



## INFERENCE FOR LINEAR REGRESSION

**Welcome to the  
course!**

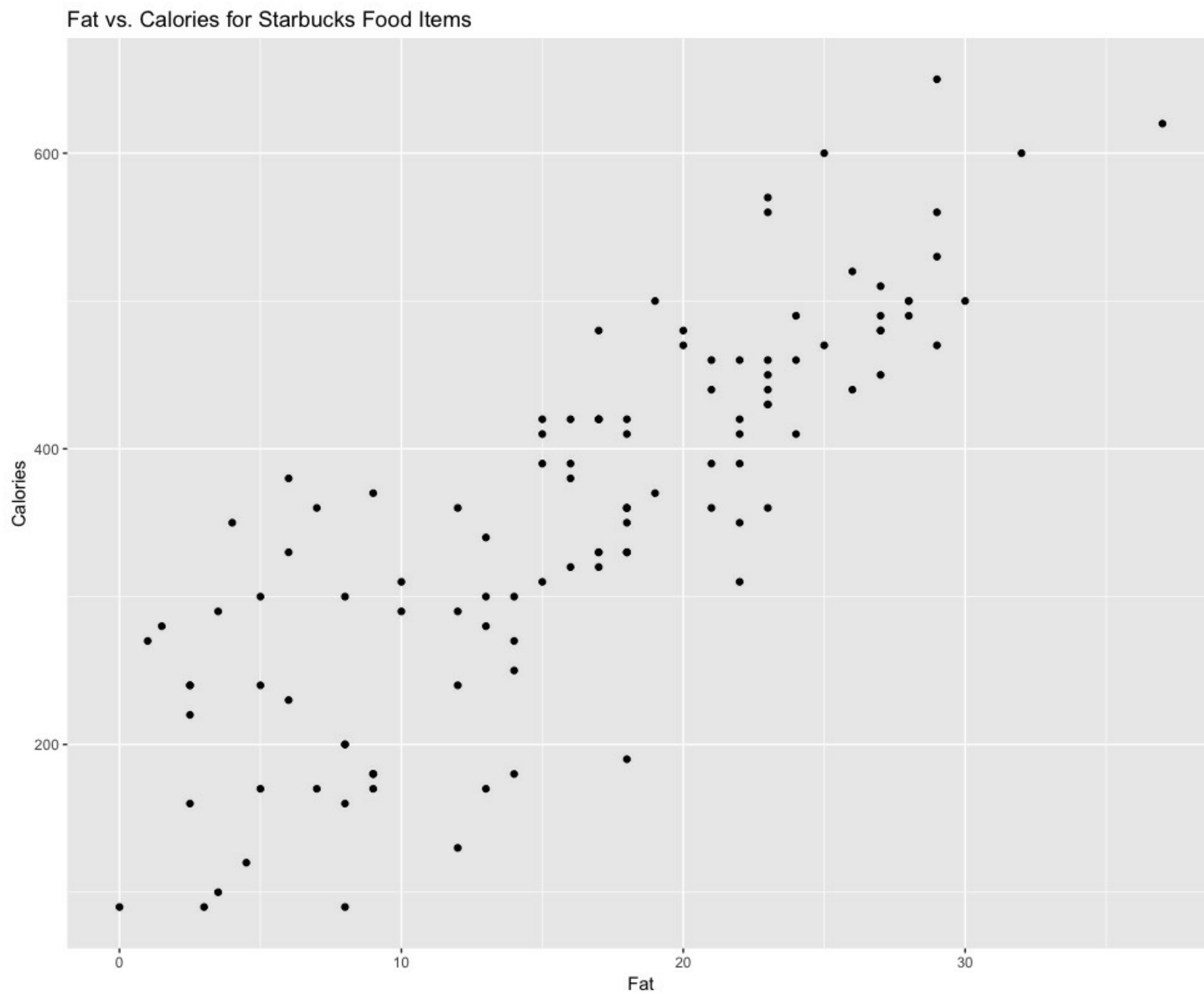
Jo Hardin

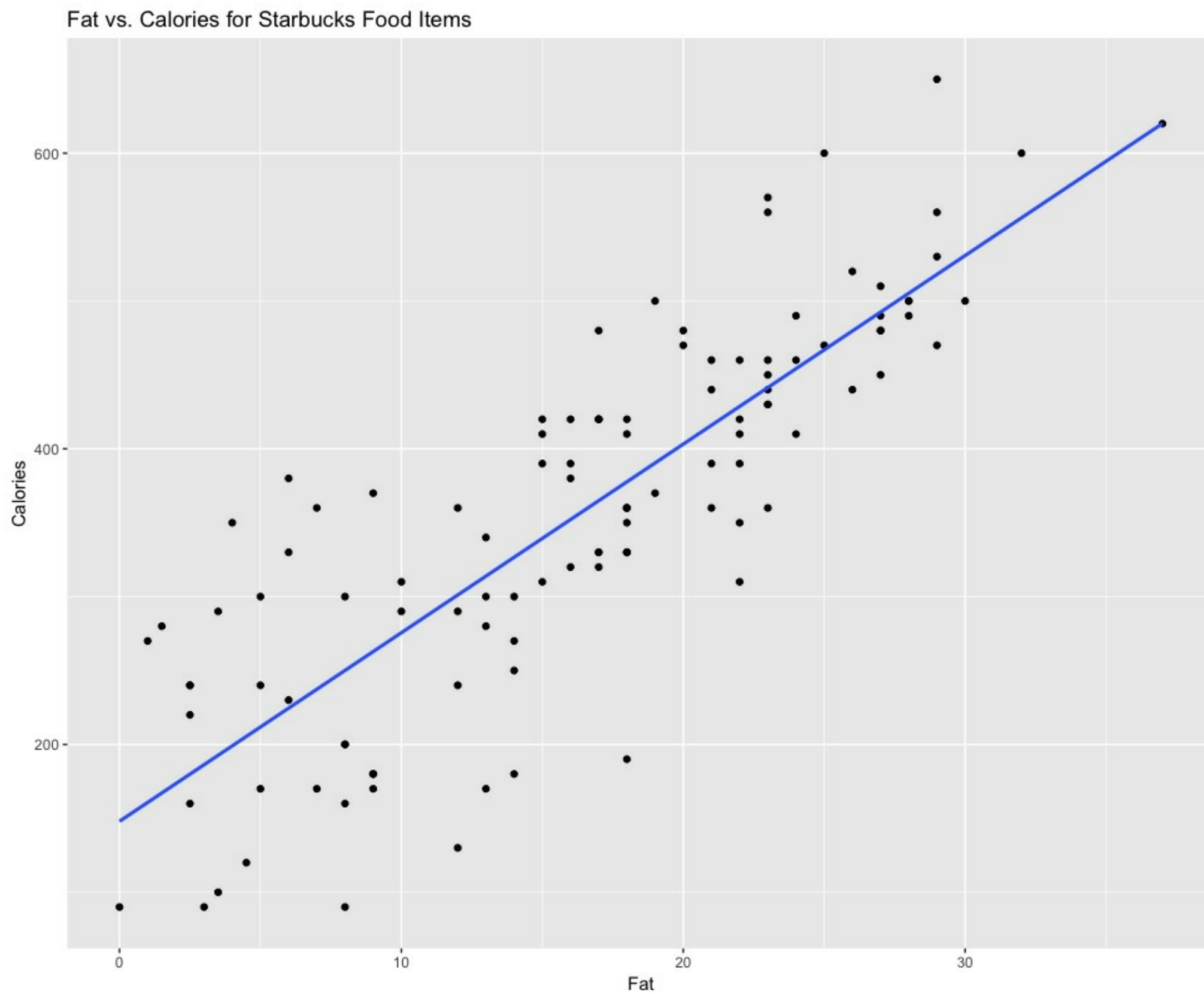
Professor, Pomona College

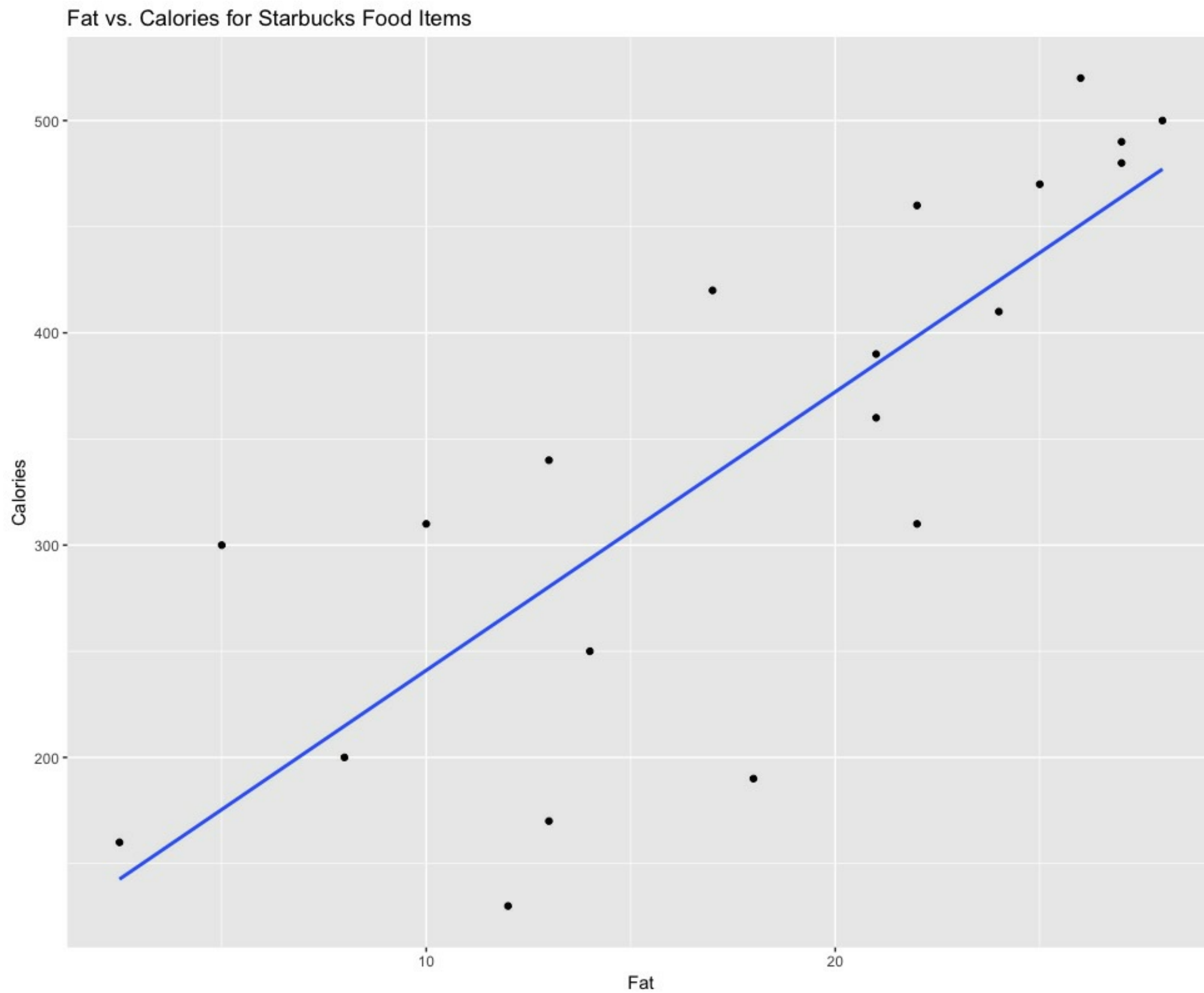


