

UNIVERSITY OF AMSTERDAM

MASTERS THESIS

Mathematically Modeling the Interactions Between Phages, Bacteria, and the Environment

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Declaration of Authorship

I, Victor PIASKOWSKI, declare that this thesis, entitled ‘Mathematically Modeling the Interactions Between Phages, Bacteria, and the Environment’ and the work presented in it are my own. I confirm that:

- This work was done wholly or mainly while in candidature for a research degree at the University of Amsterdam.
- Where any part of this thesis has previously been submitted for a degree or any other qualification at this University or any other institution, this has been clearly stated.
- Where I have consulted the published work of others, this is always clearly attributed.
- Where I have quoted from the work of others, the source is always given. With the exception of such quotations, this thesis is entirely my own work.
- I have acknowledged all main sources of help.
- Where the thesis is based on work done by myself jointly with others, I have made clear exactly what was done by others and what I have contributed myself.

Signed:



Date: May 17, 2025

“All models are wrong, but some are useful“

George E. P. Box

UNIVERSITY OF AMSTERDAM

Abstract

Faculty of Science
Informatics Institute

Master of Science in Computational Science

Mathematically Modeling the Interactions Between Phages, Bacteria, and the Environment

by Victor PIASKOWSKI

Include your abstract here Abstracts must include sufficient information for reviewers to judge the nature and significance of the topic, the adequacy of the investigative strategy, the nature of the results, and the conclusions. The abstract should summarize the substantive results of the work and not merely list topics to be discussed. Length 200-400 words.

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Contents

Declaration of Authorship	i
Abstract	iii
Acknowledgements	iv
Contents	v
List of Figures	viii
List of Tables	x
List of Algorithms	xi
Abbreviations	xii
1 Introduction	1
1.1 Biological Background	1
1.2 Phage Cocktail and Human Health	2
1.3 Industrial Usage	2
1.4 The Environment	3
1.5 Modelling Phages in a Complex Community	3
1.6 Thesis Project	4
2 Literature review	6
2.1 Methods of Modelling Phages and Bacteria	6
2.1.1 Generalized Lotka-Volterra Model	7
2.1.2 Generalized Consumer-Resource Model	7
2.1.3 Trait-Based Model	7
2.1.4 Agent-Based Models	8
2.2 Biology of Phages	9
2.2.1 What Are Phages?	9
2.2.2 How Does the Phage Cycle Work?	9
2.2.2.1 Infection Stage	9
Detection and Attachment	9

Phage DNA Injection	10
2.2.2.2 Lysogenic Cycle	10
Repression of DNA	10
Phage DNA Integration Into Bacteria DNA	10
Cellular Replication	10
Phage Induction	11
2.2.2.3 Lytic Cycle	11
Hijacking DNA Replication Process	11
Assembly of Phage Parts	11
Lysis of the Bacterial Cell	11
2.3 Bacterial Defense Against Phages	11
2.3.1 Mutations in Bacterial DNA (Genetic (Co-)Evolution)	12
2.3.2 Phage Inactivation and Decoys	13
2.3.3 CRISPR-Cas Methods	13
2.3.4 Phenotype Resistance	13
2.3.5 Spatial Refuge/Biofilms	13
2.3.6 Phage Counter Defense Against Bacteria	14
2.3.7 Genetic mutations	14
2.3.8 Viral recombination	14
2.4 Phage Defense Against Phages	15
2.4.1 Implications of Phage Against Phage Defense	15
2.4.2 Software Mathematically Modelling Phages, Bacteria, and Resources	15
2.4.2.1 Cocktail	16
2.4.2.2 PhageDyn	16
3 Methods	19
3.1 Project Overview	19
3.1.1 Part 1: Network Creation Tool	19
3.1.2 Part 2: Simulation Framework	20
3.1.3 Part 3: Analysis and Visualization	20
3.1.4 Part 4: Custom Analyses and Visualizations	20
3.2 Network Topography of Interactions Creation Tool	20
3.3 Dashboard for Analysis and Visualization	21
3.3.1 Editing Network and Parameter Values	22
Initial Condition	22
Vector Data	23
Matrix Data	23
Environment and settings	23
3.3.2 Advanced Visualization and Analysis	23
3.3.2.1 Serial Transfer	23
3.3.2.2 Parameter Analysis	25
3.3.2.3 Initial Value Analysis	26
3.3.2.4 Phase Portrait	27
3.3.2.5 SOBOL Analysis	27
3.3.2.6 Ultimate Analysis	29
3.3.2.7 Custom Advanced Analyses and Visualizations	30
3.3.3 Interaction Network	30

3.4	The Golden Model	30
3.4.1	The Adapted Golden Model	31
3.5	Software Used and Packages	32
4	Experiments and results	34
5	Discussion	35
6	Conclusion and future work	36
6.1	Conclusion	36
6.2	Future Work	36
6.2.1	Other Models	36
6.2.1.1	Spatial simulations	38
PDE	38	
Discretization	38	
7	Ethics and Data Management	39
8	Appendix A: Equation Parameters	40
9	Appendix B: Industrial and Real Life Applications of Phages	42
9.1	Controlling Foodborne Bacteria	43
9.1.1	Current Applications	43
9.2	Phage Therapy and Antibiotics	45
9.2.1	Current Applications: Bacterial Infection Control	45
9.3	Environmental Protection	46
9.3.1	Current Applications	47
10	Appendix C: Flowchart of User and System Interactions	49
Bibliography		51

List of Figures

1.1	Life cycle of a phage, inside and outside a bacteria cell. Significant steps in the life cycle of a phage include the infection stage, integration, replication, and lysing process. Figure sourced from Campbell [1].	2
2.1	The three main ways that a (dead) bacterium can transfer DNA over to another bacterium [2].	12
2.2	Example output from Cocktail. Figure A) <i>E. coli</i> infected with phage T4 in a chemostat exhibiting an oscillating growth behavior, following the model of Bohannan and Lenski [3]. Figure B) Oscillations of bacteria and phages can exist at higher titers, dependent on low resource concentration, following the model of Lenski [4]. Figure C) As the concentration of resources change, this results in increasing oscillations, but not going extinct. Figure D) A system modelling the interactions with phage A and B. See Nilsson [5] for more information on parameter values, sources, and supplementary resources.	17
2.3	Example output from PhageDyn, showing concentration of heterotrophic biomass in an aerobic plug flow across four situations. Purple is heterotrophic biomass, Blue is foaming biomass, Red is phages, Light Blue is total suspended solids. Figure A) Biomass concentration immediately post phage dosing. Figure B) Biomass concentration with low phage concentration and maintain low concentration post spike in population count. Figure C) Biomass concentration when phages are extinct. Figure D) Biomass concentration with a less virulent and low adsorption rate phage, co-existence with biomass reached. A change in phage concentration shows a decrease in heterotrophic and foaming biomass. [6]	18
3.2	The tabs where the user can edit the various parameter values and control the simulation parameters	24
3.3	Serial Transfer	25
3.4	Parameter Analysis	26
3.5	Initial value analysis	27
3.6	Phase Portrait	28
3.7	SOBOL variance analysis	29
3.8	The ultimate analysis setup tab.	30
6.1	Exponential growth curve vs logistic growth	38

9.1 SalmoLyse® reduces Salmonella contamination on various food surfaces: Mean and standard error bars shown. Statistical analyses were carried out for each food group independently. Asterisks denote significant reduction from corresponding controls based on one-way ANOVA with Tukey's post-hoc tests for multiple corrections: ** denotes $p < 0.01$, while *** denotes $p < 0.001$ compared to the corresponding controls. There was significant reduction in Salmonella on all food surfaces with the addition of SalmoLyse® compared to the controls; the mean percent reductions from the control are noted in the boxes above treatment bars. CFU/g D colony forming units per gram. Each letter denotes a food group that was tested with SalmoLyse® and compared to a control: A= chicken; B= lettuce; C= tuna; D= cantaloupe; E= ground turkey [7].	44
9.2 <i>Salmonella</i> count in a mixture of 5 <i>Salmonella</i> strains spot-inoculated (CFU/g) onto a) lettuce and b) sprouts after spraying with a mixture of bacteriophage (SalmoFresh™) relative to positive controls at 2, 10 and 25C and stored for 1, 24, 48 and 72 h. [8]	44
9.3 Cyanobacteria degradation cycle, main hazards of cyanobacteria bloom to water bodies, aquatic organisms, and the human body. (DO: dissolved oxygen; SD: water transparency; Cond: conductivity; N: nitrogen; P: phosphorus; MCs: microcystins). [9]	47
10.1 The interaction diagram of the user interacting with the system, provided input and output for subsystems, and the systems working with one another. To read the flow chart, start from the top to the bottom. First the user creates a network using the GUI Network Creation Tool. After the graph is finished, the user provides an implementation of the network as an ODE model, using Python. Once finished, the user provides the network file and ODE model to the ODE solver. The solver uses information from the network file to determine the number of agents to create, parameter details (including names, values, and dimensions), and setting values. Then the user interacts with the Visualization Dashboard Tool, for example by clicking on buttons to run simulations, changing parameter values, (un)selecting checkboxes, and zooming in and out of plots, and hovering over plots to show data. Once a user has selected the parameter values, the parameter values are sent to the solver. The solver calculates the time and population values using the provided graph and ODE model and sends the data back to the Visualization Dashboard Tool, which then outputs the visualizations. If the user has run an ultimate analysis, then the user can query the saved data to make their own custom visualizations.	50

List of Tables

- 8.1 Model parameters with variables, names, and descriptions. Subscripts on parameters indicate relationships; for example, $e_{b,r}$ is nonzero if there is an edge connecting bacteria b to resource r in the network, zero otherwise. 41

List of Algorithms

Abbreviations

ABM	Agent Based Modelling
ARD	Arms Race Dynamic
BVP	Boundary Value Problem
CBASS	Cyclic oligonucleotide-Based Antiphage Signalling Systems
CRISPR	Clustered Regularly Interspaced Short Palindromic Repeats
DDE	Delay Differential Equation
DNA	DeoxyriboNucleic Acid
FSD	Fluctuating Selection Dynamics
GUI	Graphical User Interface
ODE	Ordinary Differential Equation
PDE	Partial Differential Equation
RNA	RiboNucleic Acid
SIE	Superinfection Exclusion
SNP	Single Nucleotide Polymorphism
UvA	Universitiet van Amsterdam

Chapter 1

Introduction

Phages are small viruses on the order of 27-190nm that infect and lyse (kill) specific bacteria, acting as nature's natural anti-microbial defense. Researchers are attempting to determine how phages can be used in various medical and industrial applications to control bacterial growth. However, researchers need to know how the interactions between phages and bacteria work in order to implement a robust method to control bacterial growth.

1.1 Biological Background

Phages are small viruses on the order of 27-190nm that infect and lyse (kill) specific bacteria. The phage cycle process starts with a phage coming into contact with a bacterium. Once it has identified an injection site, the phage can inject a strain of DNA into the bacteria. The DNA strand has two options: it can either merge into the bacterial DNA, allowing the phage's DNA strand to replicate alongside the bacteria as they reproduce. This process defines the Lysogenic cycle. After a set amount of time, the DNA of the phage can unmerge and hijack the DNA replicating mechanism, creating multiple copies of itself, using the transcription, translation, and replication process to create multiple copies of itself. The phages begin to self-assemble inside the bacteria until the bacteria is full of phages and explodes, the lysis stage, releasing the phages into the environment, ready to repeat the process again.

This process can be visualized in [Figure 1.1 \[1\]](#).

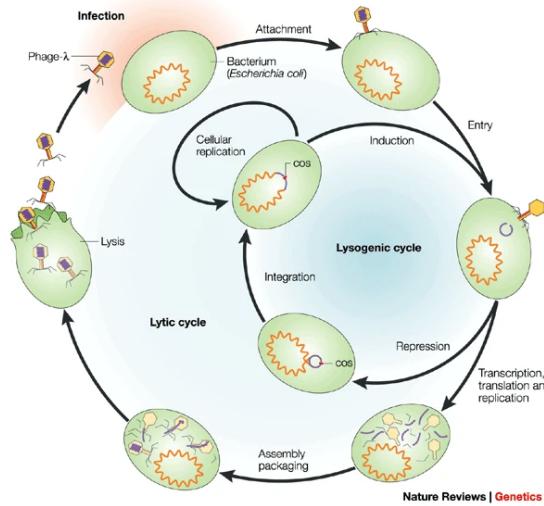


Figure 1.1: Life cycle of a phage, inside and outside a bacteria cell. Significant steps in the life cycle of a phage include the infection stage, integration, replication, and lysing process. Figure sourced from Campbell [1].

