



**DIGITAL DESIGN**

**ASSIGNMENT REPORT**

**ASSIGNMENT ID :2**

## PART 1: DIGITAL DESIGN THEORY

Provide your answers here:

### Question1

Given the Boolean functions  $F_1$  and  $F_2$ , show that

- a. The Boolean function  $E = F_1 + F_2$  contains the sum of the minterms of  $F_1$  and  $F_2$
- b. The Boolean function  $G = F_1 \cdot F_2$  contains only the minterms that are common to  $F_1$  and  $F_2$ .

One Boolean function can be expressed as the sum of minterms, suppose

$$F_1(A,B,C) = \sum m_{1i}, F_2(A,B,C) = \sum m_{2i}$$

a.

$$E = F_1 + F_2 = \sum m_{1i} + \sum m_{2i} = \sum (m_{1i} + m_{2i})$$

b.

$$F_1 \cdot F_2 = \sum m_{1i} \cdot \sum m_{2i},$$

When  $i \neq j$ , then  $m_i \cdot m_j = 0$

When  $i = j$ , then  $m_i \cdot m_j = 1$

To satisfy  $F_1 \cdot F_2 = 1$  in some combination of  $A, B, C$

$G$  can only contain the minterms that are common to  $F_1$  and  $F_2$

### Question2

Convert each of the following to the other canonical form

- a.  $F(x, y, z) = \sum(1, 3, 7)$
- b.  $F(A, B, C, D) = \prod(1, 3, 5, 8, 11, 13, 15)$

a.

$$(F(x,y,z))' = \sum(0,2,4,5,6)$$

$$((F(x,y,z))')' = F(x, y, z) = \prod(0,2,4,5,6)$$

b.

$$(F(A,B,C,D))' = \prod(0,2,4,6,7,9,10,12,14)$$

$$((F(A,B,C,D))')' = F(A,B,C,D) = \sum(0,2,4,6,7,9,10,12,14)$$

### Question3

Write the following Boolean expressions in:

a.  $(b' + d)(a' + b' + c)(a + c)$  SOP form

b.  $ab + a'c' + bc$  POS form

a.  $ab' + b'c + cd$

b.  $ab + a'c' + bc = abc + abc' + a'bc' + a'b'c' + a'bc = \sum (0,2,3,6,7) = \prod (1,4,5)$

$= (a+b+c')(a'+b+c)(a'+b+c')$

### Question4

Determine whether the following Boolean equation is true or false. Show your process

a.  $y'z' + yz' + x'z = x'z'$

b.  $x'y' + x'z' + yz = x'y + x'z$

a. False

$$y'z' + yz' + x'z = z' + x'z = z'$$

b. False

Express left part and right part as POS form

left:  $x'y'z + x'y'z' + x'yz' + xyz + x'yz$

right:  $x'yz' + x'yz + x'y'z$

thus left  $\neq$  right

### Question5

Simplify the following Boolean functions and expressions, using four-variable maps:

a.  $F(A, B, C, D) = \sum (0, 2, 5, 7, 8, 10, 13, 15)$

b.  $F(w, x, y, z) = \sum (1, 3, 4, 5, 6, 7, 9, 11, 13, 15)$

c.  $A'BCD + ABC + CD + B'D$

d.  $A'B'C'D' + BC'D + A'C'D + A'BCD + ACD$

a.  $BD + B'D'$

AB \ CD	00	01	11	10
00	$m_0$	$m_1$	$m_3$	$m_2$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

b.  $z + w'x$

wx \ yz	00	01	11	10
00	$m_0$	$m_1$	$m_3$	$m_2$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

c.  $CD + B'D + ABC$

AB \ CD	00	01	11	10
00	$m_0$	$m_1$	$m_3$	$m_2$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

d.  $BD + ACD + A'B'C'$

AB \ CD	00	01	11	10
00	$m_0$	$m_1$	$m_3$	$m_2$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

### Question6

Implement the following logical functions with two-level NOR gate circuits.

Write down the simplification process, then draw the circuit diagram.

a.  $F(A, B, C, D) = AD + BC'D + ABC + A'BC'D$

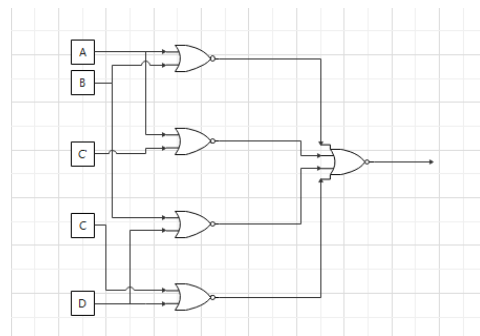
b.  $F(A, B, C, D) = (A' + C' + D')(A' + C')(C' + D')$

a.

