Parallel Huffman Coding

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Abstract—This report aims to explain the design of a parallel encoding and decoding Huffman algorithm. The application is developed with the C99 programming language, using MPI for multiprocessing and OpenMP for multithreading to scale horizontally with increasing hardware resources. Our tool is both able to exploit multiprocessing to process concurrently multiple files, and to split the Huffman coding of the same file among multiple threads.

Comparing this tool with other online implementations, we can state that...

Index Terms—Huffman, MPI, OpenMP, High Performance Computing

I. INTRODUCTION

Even if the Huffman algorithm is not directly used nowadays, its prefix mechanism is still part of Deflate (PKZIP's algorithm), JPEG, and MP3 compression algorithms

II. THE HUFFMAN ALGORITHM

The Huffman algorithm has the objective of finding a more convenient bit representation to store information through lossless compression. Instead of considering groups of eight bits as the way to encode data, the Huffman algorithm uses variable-length sequences of bits with prefixes defined as *alphabet*.

A. Priority Queue

The Huffman algorithm uses a minimum priority queue to build its alphabet efficiently. This specific data structure ensures logarithmic insertion and deletion time with respect to its size. We implemented the minimum priority queue by using a minimum heap. Practically speaking, to implement the min-heap tree, we used a standard C array ensuring that the min-heap property still holds at every insertion and deletion:

$$A[i] \le A[l(i)], A[i] \le A[r(i)] \tag{1}$$

where A[i], A[l(i)], and A[r(i)] are respectively a node, its left child, and its right child in a min-heap tree.

To implement the priority queue also a parallel approach has been considered [1], but since it contains only 256 elements (1 byte), we did not consider it too important in terms of performance.

B. Encoding

The Huffman encoding procedure makes use of a minimum priority queue to build its alphabet efficiently. The idea is to build a tree similar to Figure 1 that defines all the variable-length prefix sequences of bits: these sequences are represented by the path from the tree root to a leaf. Using a greedy approach, the Huffman encoding ensures that the less frequent a byte is in a file, the more probable is to have a longer Huffman representation, which means that his path from the root to its specific leaf is longer.

Once having computed the frequencies for each one of the 256 different bytes in a file, the Huffman algorithm populates a min priority queue with Huffman tree nodes storing the byte value and its frequency. Successively, it removes the least two frequent bytes from the queue, creates a new node with children the two extracted nodes, assigns to it a dummy character and the sum of the frequencies of its two children, and inserts it into the min priority queue. After n-1 iterations, the last node is the root of the Huffman tree [2]. Algorithm 1 explains in the detail this procedure.

Algorithm 1: Build the Huffman tree

```
1 // Populate the min priority queue with characters and
    their frequencies
\mathbf{2} \ \mathbf{for} \ i = 1 \ \mathbf{to} \ n-1 \ \mathbf{do}
       Q.insert(f[i], Tree(f[i], c[i]))
4 // Repeat until the queue has only a single element left
5 for i = 1 to n - 1 do
       // Get the two least frequent nodes
       z1 = Q.deleteMin()
       z2 = Q.deleteMin()
       // Create an inner tree node and insert it into the
       z = Tree(z1.f + z2.f, null)
10
       z.left = z1
11
12
       z.right = z2
       Q.insert(z.f, z)
13
```

- 14 // The last element in the queue is the root of the Huffman tree
- 15 **return** Q.deleteMin()

Once built the Huffman tree, it is possible to generate the

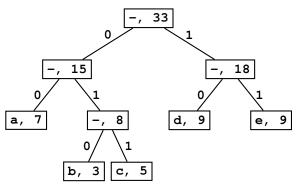


Fig. 1: An example of Huffman tree.

Huffman alphabet visiting the tree using a DFS algorithm, assigning 0 to each left-child traverse and 1 for the right one as presented in Algorithm 2. Finally, it is possible to compress the file by creating a stream of bits corresponding to its content using the Huffman alphabet.

Algorithm 2: Encode using Huffman tree

C. Decoding

Once having the encoded file and the Huffman tree, it is straightforward to decompress the file to its original shape. The prefix alphabet ensures to have that it is possible to visit the tree using a DFS approach and get a unique decoded version of the file using an approach similar to Algorithm 2.