1.2 Phage Cocktail and Human Health

There is particular interest in phage applications in human and animal health, called phage cocktail therapy, due to phages not exhibiting side effects. Phage cocktails are a medicine that sick patients with bacterial diseases, such as *Escherichia coli* can use. A patient can swallow a pill filled with a range of different phages that target *E. coli*. The phages will target the specific *E. coli* bacteria, but it will not affect the other bacteria found in the gut of the human body and will not have any side effects on the body. There are 100 trillion microbes across 5,000 different types of bacteria strains in the human gut. Medicine such as antibiotics disrupt the intricate ecosystem of the gut microbiome, acting as a scorched-earth mechanism. Phages on the other hand specifically target a specific bacterial strain, acting as a sniper, with minimal to no effects to other bacteria, while penicillin acts as a bomb. A challenge that antibiotics face is that antibiotics create antibiotic resistant bacteria, meaning that the antibiotics is less effective in the future [10, 11]. There is however hope that phage resistant bacteria become more susceptible to antibiotics due to changes in the cell structure [12, 13].

1.3 Industrial Usage

Phages have many uses in an industrial setting. Similarly, phage therapies can be used as a preventative method, by preventing the spread of common bacteria in livestock by dosing the animal feed with the phage pills. Farmers often raise livestock in tight spaces with a lack of sanitation facilities, increasing the risk of a disease spreading.

Phages can be used to control the growth of bacteria like *Salmonella* while producing food in a factory [7, 14].

1.4 The Environment

In an ecosystem like the ocean, the gut, or in soil, there are thousands of different microbes all interacting with one another or the surrounding environment. The interactions are complex, with many factors affecting the growth of bacteria, fungi, phages, plants, animals, and more. Often, the interactions between agents in the environment are synergistic. When an animal dies, bacteria start to digest and decompose the animal into simpler chemicals like carbon and nitrogen that plants can use to grow, which is then eaten by other animals.

Not every interaction in the complex community can be identified, and if an interaction has been identified, the associated parameter values are unknown and need to be experimentally derived. External factors, such as flooding, droughts, chemical spills, or introduction of new agents have a massive impact on the ecosystem. These events can add or remove resources from the system, change environmental parameters such as the surrounding temperature, introduce competition, or create an imbalance in the population by killing agents. These effects can affect the larger ecosystem and food chain as a whole. Finally, phages can potentially be used to control cyanobacterial (blue-green algae) blooms in the environment and affect other agents such as plankton in the environment [15]. With this, there is hope that water quality can be engineered without using harsh chemical processes what would otherwise pose environmental and health hazards [16].

1.5 Modelling Phages in a Complex Community

Not much is known about phages in large and complex communities between other phages, bacteria, resources, and the environment. There have been previous attempts to model the complex dynamics of the populations between phages, bacteria, and resources, with the environment using Ordinary Differential Equations (ODE) and Delay Differential Equations (DDE). however collecting the parameter values for the interactions is an expensive and laborious task, as the data has to experimentally collected in

a lab.

A Resource-Phage-Bacteria system can be described as an $p \times b \times r$ system, meaning there are p phages, b bacteria, and r resources arbitrarily interacting with one another. However, current modelling methods have mainly stayed with $1 \times 1 \times 1$ models, meaning 1 phage, 1 bacteria, and 1 resource.

There are two main ways to model phage-bacteria dynamics: a spatial model and a non-spatial one. A spatial model means that phages and bacteria can move through space and interact with their neighbors. Partial differential equations (PDE) and cellular agent based models have been created in an attempt to model spatial interactions. Special considerations have to be accounted for with spatial models, such as bacteria and phages can only interact when they are in proximity to each other. This creates areas of interaction and interest where agents are located, and areas of no interactions where there are no interactions. Spatial models can potentially lead to more interesting and complex results but are limited to smaller populations and harder to develop.

Whereas in non-spatial models such as ODEs and DDEs, the bacteria and phages are assumed to be in a well-mixed solution and no distinction is made in regard to neighbors or distances to other agents. Interactions are simplified to a probabilistic approach, where only a percentage p of bacteria and phages interact with one another at time step t . Non non-spatial models are easier to develop and are more effective in modeling large populations, at the cost of losing spatial information.

For this thesis, the focus will be modelling resource, phage, and bacteria interactions using an ODE model.

1.6 Thesis Project

The project is divided into three logical parts, with an optional fourth part. The first section is to create the network interaction. Here the user of the software can define the number of resources, phages, and bacteria, who interacts with who, and the strength and type of interactions. See [Section 3.1.1](#) for further information.

In part 2 ([Section 3.1.2](#)), the user uploads the network model and parameters and as output receives the time data and population data as an array.

Part 3 ([Section 3.1.3](#)) allows the user to interact with part 1 and part 2 with a dashboard. The user can graphically edit the attribute values of the edges and nodes of the

network, and the user can run more advanced visualizations, for example by changing a parameter value and seeing how that affects the population count. There are a few plots included out of the box that the user can test. The plots offered in part 3 offer interactivity like hiding and showing lines and dots, zooming in and out, and hovering over the lines and dots to show more details of the data.

Finally, the user can optionally run multiple simulations and download the data to their disk to create their own custom visualizations using part 4 ([Section 3.1.4](#)). The visualizations created in part 3 can theoretically be recreated in part 4. The user can choose the same parameter values used for a specific plot in part 3, run the simulation (under the "Ultimate Analysis" section ([Section 3.3.2.6](#))), download the data, and reimplement the graphs.

Chapter 2

Literature review

2.1 Methods of Modelling Phages and Bacteria

There are numerous ways to model the interactions between phages and bacteria. Models can be built at a molecular level, where the model simulates the mechanical and chemical behavior of a phage as it interacts with the surface of a bacterium using computational chemistry methods. On the other end of the spectrum, a different type of model can be built where populations of phages, bacteria, and resources can be modeled using Ordinary Differential Equations (ODEs) or Delay Differential Equations (DDEs). DDEs are similar to ODEs, except where when ODEs are calculating the values of the equations at time t using time $t - 1$, DDEs can, but don't have to, use the value of the equation at time $t - \tau$, where $1 \leq \tau \leq t$. DDEs are a generalized version of ODEs and are significantly harder to analyze and find stability conditions than ODEs due to the dependence on the past [17].

One way to introduce DDE like behavior is to force agents to go through stages, causing a delay in other events. For example, in the paper Geng et al. [18], infected bacteria go through M stages of infection, before lysing. The more stages there are, the longer the delay in seeing a rise in phage population. By changing the value of τ in the model proposed by Geng et al. [18], the throughput of bacteria going from stage i to stage $i + 1$ of infection increases, thus seeing a larger rise in phage population.

Each type of model has its pros and cons. With the molecular level model, the model is more complex and needs significantly more startup time, simulation time, and is in general much more complex. However, more information can be gained from the simulations and can guide research in creating phages for a certain type of bacteria. The ODE method is simpler and easier to set up, however it can only capture large

population dynamics. Certain assumptions about the community interactions have to be made. For example, ω percent of the bacteria population is washed out. The model can be made more complicated, by modelling each stage of the phage replication and lysis process, or instead of assuming exponential growth, there is a maximum carrying capacity of the population. The model can be further altered by using a normally distributed variable $\mathbf{N}(\mu = \omega, \sigma = 1)$ to account for noise when measuring the data. Ensuring the use of a seed value will ensure that each run of the model results in the same output.

2.1.1 Generalized Lotka-Volterra Model

The Lotka-Volterra model, a first-order non-linear differential model, is a model that captures the dynamics between predators and prey, with phages being the predator and bacteria being the prey. Any population can be modelled as such:

$$\frac{dB_i}{dt} = B_i \left(\left(r_i + \sum_j^N \alpha_{ij} B_j \right) - m_i \right)$$

where \dots .

2.1.2 Generalized Consumer-Resource Model

The generalized Consumer-Resource Model models the growth of a population and resource dynamics between a population of bacteria B_i and a resource R_i .

$$\frac{dB_i}{dt} = r_i B_i \left(\sum_{\alpha} \Delta w_{i\alpha} C_{i\alpha} R_{\alpha} \right) - m_i B_i \quad (2.1)$$

$$\frac{R_{\beta}}{dt} = - \sum_i C_{i\beta} R_{\beta} B_i + \sum_{\alpha,i} D_{\beta\alpha}^i C_{i\alpha} R_{\beta} B_i \quad (2.2)$$

$$\Delta w_{i\alpha} = \sum_{\beta} D_{\beta\alpha}^i w_{\beta} \quad (2.3)$$

2.1.3 Trait-Based Model

The Trait-Based Model is a model that takes into account external factors such as the temperature or pH of the system and can be modeled as follows:

$$\frac{dB_i}{dt} = (r_i - m_i) B_i \quad (2.4)$$

$$r_i = \frac{r_{i\alpha}^{max} R_{\alpha}}{R_{\alpha} + K_{i\alpha}} e^{S_i(T - T_{ref})} \quad (2.5)$$

where S_i is the sensitivity to B_i to factor T , and with trade off if $r_i^{max} > \text{mean } r^{max}$ then $S_i > \text{mean } S$.

2.1.4 Agent-Based Models

Agent-based Models (ABM) model the system through space and time. An $x \times y \times z$ grid (often z is left out for a 2D system) is created and split into smaller subcells containing resources and microbes. Each cell acts as its own tiny environment, where resources and microbes interact within the environment, but not with the neighboring cells. Resources diffuse through the system using a PDE solver for a Boundary Value Problem (BVP). Agents can move into neighboring grids with a probability p , where p can depend on any number of parameters such as resource density, microbe density, or stochastic chance. ABMs are useful when simulating many individual elements interacting in a system. Chaotic or emergent behavior can arise from these interactions. Chaotic behavior refers to the irregular and unpredictable evolution of a system's behavior due to nonlinear equations, exhibiting sensitive dependence on initial conditions [19].

Emergent behavior is behavior that arises from the interactions of various agents in a system, that was not explicitly programmed into the system. The behavior can be beneficial, neutral, or harmful, but it can not be predicted until it arises, *if* it arises. Agents can have simple rules, but when interacting with other agents, behavior that hasn't been programmed can arise. Sometimes, people consider systems with emergent behaviors more complex than the sum of their parts.

$$\frac{\delta R_\alpha(r, t)}{\delta t} = \nabla [D(R_\alpha, r) \nabla R_\alpha(r, t)], r = (x, y) \quad (2.6)$$

, where r is a function of cell position (x, y) , and t represents time. The cellular agents rules are as follows:

$$\frac{di}{dt} = r_i \left(\sum_{\alpha} \Delta w_{i\alpha} C_{i\alpha} R_{\alpha} \right) \quad (2.7)$$

, where if $i >$ threshold, $\frac{i}{2}$ expands into the neighboring grid cell with a probability p . The system consumes resources and converts them into new sub-resource types with the following equation:

$$\frac{dR_\alpha}{dt} = - \sum_i C_{i\alpha} R_{\alpha} I \quad (2.8)$$

$$\frac{dR_\beta}{dt} = \sum_i C_{i\beta} R_{\beta} I + \sum_{\alpha, i} D_{\beta\alpha}^i C_{i\alpha} R_{\alpha} i \quad (2.9)$$

2.2 Biology of Phages

2.2.1 What Are Phages?

2.2.2 How Does the Phage Cycle Work?

There are 3 main parts to the phage-bacteria host cycle, the infection stage, the lysogenic cycle, and the lytic cycle. In the infection stage, a phage floating through the environment detects and attaches to the surface of a bacteria cell. Once injected, the phage-cell pair can directly go into the lysogenic cycle or into the lytic cycle. [Figure 1.1](#) shows a detailed overview of the phage cycle.

In the lysogenic cycle, the phage DNA injects integrates into the genome of the bacteria. As the bacteria undergoes cellular replication, the DNA of the phage will be copied with the cell. After a set amount of time, the phage DNA can cut itself from the genome and enters the Lytic cycle.

In the lytic cycle, the phage hijacks the cellular process of the bacteria. The phage DNA hijacks the replication, transcription, and replication process of the cell, making more and more copies of phage. The phage parts build together to make a full part. Eventually the cell wall bursts releasing the phages into the environment ready to infect more bacteria.

2.2.2.1 Infection Stage

The infection stage is characterized as the searching for a bacterium, detection, and subsequent attachment and injection of DNA into the bacteria.

Detection and Attachment Phages float through the medium and by chance land on a bacteria. The phage detects the cell via host cell surface receptors tuned to a specific bacteria cell wall [20]. Various inter-molecular forces such as hydrogen bonds help the phage attach to the cell.