CD \ AB	00	01	11	10
00	$m_0$	$m_1$	$m_2$	$m_3$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

$$F' = A'B' + C'D' + A'C + B'D' = (A+B)' + (C+D)' + (A+C')' + (B+D)'$$

$$(F')' = ((A+B)' + (C+D)' + (A+C')' + (B+D)')'$$



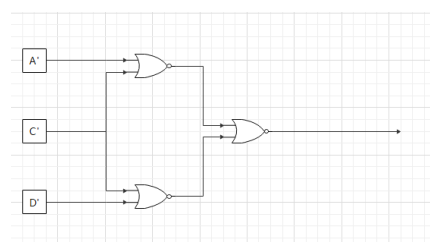
b.

CD \ AB	00	01	11	10
00	$m_0$	$m_1$	$m_2$	$m_3$
01	$m_4$	$m_5$	$m_7$	$m_6$
11	$m_{12}$	$m_{13}$	$m_{15}$	$m_{14}$
10	$m_8$	$m_9$	$m_{11}$	$m_{10}$

$$F = (A' + A'C' + C' + A'D' + C'D')(C' + D') = C' + A'D'$$

$$F' = CD + AC = (C' + D')' + (A' + C')'$$

$$(F')' = ((C' + D')' + (A' + C')')'$$



### Question7

Simplify the following Boolean function F, together with the don't-care conditions d, and then express the simplified function in sum-of-minterms form:

a.  $F(x, y, z) = \sum(0, 1, 4, 5, 6)$  with  $d(x, y, z) = \sum(2, 3, 7)$

b.  $F(A, B, C, D) = \sum(5, 6, 7, 12, 14)$  with  $d(x, y, z) = \sum(3, 9, 11)$

a.  $F(x,y,z) = 1 = \sum(1,2,3,4,5,6,7)$

yz \ x	00	01	11	10
0	m <sub>0</sub>	m <sub>1</sub>	m <sub>2</sub>	m <sub>3</sub>
1	m <sub>4</sub>	m <sub>5</sub>	m <sub>6</sub>	m <sub>7</sub>

b.  $F(A,B,C,D) = A'BD + A'BC + ABD' = \sum(5,6,7,12,14)$

CD \ AB	00	01	11	10
00	m <sub>0</sub>	m <sub>1</sub>	m <sub>3</sub>	m <sub>2</sub>
01	m <sub>4</sub>	m <sub>5</sub>	m <sub>7</sub>	m <sub>6</sub>
11	m <sub>12</sub>	m <sub>13</sub>	m <sub>15</sub>	m <sub>14</sub>
10	m <sub>8</sub>	m <sub>9</sub>	m <sub>11</sub>	m <sub>10</sub>

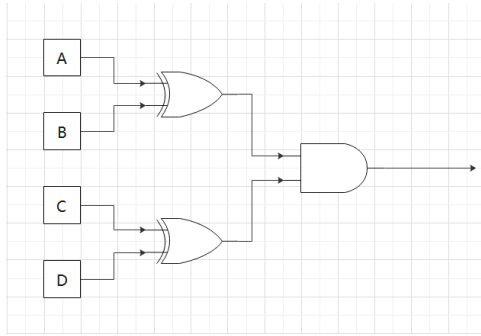
### Question8

Implement the following Boolean expression with exclusive-OR and AND gates, draw the circuit diagram:  $F = AB'CD' + A'BCD' + AB'C'D + A'BC'D$

In four-variables map, F is as follow

CD \ AB	00	01	11	10
00	m <sub>0</sub>	m <sub>1</sub>	m <sub>3</sub>	m <sub>2</sub>
01	m <sub>4</sub>	m <sub>5</sub>	m <sub>7</sub>	m <sub>6</sub>
11	m <sub>12</sub>	m <sub>13</sub>	m <sub>15</sub>	m <sub>14</sub>
10	m <sub>8</sub>	m <sub>9</sub>	m <sub>11</sub>	m <sub>10</sub>

$$F = A'B(CD' + C'D) + AB'(CD' + C'D) = (CD' + C'D)(A'B + AB') = (A \oplus B)(C \oplus D)$$



## PART 2: DIGITAL DESIGN LAB (TASK1)

All the tasks have been checked in-class