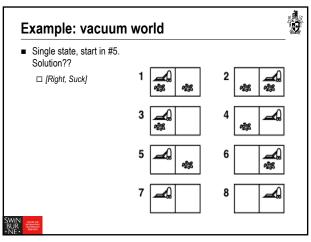


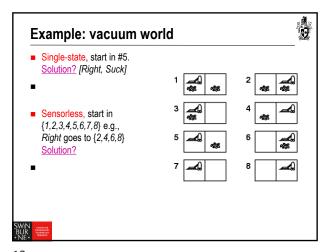
Example: vacuum world

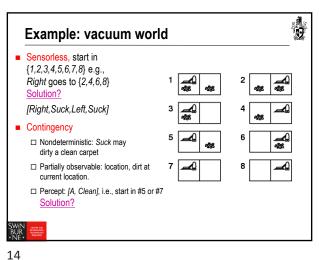
Single state, start in #5. Solution??

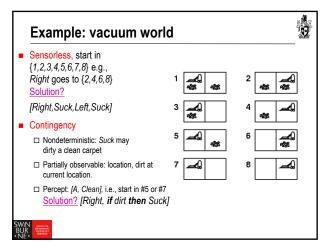
1 2 3 4 4 4 5 5 6 6 7 7 2 8 2

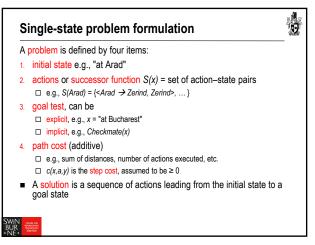


11 12

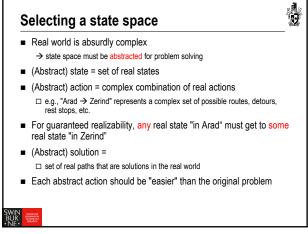


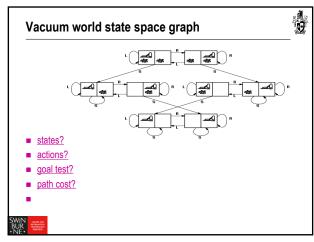


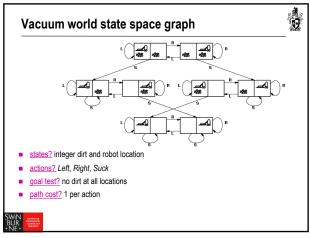


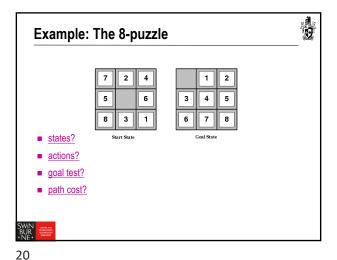


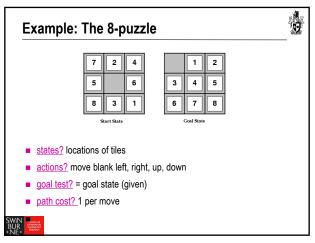
15 16

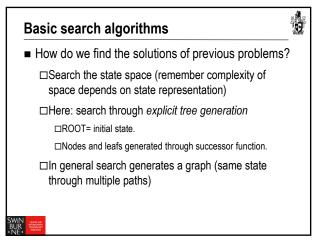


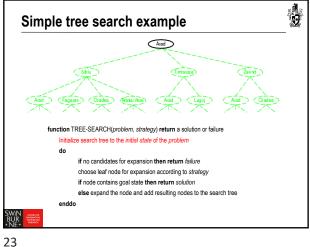


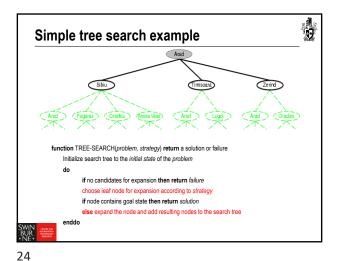


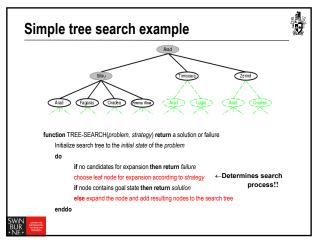


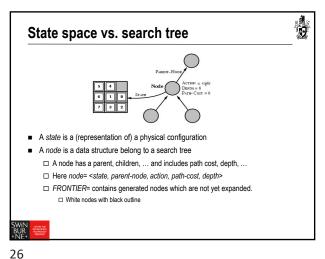


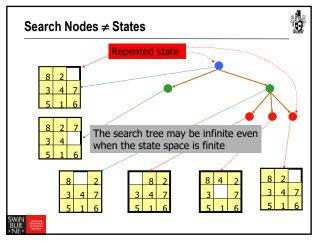












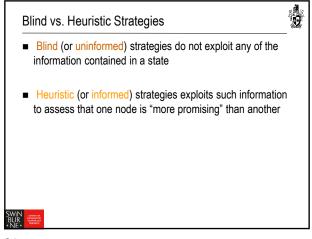
Tree search algorithm function TREE-SEARCH(problem, frontier) return a solution or failure frontier ← INSERT(MAKE-NODE(INITIAL-STATE[problem]), frontier) loop do if EMPTY?(frontier) then return failure  $node \leftarrow \mathsf{REMOVE}\text{-}\mathsf{FIRST}(frontier)$ if GOAL-TEST[problem] applied to STATE[node] succeeds then return SOLUTION(node) frontier ← INSERT-ALL(EXPAND(node, problem), frontier)

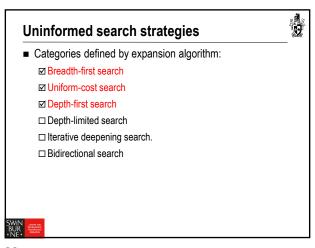
28