Phage DNA Injection The injection is triggered by the recognition between the phage's receptor-binding protein located at the tip of the tail and a specific receptor located on the surface of the bacteria. Once a suitable injection site has been identified, the phage injects the DNA into the cytoplasm of the cell. The specificity of recognition is directly related to the specificity of adsorption, which correlates to the structure of receptors located on the host's cell surface [20]. The injected DNA is called a plasmid, genetic structure usually in the shape of a circle that can replicate independently of chromosomes.

2.2.2.2 Lysogenic Cycle

The lysogenic cycle describes the process in which the viral DNA of the phage evades detection, integrates into the cell's DNA, replicates with the cell, and inducts from the DNA. Phages that have integrated into the host's DNA are called prophages.

Repression of DNA As phages are viruses, they need to evade viral detection methods such as Cyclic oligonucleotide-based antiphage signalling systems (CBASS). CBASS triggers effector proteins that cause cell death, preventing phage replication and lysis [21]. Two big benefits of programmed cell death is that the cell death slows the growth of phages and the dead cells release nutrients into the environment, allowing other bacteria to recycle the nutrients and grow [22].

CRISPR-Cas is another method that bacteria can use to detect the presence of phage DNA. CRISPR-Cas is an adaptive immune system in bacteria that defends against phages by acquiring foreign DNA sequences (spacers) into its CRISPR array, transcribing them into CRISPR RNAs (crRNAs), and using these crRNAs with Cas proteins to identify and degrade foreign DNA [23].

Phage DNA Integration Into Bacteria DNA The DNA of the phage is able to integrate into the bacteria's DNA. Prophages can alter the fitness of the cell, by changing metabolic routes and other cellular structures and functions to better survive under nutrient limitations or by increasing resistance against other phages. By altering the fitness of the cell, the prophage can wait until better conditions are met for a lytic approach to be favorable [22].

Cellular Replication The cell undergoes division multiple times, copying the prophage DNA into the cell copies. However prophages are still at risk of being discovered and excised by restriction enzymes [24].

Phage Induction Prophages induct (leave) from the bacteria DNA under specific conditions. The induction process starts with proteolytic cleavage and displacement of the phage repressor, which most of the time occurs upon activation of the SOS response following DNA damage [25]. Cell stressors such as DNA-damaging agents like UV light and antibiotics can jump-start the process to switch to the lytic cycle [20, 26].

2.2.2.3 Lytic Cycle

The lytic cycle describes the process in which the viral DNA hijacks the DNA replication process, assembles within the cell, and lyses the cell releasing the phages into the environment.

Hijacking DNA Replication Process The phage hijacks the cellular replication process to create the different proteins that make up the phage, like the legs, body, and head. Phenotypic reconfiguration of the host is frequently facilitated by auxiliary metabolic genes, which are genes initially sourced from host genomes but preserved and modified within viral genomes to channel energy and resources toward viral replication [22].

Assembly of Phage Parts Phage parts self-assemble by using various protein-protein and protein-nucleic interactions, along with other forms of interactions such as hydrogen bonding and hydrophobic/philic interactions [27]. Phage induction can also lead to transduction, where genetic material is transferred between bacterial cells via phages, driving bacterial evolution [26]. This can also have the unintended side effect where one bacteria will directly infect another bacteria by transferring phage DNA.

Lysis of the Bacterial Cell Internal pressure buildup causes the cell wall to explode, releasing phages, resources, and other organic matter into the environment. Genetic material from one bacteria can be transferred to other bacterial cells via phages, driving bacterial evolution.

2.3 Bacterial Defense Against Phages

There is a constant battle between phages and bacteria. The bacteria don't want to be killed by the phages, so they adapt defenses such as thickening of the cell wall, or once the viral DNA has integrated with the bacteria's DNA, the bacteria will cut the viral DNA out of their DNA using CRISPR and restriction enzymes [28].

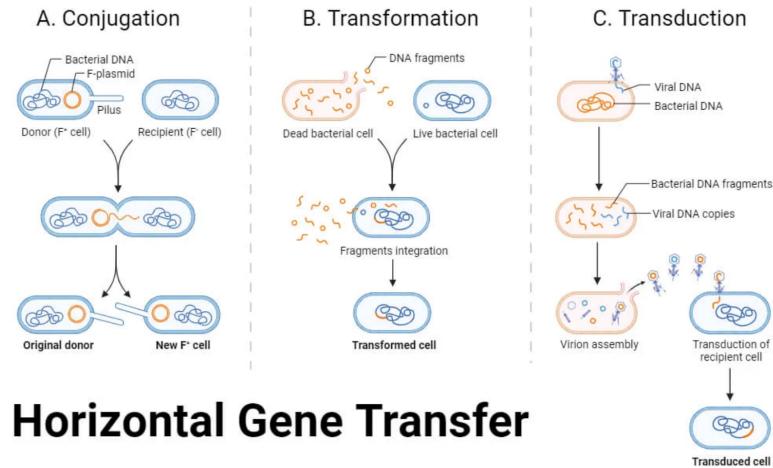


Figure 2.1: The three main ways that a (dead) bacterium can transfer DNA over to another bacterium [2].

2.3.1 Mutations in Bacterial DNA (Genetic (Co-)Evolution)

As bacteria cells grow and divide, random point mutations can occur in the DNA. These mutations can affect phage defenses, like thickening the cell wall or removing a receptor, making it harder for the phages to infect the bacteria cell. Mutations might not always work, or they can have the opposite effect. They can be partially effective if full effectiveness requires multiple steps to achieve, which can occasionally fail [29] or the mutation brings a cost to the bacteria cell by losing receptors on the cell wall.

Bacteria can horizontally transfer DNA to other bacteria on contact. There are three primary ways of this happening, which can be visualized in detail in [Figure 2.1](#).

The first method is via conjugation, where a donor cell donates DNA fragments using a mechanism called the F-factor or plasmid with a pilus. The pilus acts a tunnel connecting the donor cell to the recipient cell and the DNA can be transferred to the receiver cell.

The second method, called transformation, occurs when a cell takes up DNA fragments released by a dead or degrading cell. Once inside the receiver cell, the donor DNA can integrate itself with the receiver DNA [30].

The third method is via transduction. When a phage is assembling in the cell just before lysis, the phage can collect a piece of the hosts DNA instead of its own DNA. The dying bacterium proceeds to lyse, releasing the phages. The phage with the now dead hosts DNA can infect the next bacteria, injecting the DNA strand of the now dead cell into the new host cell. The old bacterial DNA will proceed to integrate with the new host cells DNA [2, 31].

2.3.2 Phage Inactivation and Decoys

Bacteria can further protect themselves by producing decoys that the phage will attach to instead of themselves, inactivating the phage. Freshly lysed bacteria can still contain biomarkers that phages use to detect the bacteria, but upon injection, nothing happens as the cell doesn't function anymore. Bacteria can also produce proteolytic enzymes that will damage the proteins found in a phage [32]. Some bacteria can produce outer membrane vesicles that phages can absorb to, and later detach the vesicle with the phage [33]. The vesicle will proceed to float away with the phage attached/injected inside, posing no risk to the source bacteria or to other bacteria. It is suspected that the impact of these vesicles acting as a sink is minor [34], but helpful nonetheless.

2.3.3 CRISPR-Cas Methods

CRISPR is a gene editing tool that cells can use to cut out specified/unwanted parts of a DNA strand. Researchers are commonly using CRISPR to genetically engineer plants and animals to have specific features. Strands of DNA can be selectively added or removed from a DNA strand to achieve a better, more desired DNA strand. Specialized defenses in the bacteria can detect unwanted strands and remove the strand, acting as a line of defense against phages.

2.3.4 Phenotype Resistance

2.3.5 Spatial Refuge/Biofilms

Usually bacteria and phages coexist in well mixed environments such as the ocean, however some environments offer natural structures for bacteria to hide behind. These structures can range from physical structure, like sediment in water to biochemical structures like biofilms, where the phages can't diffuse through the biofilm. In large enough quantities, bacteria and other microbial communities create biofilms, a layer of mucus containing various microbes. The thick mucus, microbes, and other spatial effects help protect the bacteria in the biofilm from external phages by making it hard for the phages to penetrate and diffuse through the mucus [35]. In the case of a lab experiment on an agar plate, bacteria protect one another by making it harder for the phages to diffuse through the system [36].

Phages can not swim and do not contain any parts that allow it to move under its own power. Movement is instead passive, relying on the environment to move through the environment, such as diffusion, changes in pressure or heat gradients [37]. The motion

that phages exhibit is called Brownian motion, the seemingly random movement of small particles throughout a medium due to other microscopic particles interacting and bouncing off of one another [38]. Unlike phages, bacteria have the ability to actively move through the environment, and they can use this to their advantage by crawling or swimming away if they detect a phage.

2.3.6 Phage Counter Defense Against Bacteria

With some of the defenses that bacteria have developed, phages are always mutating to counter their defenses. If phages don't adapt to the ever-changing bacterial defenses, the phages will experience an extinction event due to their inability to infect and multiply. It essentially becomes a race to the bottom, seeing who can out-adapt the other. However, if the phages out-adapt the bacteria too much, the bacteria die out, then eventually the phages die out due to not having any bacteria left to infect.

This can be avoided if the phages can adapt to target a second strain of bacteria, but this is unlikely. On the other hand, if bacteria out-adapt the phages, that is no problem for the bacteria because they don't need the phages to survive, and can keep on growing, limited only by the available space and resources.

This is a problem intrinsic to predator-prey systems, namely that the predators are dependent on the prey. Once the prey disappear, the predators also disappear. If the prey population goes down, and as a result the predator population goes down and becomes extinct, the prey can come back without the threat of predators.

Phages face this exact same problem: the complete removal of either the bacteria or phages will lead to the removal of the phages from the system unless reintroduced.

2.3.7 Genetic mutations

2.3.8 Viral recombination

<https://www.sciencedirect.com/science/article/pii/S1931312821004170> <https://pmc.ncbi.nlm.nih.gov/>

Multiple phages can infect a cell and replicate itself using the cells internal replication process. Each phage has its own building blocks. Phage 1 could have long legs, a long neck, and a small head, while phage 2 can have long legs, a long neck, and a medium-sized head. When the phages are building copies of themselves, they could accidentally use the body parts of other phages. The primary method for proteins to bond with other proteins and molecules is via hydrogen bonds. These attractive forces hold proteins and other molecules in defined positions, and a change in molecule shape will change the

bonds, which will force the other molecule to undergo changes in shape. If the proteins that build the subparts of each phage have similar chemical properties, they can be swapped between phages. This allows for biological diversity to spread throughout a phage population. Each phage body part can have unique characteristics such as better attachment rate, larger DNA storage capsule, or better probability of injection.

Coexistence between phages and bacteria via genetic co-evolution seems unlikely due to trade-offs imposed by the new mutations [39].

2.4 Phage Defense Against Phages

Some phages can employ defenses against other phages from infecting the bacterial cell. This is called superinfection exclusion (SIE), where a phage that has integrated with the bacterial DNA, called a prophage, prevents a secondary infection from a similar or closely related phage [40]. There are various methods of preventing further infections. The phage can alter the surface receptors of the bacteria, making it harder for other phages to detect the bacteria, reducing the chance of attachment and injection by other phages [41]. Other phages like the T4 phage can use proteins like the Spackle protein. The protein inhibits the lysozome activity used in the process of DNA injection by other phages [41, 42]. Finally, prophages can encode proteins that will interfere with the replication process of other phages. For example, the SieA protein encoded by phage P22 blocks infection from other phages [43].

2.4.1 Implications of Phage Against Phage Defense

SIE can affect the speed and development of phage and bacterial populations. A phage restricting other phages from infecting the bacteria creates a competitive environment and can outcompete and dominate the other population. This is commonly seen in wildlife populations, where invading species can out compete other species by eating more food/other species faster, breeding at a faster rate than other species, and having no natural predators.

2.4.2 Software Mathematically Modelling Phages, Bacteria, and Resources

Some software currently exists with the intended goal of modelling phage-bacteria-resource dynamics. Cocktail is a simple but yet complex software that models phages in a chemostat system [5]. Simple as it has a defined set of parameters, and only considers

one resource, one bacteria, and 2 phages, but complex due to the ability for the bacteria to gain phage resistance.

PhageDyn [6] is a Java applet that interacts with existing files in GPS-X [44] to incorporate phage dynamics into models of wastewater treatment plants.

2.4.2.1 Cocktail

The Cocktail software was developed by Anders S. Nilsson to model phage infection kinetics in a chemostat. The model assumes there is one bacteria strain that can be infected by phage A and phage B, and by both phages at the same time, phage AB. The bacteria can grow resistance to phage A, phage B, and phage AB independent of one another. The model contains inputs controlling bacterial growth rates, decay rate, resistance mutation rate against phage A, phage B, and against phage AB. The software has settings for controlling the resource concentration, available supply, and flow rate of the resource. Finally, the user can control the parameter values for phage A and B, such as the adsorption rate, patent period, and burst size. There is an option to periodically add more phages. Finally there are some settings to control the model settings, such as if the model is deterministic or stochastic, and the step size [5]. After choosing the parameter values, an output is created, with four sample plots shown in [Figure 2.2](#).