III. SERIAL HUFFMAN IMPLEMENTATION

To be able to implement the Huffman encoding and decoding algorithm, several things have been taken into account.

- The byte frequencies computed during the encoding process are saved in the compressed file. In this way, the decoding procedure can easily rebuild the Huffman tree.
- Both the encoding and decoding procedures make use of buffers to improve I/O performance: the streams of bytes are first written inside the buffer and then saved on the disk.
- \bullet The encoding procedure works with chunks of 4096 bytes. This ensures that the tool can handle even large files when dealing with bit buffers. The decoding procedure deals with chunks of maximum size of 4096*32

bytes, since the maximum length of a Huffman tree traverse from root to leaf is of 256 bits, which is 32 times a byte. As explained later, dealing with chunks makes handy the parallel implementation of the encoding and decoding algorithms.

 In the encoded file, the chunk offsets are saved at the end of the file: this ensures that the compressed stream of prefixed sequences of bits is still meaningful.

IV. PARALLEL HUFFMAN IMPLEMENTATION

To parallelize the serial Huffman algorithm over threads and processes, we decided to follow this simple yet effective structure:

- Multiple processes should handle groups of file and folders separately.
- Multiple threads of the same process should work on different chunks of the same file in parallel.

Specifically, there are multiple reasons behind our parallel architectural design for this project. Here follows a list of the main ones:

- In most operating systems a file is a resource that the OS gives to a single process to avoid race conditions. We wanted to follow a similar design philosophy.
- Most operating systems allow multiple processes to open the same file in reading mode, but only few allow to open the same file in writing mode on multiple processes. This is because that leads to potentially concurrency and data integrity issues. By ensuring to have only a single process that open a specific file, we avoid all these issues.
- Because threads of the same process share the address space, we can avoid the expensive data transfer across processes. When data is read or written to file, there is no need to transfer data between threads.

In the next section, we start by explaining the basic multithreading operations on a single file. Later on, multiprocessing with multiple files is covered.

A. Multithreading

The parallel algorithm for a single file follows the exact same procedure as for the serial version, with just a few key differences to allow multithreading.

Suppose we are dealing with m threads and a single input file. Here follows a common procedure used for both encoding and decoding, with very small differences.

- 1) A single file is divided into chunks of a fixed size. When that is done, the single process forks and creates m threads.
- 2) A single thread (may be the main one, may not) then reads m chunks in a shared memory buffer.
- 3) Each one of the *m* threads works in parallel on the processing of its assigned chunk using a buffer. Although all the chunks are in shared memory buffer, each thread is assigned only to a single memory section: in this way there is no need to care about racing conditions when writing in the buffer. This is done by creating a unsigned char buffer[m][buffer_size].

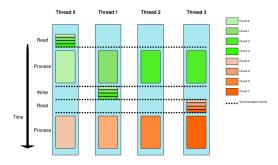


Fig. 2: Simple schema for processing a single file with multiple threads.

4) When all threads are done computing, either the encoding or decoding of their chunks, a single thread writes the processed chunks to the output file. Again, since all threads share a memory space there is no need to perform data transfer.

Moreover, our implementation also parallelize the counting of occurrences of a byte in the input file, since this is required in order to create the Huffman tree. This is done only during the encoding phase, as for the decoding the occurences are no longer required because the huffman tree is already saved in the encoded data. The procedure is very similar to the one just described, with the key difference that there is no output file to write, but only byte occurrences stored in an in-memory array unique for each thread to avoid concurrency. When the counting is done, all threads join their counts into a single array.

Figure 2 shows a schema of the parallel workflow for processing a single file.

B. Multiprocessing

Additionally, we wanted our tool to be able to process multiple files and folders: for this use case, we exploit multiprocessing.

To achieve this, we devised a simple algorithm to distribute files across multiple processes, so that each process can work on its own list of files, independently to others. In this way, we can minimize communication and therefore latency and other slowdowns between the different components of the applications. Suppose we are dealing with n process, m threads, and an input folder.

