# Memory Networks for Language Understanding

## QA problem

John is in the playground.

John picked up the football.

Bob went to the kitchen.

Where is the football? A:playground



### Intuition

- Large long term memory → read and written to
- Attention over memory reasoning

### MemNet Framework

- 1. Convert x to an internal feature representation I(x).
- 2. Update memories  $\mathbf{m}_i$  given the new input:  $\mathbf{m}_i = G(\mathbf{m}_i, I(x), \mathbf{m}), \ \forall i$ .
- 3. Compute output features o given the new input and the memory:  $o = O(I(x), \mathbf{m})$ .
- 4. Finally, decode output features o to give the final response: r = R(o).

### **Basic Model**

• O (output) component: support facts

$$o_1 = O_1(x, \mathbf{m}) = \underset{i=1,...,N}{\operatorname{arg max}} s_O(x, \mathbf{m}_i)$$

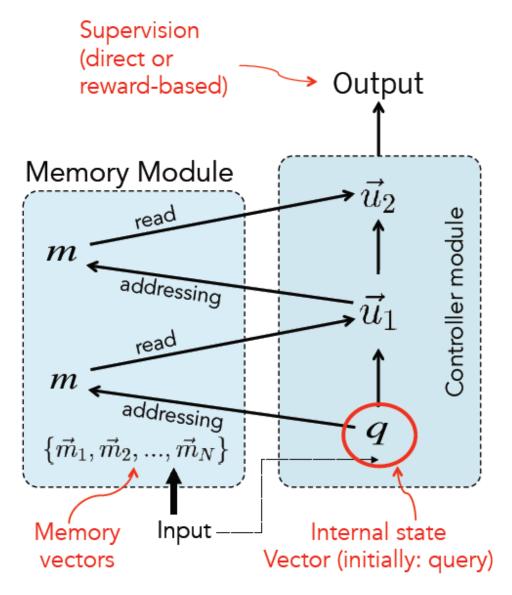
$$o_2 = O_2(x, \mathbf{m}) = \underset{i=1,...,N}{\operatorname{arg \, max}} \ s_O([x, \mathbf{m}_{o_1}], \mathbf{m}_i)$$

• R (response) component:

$$r = \operatorname{argmax}_{w \in W} s_R([x, \mathbf{m}_{o_1}, \mathbf{m}_{o_2}], w)$$

• Scoring function:

$$s(x,y) = \Phi_x(x)^{\top} U^{\top} U \Phi_y(y)$$



## Objective function

Minimize:

$$\sum_{\bar{f} \neq \mathbf{m}_{o_1}} \max(0, \gamma - s_O(x, \mathbf{m}_{o_1}) + s_O(x, \bar{f})) +$$

$$\sum_{\bar{f}' \neq \mathbf{m}_{o_2}} \max(0, \gamma - s_O([x, \mathbf{m}_{o_1}], \mathbf{m}_{o_2}]) + s_O([x, \mathbf{m}_{o_1}], \bar{f}'])) +$$

$$\sum_{\bar{f}' \neq r} \max(0, \gamma - s_R([x, \mathbf{m}_{o_1}, \mathbf{m}_{o_2}], r) + s_R([x, \mathbf{m}_{o_1}, \mathbf{m}_{o_2}], \bar{r}]))$$

Where:  $S_0$  is the matching function for the Output component.

 $S_R$  is the matching function for the Response component.

x is the input question.

 $m_{01}$  is the first true supporting memory (fact).

 $m_{02}$  is the first second supporting memory (fact).

r is the response

True facts and responses  $m_{01}$ ,  $m_{02}$  and r should have higher scores than all other facts and responses by a given margin.

### Variants of the class

- Representation of inputs: bag of words, RNN style reading at word or character level, etc. DMN
- **Different possibilities for output module:** e.g. multiclass classifier or uses an RNN to output sentences.
- If the memory is huge (e.g. Wikipedia): hash the memories to store in buckets (topics). Then, memory addressing and reading doesn't operate on *all* memories.
- If the memory is full, there could be a way of removing one it thinks is most useless; i.e. it ``forgets'' somehow. That would require a scoring function of the utility of each memory..

### bAbl dataset

- To measure understanding in several ways:
  - answer questions via chaining facts
  - simple induction
  - simple deduction
- Working with larger amount of read data tends to lead researchers to simpler models
- The dataset contains 20 nearly independent tasks, each checking one skill that the system must have (1k questions per task; About 15 sentences per story)

## Simple Tasks

#### Task 1: Single Supporting Fact

Mary went to the bathroom.

John moved to the hallway.

Mary travelled to the office.