2.4.2.2 PhageDyn

PhageDyn is an add-on for the commercial software GPS-X, an advanced wastewater and industrial wastewater treatment plants modelling simulation software created by Hydromantis Inc. The aim of the software is to model phage dynamics in multi-reactor models. Previous attempts at modelling phage dynamics are not applicable to a complex multi-reactor wastewater treatment plant model. PhageDyn models the behavior of phages in multiple interconnected reactors with the aim of reducing foaming in wastewater treatment plants caused by bacteria [45]. [Figure 2.3](#) shows the output

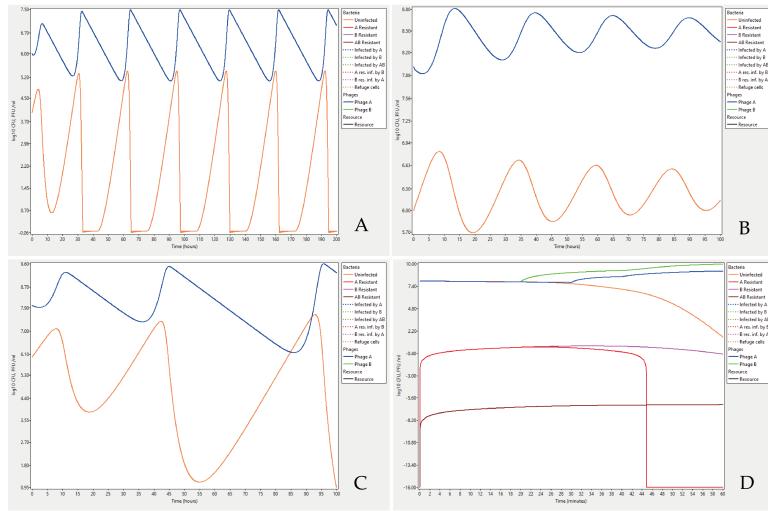


Figure 2.2: Example output from Cocktail.

Figure A) *E. coli* infected with phage T4 in a chemostat exhibiting an oscillating growth behavior, following the model of Bohannan and Lenski [3].

Figure B) Oscillations of bacteria and phages can exist at higher titers, dependent on low resource concentration, following the model of Lenski [4].

Figure C) As the concentration of resources change, this results in increasing oscillations, but not going extinct.

Figure D) A system modelling the interactions with phage A and B.

See Nilsson [5] for more information on parameter values, sources, and supplementary resources.

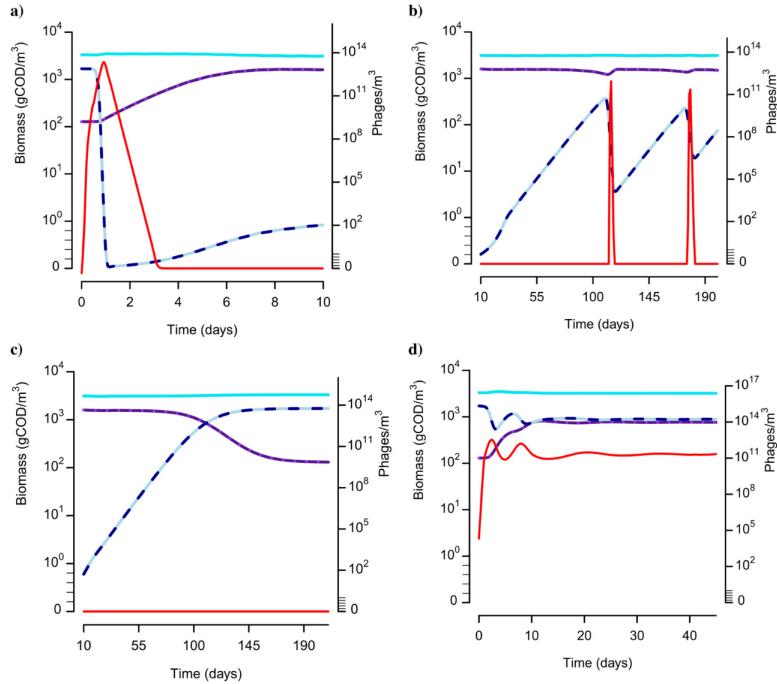


Figure 2.3: Example output from PhageDyn, showing concentration of heterotrophic biomass in an aerobic plug flow across four situations. **Purple** is heterotrophic biomass, **Blue** is foaming biomass, **Red** is phages, **Light Blue** is total suspended solids.

Figure A) Biomass concentration immediately post phage dosing.

Figure B) Biomass concentration with low phage concentration and maintain low concentration post spike in population count.

Figure C) Biomass concentration when phages are extinct.

Figure D) Biomass concentration with a less virulent and low adsorption rate phage, co-existence with biomass reached.

A change in phage concentration shows a decrease in heterotrophic and foaming biomass. [6]

Chapter 3

Methods

3.1 Project Overview

To help complete this Master thesis, I created various tools that would help create the final model outputs. The project is divided into three logical parts, with an optional fourth part.

3.1.1 Part 1: Network Creation Tool

The first part involves the development of a GUI tool to create and edit the network topography of interactions. This tool allows users to quickly and intuitively define agents, interaction parameters, environmental parameters, and setting parameters. The tool provides functionalities for adding, editing, and visualizing nodes and edges, as well as importing and exporting the network structure.

Once the user is happy with the graph shape, they can export the graph for use in part 2 ([Section 3.1.2](#)), part 3 ([Section 3.1.3](#)), and part 4 ([Section 3.1.4](#)). The most important part is that the user defines the network edges and the attributes that each node and edge has, as that can't be edited in part 2 onwards. It's not a big issue however because the user can upload the graph to the tool again to edit the edge connections and add or remove nodes and attributes. In part 3, the user can edit the values of the attributes, so the parameter values do not have to be dialed in, and the user does not need to use the GUI tool to edit parameter values.

3.1.2 Part 2: Simulation Framework

The second part focuses on the simulation framework. The user provides an ODE model and the network topography as input to the framework. The simulation framework deals with handling the input and output of the data, collecting and storing the data needed for the simulation. The framework uses SciPy's *solve_ivp()* numerical solver to simulate the provided ODE equations and calculate the population levels through time. As output, the user receives two outputs. The first output is an array of time values that the solver used to calculate the population count. The second output is an array containing the population count at each time step for every agent.

3.1.3 Part 3: Analysis and Visualization

The third part involves analyzing and visualizing the simulation results. The user can use a dashboard built using Plotly Dash to interact with the solver and network. The user can change parameter, environment values, and setting values on the fly. This allows the user to quickly change parameter values and test different situations. The dashboard includes various starter plots that allow the user to test the model.

3.1.4 Part 4: Custom Analyses and Visualizations

The final part, an optional step, allows for the user to define a number of parameters they want to simulate and download the simulation data after running the simulations. Downloading the data then allows the user to create their own custom visualizations without having to rerun the simulations, especially if there are many long and complex simulations. The data can then be further processed and visualized as the user wishes.

3.2 Network Topography of Interactions Creation Tool

Numerous interactions are occurring between agents in a microbial environment. However, not every agent can and will interact with one another. Based on which agents interact with one another, a network topography can be created, capturing the dynamics of the interactions. Every node represents a unique agent, and each agent has their own intrinsic properties. This would include the starting population or concentration, reproduction rate, and death rate.

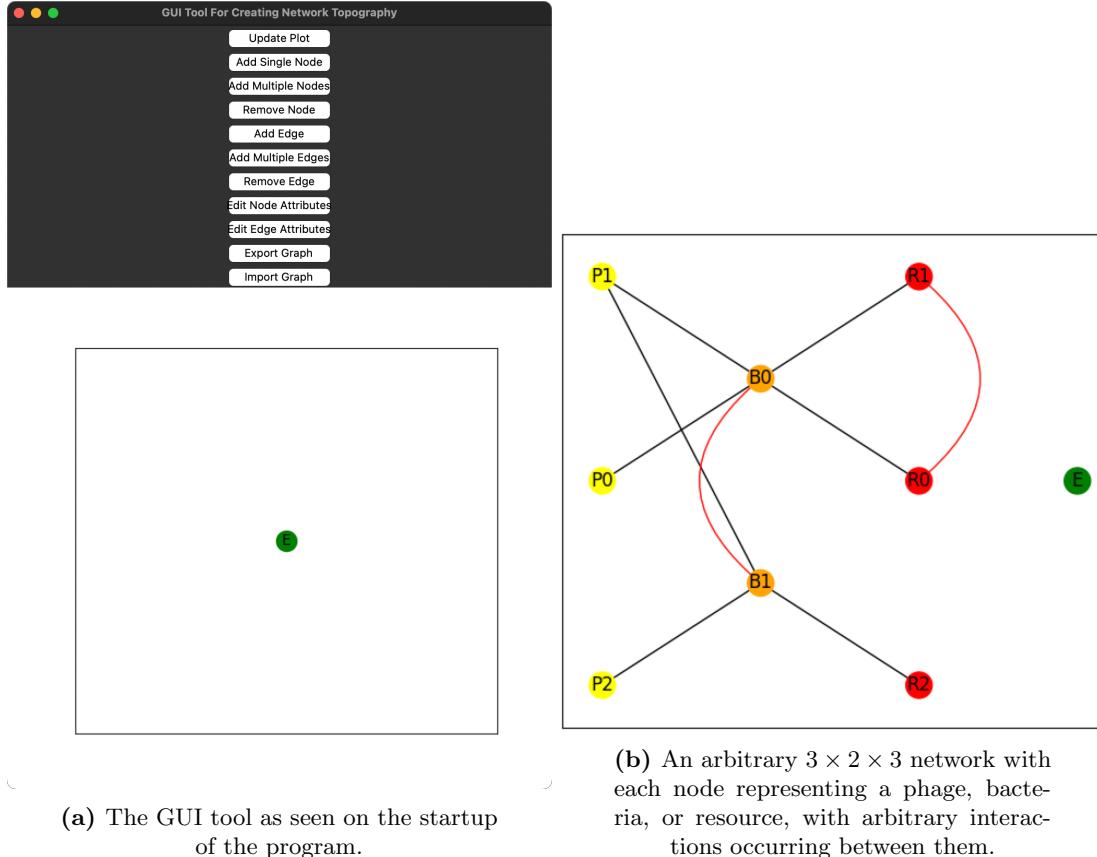
An edge links agents together if there is an arbitrary interaction occurring between two agents, with the properties exhibited in the interaction dependent on the interacting agents. Self interactions are allowed in the network. Large populations of bacteria can provide support to other bacteria and prevent phage infection. Each edge likewise also contains attributes to capture the unique dynamic interactions between the agents. This could be the probability for a successful interaction, the burst size of a specific phage-bacteria pair, or the bacteria's consumption rate of resources. Adding the attributes to the nodes and edges allow for the capture of various interaction dynamics within the context of the community.

A GUI tool has been developed using Python and NetworkX to help aid in the development of the exhibited network topography. With this tool, a network topography can be created by adding any number of phages, bacteria, and resources. There is an environment node that is used to store global environmental data, for example, the temperature of the system, the pH of the system, the wash-in/out rate, etc. The settings node holds information such as simulation length, max time step, and the type of ODE solver to use. The interactions and attributes of the agents, environment, and settings can easily be edited using the GUI tool.

[Figure 3.1a](#) shows the layout of the GUI tool built using Tkinter and NetworkX. [Figure 3.1b](#) shows an example network that can be created. There are numerous buttons that can be used to edit the graph, for example adding or removing nodes and edges. By default, an environment node holding parameters such as pH and temperature is added. A settings node is added as well, holding settings data to be used for the solver, like the type of solver or simulation length. Manually adding nodes and edges can get tedious and repetitive for large graphs, so the user can add multiple nodes and edges at the same time. Nothing can interact with the environment and setting node, as they are used to hold data about the environment and network solver. For each node and edge, default attribute names and values are added which can later be edited by the user. The user can alter the default attribute name and value by importing the GUI tool class and overriding the method implementation implementing the default names and values. The nature of the interaction needs to be defined and captured in the parameter names, values, and ODE equations.

3.3 Dashboard for Analysis and Visualization

The dashboard allows the user to interact with the network, the model, and some prebuilt visualizations, and is built into three logical sections. The first section allows for the user to edit the network parameters and setting values on the fly to quickly iterate through



different conditions and to fine-tune parameter selection without having to rebuild the network using the GUI tool. The second section allows for the user to see how the population count evolves over time for a given initial condition and parameter values, allowing to quickly test the network input. The final section allows for the user to run more advanced analyses on the network, for example, by changing multiple parameter values and visualizing the output.