- 1) First, the process with rank 0 (the main process) crawls all the files in the input directory recursively in all the subfolders.
- 2) Then the rank 0 process opens all the files and reads their size.
- 3) Once all files and their respective sizes are known, the main process creates a min priority queue where each item represents a process and its priority is the size of files that have been assigned to it.
- 4) Process 0 can iteratively insert files in the priority queue and updates the priority of each process with the

- cumulative file size. The main idea is that we can ensure an equal work division among different processes.
- 5) When all this is done, the main process sends the list of files to each process and then each starts to work independently on its own list of files.

C. Implementation details and other notes

Here follows a list of further comments and design choices for our specific Huffman implementation.

- We decided on an alphabet of 256 for the Huffman coding because this way we can encode each byte of the input data into a different Huffman code. As C language does not allow to address data at lower resolution than a byte, lowering the alphabet would not result in any perfomance benefit. We also considered encoding multiple bytes into a single huffman code, but that results in worse compression as the resulting huffman tree would have more leaves.
- We found that a chunk size of 4096 bytes had the best I/O times. This is probably due to the fact that 4096 B is the size of a page in most Linux based operating systems. The last chunk of a file may be smaller. Reading any other size at the time had resulted in significantly worse I/O times (both increasing and decreasing the chunk size).
- In general, all threads will finish processing their chunks at around the same time, but in some cases there are threads that can take longer. This is due to the very unlucky case where a whole chunk contains exclusively very infrequent bytes of data. Because the bytes are very infrequent, each one is encoded in extremely long sequences, up to 256 bits, resulting in a bigger encoded chunk than the original data. With our Huffman alphabet set to a single byte, the worst case results in having a compressed chunk being 32 times bigger than decompressed one.
- We tried to parallelize the I/O, by having each thread read its own chunk. We found that the standard file descriptor provided by C have a lock to guarantee thread safety. Unfortunately, this lock slows down the reads significantly. We also tried using multiple file descriptors to circumvent this limitation, however we found no improvement over a single-thread sequential read. This is likely because the O.S. schedules I/O requests and serves them one at the time, resulting in an impossibility of having truly parallel I/O.
- We also tested an architecture where we had two dedicated threads to I/O, one for reading and one for writing chunks. The idea is that whenever a chunk is processed, the I/O threads would immediately write the processed chunk to the output file and similarly a new chunk would be read from the input file (very similar to a queue of jobs). Theoretically this would allow to parallelize I/O and computation operations: in this scenario we avoided concurrency problems by synchronizing the I/O with locks. In later analysis we call this architecture "Locks" because of the synchronization method we are using.

• Another detail we noticed on the implementation with two dedicated threads for I/O, is that if there are not enough cores on the CPU or if the operating system decides to allocate all the threads on a single processor, the encoding and decoding times are greatly affected by the scheduler. This is because it might be that the O.S. gives priority to threads that are waiting (for example the writer cannot write any block until the first has finished, even if all others have finished). In the worst case scenario, the multithreading architecture could be even slower that the serial one.

V. PERFORMANCE AND BENCHMARKING

Performance evaluation.

Here we discuss the perfomance evaluation of our algorithm All data is resulting average of 3 runs. We tested on HPC2 of unitn cluster Each datapoint was submitted as a job to the cluster, individually. No other jobs were assigned to the cluster and and no other I/O operations was done. This is to prevent hiccups due to multiple instances of the program trying to access the same data.

Dataset were pragmatically generated using a C program, creating text files with characters that follow the frequency of letters in English language.

We read and wrote about ~ 6 TiB of data for our whole benchmark analysis.

We can see that our algorithm scales very well.

With small files, less than a few MiBs, the algorithm is actually slower with more threads. This is likely because the data is not large enough. The parallel procesng is not enough to offset the cost of parallezation using threads.

However when the data is large, we can see that our approach does actually perfom well. With the largest file (10 GiB) our algorithm has an efficiency of 93% when tested with 4 threads. This number steadily decreases with the number of threads, until a measily 32% with 24 threads.

It has to be noted that we are heavily limited by the I/O. We are unable to parallelize the I/O, resulting in long waiting times, especially the writing operations. As a proof of this, if we consider only the processing section of our algorithm, and ignore the time required by the flush() operation before a fclose(), we see significantly better times. Same from 92% at 4 threads, but we scale much better at 55% with 24 threads.

Some images

Other stuff

Folders.