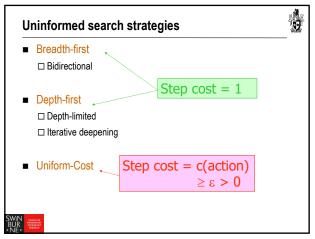
30

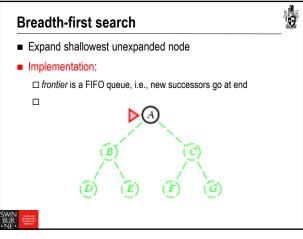
Tree search algorithm (2) function EXPAND(node,problem) return a set of nodes successors ← the empty set for each <action, result> in SUCCESSOR-FN[problem](STATE[node]) do  $s \leftarrow$  a new NODE  $STATE[s] \leftarrow result$  $\mathsf{PARENT}\text{-}\mathsf{NODE}[s] \leftarrow \mathit{node}$  $ACTION[s] \leftarrow action$  $\mathsf{PATH\text{-}COST}[s] \leftarrow \mathsf{PATH\text{-}COST}[node] + \mathsf{STEP\text{-}COST}(node, \, action, s)$  $DEPTH[s] \leftarrow DEPTH[node]+1$ add s to successors return successors 29

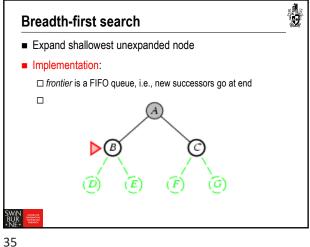
Search strategies A strategy is defined by picking the order of node expansion. Problem-solving performance is measured in four ways: □ Completeness; Does it always find a solution if one exists? □ Optimality; Does it always find the least-cost solution? ☐ Time Complexity; Number of nodes generated/expanded? □ Space Complexity; Number of nodes stored in memory during Time and space complexity are measured in terms of problem difficulty defined by:  $\square$  b - maximum branching factor of the search tree  $\square$  d - depth of the least-cost solution  $\square$  m - maximum depth of the state space (may be  $\infty$ )