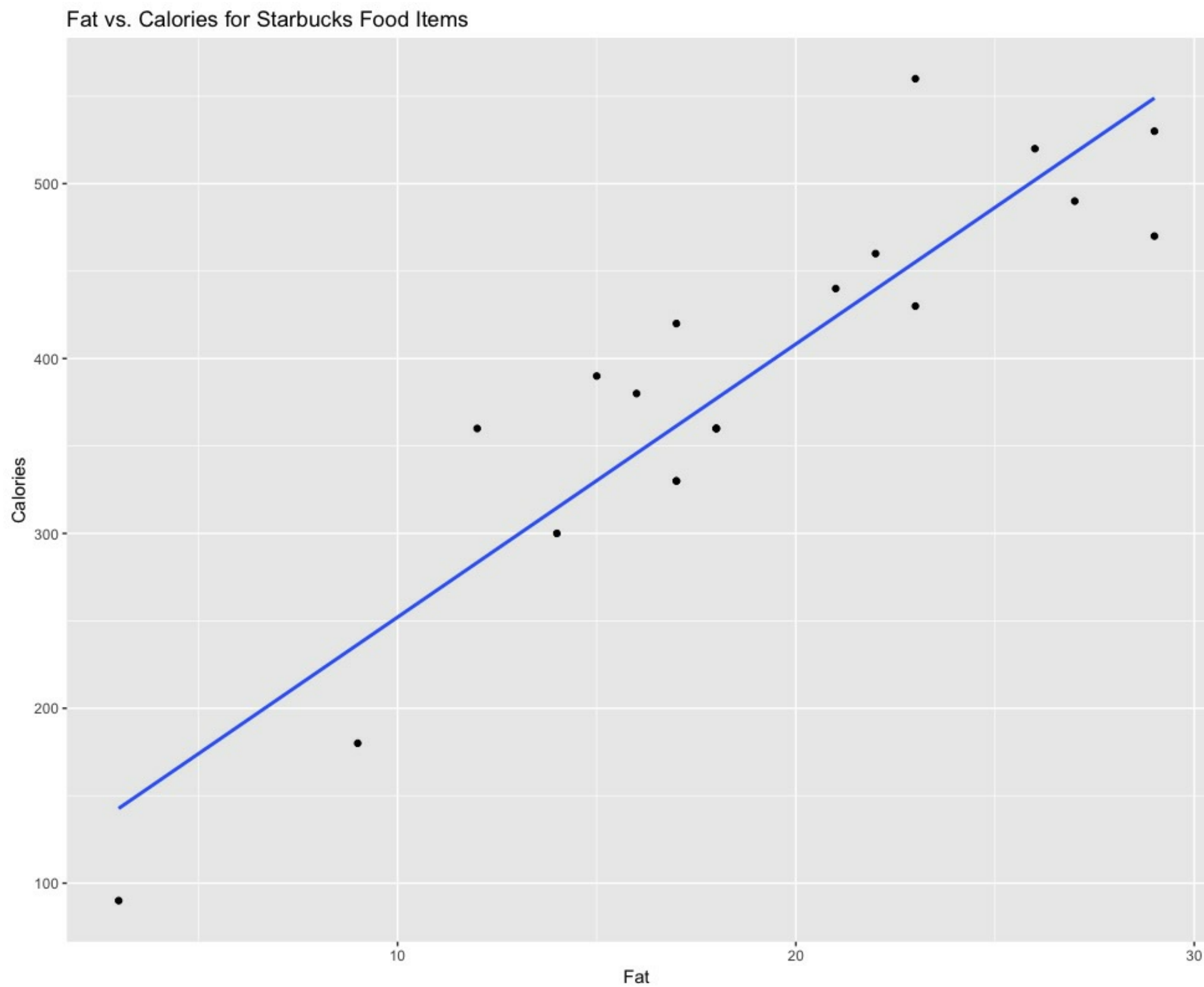
# In this course you will

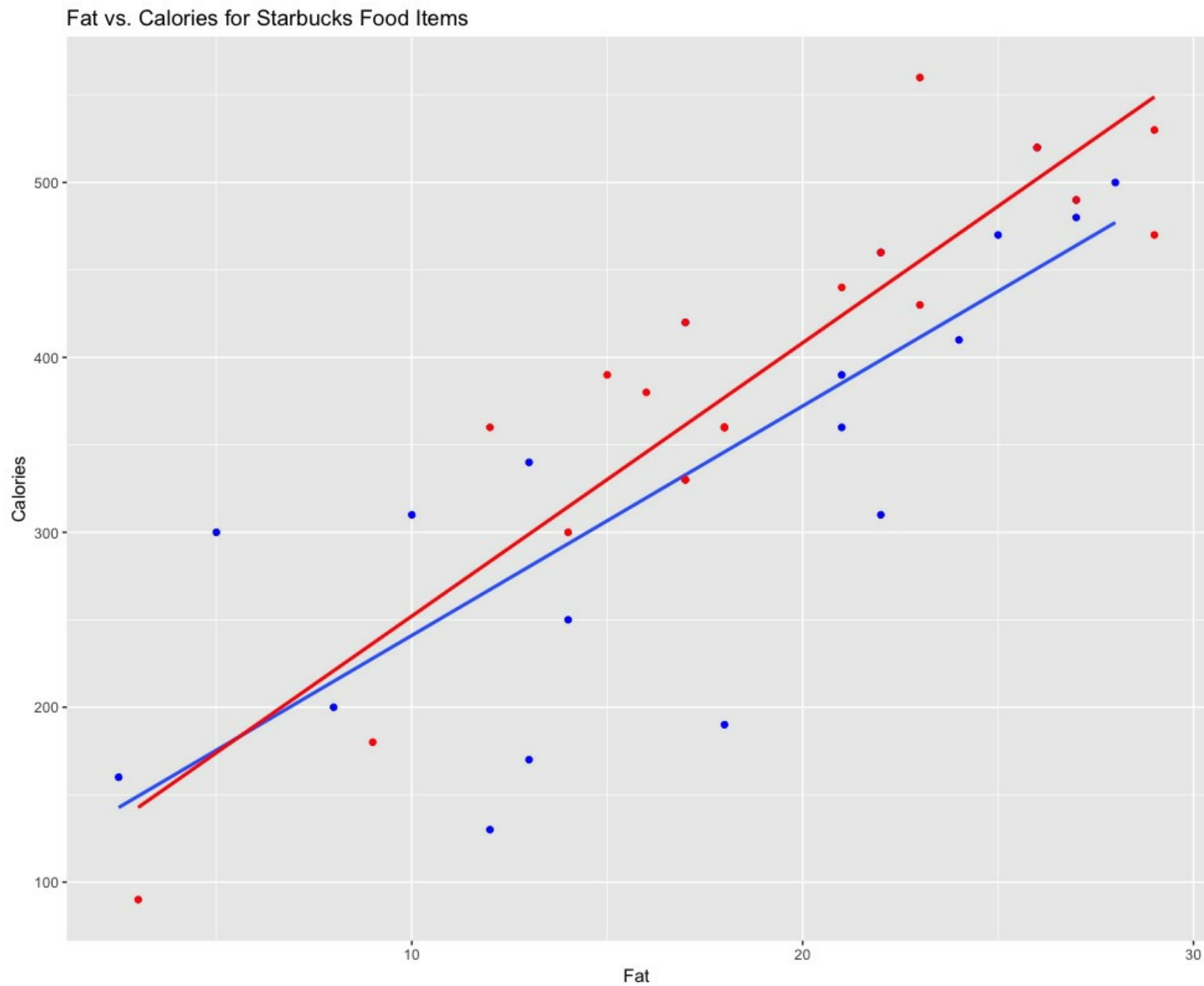
- Make inferential claims about models.
- Use least squares estimation.
- Create confidence intervals for the slope.