We also tested the ability to scale with processors. We chose as benchmark Linux kernel (available here). It is about 266 MiB of total size, with about 80.000 files.

We also tested on

The correctness of our algorithm was easily verified by encoding and then decoding a file, then comparing it to the original with the diff command.

VI. CONCLUSIONS

To conclude.

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VII. APPENDIX

A. Encoding

TABLE I: Overall encoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.1084	0.1029	0.0826	0.0905	0.0718	0.1100	0.1338	0.2110	0.1705	0.2531
5 MiB		0.4073	0.2008	0.1255	0.1037	0.0970	0.0786	0.0789	0.0767	0.0906	0.0883
10 MiB		0.7611	0.4737	0.2658	0.2084	0.1804	0.1861	0.2204	0.3353	0.2432	0.3930
50 MiB		3.9241	2.1378	1.2788	1.0203	0.8575	0.7589	0.7773	0.6583	0.7523	0.9954
100 MiB		7.7270	4.0680	2.4028	1.8596	1.5545	1.4324	1.2994	1.2468	1.2308	1.5375
500 MiB		35.7753	18.3831	11.4959	8.3511	7.5589	5.7548	6.0857	5.5698	5.1431	5.0972
1 GiB		73.1120	38.1679	22.5066	16.3364	14.2131	13.7565	12.6196	10.8261	10.3345	9.7426
5 GiB		359.8495	186.6294	99.8038	77.4620	65.6555	67.3056	52.9090	48.4594	48.0126	48.8973
10 GiB		694.9750	370.5490	188.2278	136.1719	113.5878	104.0254	93.7227	116.8249	83.2084	82.0529

TABLE II: Pure encoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.0637	0.0338	0.0184	0.0128	0.0100	0.0085	0.0388	0.0938	0.0351	0.1032
5 MiB		0.2980	0.1522	0.0782	0.0537	0.0413	0.0341	0.0296	0.0243	0.0207	0.0264
10 MiB		0.6547	0.3523	0.1845	0.1254	0.0977	0.0812	0.0730	0.1533	0.0570	0.1505
50 MiB		3.3027	1.7545	0.9147	0.6244	0.4884	0.4326	0.3432	0.2658	0.2953	0.3141
100 MiB		6.7211	3.4461	1.8267	1.2448	0.9903	0.8153	0.6873	0.5415	0.4856	0.6148
500 MiB		32.3825	16.6046	8.6817	6.2457	4.8624	4.0588	3.4132	2.6616	2.3853	2.0639
1 GiB		67.1756	34.0970	17.7353	12.6548	9.8790	8.2365	7.0042	5.4307	4.8915	4.2098
5 GiB		331.2526	174.0889	90.5618	63.4905	48.6453	38.9458	33.1852	26.1005	23.6226	20.4274
10 GiB		639.3369	328.5801	170.4086	119.6824	95.1232	79.8054	68.8753	53.3415	47.5727	48.6436

TABLE III: Overall encoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.5272	0.3283	0.1997	0.1889	0.0986	0.0676	0.0321	0.0318	0.0179
5 MiB		1.0	1.0144	0.8111	0.6544	0.5250	0.5182	0.4302	0.3317	0.2247	0.1922
10 MiB		1.0	0.8034	0.7158	0.6086	0.5273	0.4090	0.2878	0.1419	0.1565	0.0807
50 MiB		1.0	0.9178	0.7671	0.6410	0.5721	0.5171	0.4207	0.3726	0.2608	0.1643
100 MiB		1.0	0.9497	0.8040	0.6925	0.6213	0.5394	0.4956	0.3873	0.3139	0.2094
500 MiB		1.0	0.9731	0.7780	0.7140	0.5916	0.6217	0.4899	0.4014	0.3478	0.2924
1 GiB		1.0	0.9578	0.8121	0.7459	0.6430	0.5315	0.4828	0.4221	0.3537	0.3127
5 GiB		1.0	0.9641	0.9014	0.7742	0.6851	0.5346	0.5668	0.4641	0.3747	0.3066
10 GiB		1.0	0.9378	0.9231	0.8506	0.7648	0.6681	0.6179	0.3718	0.4176	0.3529