3.3.1 Editing Network and Parameter Values

The editing network and parameter value contain five separate sections.

Initial Condition The initial condition settings panel ([Figure 3.2a](#)) allows for the user to edit the initial starting values of the agents. Each agent type has a table containing the initial population count. Extra hidden agents can be included. When a bacteria has been infected, the bacteria goes through multiple stages before lysing. Each bacteria agent starts out as uninfected, and once infected, the bacteria goes through 4 stages of infection before lysing as seen in [Figure 3.2a](#).

Vector Data Data that can be represented as a vector, for example the data attributed to an agent type have their own section, [Figure 3.2c](#).

Matrix Data Data that is stored as a matrix, the data stored on edges between agents, is stored in the matrix tab ([Figure 3.2b](#)).

Environment and settings The environment data and settings data also have their own tab, [Figure 3.2d](#) and [Figure 3.2e](#) respectively.

3.3.2 Advanced Visualization and Analysis

In the advanced analysis section, the user can run different analysis methods to gain a greater understanding of the model. The visualizations only support a $1 \times 1 \times 1$ model, in order to make the analysis easier for the user, and to make it easier to analyze the visualization. These advanced visualizations were created with the mind of understanding a simple network. There are five different analysis and visualization methods, and one system where the user can run a large simulation on the whole network and receive an output file containing the raw simulation file data. The raw data is stored as a *parquet* file, a tabular-like data format, which when combined with Dask (not Dash), allows for querying of the data similarly to Pandas. Parquet with Dask offers superior performance and data storage solutions that Pandas can't offer. Once queried, the user can create their own graphs and plots as they have access to the parameter values used and the raw simulation data.

3.3.2.1 Serial Transfer

Serial transfer is a method employed by bacteriologist where after a set amount of time, the bacteriologist pipettes a specified amount of media (for example 10ml of liquid) containing bacteria and resources, possibly with phages, and transfers the old media into a solution containing new media. At this stage, the bacteriologist can introduce new agents, or re-introduce agents if the agent population or concentration has died out. However, usually only resources are added during the transfer process. An example would be an experiment starts with 50ml of solution. The experiment runs for 24 hours before 5ml is removed. Researchers can run various tests, such as using optical density measurements to assess bacterial density in the solution or employing a mass spectrometer to determine the concentration of the resources. The 5ml is then re-added to a new solution of 45ml containing fresh resources. The effect that this has is it creates a sort

Resources

Initial Condition	Vector Data	Matrix Data	Environment Parameters	Settings
R0	R1	R2		
200	250	190		

Uninfected Bacteria

B0	B1	B2
40	50	55

Infected Bacteria

Row names: ['B0', 'B1', 'B2']

Infected B0	Infected B1	Infected B2	Infected B3
0	0	0	0
0	0	0	0
0	0	0	0

Phages

P0	P1
10	8

(a) The tab where the user can edit the initial conditions of the agents.

v_matrix

Row Names: ['B0', 'B1', 'B2']

R0	R1	R2
1	1.3	0
0	1.7	1.43
1.1	1.6	0.9

K_matrix

Row Names: ['B0', 'B1', 'B2']

R0	R1	R2
30	13	0
0	40	60
43	20	36

r_matrix

Row Names: ['P0', 'P1']

B0	B1	B2
0.05	0.09	0.04
0.01	0	0

B_matrix

Row Names: ['P0', 'P1']

B0	B1	B2
17	14	15
11	0	0

(b) The tab where the user can edit the matrix attribute values.

e_vector

R0	R1	R2
0.18	0.12	0.15

tau_vector

B0	B1	B2
0.7	0.92	1.2

(c) The tab where the user can edit the vector attribute values.

Environment Parameters

Initial Condition	Vector Data	Matrix Data	Environment Parameters	Settings
Temperature	pH	M	washout	
25	7	4	0	

(d) The tab where the user can edit the environment values.

Solver Type

RK45

t_eval option

Use your own t_eval (checked) with selecting t_start, simulation length, and number of steps, or the solver suggested t_values (unchecked)

Number timesteps for own t_eval

100

Minimum Step Size

0.01

Max Step Size

0.1

Cutoff value for small numbers

0.000001

Dense Output

Use Dense Output

Relative and Absolute Tolerance

0.001 | 0.000001

Simulation Start Time

0

Simulation Length Time

10

(e) The tab where a user can edit the settings of the solver and simulation.

Figure 3.2: The tabs where the user can edit the various parameter values and control the simulation parameters

of artificial stable point. As the bacteria grow, they consume the resources found in the solution. However eventually the resources run out, and the bacteria die out due to a lack of resources. By introducing new resources at set time intervals, the bacteria can regrow and exhibit a semi-stationary behavior.

The implementation of serial transfer is slightly different. A user can select a number which will divide the population count of the agents by that number (Figure 3.3a). Then the program takes the initial condition values defined for the resources the initial condition in Section 3.3.1 and adds those values to the resources respectively. By selecting a checkbox, the values as defined in the initial condition box for phages and bacteria in Section 3.3.1 can optionally be added as well. As an example, if at the end of a simulation, there are 120 resources, 5000 bacteria, and 1000 phages remaining and the chosen serial transfer value is 15, then the resource, bacteria, and phage values would be decreased to 8, 333.33, and 66.66 respectively. Then, if the initial condition for the resources, bacteria, and phages in Section 3.3.1 are 500, 80, and 10 respectively, and the checkbox is unchecked, the new population count will be 508, 333.33 and 66.66 respectively. If the checkbox is checked, the new population count will be 508, 413.33, and 76.66 respectively. These new values would be used as the new starting initial condition for a new simulation, and the run results will be appended to the previous run. As output, new graphs are created showing the runs appended to one another, with an example output shown in Figure 3.3b.

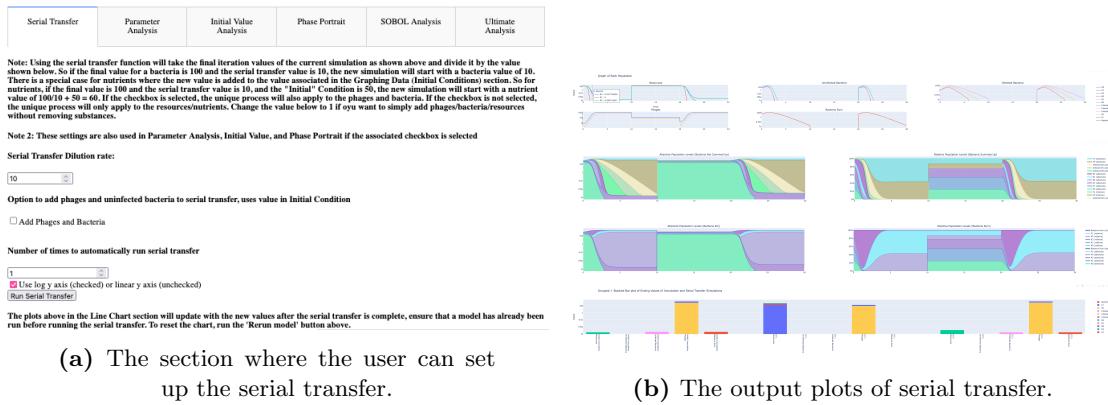


Figure 3.3: Serial Transfer

3.3.2.2 Parameter Analysis

The parameter analysis settings tab as shown in Figure 3.4a allows the user to choose two parameters and individually run the model with the varying input values. The values that can be tested and changed include all initial condition values, vector and matrix data, and environmental data. As input, the user can select 2 parameters of choice. After the parameter name selection, the user can manually choose which parameter values they want to test or test a range of values equally spaced by selecting the number of values to test. Finally, the user can optionally run a serial transfer, where the serial transfer uses the settings found on the Serial Transfer tab.

Figure 3.4b shows the heatmap that the user can expect, one heatmap for each agent type. Each heatmap has cells that unique model input, and contains the value of A heatmap matrix is created for each agent type, with dimension of the input values. Each box corresponds to each pair of parameter inputs, and shows the population count of the agent at the time selected on the slider. As the user slides the slider, the value inside the cell changes to correspond with the chosen time. Note that the heatmap color range resets for each heatmap, so similar colors across heatmaps will not correspond to the same values.

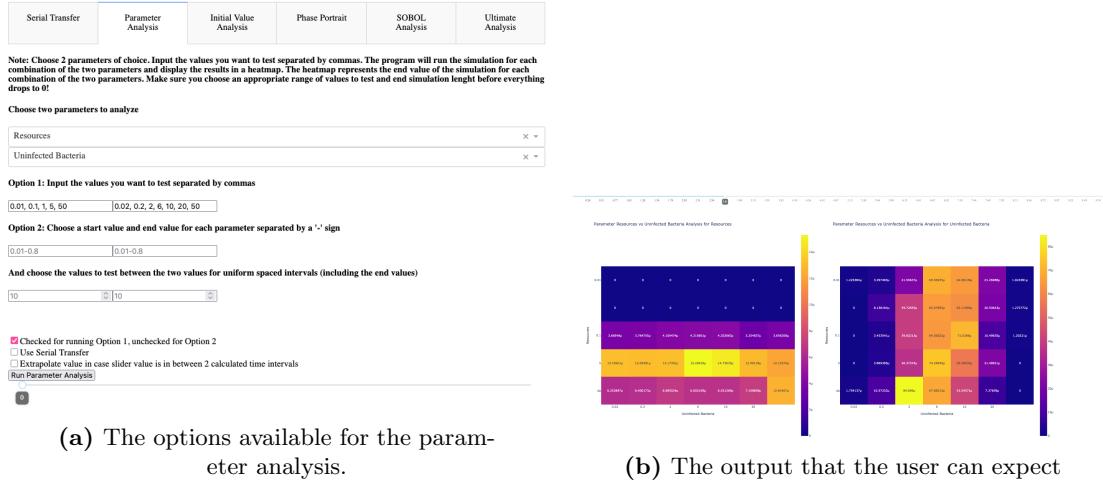


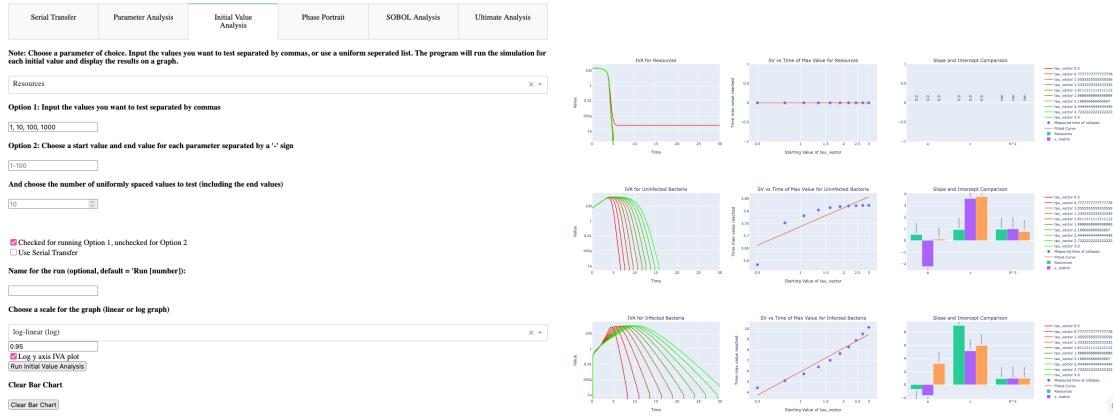
Figure 3.4: Parameter Analysis

3.3.2.3 Initial Value Analysis

The initial value analysis settings tab as shown in **Figure 3.5a** allows the user to choose a single parameter and vary the value of that parameter, visualizing how a change in parameter value affects the population count of the agents.

Figure 3.5b shows the plots that the user receives. For each agent type, there are three plots made. The left plot shows the population count through time, one line for each parameter value submitted. The middle plot takes each run and calculates the “percentage from the max value” (default value of 0.95 → 95%) reached of the peak. This value is considered the time of peak, and is used to fix some issues that can arise where the population plateaus or only keeps on rising. The initial value is plotted on the x-axis, with the time at which the max value is reached on the y-axis. Using the plotted data, a linear or log fit can be created. Using this data can be useful for understanding how a change in parameter value affects the time at which the population count reaches a maximum. The slope, intercept and R^2 value is stored and saved in the third plot, a bar chart, with an editable name. For every re-run of the initial value analysis, the

slope, intercept and R^2 value is stored in the bar chart, allowing comparison of the slope-intercept data across different parameters.



(a) The settings for the initial value analysis tab.

(b) An example initial value analysis output.