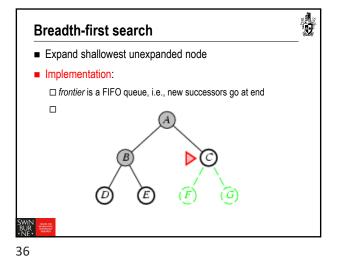


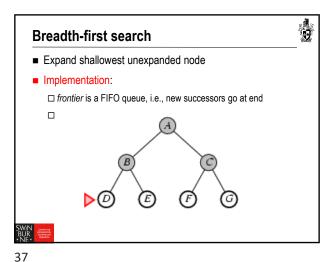


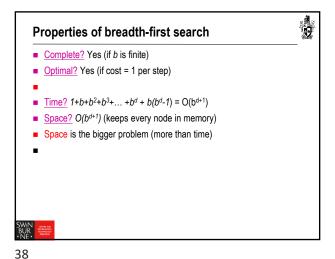






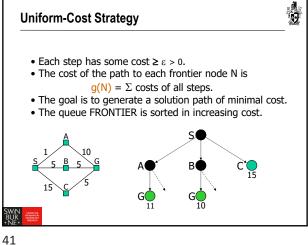


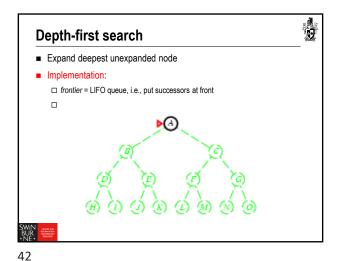


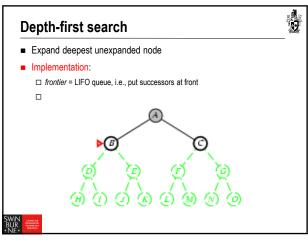


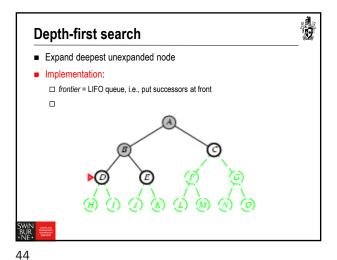
d	#Nodes	Time	Memory
2	111	.01 msec	11 Kbytes
4	11,111	1 msec	1 Mbyte
6	~106	1 sec	100 Mb
8	~108	100 sec	10 Gbytes
10	~1010	2.8 hours	1 Tbyte
12	~1012	11.6 days	100 Tbytes
14	~1014	3.2 years	10,000 Tb

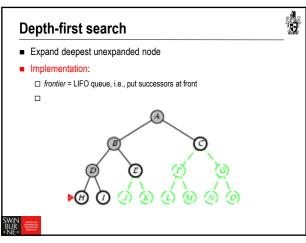
	#Nodes	Time	Memory
2	111	.01 msec	11 Kbytes
1	11,111	1 msec	1 Mbyte
3	~106	1 sec	100 Mb
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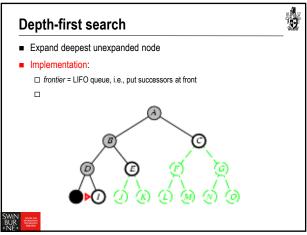




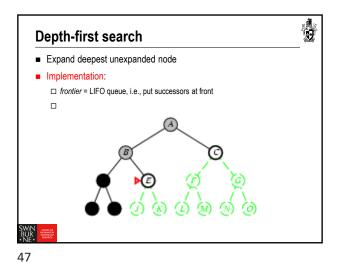


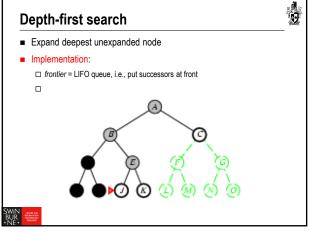


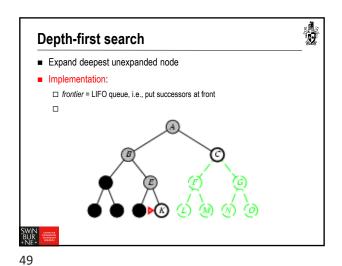


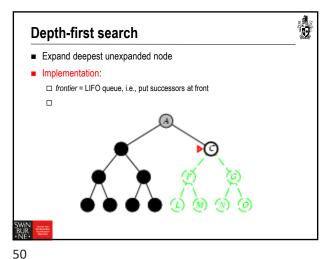


45 46







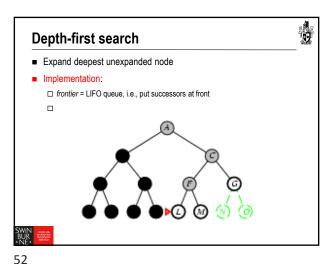


Depth-first search

Expand deepest unexpanded node

Implementation:

frontier = LIFO queue, i.e., put successors at front



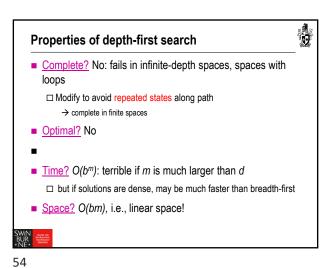
Depth-first search

■ Expand deepest unexpanded node

■ Implementation:

□ frontier = LIFO queue, i.e., put successors at front

□



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## **Summary**



- Search tree ≠ state space
- Search strategies: breadth-first, depth-first, and variants
- Evaluation of strategies: completeness, optimality, time and space complexity
- Avoiding repeated states
- Optimal search with variable step costs

