bubble Sort and Insertion Sort.

In regards to the built-in Python `sorted` function and the `numpy.sort()` function, the `numpy.sort()` function is faster than the `sorted` function. In comparison to our code, the `sorted` function is slower than our C implementations of Merge Sort, Heap Sort, and Counting Sort. However, the `numpy.sort()` function is faster.

5 Appendix

5.1 mySort.c

This file contains the implementation of the sorting algorithms in C:


```

1 // CODE: include necessary library(s)
2 // you have to write all the functions and algorithms from
  scratch,
3 // You will submit this file, mySort.c holds the actual
  implementation of sorting functions
4 #include "mySort.h"
5 #include <math.h>
6 #include <stdbool.h>
7 #include <stdlib.h>
8 #include <string.h>
9
10 void swap(int *x, int *y) {
11     int temp = *x;
12     *x = *y;
13     *y = temp;
14 }
15
16 // Bubble Sort
17 void bubbleSort(int arr[], int n) {
18     for (int i = 0; i < n - 1; i++) {
19         for (int j = 0; j < n - i - 1; j++) {
20             if (arr[j] > arr[j + 1])
21                 swap(&arr[j], &arr[j + 1]);
22         }
23     }
24 }
25
26 // CODE: implement the algorithms for Insertion Sort, Merge
  Sort, Heap Sort, Counting Sort
27
28 // Insertion Sort
29 void insertionSort(int arr[], int n) {
30
31     // Iterate through each index in the array
32     for (int i = 0; i < n-1; i++) {
33
34         // Find the lowest element in the array beyond
          this point and swap it with the initial
          point
35         int *lowest = &arr[i];
36         for (int j = i+1; j < n; j++) {
37             if (arr[j] < *lowest) swap(&arr[j],
          lowest);
38         }

```

```

39     }
40 }
41
42 // Merge Sort. Given an array and the indexes of the subarray
    inclusive
43 void mergeSort(int arr[], int l, int r) {
44
45     // Get the length of the subarray
46     int n = r - l + 1;
47
48     // Base case is when only one element is in the array
49     if (n == 1) return;
50
51     // Midpoint of the array
52     int mid = (l+r) / 2;
53
54     // Recursively split the array up
55     mergeSort(arr, l, mid);
56     mergeSort(arr, mid+1, r);
57
58     // Temporary array to store the combination of the left
        and right arrays, both of which should be in sorted
        form individually
59     int tmp[n];
60
61     // Stores the indexes of the array halves
62     int indexSortedL = l;
63     int indexSortedR = mid+1;
64
65     // To check if either half is empty
66     bool depletedR = false;
67     bool depletedL = false;
68
69     // Iterate through the entire tmp array and assign the
        lesser value between the left and right half
70     for (int i = 0; i < n; i++) {
71
72         // If the current left element is less than the
            current right element, or if the right
            array has been used up, go ahead and insert
            into tmp
73         if ((arr[indexSortedL] <= arr[indexSortedR] ||
            depletedR == true) && !depletedL) {
74             tmp[i] = arr[indexSortedL];
75             indexSortedL++;

```

```

76
77         // If all the elements have been used
           up make the corresponding boolean
           true
78         if (indexSortedL > mid) {
79             depletedL = true;
80             indexSortedL=0; // To ensure no
               unsafe memory access
81         }
82     }
83
84     // If the current right element is less than
           the current left element, or if the left
           half has been used up, insert the right
           element into tmp
85     else if (arr[indexSortedR] < arr[indexSortedL]
           || depletedL == true) {
86         tmp[i] = arr[indexSortedR];
87         indexSortedR++;
88
89         // If all the right elements have been
           used up make the corresponding
           boolean true
90         if (indexSortedR > r) {
91             depletedR = true;
92             indexSortedR=0; // To ensure no
               unsafe memory access
93         }
94     }
95 }
96
97     // Replace the elements in the original array with the
           sorted elements in the same range
98     memcpy(&arr[1], tmp, n * sizeof(int));
99 }
100
101 // Function to make heap (used in the heapSort function)
102 void makeHeap(int arr[], int n, int currNodeIndex) {
103
104     // Index of the largest amongst the parent and 2 child
           nodes
105     int largest = currNodeIndex;
106
107     // Get the indexes of the child nodes
108     int leftChildIndex = currNodeIndex * 2 + 1;