Figure 3.5: Initial value analysis

3.3.2.4 Phase Portrait

The phase portrait plot allows for the user to analyze how an agent population evolves with respect to the other agent population through time. Phase portraits indicate how one population increases while the other decreases, and vice versa. Steady states can be identified and classified as either stable, unstable, or as saddle points. By comparing different starting points, it is possible to see if the system is chaotic or not. The setup for the phase portrait can be seen in Figure 3.6a, and a sample output can be seen in Figure 3.6b.

3.3.2.5 SOBOL Analysis

SOBOL analysis, a variance-based sensitivity analysis, is a method that allows a user to quantify how important an input parameter has on a measured aspect of the output by changing the parameter values of the model and measuring the change in model output. SOBOL quantifies how much variance in the output can be attributed to a specific parameter and can measure the effect of global, first, and second order sensitivity. When a model is viewed as a black-box model, the model can be seen as a function $Y = f(X)$, where X is an input vector of d elements, and Y is a univariate model output. X is assumed to be independently and uniformly distributed within a hypercube $X_i \in [0, 1]$ for $i = 1, \dots, d$. The first order sensitivity measures the output variance of the main affect of parameter X_i . Measuring the effect of varying X_i averaged over other input

Serial Transfer	Parameter Analysis	Initial Value Analysis	Phase Portrait	SOBOL Analysis	Ultimate Analysis
-----------------	--------------------	------------------------	----------------	----------------	-------------------

Note: Choose 2 parameters of choice. The program will run a simulation and plot a phase portrait of the two parameters. The phase portrait will show the relationship between the two parameters over time.

Resources

Option 1: Input the values you want to test separated by commas

Option 2: Choose a start value and end value for each parameter separated by a '-' sign

Parameter 1:

Parameter 2:

Use option 1 (checked) or option 2 (unchecked)

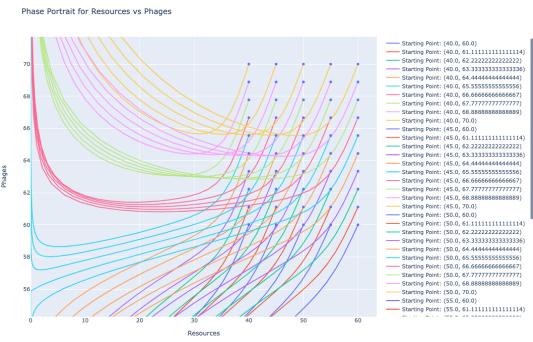
Log x graph

Log y graph

Use Serial Transfer

Run Phase Portrait

(a) The user can select two starting values for the initial condition, but they can't choose vector, matrix, or environment settings due to the plot showing the development of agent populations against other agent populations. As typical, the user can select their own values or auto-generate values between two values, as well as use a serial transfer option. There is also an option to take the logarithm of the x and/or y-axis.



(b) An example run of a phase portrait.

Figure 3.6: Phase Portrait

parameters, and standardized to provide a fractional contribution to the overall output variance. The first order sensitivity is described as

$$S_i = \frac{V_i}{Var(Y)}$$

where $V_i = Var_{X_i}(\mathbb{E}_{X_{\sim i}}[Y|X_i])$ and where $X_{\sim i}$ represents all the parameters that are not X_i .

The second order index measures the impact of input X_i interacting with X_j . For many inputs, this becomes unwieldy to analyze. The global sensitivity is used to analyze the global sensitivity without evaluating $2^d - 1$ indices, and measures the contribution to the output variance of X_i , including all variance due to X_i 's interaction with other variables.

$$S_{T_i} = \frac{\mathbb{E}_{X_{\sim i}}[Var_{X_i}(Y|X_{\sim i})]}{Var(Y)} = 1 - \frac{Var_{X_i}(\mathbb{E}_{X_i}[Y|X_{\sim i}])}{Var(Y)}$$

SOBOL can analyze various univariate outputs. This could be either the average value of an agent population, the variance in population count, the time at the peak of an agent count, the final population value, etc.

SOBOL accepts a list of parameter names and a list of range of values to sample from, which the user can input in the SOBOL settings tab, [Figure 3.7a](#). If no values are added, the parameter is not included in the simulation and the default value is instead used. The user then needs to select the number of samples to run, using the formula 2^x , where x is the number they input, and 2^x is the number of samples that SOBOL will create

and run. The larger x is, the more accurate the SOBOL analysis results will be, but the more simulations would need to be run.

If the user wants to analyze the second order interactions, then the model will run the system $N(2D + 2)$ times with the randomly sampled input values, where N is a multiple of 2, and D is the number of parameters being tested. Otherwise, if 2nd order is not chosen, the model is run $N(D + 2)$ times. Due to the randomness of the sampling method, the user can, but does not need to, submit a seed value.

Three SOBOL analyses are included by default in the dashboard, as shown in Figure 3.7b. An analysis of the final value of the simulation, the average population count, and the variance in population count. The global and first sensitivity are shown next to one another, and each sub-row within a plot represents each agent type. The proportion of the global and local sensitivity can be seen for each agent type and each parameter.

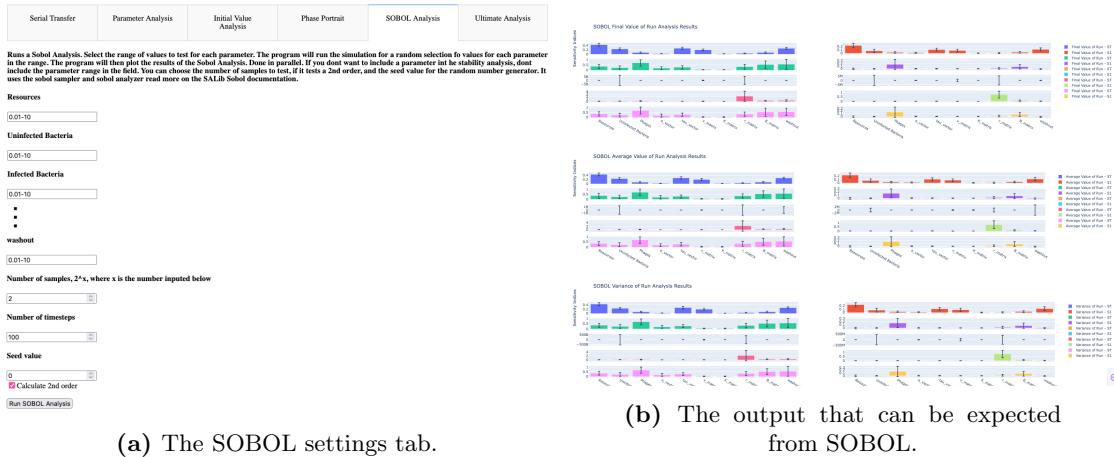


Figure 3.7: SOBOL variance analysis

3.3.2.6 Ultimate Analysis

The Ultimate Analysis section does not produce any visualizations or analysis, but instead allows for the user to define which initial conditions and parameter values they want to run a simulation on. The solver will iterate over every single parameter input possibility and save the results in a *.parquet* file. Similarly to the other sections, the user can specify a start and end value, along with the number of values to generate evenly spaced within that range, including both the start and end values.

Using Dask and the saved *.parquet* file, the user can query for specific runs, for example runs where a parameter value was greater than 0.05, and use the simulation data to create their own plots.

Serial Transfer	Parameter Analysis	Initial Value Analysis	Phase Portrait	SOBOL Analysis	Ultimate Analysis
-----------------	--------------------	------------------------	----------------	----------------	-------------------

Choose values you want to test for the ultimate analysis. The program runs the simulation for each combination of the parameters (so watch out for exponential explosion!). It overwrites all values in the associated vector/matrix. Then it saves a pickle file with the combinations, and other data, and saves a parquet file with the results of the full simulation (time and y values), without any processing to it. The system periodically updates the parquet file with the results of the simulation to prevent old data from using up ram. Read the documentation on Disk to load the data into your own program for later processing. Partitioning the data allows for faster querying on the data, so select a small subsection of data where you will want to do frequent queries on.

Option 1: Input the values you want to test separated by commas

Resources

Opt 1: your selected values	Opt 2: range of values	Opt 2: number of steps
<input checked="" type="checkbox"/> Use Opt 1 or 2		
<input checked="" type="checkbox"/> Include parameter in simulation		
<input type="checkbox"/> Partition data on this attribute		

Uninfected Bacteria

Opt 1: your selected values	Opt 2: range of values	Opt 2: number of steps
<input checked="" type="checkbox"/> Use Opt 1 or 2		
<input checked="" type="checkbox"/> Include parameter in simulation		
<input type="checkbox"/> Partition data on this attribute		

Infected Bacteria

Opt 1: your selected values	Opt 2: range of values	Opt 2: number of steps
<input checked="" type="checkbox"/> Use Opt 1 or 2		
<input checked="" type="checkbox"/> Include parameter in simulation		
<input type="checkbox"/> Partition data on this attribute		

▪

▪

▪

washout

Opt 1: your selected values	Opt 2: range of values	Opt 2: number of steps
<input checked="" type="checkbox"/> Use Opt 1 or 2		
<input checked="" type="checkbox"/> Include parameter in simulation		
<input type="checkbox"/> Partition data on this attribute		
<input type="button" value="Run Ultimate Analysis"/>		

Figure 3.8: The ultimate analysis setup tab.

3.3.2.7 Custom Advanced Analyses and Visualizations

As the dashboard can not create a graph for every situation, or analyze every situation, Ultimate Analysis (Section 3.3.2.6) can be used to run and download the simulation data to the disk to create later create your own custom visualizations. Depending on the used model, different behavior might appear, for example the population count can exhibit cyclic behavior. A custom visualization would then perform a Fourier transformation to obtain the predominant frequencies.

3.3.3 Interaction Network

A flowchart of the interactions between the user and systems can be seen in Chapter 10.

3.4 The Golden Model

In this report, the default model, called the “Golden model” [18] that will be used for all simulations is as follows:

$$\frac{dR}{dt} = -e \cdot g(R) \cdot (U + \sum_{i=1}^M I_M) \quad (3.1)$$

$$\frac{dU}{dt} = g(N) \cdot U - r \cdot U \cdot P \quad (3.2)$$

$$\frac{dI_1}{dt} = r \cdot U \cdot P - \frac{M}{\tau} \cdot I_1 \quad (3.3)$$

$$\frac{dI_k}{dt} = \frac{M}{\tau} (I_{k-1} - I_k) \text{ for } k = 2, \dots, M \quad (3.4)$$

$$\frac{dP}{dt} = \beta \cdot \frac{M}{\tau} \cdot I_M - r \cdot (U + \sum_{i=1}^M I_M) \cdot P \quad (3.5)$$

$$g(N) = \frac{v \cdot N}{N + K} \quad (3.6)$$

where N is resources, U is uninfected bacteria, $I_{1,\dots,M}$ is the infected stage of the bacteria, and P is the phage population.

The model describes three biological processes, cell consumption of resources and growing, phage/cell encounters and infection, and cell lysis. The cell growth process is described by $g(N)$, the instantaneous growth rate dependent on the Monod equation, where v is the maximal growth rate and K is the Monod constant. The consumption rate of a resource by a bacteria is e .

Once infected by a phage, the bacteria goes from U to I_1 . The bacteria goes through M stages of infection I_1, \dots, I_M before lysing, where the bacteria goes from state I_k to state I_{k+1} with equal transition rate $\frac{M}{\tau}$. The probability of a successful infection of a cell is r .

After a bacteria lyses after stage I_M , β phages are released, the burst size of the phage.

However this model is specifically designed for a $1 \times 1 \times 1$ model. In order to adapt this model to fit an $p \times b \times r$ model, the model needs to be adapted. There are other changes that can be made, to the model, for example by adding a washin rate ω^i , where resources are constantly being introduced, and a washout rate ω^o where phages, bacteria, and resources are being washed out.

3.4.1 The Adapted Golden Model

The adapted model accounts for the interactions of multiple agents.

$$\frac{dN_n}{dt} = - \sum_{b \in B} e_{b,n} \cdot g(N_n, b) \cdot (U_b + \sum_{i=1}^M I_{i_b}) + w_n^i - w^o \cdot N_n \quad (3.7)$$

$$\frac{dU_b}{dt} = U_b \cdot \sum_{b \in B} g(N_n, b) \cdot -U_b \cdot (\sum_{p \in P} r_{p,b} \cdot P_p) - w^o \cdot U_b \quad (3.8)$$

$$\frac{dI_{b_1}}{dt} = U_b \cdot (\sum_{p \in P} r_{p,b} \cdot P_p) - \frac{M}{\tau_b} \cdot I_{b_1} - w^o \cdot I_{b_1} \quad (3.9)$$

$$\frac{dI_{b_k}}{dt} = \frac{M}{\tau_b} (I_{b_{k-1}} - I_{b_k}) - w^o \cdot I_{b_k} \text{ for } k = 2, \dots, M \quad (3.10)$$

$$\frac{dP_p}{dt} = \beta_{p,b} \cdot \frac{M}{\tau_b} \cdot I_{b_M} - r_{p,b} \cdot (U_b + \sum_{i=1}^M I_{i_b}) \cdot P_p - w^o \cdot P_p \quad (3.11)$$

$$g(N_n, b) = \frac{v_{b,n} \cdot N_n}{N_n + K_{b,n}} \quad (3.12)$$

3.5 Software Used and Packages

The program was created exclusively in Python, and makes extensive usages of various packages, ranging from the standard scientific packages such as NumPy and SciPy to more niche packages such as pickle and SALib.