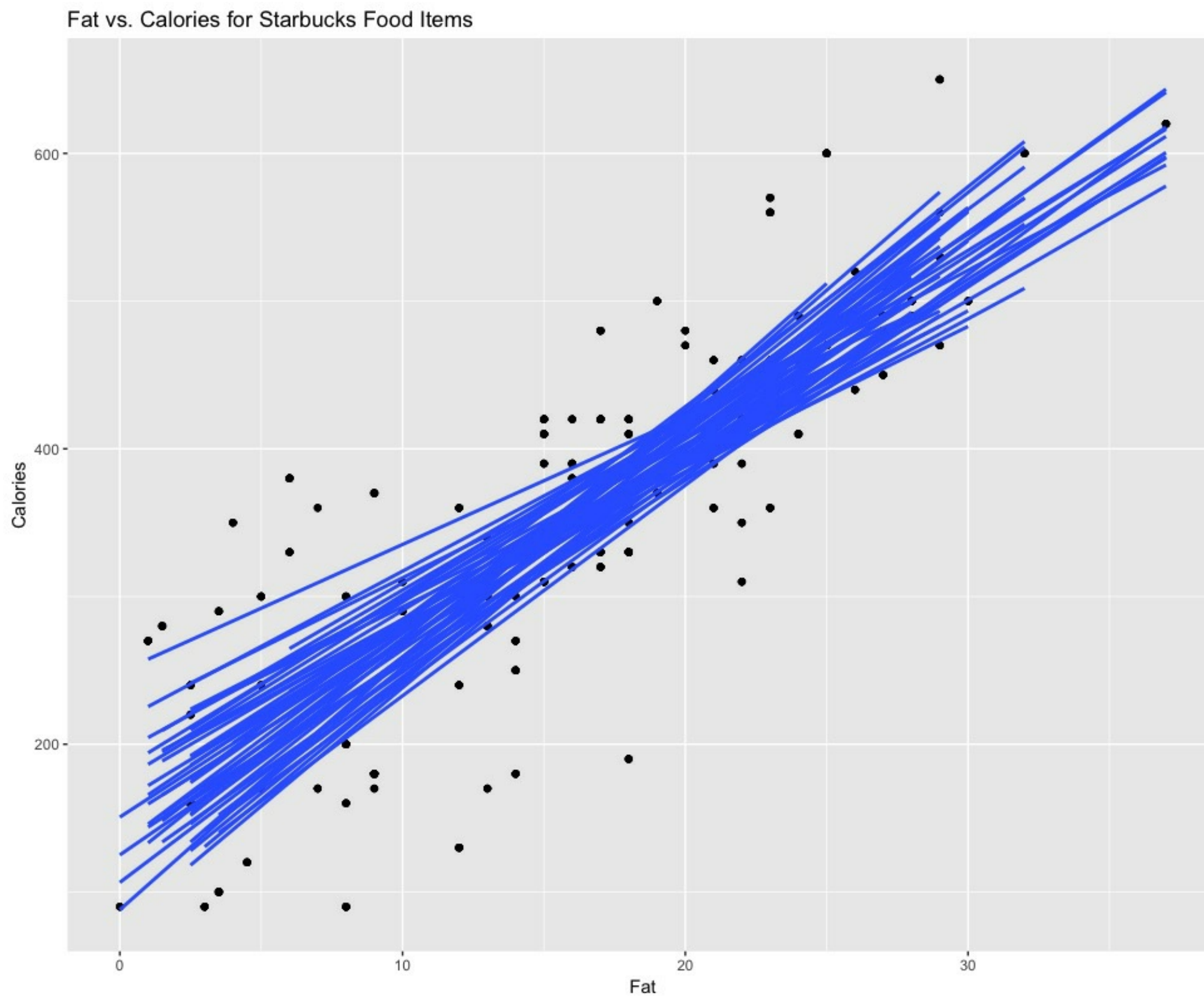


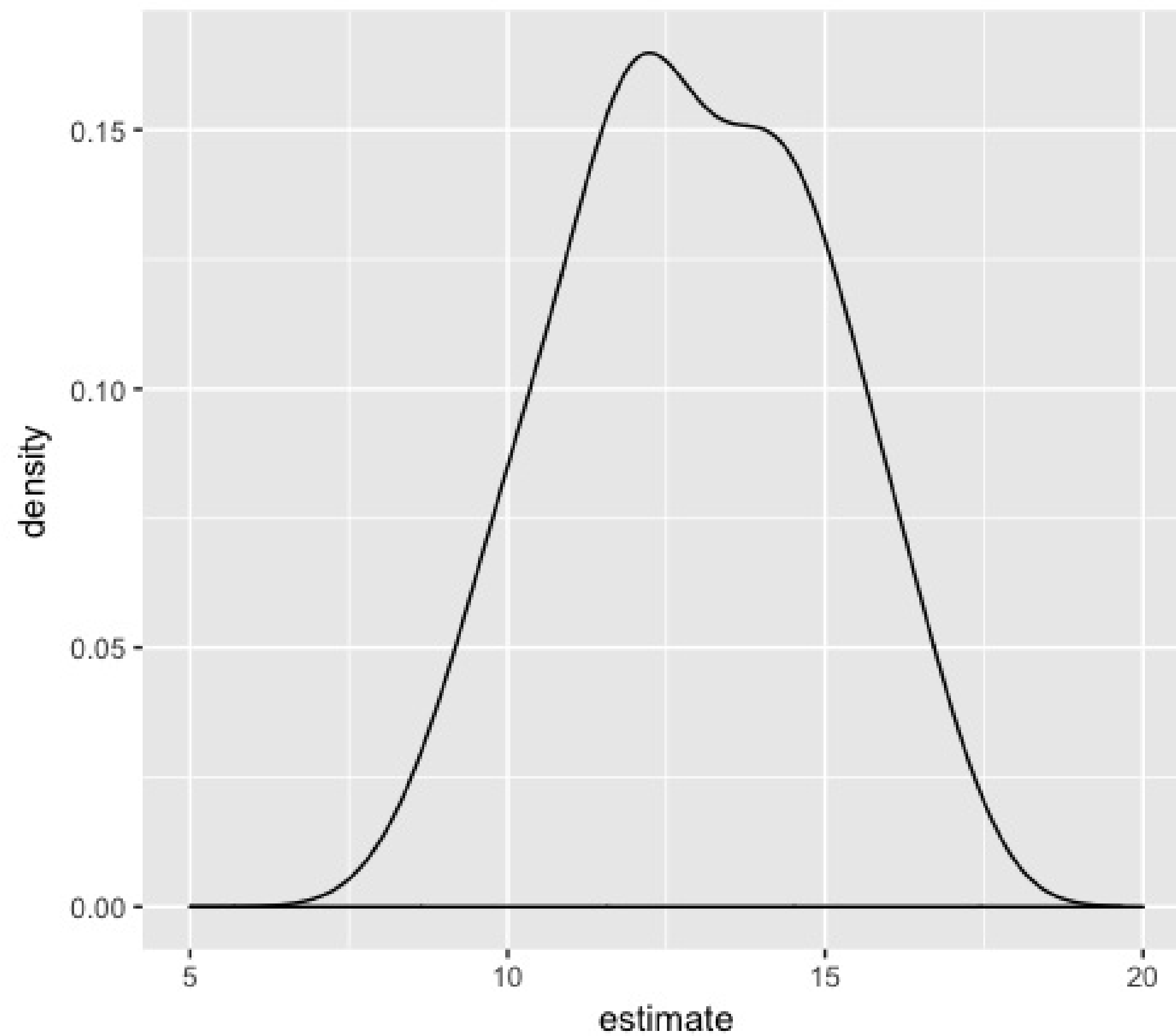


# Sampling variability

- Variability in the regression line



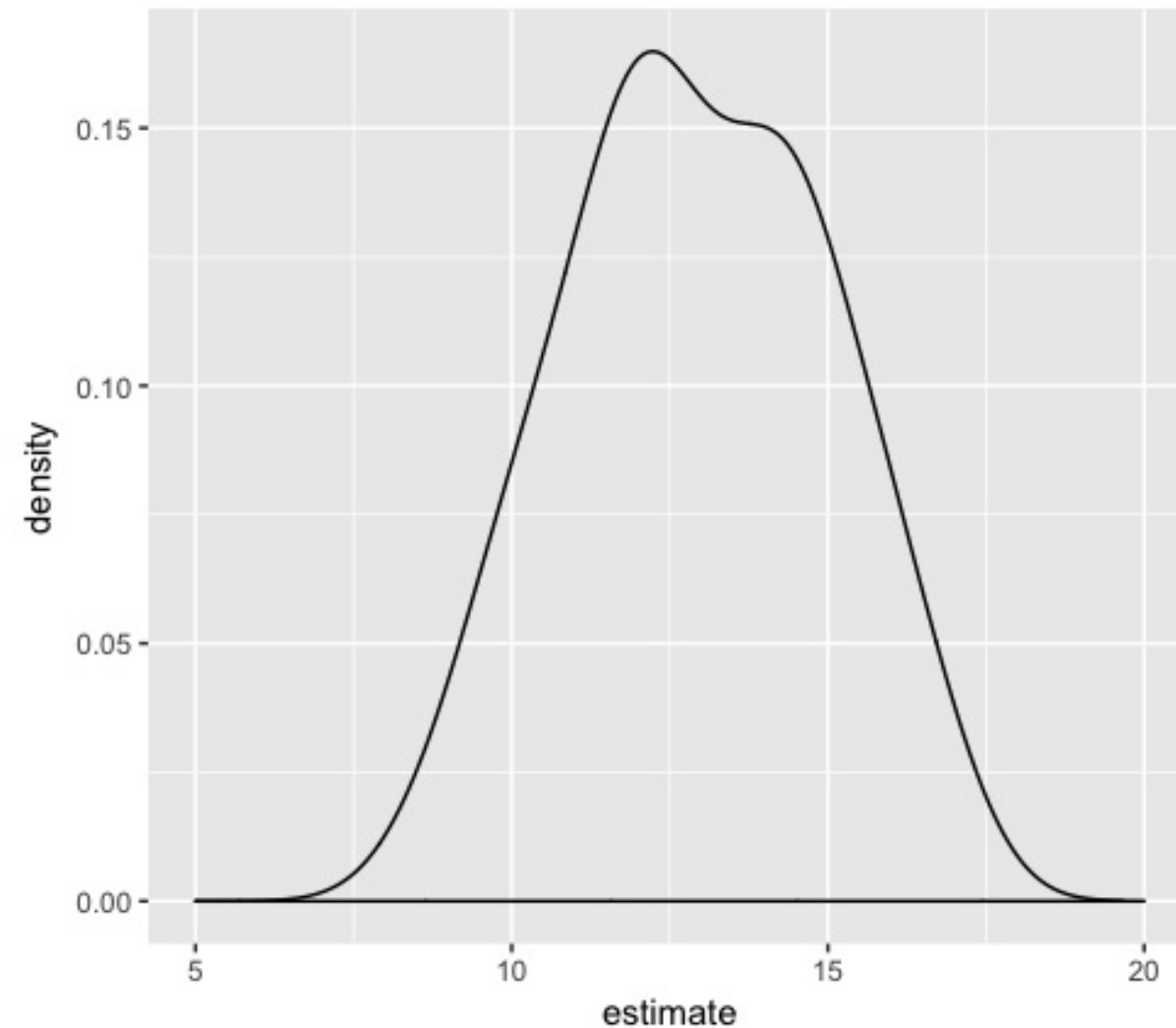


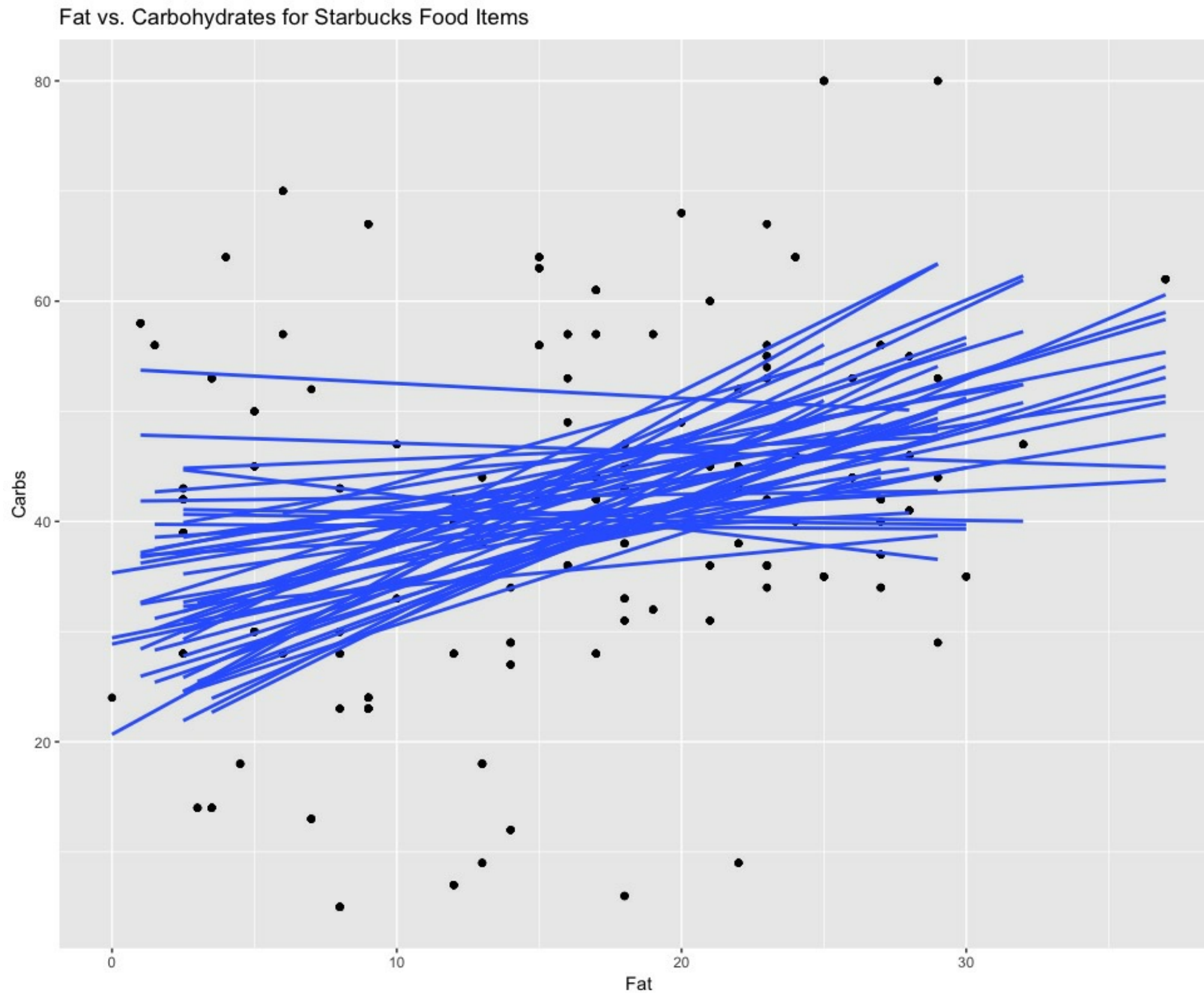


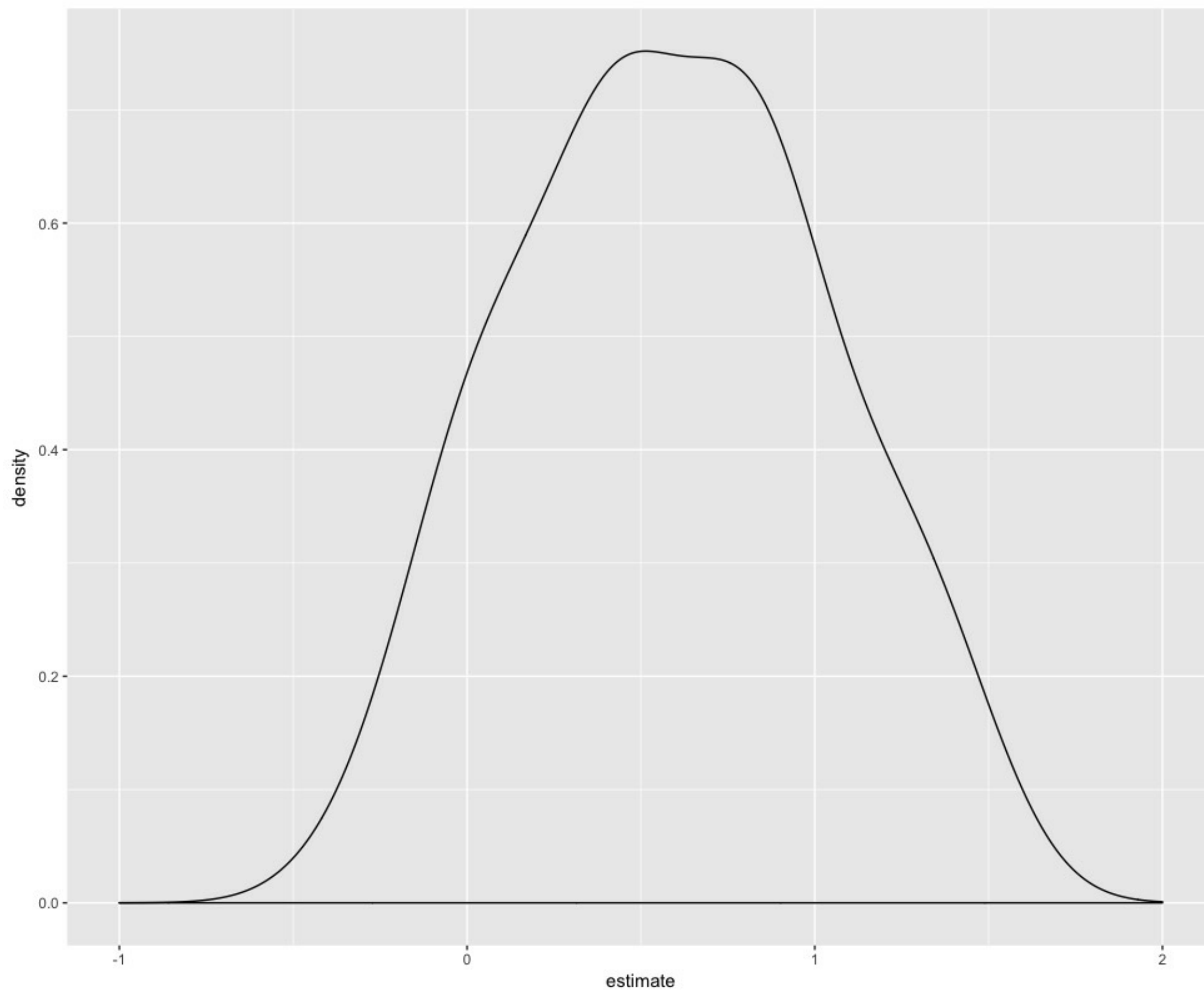


# Interpret the density plot

- Slopes between 8 and 17
- None close to zero
- Strong evidence the association is positive



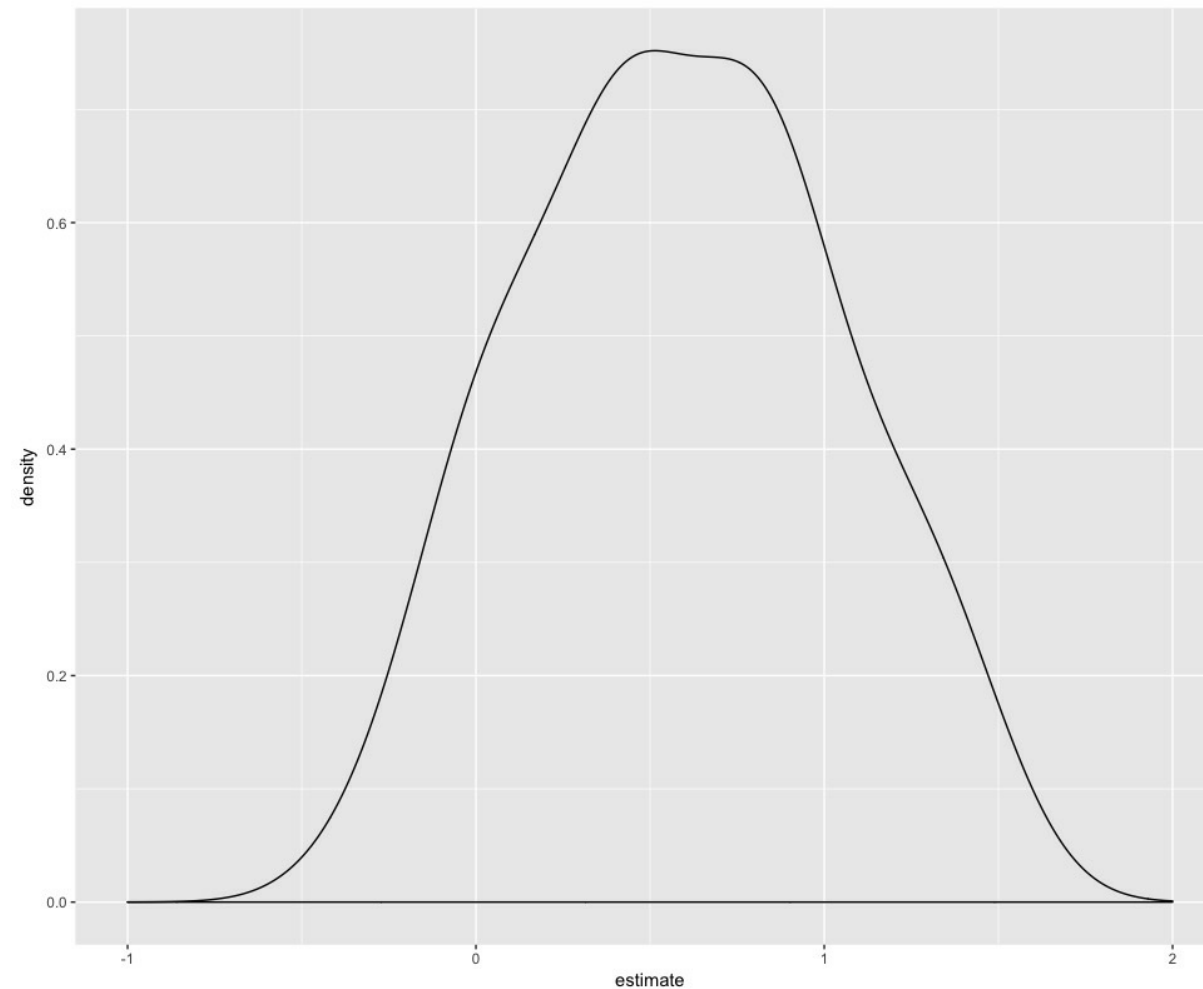






# Interpreting the density plot

- Some slopes close to zero
- High variability
- We can't make any conclusions





## INFERENCE FOR LINEAR REGRESSION

**Let's practice!**



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# Research question

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# Protein & carbohydrates: research question

## CONSIDER POSSIBLE RESEARCH QUESTIONS FOR THE STARBUCKS DATA

- Are protein and carbohydrates linearly associated in the population?  
(two-sided research question)
- Are protein and carbohydrates linearly associated in a **positive** direction in the population? (one-sided research question)

```
head(starbucks)