Where is Mary? A:office

#### Task 3: Three Supporting Facts

John picked up the apple.

John went to the office.

John went to the kitchen.

John dropped the apple.

Where was the apple before the kitchen? A:office

#### Task 4: Two Argument Relations

Task 2: Two Supporting Facts

John is in the playground.

Bob went to the kitchen

John picked up the football.

The office is north of the bedroom.

The bedroom is north of the bathroom.

Where is the football? A:playground

The kitchen is west of the garden.

What is north of the bedroom? A: office

What is the bedroom north of? A: bathroom

## Bag of words will not work

#### Task 5: Three Argument Relations

Mary gave the cake to Fred.

Fred gave the cake to Bill.

Jeff was given the milk by Bill.

Who gave the cake to Fred? A: Mary

Who did Fred give the cake to? A: Bill

#### Task 6: Yes/No Questions

John moved to the playground.

Daniel went to the bathroom

John went back to the hallway.

Is John in the playground? A:no

Is Daniel in the bathroom? A:yes

#### Task 7: Counting

Daniel picked up the football.

Daniel dropped the football.

Daniel got the milk.

Daniel took the apple.

How many objects is Daniel holding? A: two

#### Task 8: Lists/Sets

Daniel picks up the football.

Daniel drops the newspaper.

Daniel picks up the milk.

John took the apple.

What is Daniel holding? milk, football

#### Task 10: Indefinite Knowledge

John is either in the classroom or the playground.

Sandra is in the garden.

Is John in the classroom? A:maybe

Is John in the office? A:no

### $|\rightarrow$

harder ones

#### Task 9: Simple Negation

Sandra travelled to the office.

Fred is no longer in the office.

Is Fred in the office? A:no

Is Sandra in the office? A:yes

### Harder ones

• (17) Positional Reasoning

The triangle is to the right of the blue square.
The red square is on top of the blue square.
The red sphere is to the right of the blue square.
Is the red sphere to the right of the blue square? A:yes
Is the red square to the left of the triangle? A:yes

• (19) Path Finding

The kitchen is north of the hallway.

The den is east of the hallway.

How do you go from den to kitchen? A:west,north

### Contributions of MemNet

Global long term memory

Attention mechanism for inference

Make use of strong supervision information (supporting facts)

# End-to-end Memory Network (MemN2N)

- New end-to-end (MemN2N) model (Sukhbaatar '15):
  - Reads from memory with soft attention
  - Performs multiple lookups (hops) on memory
  - End-to-end training with backpropagation
  - Only need supervision on the final output

performance

diminish

- It is based on "Memory Networks" by [Weston, Chopra & Bordes ICLR 2015] but that had:
  - Hard attention
  - requires explicit supervision of attention during training
  - Only feasible for simple tasks

### Model

### • Single Hop

 $m_i, u \in \mathbb{R}^d$   $A, B, C \in \mathbb{R}^{d \times V}$   $W \in \mathbb{R}^{V \times d}$ 