The graphical tool uses Tkinter acting as the front end, handling the user inputs, while NetworkX stores the graph and contains the attribute data. The GUI tool also uses Matplotlib to create the figure of the graph to display to the user in the GUI tool.

The simulation framework, the backend of the modelling, makes extensive usage of SciPy's *solve_ivp()* to create the ODE data. It also makes light usage of NetworkX to load the graph, as it initially takes a graph as an input, and light usage of NumPy to setup the parameters at startup.

The visualization part makes heavily usage of Dash and Plotly. Dash acts as the server and is used for displaying the HTML aspect of the frontend and dealing with any input and output. Upon choosing parameter values and clicking on "submit", Dash registers the activity and calls the function registered to the button, sending data such as parameter values and options like "log x-axis" form the frontend to the backend server. In the backend, the various inputs are handled, like changing the input string "0.05, 0.1, 0.15,

0.2” provided by the user into an iterable list [0.05, 0.1, 0.15, 0.2] that the simulation framework can iterate over to vary the parameter value. Then a call to the simulation solver is done.

If there are many simulations to run through, in the case of SOBOL ([3.3.2.5](#)) or ultimate analysis ([3.3.2.6](#)), then an intermediate call to a parallel computing library Joblib is called, where Joblib parallelizes the for-loop to compute the simulations in parallel. The ultimate analysis makes use of pandas to store the data as a dataframe to then be stored as a *.parquet* file. To effectively load the data saved from the ultimate analysis section, the user can use Dask to query and load large datasets into memory.

SOBOL makes use of the SALib library to sample and analyze the parameter input. Both the ultimate analysis and SOBOL also save a *.pickle* file containing a dictionary with the parameter values tested, and other important information regarding the simulation in question.

The initial value analysis visualization ([Section 3.3.2.3](#)) uses SciPy’s *curve_fit()* function to curve fit the points in the middle plot ([Figure 3.5b](#)).

Other packages that are used include Pandas, collections, copy, warnings, itertools, os, datetime, json, gc, and time.

Chapter 4

Experiments and results

Chapter 5

Discussion

Chapter 6

Conclusion and future work

6.1 Conclusion

6.2 Future Work

Next steps would be to give the model to the lab technicians running lab experiments so that they can verify the results as seen in the output by comparing the lab results with the model output. With the lab results, the model can be adapted to better fit the lab results. This can be done by changing parameter values, or by changing the model equation. The user can decide to add the Monod microbial growth model to the growth of the bacteria, or adapt the Monod equation to being dependent on multiple sources. Using the model, the technicians can improve and validate their methods. If the empirical results significantly deviate from the model results, the technician can review to see if their method is good. They might have accidentally not added enough resources, or accidentally miscalculated the initial concentration of bacteria.

6.2.1 Other Models

“All models are wrong, but some are useful” — George E. P. Box

This quote could not be more true for modelling phages and bacteria. There are numerous considerations to account for, and there are numerous ways to go about the considerations. Each model has its pros and cons. Take the exponential population

growth model

$$\frac{dP}{dt} = rP \quad (6.1)$$

$$P(t) = P_0 e^{rt} \quad (6.2)$$

where $P(t)$ is the population at time t , P_0 is the initial population, and r is the growth rate. This model acts as a nice introduction to population modelling. It can accurately fit the exponential growth bacteria experience in a petri dish. However, this basic model does not account for a spatial and resource consumption. Eventually the bacteria run out of space and resources, and start to die out. A population can not grow exponentially forever, the resources can only support a maximum population, the carrying capacity. The model can be adapted to include a carrying capacity (the max population level that can be reached), where the new updated model is

$$\frac{dP}{dt} = rP\left(1 - \frac{P}{K}\right) \quad (6.3)$$

$$P = \frac{K}{1 + \left(\frac{K-N_0}{N_0}\right)e^{-rt}} \quad (6.4)$$

where K is the carrying capacity. This adapted model, the logistic growth model better accounts for the eventual restriction of population growth.

[Figure 6.1](#) shows how the carrying capacity has a large influence on the speed and growth trajectory of a population. The logistic curve initially follows the exponential curve before the maximum growth rate is reached and starts to slow down and taper off as the population asymptotically approaches the carrying capacity $K = 200$.

A further step would be to introduce competition between other bacteria. For example, a $p_{0,1} \cdot P_0 \cdot P_1$ term can be subtracted from the logistic growth curve. This term accounts for competition between Populace 0 and Populace 1, with $p_{0,1}$ being the interaction factor between P_0 and P_1 . Assuming P_0 is being looked at and P_0 has a high value, if P_1 is high, then a lot of P_0 is going to die out due to the competition with P_1 . If P_1 has a low population, then not many P_0 are going to die out due to less competition with P_1 .

The model can be further extended by accounting for temperature, pH, more interactions between other agents, the constant addition and removal of other agents, and other considerations.

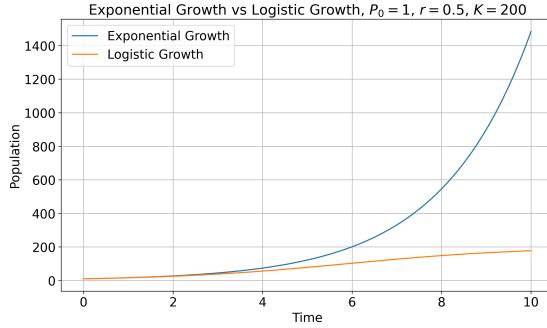


Figure 6.1: Exponential growth curve vs logistic growth

6.2.1.1 Spatial simulations

<https://www.sciencedirect.com/science/article/abs/pii/S0022519318305368> The ODE models work very nicely when there is no consideration for space and 2D/3D-space dimensionality. Spatial models complicate the simulation, making it harder to analyze. Data collection and analysis becomes harder. Unique and novel analysis and visualization methods have to be created to be able to represent and visualize the data through space and time.

PDE PDE are the next logical step to add space to an ODE model. The general formula, as given by

$$\frac{\partial u}{\partial t} = D \nabla^2 u + f(u, x, y, \dots, t)$$

where $u(x, y, \dots, t)$ is the population density of interest, D is the diffusion constant, ∇^2 is the derivative of each spatial direction, and $f(x, y, \dots, t)$ is the function encapsulating growth, death, and interactions dynamics.

Discretization The dimensions can be discretized into boxes of dimensions $\delta x, \delta y, \dots$. This transforms the PDE into a system of difference equations, which can be solved numerically. For example, the Laplacian term $\nabla^2 u$ in 2D can be approximated using finite differences as:

$$\nabla^2 u \approx \frac{u_{i+1,j} - 2u_{i,j} + u_{i-1,j}}{\delta x^2} + \frac{u_{i,j+1} - 2u_{i,j} + u_{i,j-1}}{\delta y^2}$$

where $u_{i,j}$ represents the value of u at the grid point (i, j) . This discretization allows the PDE to be solved iteratively over a grid, enabling spatial simulations of population dynamics. Each box can be represented by a matrix, and the population value can be displayed as a heatmap using visualization software.

Chapter 7

Ethics and Data Management

A new requirement for the thesis is that there must be a short section in which you reflect on the ethical aspects of your project. This requirement is related to one of the final objectives that a graduated student of the Master of Computational Science must meet: “The graduate of the program has insight into the social significance of Computational Science and the responsibilities of experts in this field within science and in society”. You don’t need to devote an entire chapter to this; a short section or paragraph is sufficient.

I acknowledge that the thesis adheres to the ethical code (<https://student.uva.nl/en/topics/ethics-in-research>) and research data management policies (<https://rdm.uva.nl/en>) of UvA and IvlI.

The following table lists the data used in this thesis (including source codes). I confirm that the list is complete and the listed data are sufficient to reproduce the results of the thesis. If a prohibitive non-disclosure agreement is in effect at the time of submission “NDA” is written under ”Availability” and ”License” for the concerned data items.

Short description (max. 10 words)	Availability (e.g., URL, DOI)	License (e.g., MIT, GPL, Creative Commons)
Example dataset 1	<github url>or Figshare	GPL
Example source code	DOI (from Zenodo)	MIT
Example sensitive data	NDA	NDA

Chapter 8

Appendix A: Equation Parameters

Parameters used in equations.

Golden Model		
Variable	Name	Description
P_p	Phages agent	Phage population for phage p
U_b	Uninfected Bacteria agent	Uninfected population for bacteria b
I_{b_i}	Infected Bacteria agent	Infected population for bacteria b at stage $1, \dots, i, \dots, M$
B_b	Bacteria agent	Total bacteria population for bacteria b , assuming $B_b = U_b + \sum_{i=1}^M I_{b_i}$
R_r	Resource agent	Resource r concentration
$e_{b,r}$	Consumption rate	
$\beta_{p,b}$	Burst size	Lytic burst size for phage p and bacteria b
$r_{p,b}$	Successful phage/cell encounter	Probability of a successful bacteria b infection from phage p
τ_b	Latent period	Time it takes bacteria b to go through one infection stage
$v_{b,n}$	Maximal growth rate	Growth rate of bacteria b from resource r
$K_{b,n}$	Monod Constant	Monod constant for resource consumption rate dependent on resource r concentration
ω_r^i	wash-in rate	Rate of resources r being added
ω^o	wash-out rate	Rate of agents being removed, acts on all agents equally
M	Number of infection stages	Number of infection stages that a bacteria goes through, constant for all bacteria agents
t	time	time value

SOBOL		
Variable	Name	Description
Y	Univariate parameter output	univariate model output, such as mean μ or variance σ
X	Input vector	Vector of size d , input vector to f
X_i	Parameter input	Value of vector X at position $i = 1, \dots, d$
d	Input size	Size of input vector X
$X_{\sim i}$	Parameter input	All values of X that are not X_i
f	Function f	Arbitrary black-box function describing model
N	Samples	Number of samples, power of 2, 2^x
D	Parameter input size	Number of parameters inputted into SOBOL, d
S_{T_i}	Global sensitivity	Contribution of X_i to output variance of Y due to interactions with other variables
S_i	First order sensitivity	Contribution of X_i to output variance of Y

Linear Regression		
Variable	Name	Description
a	slope of linear regression line	
c	Intercept of linear regression line	
R^2	Coefficient of determination of linear regression fit, quality of regression	

Table 8.1: Model parameters with variables, names, and descriptions. Subscripts on parameters indicate relationships; for example, $e_{b,r}$ is nonzero if there is an edge connecting bacteria b to resource r in the network, zero otherwise.

Chapter 9

Appendix B: Industrial and Real Life Applications of Phages

Due to the nature of killing bacteria, there are numerous applications where a researcher or an organization might be interested in controlling bacterial populations.

A Food Safety Specialist might be interested in introducing a solution containing a high concentration of phages during food production to prevent the spread and growth of *Salmonella* or *E. coli* in the pet food. Alternatively, the Food Safety Specialist might want to promote beneficial bacteria like *Streptococcus thermophilus* used in the production of Emmental cheese, which heat would kill when the milk undergoes the pasteurization process.

A doctor might be interested in providing swallowable pills, more commonly known as phage cocktails, to a patient with a bacterial infection. There is evidence that phage-resistant bacteria are more susceptible to antibiotics, so the doctor might prescribe both medicines to effectively deal with the infection.

An Environmental Protection Officer might be interested to see how they can use phages to stop the spread of *Cyanobacteria* blooms in waterways, more commonly known as blue-green algae, a photosynthetic microscopic organism that is technically a type of bacteria. This would keep waterways safe for boating and swimming activity, aquatic life, and water consumption in farms, factories, and homes.

When there are a few known bacterial strains, a targeted concoction of phages can be used to control the bacterial population growth in any setting, either be it food, healthcare, or environmental. Phages offer properties of microbial control that other methods do not, making them an ideal candidate for some applications.

9.1 Controlling Foodborne Bacteria

Foodborne diseases are one of the primary ways for bacteria to spread to humans and animals. Some bacteria use the food as a vector to infect hosts, while some bacteria will deposit toxins on the food that is then ingested. If consumed in large enough quantities, or further produced in the host, the toxins can be fatal to the host.