TABLE IV: Pure encoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.9432	0.8677	0.8304	0.7960	0.7472	0.1370	0.0424	0.0908	0.0257
5 MiB		1.0	0.9788	0.9521	0.9253	0.9025	0.8729	0.8402	0.7654	0.7194	0.4697
10 MiB		1.0	0.9290	0.8872	0.8703	0.8373	0.8061	0.7476	0.2668	0.5743	0.1813
50 MiB		1.0	0.9412	0.9027	0.8816	0.8454	0.7635	0.8021	0.7767	0.5593	0.4381
100 MiB		1.0	0.9752	0.9198	0.8999	0.8484	0.8244	0.8149	0.7757	0.6920	0.4555
500 MiB		1.0	0.9751	0.9325	0.8641	0.8325	0.7978	0.7906	0.7604	0.6788	0.6538
1 GiB		1.0	0.9851	0.9469	0.8847	0.8500	0.8156	0.7992	0.7731	0.6867	0.6649
5 GiB		1.0	0.9514	0.9144	0.8696	0.8512	0.8505	0.8318	0.7932	0.7011	0.6757
10 GiB		1.0	0.9729	0.9379	0.8903	0.8401	0.8011	0.7735	0.7491	0.6720	0.5476

B. Encoding with Locks

TABLE V: Overall encoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.0880	0.0837	0.0732	0.0654	0.0724	0.0724	0.0672	0.0667	0.0752	0.0712
5 MiB		0.4246	0.4062	0.2753	0.1725	0.1674	0.1642	0.1479	0.1389	0.1387	0.1362
10 MiB		0.7128	0.6782	0.2417	0.1939	0.1762	0.1471	0.1676	0.1286	0.1403	0.1570
50 MiB		3.5854	3.3710	1.1411	0.8380	0.7478	0.6985	0.9610	0.9681	0.7327	0.8949
100 MiB		6.8047	6.6007	2.1585	1.6222	1.3589	1.2004	1.0981	0.9736	0.8877	0.8418
500 MiB		33.4643	31.9953	10.5641	7.8537	6.6834	6.0406	5.5178	5.9307	4.5767	4.2484
1 GiB		68.4891	65.9418	21.1728	16.4254	13.6481	12.0767	10.9664	9.7954	9.0356	8.3424
5 GiB		367.2282	370.8502	110.2986	84.1276	75.3192	66.4084	59.6663	59.4788	51.1808	48.9043
10 GiB		676.5289	642.9220	187.6202	135.9907	123.8217	109.7696	96.6426	93.2259	90.8253	88.1542

TABLE VI: Pure encoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.0612	0.0621	0.0360	0.0278	0.0303	0.0216	0.0244	0.0239	0.0301	0.0158
5 MiB		0.3611	0.3633	0.2093	0.1092	0.1031	0.0923	0.0792	0.0657	0.0530	0.0501
10 MiB		0.6167	0.6074	0.1689	0.1167	0.0905	0.0756	0.0784	0.0540	0.0529	0.0590
50 MiB		3.1314	3.0569	0.8470	0.5946	0.4641	0.4157	0.6712	0.6516	0.4349	0.4997
100 MiB		6.0792	6.0371	1.6635	1.1509	0.8906	0.7352	0.6421	0.5210	0.4383	0.3862
500 MiB		31.0011	30.4712	8.2873	5.8097	4.5192	3.7783	3.2265	2.6096	2.2273	1.9458
1 GiB		62.7481	62.3551	17.2300	11.9387	9.1530	7.5818	6.5052	5.3627	4.6125	4.1011
5 GiB		343.8756	351.0666	99.9091	73.8247	62.6944	54.0495	47.8488	42.7941	33.9437	29.9516
10 GiB		629.4486	623.7099	172.8286	120.5519	94.6229	78.7281	68.0250	55.2154	46.7232	41.4739