 $J_i$ : The length of the  $i^{th}$  Sentence

Sentences

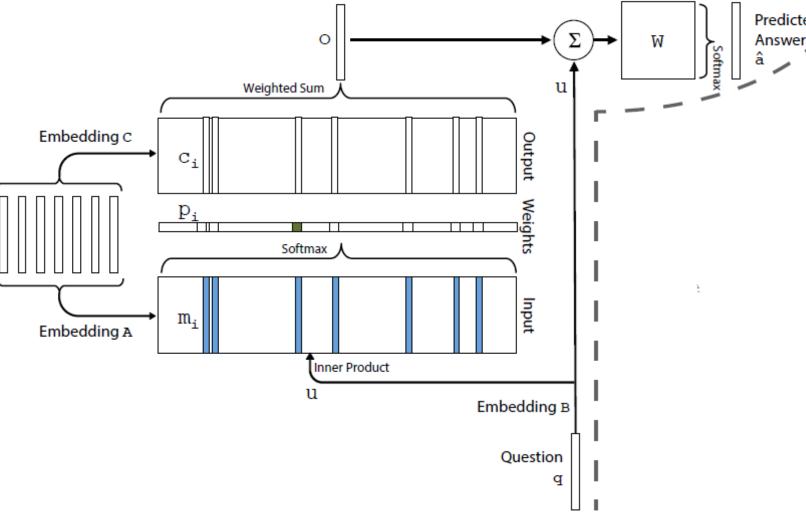
 $\{x_i\}$ 

$$x_i = \{x_{i1}, \dots, x_{iJ_i}\}$$
$$m_i = \sum_j Ax_{ij}$$

 $p_i = \text{Softmax}(u^T m_i).$ 

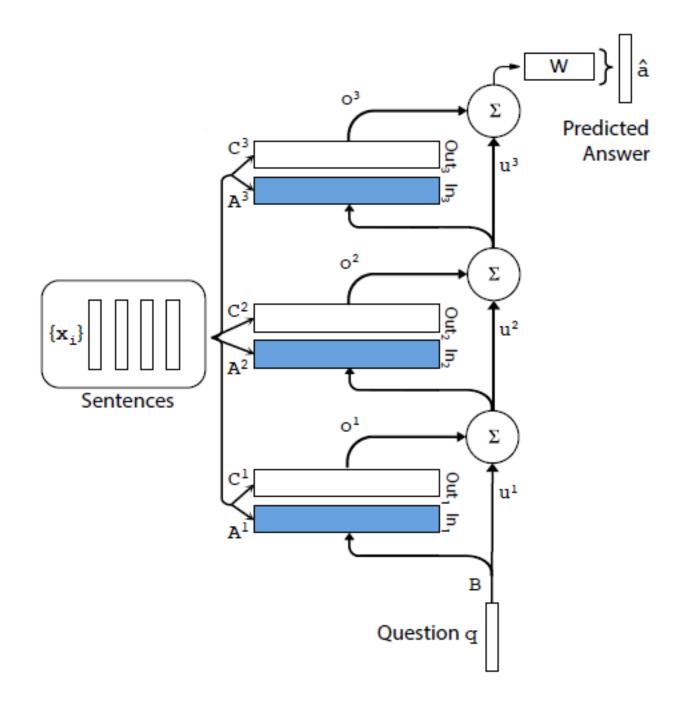
$$o = \sum_{i} p_i c_i.$$

 $\hat{a} = \text{Softmax}(W(o+u))$ 



## Model

Multi Hops



### Model details

Weight Sharing:

### Adjacent:

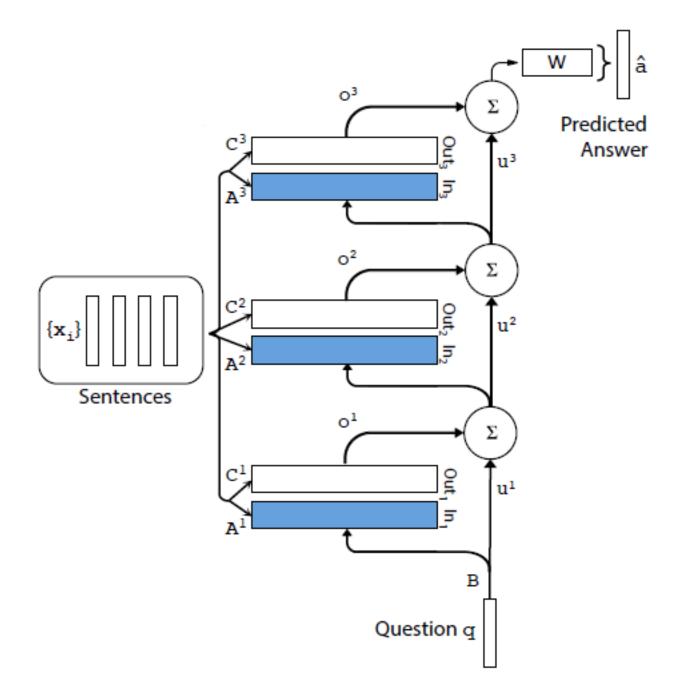
$$B = A^{1}$$
  
 $A^{k+1} = C^{k}, k = 1, ..., K - 1$   
 $C^{K} = W$ 

Layer-wise (RNN-like):

$$A^{1} = \cdots = A^{K}$$

$$C^{1} = \cdots = C^{K}$$

$$u^{k+1} = Hu^{k} + o^{k}$$



### Model details

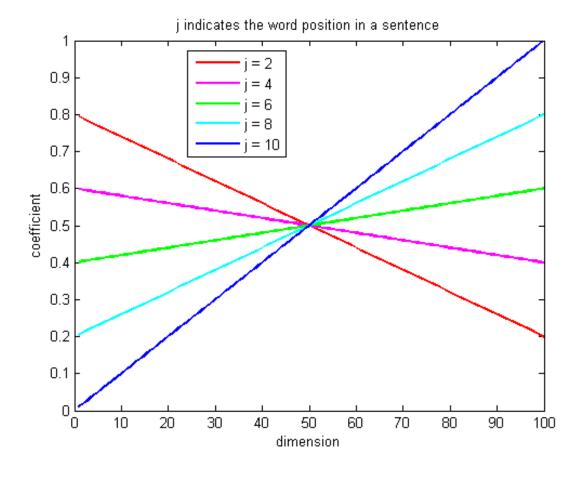
Position encoding other than BoW:

$$x_i = \{x_{i1}, \dots, x_{iJ_i}\}$$

$$(m_i = \sum_j Ax_{ij})$$

$$m_i = \sum_j l_j \cdot Ax_{ij}$$

$$l_j \in \mathbb{R}^d, l_{jk} = \left(1 - \frac{j}{J_i}\right) - (\frac{k}{d})(1 - \frac{2j}{J_i})$$



$$d = 100, J_i = 10$$

### Model details

Temporal Encoding:

$$m_i = \sum_j Ax_{ij} + T_A(i)$$

Random Noise:

Randomly add 10% of empty memories to the stories when training

• Linear Start:

At the beginning of training, remove the softmax layer when calculating p\_i. When the validation loss stopped decreasing, the softmax layers were re-inserted.

## Experiments

### Training on 1k stories

TASK	N-grams	LSTMs	MemN2N	Memory Networks
T1. Single supporting fact	36	50	PASS	PASS
T2. Two supporting facts	2	20	87	PASS
T3. Three supporting facts	7	20	60	PASS
T4. Two arguments relations	50	61	PASS	PASS
T5. Three arguments relations	20	70	87	PASS
T6. Yes/no questions	49	48	92	PASS
T7. Counting	52	49	83	85
T8. Sets	40	45	90	91
T9. Simple negation	62	64	87	PASS
T10. Indefinite knowledge	45	44	85	PASS
T11. Basic coreference	29	72	PASS	PASS
T12. Conjunction	9	74	PASS	PASS
T13. Compound coreference	26	PASS	PASS	PASS
T14. Time reasoning	19	27	PASS	PASS
T15. Basic deduction	20	21	PASS	PASS
T16. Basic induction	43	23	PASS	PASS
T17. Positional reasoning	46	51	49	65
T18. Size reasoning	52	52	89	PASS
T19. Path finding	0	8	7	36
T20. Agent's motivation	76	91	PASS	PASS

### Experiments

- The position encoding representation improves over bag-of-words on tasks where word ordering is particularly important.
- The linear start to training seems to help avoid local minima.
- Random empty memories gives a small but consistent boost in performance, especially for the smaller 1k training set.
- Joint training on all tasks helps.
- More computational hops give improved performance.

## Attention during memory lookups

Story (1: 1 supporting fact)	Support	Hop 1	Hop 2	Hop 3
Daniel went to the bathroom.		0.00	0.00	0.03
Mary travelled to the hallway.		0.00	0.00	0.00
John went to the bedroom.		0.37	0.02	0.00
John travelled to the bathroom.	yes	0.60	0.98	0.96
Mary went to the office.		0.01	0.00	0.00
Where is John? Answer: bathroom	Predict	ion: bath	room	

Story (16: basic induction)	Support	Hop 1	Hop 2	Hop 3			
Brian is a frog.	yes	0.00	0.98	0.00			
Lily is gray.		0.07	0.00	0.00			
Brian is yellow.	yes	0.07	0.00	1.00			
Julius is green.		0.06	0.00	0.00			
Greg is a frog.	yes	0.76	0.02	0.00			
What color is Greg? Answer: yellow	Predict	Prediction: yellow					

Story (2: 2 supporting facts)	Support	Hop 1	Hop 2	Нор 3		
John dropped the milk.		0.06	0.00	0.00		
John took the milk there.	yes	0.88	1.00	0.00		
Sandra went back to the bathroom.		0.00	0.00	0.00		
John moved to the hallway.	yes	0.00	0.00	1.00		
Mary went back to the bedroom.		0.00	0.00	0.00		
Where is the milk? Answer: hallway	Prediction: hallway					

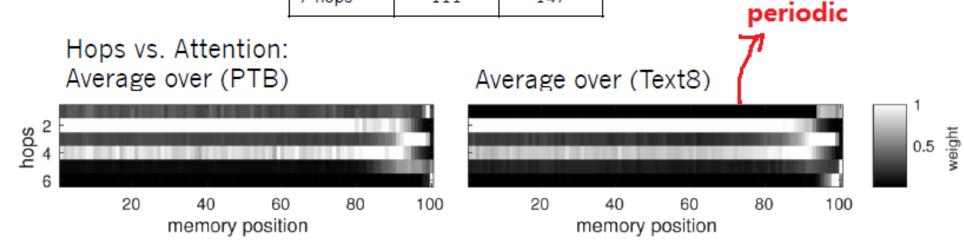
Story (18: size reasoning)	Support	Hop 1	Hop 2	Hop 3			
The suitcase is bigger than the chest.	yes	0.00	0.88	0.00			
The box is bigger than the chocolate.		0.04	0.05	0.10			
The chest is bigger than the chocolate.	yes	0.17	0.07	0.90			
The chest fits inside the container.		0.00	0.00	0.00			
The chest fits inside the box.		0.00	0.00	0.00			
Does the suitcase fit in the chocolate? Answer: no Prediction: no							

## Language Modeling

The goal is to predict the next word in a text sequence given the previous words. Results on the Penn Treebank and Text8 (Wikipediabased) corpora.