# A tibble: 6 x 6
#           Item Calories    Fat Carbs
#           <chr>    <int> <dbl> <int>
# 1      Chonga Bagel     300     5    50
# 2    8-Grain Roll     380     6    70
# 3  Almond Croissant     410    22    45
# 4    Apple Fritter     460    23    56
# 5  Banana Nut Bread     420    22    52
# 6 Blueberry Muffin with Yogurt and Honey 380    16    53
# ... with 2 more variables: Fiber <int>, Protein <int>
```

# Linear model output: estimates

```
summary(lm(Carbs ~ Protein, data = starbucks))

# Call:
# lm(formula = Carbs ~ Protein, data = starbucks)

# Residuals:
#      Min       1Q   Median       3Q      Max
# -35.360 -11.019   0.125   9.970  35.640

# Coefficients:
#              Estimate Std. Error t value Pr(>|t|)
# (Intercept)  37.1116     2.4680   15.04  <2e-16 ***
# Protein       0.3815     0.1734    2.20   0.0299 *
# ---
# Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
# ...
```

```
lm(Carbs ~ Protein, data = starbucks) %>% tidy()
#      term      estimate std.error statistic    p.value
# 1 (Intercept) 37.1116401 2.4680349 15.036919 1.539345e-28
# 2 Protein    0.3814696 0.1734226  2.199654 2.990434e-02
```

# Linear model output: standard error

```
Call:
lm(formula = Carbs ~ Protein,
    data = starbucks)

Residuals:
