# Redes Bayesianas: Grafo acíclico dirigido

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#### Bibliografía

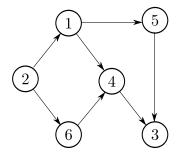
Castillo97: E. Castillo, J.M. Gutiérrez, y A.S. Hadi (1997). Sistemas Expertos y Modelos de Redes Probabilísticas. Academia de Ingeniería.

# Grafo acíclico dirigido [Castillo97, Sec 4.4, p.124]

#### Formalismo

- Un grafo acíclico dirigido G es un par (V, E)
- $V = \{1, ..., n\}$  es el conjunto de **vértices**
- $E \subset \{(u, v) : u, v \in V, u \neq v\}$  es el conjunto de arcos
- No hay ciclos dirigidos en G

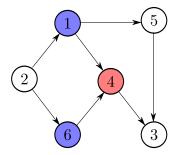
# Ejemplo



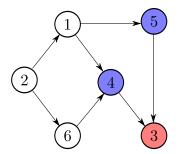
#### Conceptos

Padres, hijos, caminos, ancestros, orden ancestral, subgrafo, grafo moralizado

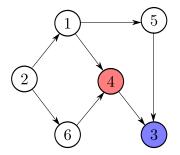
# **Padres**



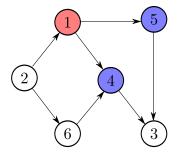
# **Padres**

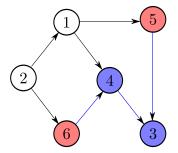


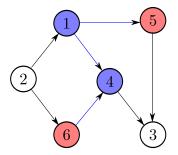
# Hijos

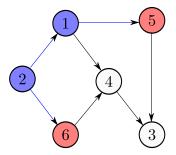


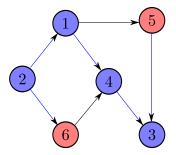
# Hijos



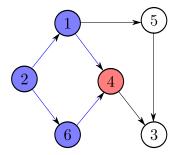




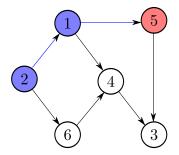




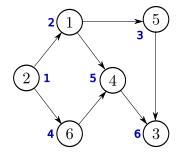
# Conjunto ancestral



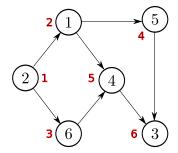
# Conjunto ancestral



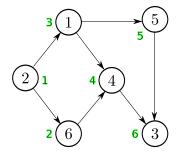
#### Orden ancestral



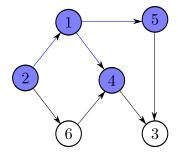
#### Orden ancestral



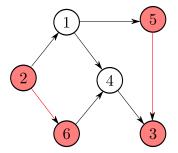
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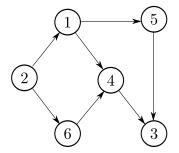
# Subgrafo inducido



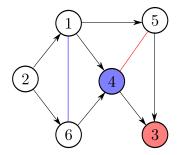
# Subgrafo inducido



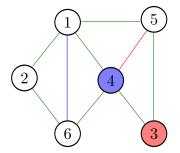
#### Grafo moralizado



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#### Grafo moralizado



#### Para qué sirven?

- Soporte gráfico de las redes Bayesianas
- Determinan su factorización
- Determinan su modelo de dependencia: criterio de separaciónn gráfica