TABLE VII: Overall encoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.5258	0.3004	0.2242	0.1519	0.1216	0.1091	0.0825	0.0585	0.0515
5 MiB		1.0	0.5227	0.3856	0.4104	0.3171	0.2585	0.2392	0.1911	0.1531	0.1299
10 MiB		1.0	0.5255	0.7371	0.6127	0.5057	0.4845	0.3543	0.3465	0.2541	0.1892
50 MiB		1.0	0.5318	0.7855	0.7130	0.5994	0.5133	0.3109	0.2315	0.2447	0.1669
100 MiB		1.0	0.5155	0.7881	0.6991	0.6260	0.5669	0.5164	0.4368	0.3833	0.3368
500 MiB		1.0	0.5230	0.7919	0.7102	0.6259	0.5540	0.5054	0.3527	0.3656	0.3282
1 GiB		1.0	0.5193	0.8087	0.6949	0.6273	0.5671	0.5204	0.4370	0.3790	0.3421
5 GiB		1.0	0.4951	0.8323	0.7275	0.6095	0.5530	0.5129	0.3859	0.3588	0.3129
10 GiB		1.0	0.5261	0.9015	0.8291	0.6830	0.6163	0.5834	0.4536	0.3724	0.3198

TABLE VIII: Pure encoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.4928	0.4246	0.3672	0.2522	0.2831	0.2086	0.1598	0.1015	0.1611
5 MiB		1.0	0.4969	0.4312	0.5511	0.4378	0.3912	0.3801	0.3437	0.3409	0.3001
10 MiB		1.0	0.5077	0.9129	0.8805	0.8520	0.8159	0.6554	0.7144	0.5827	0.4356
50 MiB		1.0	0.5122	0.9243	0.8778	0.8433	0.7532	0.3888	0.3003	0.3601	0.2611
100 MiB		1.0	0.5035	0.9136	0.8804	0.8532	0.8268	0.7890	0.7292	0.6934	0.6560
500 MiB		1.0	0.5087	0.9352	0.8893	0.8575	0.8205	0.8007	0.7425	0.6959	0.6638
1 GiB		1.0	0.5032	0.9104	0.8760	0.8569	0.8276	0.8038	0.7313	0.6802	0.6375
5 GiB		1.0	0.4898	0.8605	0.7763	0.6856	0.6362	0.5989	0.5022	0.5065	0.4784
10 GiB		1.0	0.5046	0.9105	0.8702	0.8315	0.7995	0.7711	0.7125	0.6736	0.6324

C. Decoding

TABLE IX: Overall decoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.1304	0.0907	0.0793	0.0986	0.0912	0.0975	0.1179	0.1152	0.1185	0.1039
5 MiB		0.4219	0.2527	0.1772	0.1663	0.1411	0.1563	0.1507	0.1395	0.1296	0.1214
10 MiB		0.8712	0.5173	0.3839	0.2955	0.2931	0.4331	0.3716	0.3557	0.3683	0.3546
50 MiB		4.1082	2.2768	1.5108	1.2518	1.2762	1.3824	1.4124	1.4088	1.4343	1.3277
100 MiB		7.9605	4.5073	2.9151	2.2752	1.8842	2.4183	2.4003	2.4222	2.3432	2.2511
500 MiB		37.6189	22.5113	13.5012	11.3339	10.0352	9.3255	9.6405	11.1822	11.0692	10.0214
1 GiB		76.6794	43.2517	27.5849	23.2715	18.5904	17.8240	18.5319	22.0271	19.8127	17.1276
5 GiB		361.8713	193.1122	108.8124	96.7901	81.0661	84.8969	79.1422	73.7254	79.3745	75.9761
10 GiB		759.0719	391.2016	212.3814	156.3964	135.8435	135.4010	134.0983	137.9998	134.0065	132.2553

TABLE X: Pure decoding times

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		0.0833	0.0579	0.0519	0.0737	0.0693	0.0712	0.0920	0.0903	0.0924	0.0761
5 MiB		0.3397	0.1883	0.1231	0.1014	0.0843	0.0942	0.0893	0.0789	0.0729	0.0623
10 MiB		0.7516	0.4136	0.2667	0.1912	0.1905	0.2648	0.2672	0.2459	0.2821	0.2490
50 MiB		3.6338	1.8884	1.0578	0.7449	0.6699	0.9762	0.9542	0.9429	0.9658	0.8575
100 MiB		7.1318	3.6134	2.0121	1.3884	1.1225	1.5401	1.5201	1.5413	1.4775	1.4684
500 MiB		36.3947	18.5941	9.8736	6.9800	5.4581	4.7071	5.7395	6.9697	6.4991	5.4733
1 GiB		74.7637	38.4079	19.7644	13.8396	10.9082	10.2419	9.2313	12.5040	12.0604	9.8245
5 GiB		359.8834	188.8855	97.7879	82.3554	56.9994	59.9356	50.8868	39.2907	48.5617	48.8765
10 GiB		754.8416	385.0213	199.8499	138.7388	113.1048	95.2621	81.1119	108.7269	94.3171	81.2615