```

```

109     int rightChildIndex = currNodeIndex * 2 + 2;
110
111     // Ensure that the left child index exists in the array
112     if (leftChildIndex < n) {
113
114         // If the left child index is greater than the
115         // existing largest (parent) assign it as the
116         // largest
117         if (arr[leftChildIndex] > arr[largest]) largest
118             = leftChildIndex;
119     }
120
121     // Ensure that the right child index is in the array
122     if (rightChildIndex < n) {
123
124         // If the right child index is greater than the
125         // existing largest (parent or left child)
126         // assign it as the largest
127         if (arr[rightChildIndex] > arr[largest])
128             largest = rightChildIndex;
129     }
130
131     // If the largest is not the parent we started with,
132     // swap it and ensure the subheap that was swapped is
133     // still a heap
134     if (largest != currNodeIndex) {
135         swap(&arr[currNodeIndex], &arr[largest]);
136         makeHeap(arr, n, largest);
137     }
138 }
139
140 // Heap sort
141 void heapSort(int arr[], int n) {
142
143     // Ensure we start with a max heap by going from the
144     // bottom to the top
145     for (int i = n-1; i >= 0; i--) {
146         makeHeap(arr, n, i);
147     }
148
149     // Begin actually sorting
150     for (int i = n-1; i >= 1; i--) {
151
152         // Swap the first and last indexes
153         swap(&arr[0], &arr[i]);

```

```

145
146         // Ensure max heap is made starting at the root
           node (it should be the largest)
147         makeHeap(arr, i, 0);
148     }
149 }
150
151 // Counting Sort
152 void countingSort(int arr[], int n) {
153
154     // Find the maximum and minimum value in the array
155     int max = arr[0];
156     int min = arr[0];
157     for (int i = 0; i < n; i++) {
158         if (arr[i] > max) max = arr[i];
159         if (arr[i] < min) min = arr[i];
160     }
161
162     // Length of the counting array should be the the
           number of negatives plus the number of positives
           plus another spot for 0
163     int counts[abs(min) + max + 1];
164
165     // Initialize the array as full of zeros
166     for (int i = 0; i < abs(min) + max + 1; i++) {
167         counts[i] = 0;
168     }
169
170     // Count the number of each element in the array
171     for (int i = 0; i < n; i++) {
172
173         // Increment the number of counts for whatever
           element is in the array
174         // The minimum number is added to the index to
           take care of negative values
175         counts[arr[i]+abs(min)]++;
176     }
177
178     // Go through the possible numbers
179     int index = 0;
180     for (int i = min; i <= max; i++) {
181
182         // Put the number of each element in the array
           in the actual array
183         // The index of number has the minimum number

```

```

184         added to it which is to take care of
185         negative elements
186         for (int j = 0; j < counts[i+abs(min)]; j++) {
187             arr[index] = i;
188             index++;
189     }
190 }

```

5.2 main.c

This file contains the main function that tests the sorting algorithms:

```

1 // CODE: include necessary library(s)
2 #include <stdio.h>
3 #include <string.h>
4 #include "mySort.h"
5
6 // Utility functions
7 void printArray(int arr[], int n);
8
9
10 // Test the sorting algorithms
11 int main() {
12
13     // Test cases. Uncomment the test case you want to test
14     /*int arr[] = {64, 64, -134, -5, 0, 25, 12, 22, 11, 90,
15     -500};*/
16     /*int arr[] = {9, 4, 3, 8, 10, 2, 5};*/
17     /*int arr[] = {3, 9, 2, 1, 4, 5};*/
18     int arr[] = {15, 8, -465, -500, 8, 18, 18, 30, 10, 5,
19     20, 25, 8, 3, 2, 18, 6, -28, -40, -465};
20     /*int arr[] = {1, 99, 56, 87, 322, 34, 2175, 217, 8};*/
21     /*int arr[] = {-1};*/
22
23     // Get the size of the array
24     int n = sizeof(arr) / sizeof(arr[0]);
25
26     // Copy the array to test the sorting algorithms
27     int testArr[n];
28
29     // Bubble Sort
30     memcpy(testArr, arr, n * sizeof(int));
31     printf("Original array: ");
32     printArray(testArr, n);