    Min       1Q   Median       3Q      Max
-35.360 -11.019   0.125   9.970  35.640

Coefficients:
            Estimate Std. Error
(Intercept)  37.1116     2.4680
Protein       0.3815     0.1734

            t value Pr(>|t|)
(Intercept)  15.04   <2e-16 ***
Protein       2.20   0.0299 *
--
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summary(lm(Carbs ~ Protein,
            data = starbucks))
```

```
Std. Error
2.4680
0.1734
```

```
lm(Carbs ~ Protein,
    data = starbucks) %>%
  tidy()
```

```
std.error
2.4680349
0.1734226
```

# Linear model output: statistic

```
Call:
lm(formula = Carbs ~ Protein,
    data = starbucks)

Residuals:
    Min       1Q   Median       3Q      Max
-35.360 -11.019   0.125   9.970  35.640

Coefficients:
            Estimate Std. Error
(Intercept)  37.1116     2.4680
Protein       0.3815     0.1734
            t value Pr(>|t|)
(Intercept)  15.04   <2e-16 ***
Protein       2.20   0.0299 *
--
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
summary(lm(Carbs ~ Protein,
            data = starbucks))
```

```
t value
15.04
2.20
```

```
lm(Carbs ~ Protein,
    data = starbucks) %>%
  tidy()
```

```
statistic
15.036919
2.199654
```