TABLE XI: Overall decoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.7186	0.4108	0.2204	0.1787	0.1338	0.0921	0.0707	0.0550	0.0523
5 MiB		1.0	0.8349	0.5953	0.4228	0.3739	0.2700	0.2334	0.1890	0.1628	0.1448
10 MiB		1.0	0.8421	0.5673	0.4913	0.3715	0.2012	0.1954	0.1531	0.1183	0.1024
50 MiB		1.0	0.9022	0.6798	0.5469	0.4024	0.2972	0.2424	0.1823	0.1432	0.1289
100 MiB		1.0	0.8831	0.6827	0.5831	0.5281	0.3292	0.2764	0.2054	0.1699	0.1473
500 MiB		1.0	0.8356	0.6966	0.5532	0.4686	0.4034	0.3252	0.2103	0.1699	0.1564
1 GiB		1.0	0.8864	0.6949	0.5492	0.5156	0.4302	0.3448	0.2176	0.1935	0.1865
5 GiB		1.0	0.9369	0.8314	0.6231	0.5580	0.4262	0.3810	0.3068	0.2280	0.1985
10 GiB		1.0	0.9702	0.8935	0.8089	0.6985	0.5606	0.4717	0.3438	0.2832	0.2391

TABLE XII: Pure decoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.7196	0.4013	0.1884	0.1504	0.1170	0.0755	0.0577	0.0451	0.0456
5 MiB		1.0	0.9021	0.6897	0.5580	0.5038	0.3606	0.3168	0.2689	0.2330	0.2271
10 MiB		1.0	0.9087	0.7046	0.6550	0.4931	0.2839	0.2344	0.1911	0.1332	0.1258
50 MiB		1.0	0.9621	0.8588	0.8131	0.6781	0.3722	0.3174	0.2409	0.1881	0.1766
100 MiB		1.0	0.9869	0.8861	0.8562	0.7942	0.4631	0.3910	0.2892	0.2413	0.2024
500 MiB		1.0	0.9787	0.9215	0.8690	0.8335	0.7732	0.5284	0.3264	0.2800	0.2771
1 GiB		1.0	0.9733	0.9457	0.9004	0.8567	0.7300	0.6749	0.3737	0.3100	0.3171
5 GiB		1.0	0.9526	0.9201	0.7283	0.7892	0.6004	0.5894	0.5725	0.3705	0.3068
10 GiB		1.0	0.9803	0.9443	0.9068	0.8342	0.7924	0.7755	0.4339	0.4002	0.3870

D. Decoding with Locks

TABLE XIII: Overall decoding times

Threads File sizes	1	2	4	6	8	10	12	16	20	24
1 MiB	0.2719	0.2116	0.1162	0.1006	0.0699	0.0677	0.0656	0.0695	0.0748	0.0928
5 MiB	0.6351	0.9155	1.2650	0.6553	0.6837	0.2889	0.4825	0.2982	0.3296	0.1795
10 MiB	0.8607	0.5007	0.3328	0.2710	0.2687	0.2580	0.2364	0.2169	0.1899	0.1830
50 MiB	3.9914	2.2478	1.4618	1.1756	1.1596	1.0884	1.0173	0.9127	0.8369	0.7747
100 MiB	7.6155	33.6453	15.2498	11.6282	13.0181	10.7612	9.1921	3.6613	5.6912	4.4747
500 MiB	37.0819	20.4215	13.2360	11.3439	10.7738	10.4405	9.7670	8.6608	7.3871	7.0508
1 GiB	73.8554	41.1849	26.9294	23.0511	17.9771	18.7808	19.7312	17.8374	16.1711	15.4367
5 GiB	352.3856	475.0869	265.8940	204.6614	156.2271	139.8945	127.6489	109.2454	100.9185	89.8899
10 GiB	714.9067	375.6862	202.7149	127.0707	435.2239	145.6734	133.3188	122.7745	117.5286	115.2620