```

```

31 bubbleSort(testArr, n);
32 printf("Bubble sorted array: ");
33 printArray(testArr, n);
34     printf("\n");
35
36 // CODE: do the same test cases for Insertion Sort, Merge
37 // Sort, Heap Sort, Counting Sort
38 // You will submit main.c, and your project will be marked
39 // based on main.c as well
40
41 // Insertion Sort
42     memcpy(testArr, arr, n * sizeof(int));
43     printf("Original array: ");
44     printArray(testArr, n);
45     insertionSort(testArr, n);
46     printf("Insertion sorted array: ");
47     printArray(testArr, n);
48     printf("\n");
49
50 // Merge sort
51     memcpy(testArr, arr, n * sizeof(int));
52     printf("Original array: ");
53     printArray(testArr, n);
54     mergeSort(testArr, 0, n-1); // Given the start and end
55 // index inclusive
56     printf("Merge sorted array: ");
57     printArray(testArr, n);
58     printf("\n");
59
60 // Heap sort
61     memcpy(testArr, arr, n * sizeof(int));
62     printf("Original array: ");
63     printArray(testArr, n);
64     heapSort(testArr, n);
65     printf("Heap sorted array: ");
66     printArray(testArr, n);
67     printf("\n");
68
69 // Counting sort
70     memcpy(testArr, arr, n * sizeof(int));
71     printf("Original array: ");
72     printArray(testArr, n);
73     countingSort(testArr, n);
74     printf("Counting sorted array: ");
75     printArray(testArr, n);

```

```

73     printf("\n");
74
75
76     return 0;
77 }
78
79 // Helper functions
80 void printArray(int arr[], int n) {
81     for (int i = 0; i < n; i++)
82         printf("%d ", arr[i]);
83     printf("\n");
84 }

```

5.3 Makefile

This Makefile compiles the sorting algorithms into a shared library for Python. To compile the shared library, you can use the following command:

```
1 make
```

The Makefile is as follows:

```

1 libmysort.so: mySort.c
2     gcc -O3 -shared -o libmysort.so -fPIC mySort.c

```

5.4 Python Code

The raw Python code from the notebook (mySort_test.ipynb) used to time the sorting algorithms is as follows:

```

1 """mySort_test.ipynb
2
3 Automatically generated by Colab.
4
5 Original file is located at
6     https://colab.research.google.com/drive/1
7         QpWZWsyh7En4xVvJXfTrWkuDg-Yc0toK
8
9 """
10 If you are using Python on your OS, you don't need to mount
11     your Google Drive.
12 You can mount your Google Drive to access files stored there.
13     In Colab, run the
14 following code:
15 """

```



```

14 from google.colab import drive
15 drive.mount('/content/drive')
16 """
17 This will prompt you to authenticate and allow access to your
    Google Drive.
18 """
19
20 """
21 We use `time` to measure the time taken by each function.
22 """
23 import time
24
25 """
26 You can use Python's `ctypes` library to interface with the C
    shared library.
27 This allows you to call functions from the shared library in
    Python.
28
29 After compiling your C source code and creating `libmysort.so`
    shared lib with:
30 `gcc -fPIC -shared -o libmysort.so mysort.c`,
31 We will be able to load the shared library named `libmysort.so`
    in Python using
32 `ctypes.CDLL` function.
33
34 Ensure the shared library is in the same directory as the
    Python script or in a
35 location where it can be found by the loader.
36 """
37 import ctypes
38
39 """
40 We use `numpy` library to create a manipulate multidimensional
    arrays.
41 """
42 import numpy as np
43
44 """
45 You can share the memory between Python and C directly using
    the ndpointer class
46 from the numpy.ctypeslib module. This avoids copying the data
    and instead passes
47 a pointer to the NumPy arrays underlying memory buffer. We will
    use ndpointer
48 to specify the data type of inputs to the functions.