	Penn Tree	Text8
RNN	129	184
LSTM	115	154
MemN2N 2 hops	121	187
5 hops	118	154
7 hops	111	147

Test perplexity



# Q & A

	E	Baseline		MemN2N								
	Strongly						PE	1 hop	2 hops	3 hops	PE	PE LS
	Supervised	LSTM	MemNN			PE	LS	PE LS	PE LS	PE LS	LS RN	LW
Task	MemNN [22]	[22]	WSH	BoW	PE	LS	RN	joint	joint	joint	joint	joint
1: 1 supporting fact	0.0	50.0	0.1	0.6	0.1	0.2	0.0	0.8	0.0	0.1	0.0	0.1
2: 2 supporting facts	0.0	80.0	42.8	17.6	21.6	12.8	8.3	62.0	15.6	14.0	11.4	18.8
<ol><li>3: 3 supporting facts</li></ol>	0.0	80.0	76.4	71.0	64.2	58.8	40.3	76.9	31.6	33.1	21.9	31.7
4: 2 argument relations	0.0	39.0	40.3	32.0	3.8	11.6	2.8	22.8	2.2	5.7	13.4	17.5
5: 3 argument relations	2.0	30.0	16.3	18.3	14.1	15.7	13.1	11.0	13.4	14.8	14.4	12.9
6: yes/no questions	0.0	52.0	51.0	8.7	7.9	8.7	7.6	7.2	2.3	3.3	2.8	2.0
7: counting	15.0	51.0	36.1	23.5	21.6	20.3	17.3	15.9	25.4	17.9	18.3	10.1
8: lists/sets	9.0	55.0	37.8	11.4	12.6	12.7	10.0	13.2	11.7	10.1	9.3	6.1
9: simple negation	0.0	36.0	35.9	21.1	23.3	17.0	13.2	5.1	2.0	3.1	1.9	1.5
<ol><li>indefinite knowledge</li></ol>	2.0	56.0	68.7	22.8	17.4	18.6	15.1	10.6	5.0	6.6	6.5	2.6
<ol> <li>basic coreference</li> </ol>	0.0	38.0	30.0	4.1	4.3	0.0	0.9	8.4	1.2	0.9	0.3	3.3
12: conjunction	0.0	26.0	10.1	0.3	0.3	0.1	0.2	0.4	0.0	0.3	0.1	0.0
<ol><li>compound coreference</li></ol>	0.0	6.0	19.7	10.5	9.9	0.3	0.4	6.3	0.2	1.4	0.2	0.5
14: time reasoning	1.0	73.0	18.3	1.3	1.8	2.0	1.7	36.9	8.1	8.2	6.9	2.0
15: basic deduction	0.0	79.0	64.8	24.3	0.0	0.0	0.0	46.4	0.5	0.0	0.0	1.8
16: basic induction	0.0	77.0	50.5	52.0	52.1	1.6	1.3	47.4	51.3	3.5	2.7	51.0
17: positional reasoning	35.0	49.0	50.9	45.4	50.1	49.0	51.0	44.4	41.2	44.5	40.4	42.6
18: size reasoning	5.0	48.0	51.3	48.1	13.6	10.1	11.1	9.6	10.3	9.2	9.4	9.2
19: path finding	64.0	92.0	100.0	89.7	87.4	85.6	82.8	90.7	89.9	90.2	88.0	90.6
20: agent's motivation	0.0	9.0	3.6	0.1	0.0	0.0	0.0	0.0	0.1	0.0	0.0	0.2
Mean error (%)	6.7	51.3	40.2	25.1	20.3	16.3	13.9	25.8	15.6	13.3	12.4	15.2
Failed tasks (err. > 5%)	4	20	18	15	13	12	11	17	11	11	11	10
On 10k training data	2.2	26.	20.2		0.1			2:5	40.0			44.5
Mean error (%)	3.2	36.4	39.2	15.4	9.4	7.2	6.6	24.5	10.9	7.9	7.5	11.0
Failed tasks (err. > 5%)	2	16	17	9	6	4	4	16	7	6	6	6