# Linear model output: p.value (two-sided)

```
Call:
lm(formula = Carbs ~ Protein,
    data = starbucks)

Residuals:
    Min       1Q   Median       3Q      Max
-35.360 -11.019   0.125   9.970  35.640

Coefficients:
            Estimate Std. Error
(Intercept)  37.1116     2.4680
Protein       0.3815     0.1734
            t value Pr(>|t|)
(Intercept)  15.04   <2e-16 ***
Protein       2.20   0.0299 *
--
Signif. codes:
  0 '***' 0.001 '**' 0.01 '*' 0.05
  '.' 0.1 ' ' 1
```

```
summary(lm(Carbs ~ Protein,
            data = starbucks))
```

```
Pr(>|t|)
<2e-16 ***
0.0299 *
```

```
lm(Carbs ~ Protein,
    data = starbucks) %>%
  tidy()
```

```
p.value
1.539345e-28
2.990434e-02
```



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**Let's practice!**

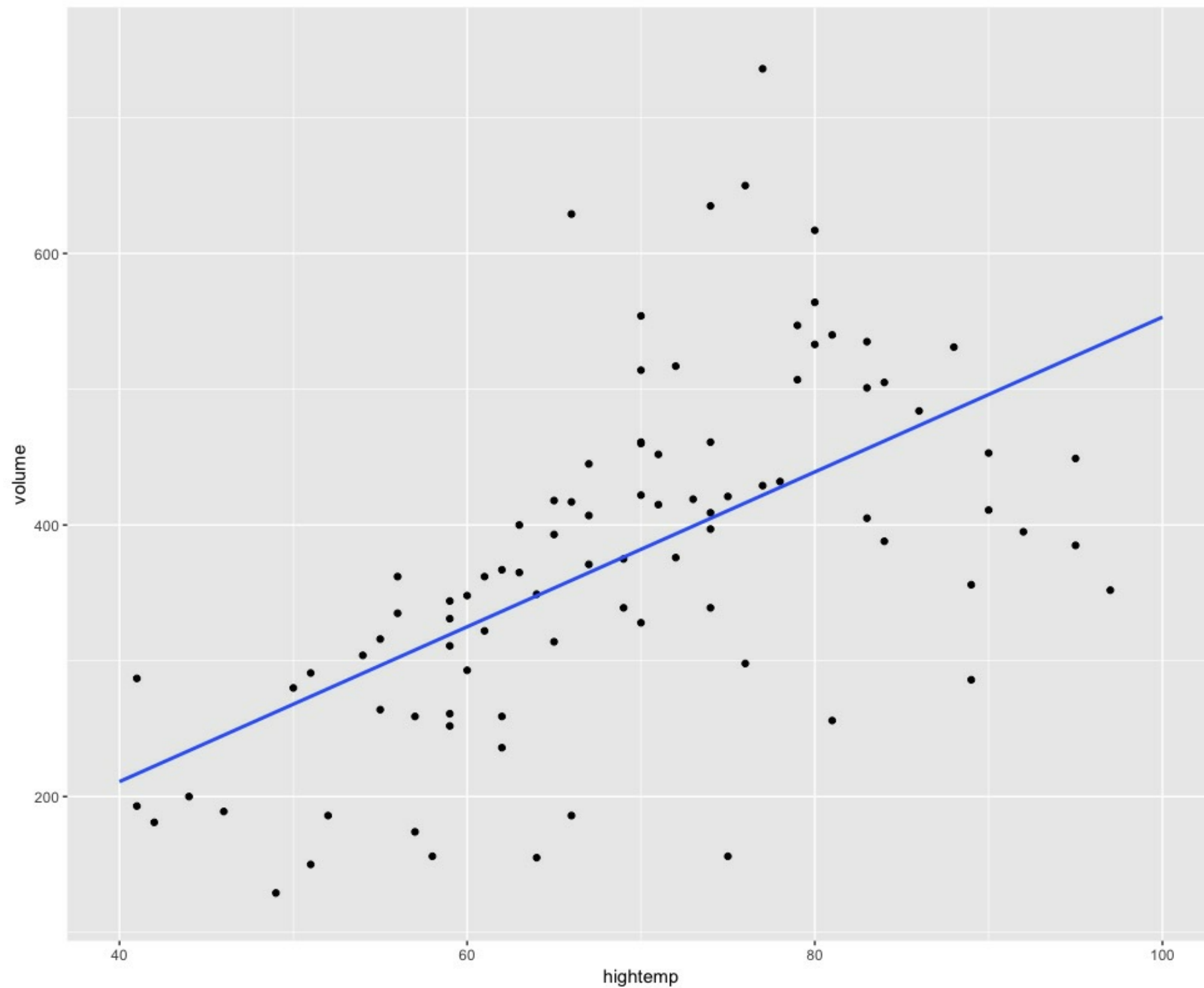


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# Variability of coefficients

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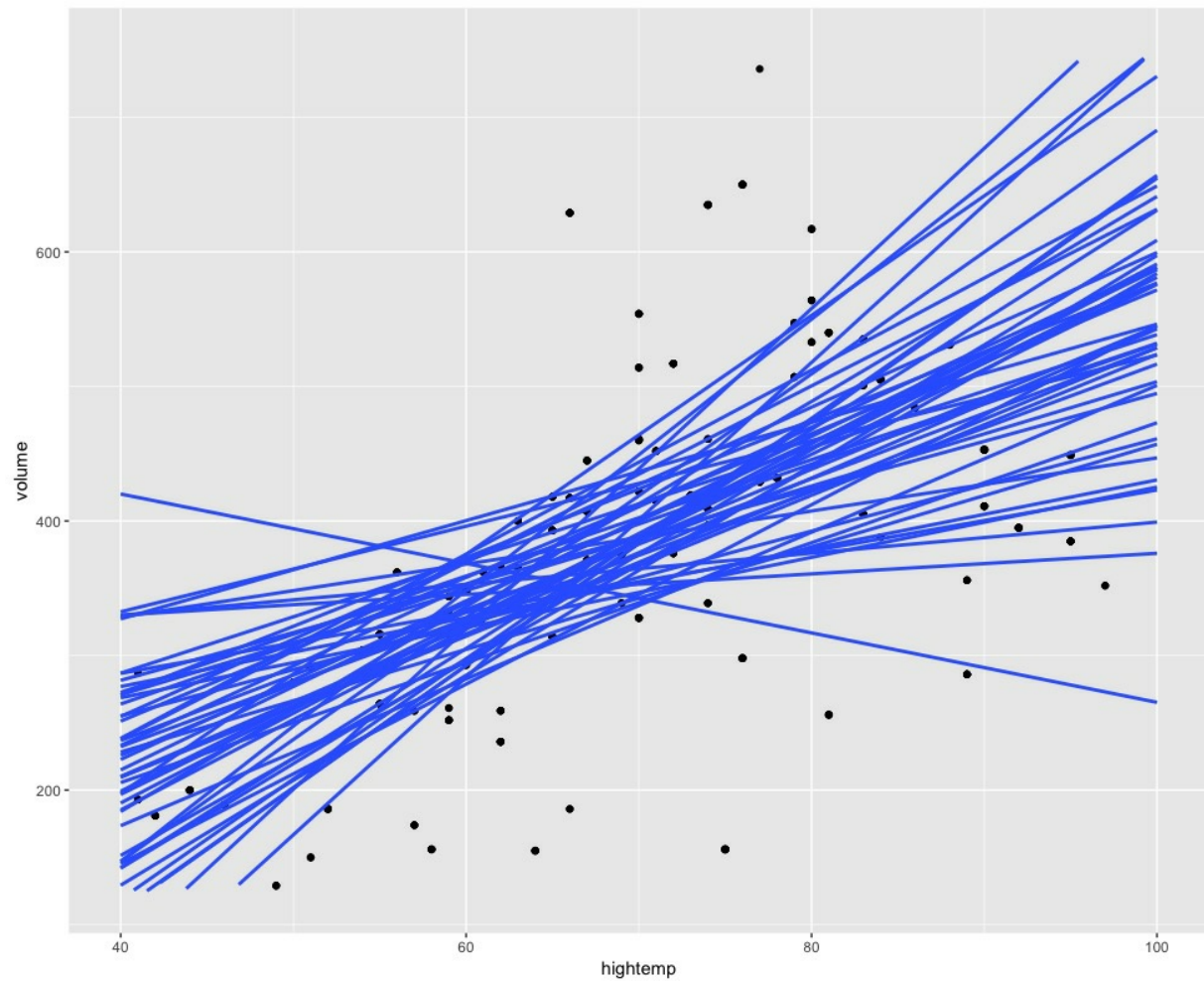




