

$$\begin{aligned}
P(S=si) &= 0.75 \\
P(C = si \mid S = si) &= 0.8 \\
P(C = si \mid S = no) &= 0.45 \\
P(A = si \mid C = si) &= 0.95 \\
P(A = si \mid C = no) &= 0.25
\end{aligned}$$

**¿Cuál es la probabilidad de que un alumno, no habiendo estudiado (S=no), comprenda la asignatura (C=si) y, aún así, suspenda (A=no)?**

$$P(A = no \mid S=no, C =si) = P(A=no \mid C=si) = 1 - P(A = si \mid C = si) = 1-0.95 = \mathbf{0.05}$$

**¿Cuál es la probabilidad de que un estudiante comprenda la asignatura? ¿y de que la apruebe?**

$$P(S = no) = 1-P(S=si) = 1-0.75 = \mathbf{0.25}$$

$$P(C = no \mid S = si) = 1 - P(C = si \mid S = si) = 1 - 0.8 = \mathbf{0.2}$$

$$P(C = no \mid S = no) = 1 - P(C = si \mid S = no) = 1 - 0.45 = \mathbf{0.55}$$

$$\begin{aligned}
P(A = si) &= P(S = si) P(C = si \mid S = si) P(A = si \mid C = si) + \\
&\quad P(S = si) P(C = no \mid S = si) P(A = si \mid C = no) + \\
&\quad P(S = no) P(C = si \mid S = no) P(A = si \mid C = si) + \\
&\quad P(S = no) P(C = no \mid S = no) P(A = si \mid C = no)
\end{aligned}$$

$$\begin{aligned}
&= 0.75 * 0.8 * 0.95 + \\
&\quad 0.75 * 0.2 * 0.25 + \\
&\quad 0.25 * 0.45 * 0.95 + \\
&\quad 0.25 * 0.55 * 0.25
\end{aligned}$$

$$= 0.57 + 0.0375 + 0.1068 + 0.034375 = \mathbf{0.748675}$$

$$P(A = no) = 1-P(A=si) = 1 - 0.748675 = \mathbf{0.251325}$$

$$\begin{aligned}
P(C = si) &= P(A = si) P(S = si \mid A = si) P(C = si \mid S = si) + \\
&\quad P(A = si) P(S = no \mid A = si) P(C = si \mid S = no) + \\
&\quad P(A = no) P(S = si \mid A = no) P(C = si \mid S = si) + \\
&\quad P(A = no) P(S = no \mid A = no) P(C = si \mid S = no)
\end{aligned}$$

$$\begin{aligned}
&= P(A = si) P(S = si) P(C = si \mid S = si) + \\
&\quad P(A = si) P(S = no) P(C = si \mid S = no) + \\
&\quad P(A = no) P(S = si) P(C = si \mid S = si) + \\
&\quad P(A = no) P(S = no) P(C = si \mid S = no)
\end{aligned}$$

$$\begin{aligned}
&= 0.748675 * 0.75 * 0.8 + \\
&\quad 0.748675 * 0.25 * 0.45 + \\
&\quad 0.251325 * 0.75 * 0.8 + \\
&\quad 0.251325 * 0.25 * 0.45
\end{aligned}$$

$$= 0.449205 + 0.08422 + 0.1507 + 0.0282 = \mathbf{0.712325}$$

Sabiendo que un alumno ha aprobado, ¿cuál es la probabilidad de que haya comprendido la asignatura?

$$P(C = \text{si} \mid A = \text{si}) = (P(A = \text{si} \mid C = \text{si}) P(C = \text{si})) / P(A = \text{si}) = (0.95 * 0.71) / 0.75 = \mathbf{0.899}$$