```

```

49 """
50 from numpy.ctypeslib import ndpointer
51
52 """Path to the shared library on Google Drive. Mine is in this
    directory, you can
53 change it based on your needs. If you are using your own OS,
    not colab, just use
54 './libmysort.so' if it is in the corrent directory.
55 """
56 lib_path = '/content/drive/MyDrive/libmysort.so'
57
58 # Load the shared library
59 mySortLib = ctypes.CDLL(lib_path)
60
61 # Define input argument types without conversion using
    ndpointer
62 mySortLib.bubbleSort.argtypes = [ndpointer(ctypes.c_int, flags=
    "C_CONTIGUOUS"), ctypes.c_int]
63 mySortLib.bubbleSort.restype = None
64
65 """
66 CODE: do the same for insertion sort, merge sort, heap sort,
    and counting sort.
67 """
68 mySortLib.insertionSort.argtypes = [ndpointer(ctypes.c_int,
    flags="C_CONTIGUOUS"), ctypes.c_int]
69 mySortLib.insertionSort.restype = None
70
71 # Merge sort takes an extra number input
72 mySortLib.mergeSort.argtypes = [ndpointer(ctypes.c_int, flags="
    C_CONTIGUOUS"), ctypes.c_int, ctypes.c_int]
73 mySortLib.mergeSort.restype = None
74
75 mySortLib.heapSort.argtypes = [ndpointer(ctypes.c_int, flags="
    C_CONTIGUOUS"), ctypes.c_int]
76 mySortLib.heapSort.restype = None
77
78 mySortLib.countingSort.argtypes = [ndpointer(ctypes.c_int,
    flags="C_CONTIGUOUS"), ctypes.c_int]
79 mySortLib.countingSort.restype = None
80
81 # Running a simple test
82 arr0 = np.array([64, -134, -5, 0, 25, 12, 22, 11, 90], dtype=np
    .int32)
83 n = len(arr0)

```

```

84 print("Original array:", arr0)
85
86 mySortLib.bubbleSort(arr0, n)
87 print("Sorted array using Bubble Sort:", arr0)
88
89 mySortLib.insertionSort(arr0, n)
90 print("Sorted array using Insertion Sort:", arr0)
91
92 mySortLib.mergeSort(arr0, int(n/2), int(n - n/2))
93 print("Sorted array using Merge Sort:", arr0)
94
95 mySortLib.heapSort(arr0, n)
96 print("Sorted array using Heap Sort:", arr0)
97
98 mySortLib.countingSort(arr0, n)
99 print("Sorted array using Counting Sort:", arr0)
100
101 # Creating a large test case
102 arr = np.random.choice(np.arange(-1000000, 1000000, dtype=np.
    int32), size=500000, replace=False)
103 n = len(arr)
104 print("Original array:", arr)
105
106 arr_copy = np.copy(arr)
107 start = time.time()
108 mySortLib.bubbleSort(arr_copy, n)
109 end = time.time()
110 print("Sorted array using Bubble Sort:", arr_copy)
111 print(f"Time to convert: {end - start} seconds")
112
113 """
114 CODE: do the same for insertion sort, merge sort, heap sort,
    and counting sort.
115 """
116 arr_copy = np.copy(arr)
117 start = time.time()
118 mySortLib.insertionSort(arr_copy, n)
119 end = time.time()
120 print("Sorted array using Insertion Sort:", arr_copy)
121 print(f"Time to convert: {end - start} seconds")
122
123 arr_copy = np.copy(arr)
124 start = time.time()
125 mySortLib.mergeSort(arr_copy, 0, n-1)
126 end = time.time()

```

```

127 print("Sorted array using Merge Sort:", arr_copy)
128 print(f"Time to convert: {end - start} seconds")
129
130 arr_copy = np.copy(arr)
131 start = time.time()
132 mySortLib.heapSort(arr_copy, n)
133 end = time.time()
134 print("Sorted array using Heap Sort:", arr_copy)
135 print(f"Time to convert: {end - start} seconds")
136
137 arr_copy = np.copy(arr)
138 start = time.time()
139 mySortLib.countingSort(arr_copy, n)
140 end = time.time()
141 print("Sorted array using Counting Sort:", arr_copy)
142 print(f"Time to convert: {end - start} seconds")
143
144 # Compare with built-in sort
145 start = time.time()
146 sorted_arr = sorted(arr) # Python's built-in sort
147 end = time.time()
148 print("Sorted array with built-in sort:", sorted_arr)
149 print("Time taken by built-in sort:", end - start, "seconds")
150
151 # You can also use NumPy's np.sort(), which is highly optimized
152 :
153 start = time.time()
154 np_sorted_arr = np.sort(arr) # NumPy's optimized sort
155 end = time.time()
156 print("Sorted array using Numpy sort:", np_sorted_arr)
157 print("Time taken by NumPy sort:", end - start, "seconds")

```