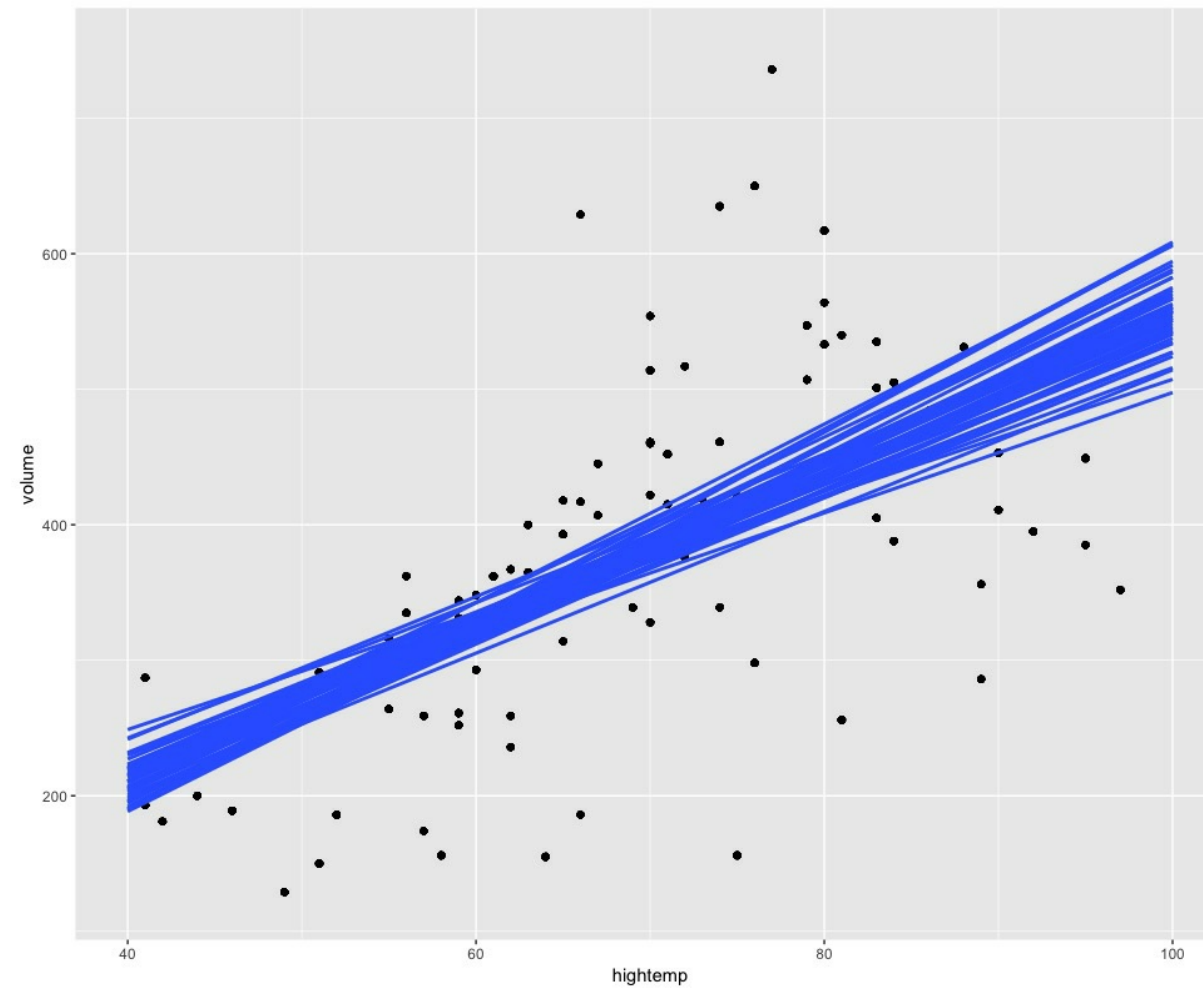


# RailTrails -- a change in sample size

n=10



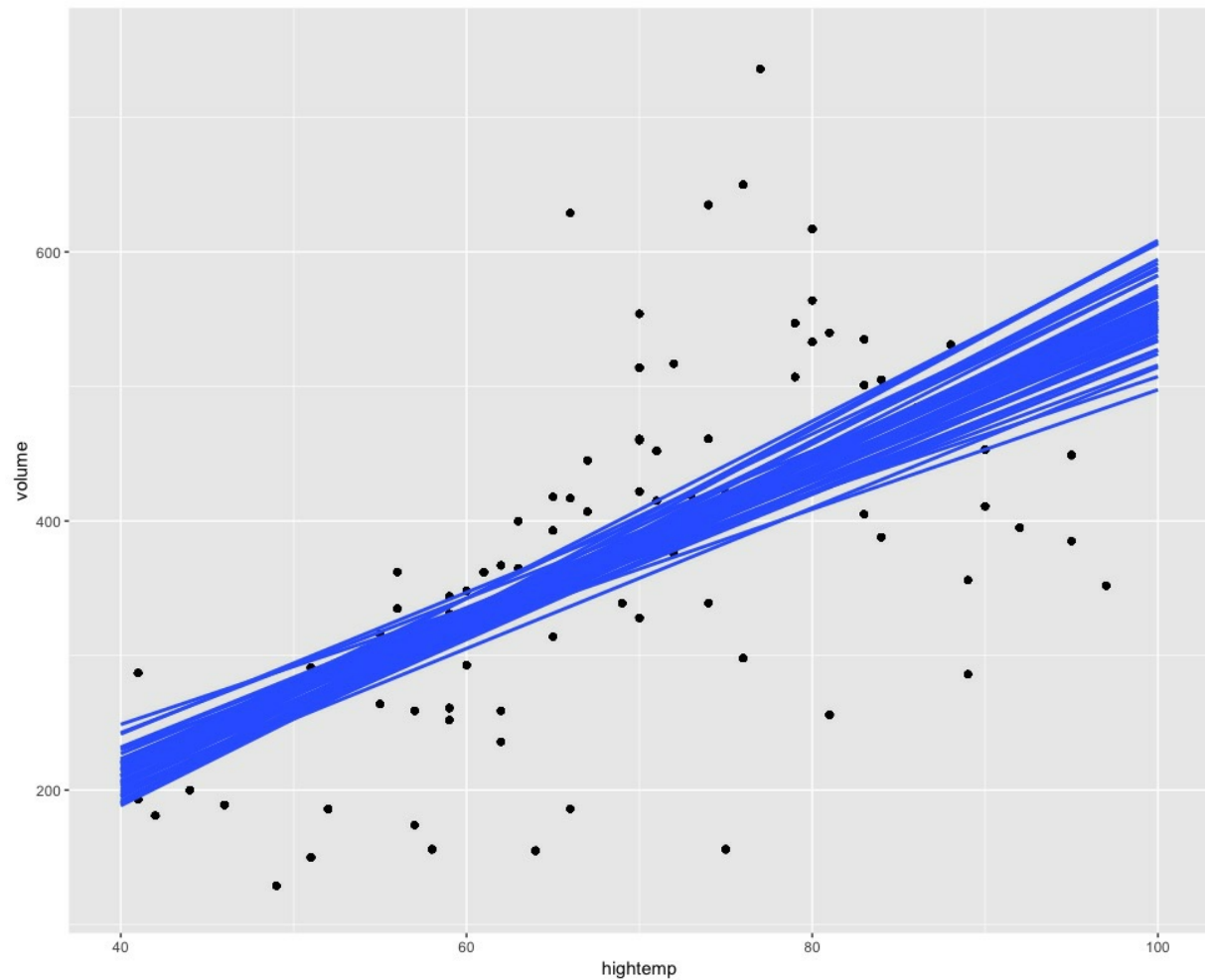
n=50



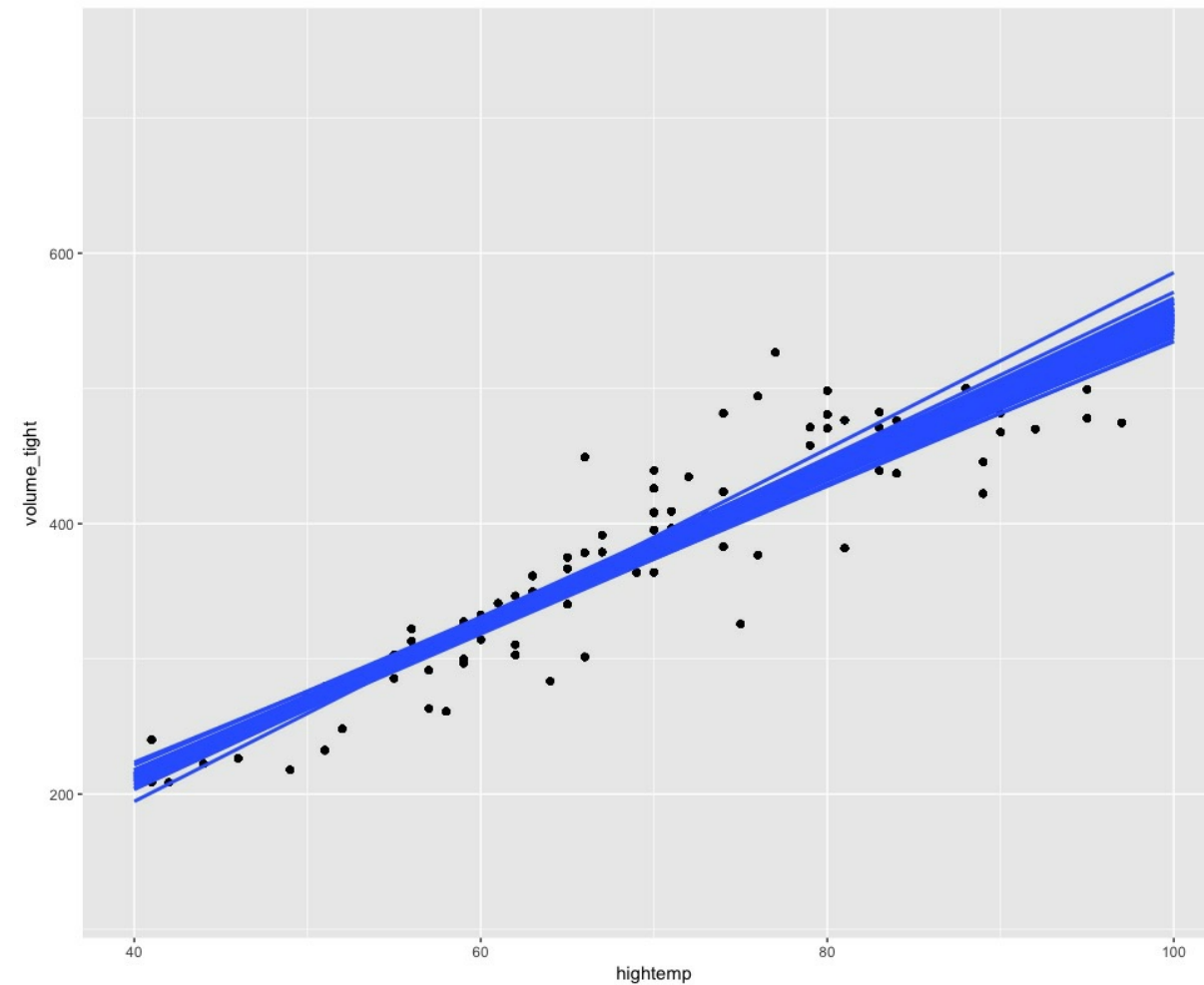


# RailTrails -- less variability around the line

n=50, original data