TABLE XIV: Pure decoding times

File sizes	Threads	1 2	4	6	8	10	12	16	20	24
1 MiB	0.116	2 0.0645	0.0563	0.0555	0.0407	0.0408	0.0379	0.0413	0.0382	0.0351
5 MiB	0.565	0.8586	1.2021	0.5983	0.6266	0.2339	0.4245	0.2443	0.2693	0.1130
10 MiB	0.714	9 0.3986	0.2338	0.1743	0.1690	0.1591	0.1363	0.1187	0.0949	0.0849
50 MiB	3.531	0 1.8481	1.0339	0.7423	0.7299	0.6557	0.6202	0.4858	0.4169	0.3519
100 MiB	6.874	4 33.3659	14.8835	10.7860	12.3773	9.9066	8.3482	2.8794	5.0465	3.6955
500 MiB	35.449	7 18.2381	10.0089	7.1791	6.7919	6.3173	5.6216	4.6675	3.8306	3.2797
1 GiB	72.113	8 36.9260	20.1134	14.5033	11.5997	12.6916	11.3021	9.2808	7.6540	6.4776
5 GiB	349.890	4 471.3404	257.7142	197.0613	140.1541	124.8532	110.6343	91.4010	74.5820	62.5393
10 GiB	711.984	6 370,5192	191.8006	121.5451	421.9179	126.6782	113.4824	92.0815	76.3088	64.4831

TABLE XV: Overall decoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.6424	0.5848	0.4504	0.4859	0.4018	0.3456	0.2446	0.1818	0.1220
5 MiB		1.0	0.3469	0.1255	0.1615	0.1161	0.2199	0.1097	0.1331	0.0963	0.1474
10 MiB		1.0	0.8595	0.6466	0.5293	0.4005	0.3336	0.3033	0.2480	0.2266	0.1959
50 MiB		1.0	0.8878	0.6826	0.5659	0.4303	0.3667	0.3269	0.2733	0.2385	0.2147
100 MiB		1.0	0.1132	0.1248	0.1092	0.0731	0.0708	0.0690	0.1300	0.0669	0.0709
500 MiB		1.0	0.9079	0.7004	0.5448	0.4302	0.3552	0.3164	0.2676	0.2510	0.2191
1 GiB		1.0	0.8966	0.6856	0.5340	0.5135	0.3932	0.3119	0.2588	0.2284	0.1993
5 GiB		1.0	0.3709	0.3313	0.2870	0.2819	0.2519	0.2300	0.2016	0.1746	0.1633
10 GiB		1.0	0.9506	0.8817	0.9377	0.2053	0.4908	0.4469	0.3639	0.3041	0.2584

TABLE XVI: Pure decoding efficiency

File sizes	Threads	1	2	4	6	8	10	12	16	20	24
1 MiB		1.0	0.9006	0.5154	0.3487	0.3568	0.2845	0.2554	0.1758	0.1518	0.1379
5 MiB		1.0	0.3290	0.1175	0.1574	0.1127	0.2416	0.1109	0.1446	0.1049	0.2083
10 MiB		1.0	0.8967	0.7645	0.6835	0.5286	0.4492	0.4369	0.3764	0.3766	0.3507
50 MiB		1.0	0.9553	0.8538	0.7928	0.6047	0.5385	0.4745	0.4543	0.4234	0.4181
100 MiB		1.0	0.1030	0.1155	0.1062	0.0694	0.0694	0.0686	0.1492	0.0681	0.0775
500 MiB		1.0	0.9719	0.8855	0.8230	0.6524	0.5612	0.5255	0.4747	0.4627	0.4504
1 GiB		1.0	0.9765	0.8963	0.8287	0.7771	0.5682	0.5317	0.4856	0.4711	0.4639
5 GiB		1.0	0.3712	0.3394	0.2959	0.3121	0.2802	0.2635	0.2393	0.2346	0.2331
10 GiB		1.0	0.9608	0.9281	0.9763	0.2109	0.5620	0.5228	0.4833	0.4665	0.4601