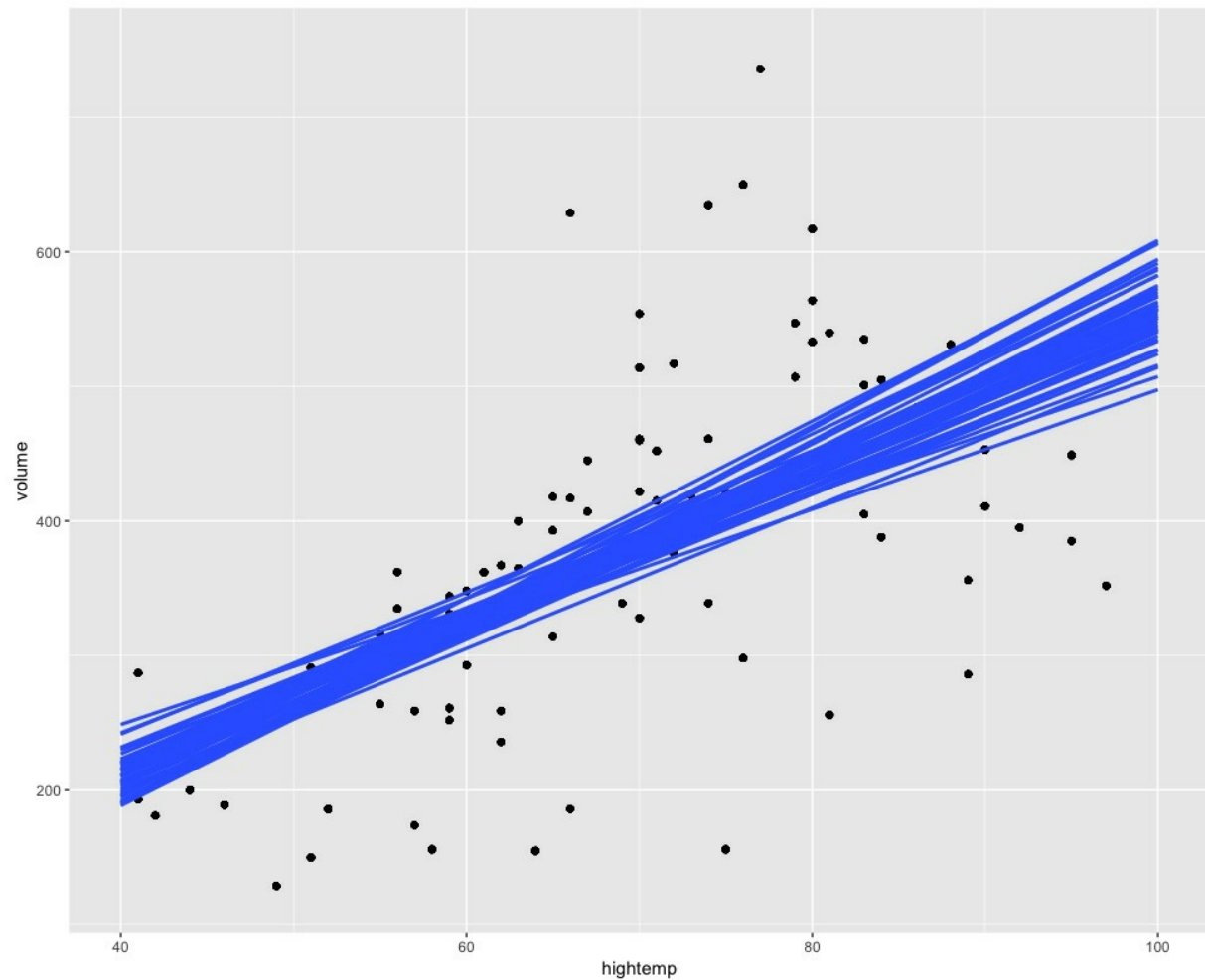
n=50, tighter data



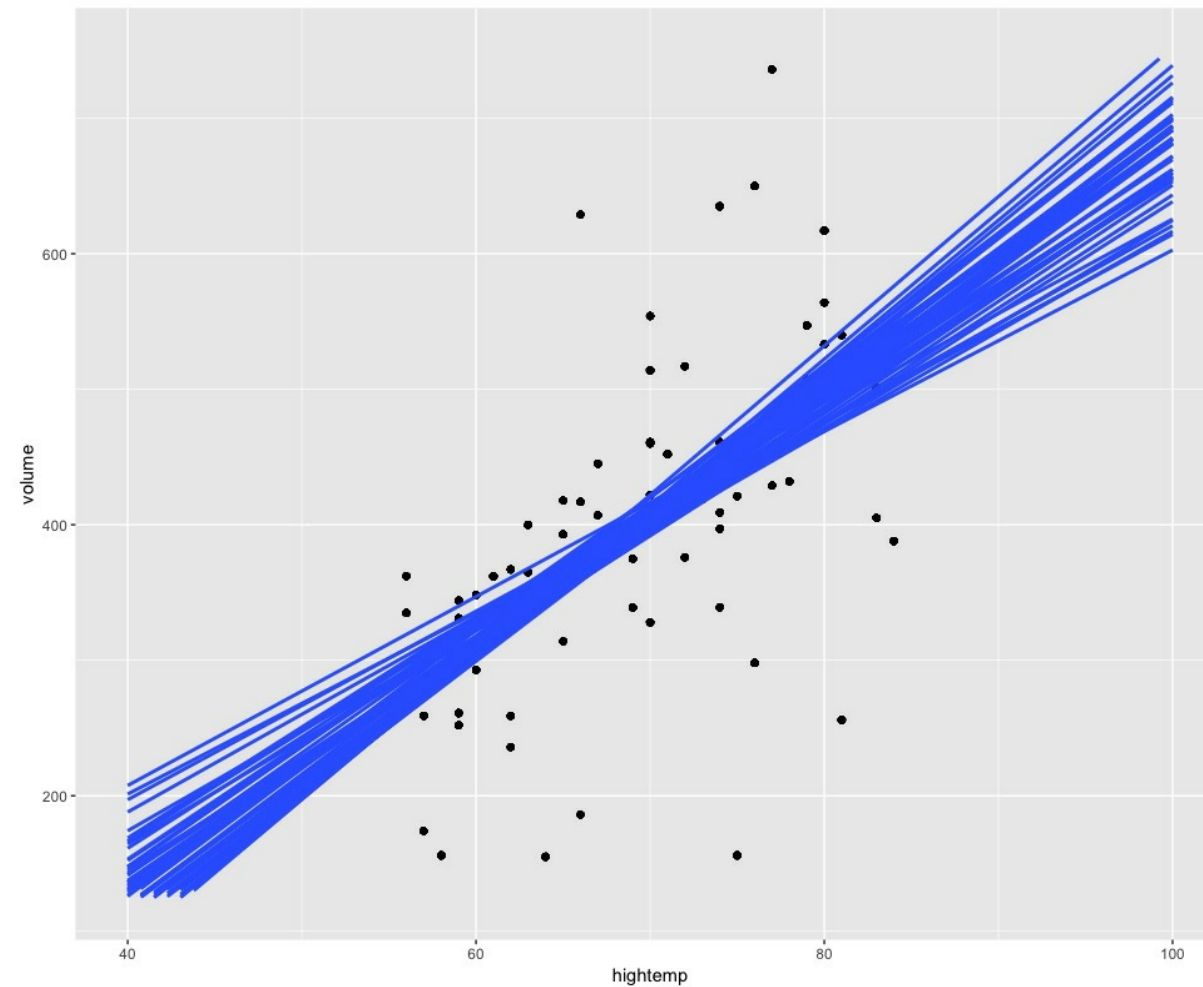


# RailTrails -- less variability in the x direction

n=50, original data



n=50, less data in x-direction





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**Let's practice!**