Methods exist to control bacterial growth, for example by storing food below 5°C or above 60°C. Bacteria need moisture to grow, so starches like rice will have minimal bacterial growth. Bacteria prefer to live in slightly acidic to neutral pH environments, so having an environment that is extremely acidic like vinegar will prevent bacterial growth. The use of chemical antibacterial agents such as bleach is not desirable due to leaving chemicals on the food, which can be fatal if ingested. Physical agents like heat or radiation can kill bacteria, but at the cost of altering the food quality [46].

For example, *Streptococcus thermophilus* is one of three different bacteria strains used to create Emmental cheese. However, Emmental cheese does not use pasteurized milk, increasing the risk of *E. coli*. Emmental cheese producers can add phages that target *E. coli* to the milk during the production stage, while not affecting the bacteria used to produce the cheese.

9.1.1 Current Applications

Phage cocktails like SalmoFresh™ have been proven to safely reduce *Salmonella* contamination in pet food and raw pet food ingredients [7], as well as in romaine lettuce and bean sprouts [8]. Pet food contains meat and vegetables, where vegetables grown in or on the ground are at risk of *Salmonella* due to contact with soil, manure, compost, and other agricultural runoff from neighboring farms [14]. Figure 9.1 [7] and Figure 9.2 [8] show how applications of phages have reduced the count of *Salmonella* in ingredients used in pet food as well as romaine lettuce and bean sprouts. In Figure 9.1, each food group noticed at least a 68% reduction in CFU/g compared to the control when the 9×10^6 phage treatment was applied. There was at least an 80% reduction in CFU/g across all food groups when treated with a 9×10^6 or stronger phage solution. In Figure 9.2, the lettuce and bean sprouts noticed a reduction of at least 0.6 log CFU/mL in *Salmonella* count across all temperature ranges. The smallest reduction in bacteria count in lettuce was noticed at 1 hour at 2°C with an absolute reduction in 62.0% between the control and treatment, while the largest reduction in bacteria of 90.0% was found at 72 hours at 2°C. For the bean sprouts, the lowest reduction in phages was found

at 1 hour at 2°C with a reduction of 78.1%, and the largest reduction was 90.0% at 25°C after 48 hours. Although these values are still high above food safe, the ability to reduce the *Salmonella* population by at least 62% and up to 90% at different temperatures and incubation periods is impressive and can prolong shelf life, especially for foods that do not have long shelf lives before spoiling due to bacteria. As such, phages can be shown to control the spread of *Salmonella* in food sources and extend the potential shelf life of certain foods.

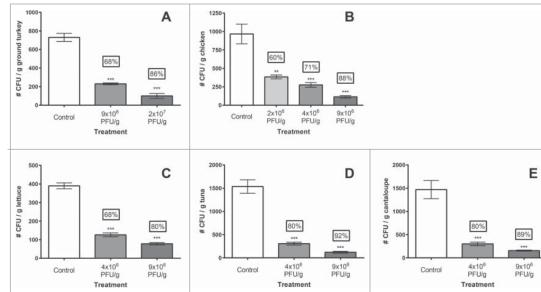


Figure 9.1: SalmoLyse® reduces *Salmonella* contamination on various food surfaces: Mean and standard error bars shown. Statistical analyses were carried out for each food group independently. Asterisks denote significant reduction from corresponding controls based on one-way ANOVA with Tukey's post-hoc tests for multiple corrections: ** denotes $p < 0.01$, while *** denotes $p < 0.001$ compared to the corresponding controls. There was significant reduction in *Salmonella* on all food surfaces with the addition of SalmoLyse® compared to the controls; the mean percent reductions from the control are noted in the boxes above treatment bars. CFU/g D colony forming units per gram. Each letter denotes a food group that was tested with SalmoLyse® and compared to a control: A= chicken; B= lettuce; C= tuna; D= cantaloupe; E= ground turkey [7].

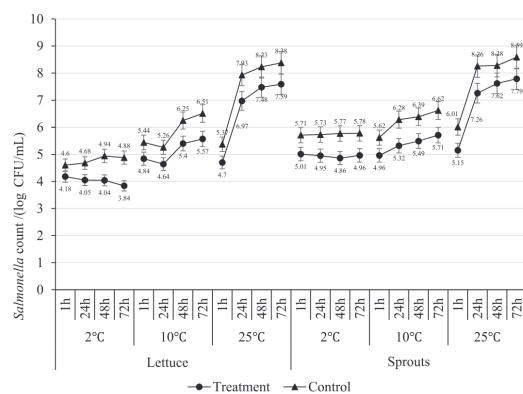


Figure 9.2: *Salmonella* count in a mixture of 5 *Salmonella* strains spot-inoculated (CFU/g) onto a) lettuce and b) sprouts after spraying with a mixture of bacteriophage (SalmoFresh™) relative to positive controls at 2, 10 and 25°C and stored for 1, 24, 48 and 72 h. [8]

9.2 Phage Therapy and Antibiotics

Antibiotics are a common way to treat bacterial infections. However, antibiotics are not selective in the bacteria they kill, killing both harmful and beneficial bacteria. This can lead to the development of antibiotic-resistant bacteria, which makes it harder to combat that bacteria in the future. It has also been shown that antibiotics have a negative effect on the gut microbiome and brain development in mice. Phages are an alternative to antibiotics, as they are selective in the bacteria they kill and do not interact with cells or other important biological functions. The rise in antibiotic resistant bacteria can be attributed to the overuse and over-prescription of antibiotics and incorrect usage of antibiotics (for example prematurely stopping) [10]. These actions provide an evolutionary pressure on bacteria to mutate and gain resistance to the antibiotics. The phage therapy can contain any number of different phages that can target specific bacterial infections such as *Streptococcus pneumoniae* with minimal risk of side effects.

9.2.1 Current Applications: Bacterial Infection Control

One active area of research is the use of phages to control bacterial infections. Due to the specificity of phages, they can be used to target specific bacteria strains without affecting other beneficial bacteria. When sick with a bacterial infection, patients swallow antibiotic pills to help the body fight the infection. Antibiotics work by either interrupting intercellular processes like the synthesis of RNA [47], by disrupting the structural integrity of the cell wall [48], or by inhibiting protein synthesis [49].

However, antibiotics are not strain specific and indiscriminately kill gut and other bacteria. Common side effects of antibiotics, although usually not serious, include diarrhea, nausea, and headaches. It has also been shown that the effects of early-stage penicillin exposure in mice has found to have a long-lasting effect on the gut microbiome, frontal cortex gene expression, and amygdala gene expression [11]. Penicillin increases cytokine expression (small proteins used in cell signaling) in the frontal cortex of the brain, modifies the blood-brain barrier integrity, and alters behavior. The mice exhibited an increase in aggression and anxiety-like behavior [50]. Phages can be used as an alternative to antibiotics without the side effects and without affecting the gut biome.

With an increase in antibiotic usage, there has been an increase in antibiotic-resistant bacteria. The World Health Organization has stated that antibiotic resistance threatens the modern medicine and the sustainability of an effective, global public health response to the enduring threat from infectious diseases. Common infections, that previously would have been easy to treat, are harder to treat, and can increase the risk of disease

spread, severe illness, and death [51].

One area of research is exploring how bacteria can exchange traits such as phage resistance and antibiotic resistance. Some bacteria are multi-drug resistant, and don't react with the medicine anymore.

Nana Nguefang Laure et al. showed evidence that *Salmonella Typhimurium* is more susceptible to ampicillin in the presence of phages, and phage-resistance can lead to reduced virulence and decreased antibiotic resistance [12].

Yuanyang Zhao et al. showed that there exists an antagonist coevolution between the bacteria and phages, where the dynamics changed from an arms race dynamic (ARD) to a fluctuating selection dynamics (FSD). Due to phage selection and bacterial competition pressure, when the bacteria gained phage resistance, it lost antibiotic resistance. A genome analysis revealed mutations in the btuB gene of *Salmonella anatum*, with q higher mutation frequency in the ARD stage. A knockout experiment confirmed that the btuB gene is a receptor for the JNwz02 phage and resulted in reduced bacterial competitiveness. Further analysis detected multiple single nucleotide polymorphism (SNP) mutations in the phage-resistant strains. The SNPs potentially affected the membrane components, partially weakening the cell defense against antibiotics. These findings help advance our understanding of phage-host-antibiotics interactions and the impact of adaptations to antibiotic resistance. The research shows how phages can be used to re-introduce antibiotic susceptibility to previous insusceptible bacteria, preventing costly and lengthy research in new antibiotics [13].

Phage research is facing challenges due to bacterial strains evolving resistance to phages. Understanding the interplay between antibiotics and phages is essential for shaping future research [13].

9.3 Environmental Protection

Algae blooms, also called red tides, is the rapid spread of bacterial or algae organisms. Blooms are a growing environmental concern impacting water quality, aquatic ecosystems, and human health. These rapid increases in algae populations, often fueled by excess resources like nitrogen and phosphorus, can occur in freshwater, coastal, and marine environment.

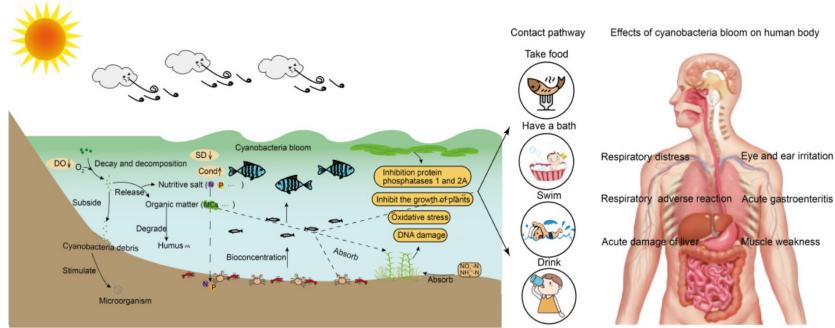


Figure 9.3: Cyanobacteria degradation cycle, main hazards of cyanobacteria bloom to water bodies, aquatic organisms, and the human body. (DO: dissolved oxygen; SD: water transparency; Cond: conductivity; N: nitrogen; P: phosphorus; MCs: microcystins).

[9]

Cyanobacteria blooms have major effects on the aquatic environment as well as human health. Cyanobacteria release nitrogen and phosphorous, which the bacteria use to grow with oxygen, outpacing other aquatic growth, and killing aquatic marine life. Toxins can make their way into the food and water consumed by humans, causing muscle fatigue, respiratory issues, liver damage, and gastrointestinal issues [9]. Figure 9.3 shows the process of how cyanobacteria degrade and are absorbed into the environment, eventually making their way into the human body via various contact points.

9.3.1 Current Applications

There is interest in using phages to control cyanobacteria blooms. Phages can offer better and safer options than chemical options when trying to control bacterial blooms. Chemical options are indiscriminate, killing cyanobacteria, while also killing other beneficial bacteria and aquatic life, and can eventually seep into groundwater. Although not used to control bacteria blooms, some chemicals like PFAS, also called “Forever Chemicals”, can last a long time in the environment and don’t degrade and keep on negatively affecting the environment. Due to the specificity of phages, only the cyanobacteria will be targeted, and will not affect the surrounding environment.

Tucker and Pollard found that an isolated phage cocktail collected from Lake Baroon in Australia could decrease the abundance of *M. aeruginosa* by 95% within 6 days in a lab setting, before recovering within 3 weeks time [16].

There is evidence that phage-resistant bacteria can influence the population dynamics of other bacteria. It has been shown that the plankton level has been experimentally affected by the frequency of the phage-resistant *Nodularia* marine bacteria. Populations with high phage resistance (> 50%) dominate the plankton communities despite

a high phage count and eventually out compete other bacteria due to their slower loss in population count. Contrastingly, populations of bacteria with low phage resistance (between 0% and 5%) were lysed to extinction, releasing resources like nitrogen. This allows for other bacterial strains to absorb the resources and dominate the bacterial community. Phages and the lysis of bacterial strains can have a dramatic effect on community dynamics and composition of other agents like phages, bacteria, and resources [15]. Phages have the potential to be used as a highly specific strategy for the control of cyanobacterial blooms, with minimal effects to the environment, and offer control of bacterial blooms, with limited impact to the environment. Usage should be relatively safe, novel, efficient, and sensitive.

However, there are issues with using phages to control bacterial blooms. Bacterial blooms can cover vast areas, or be in areas that would be hard to reach like marshlands, applying phages to combat the bloom might be infeasible. If the method of choice was to spray a solution of water containing phages, the solution needs to be shipped to the site and loaded onto special boats to spray the solution into the water, or the trucks need to drive along the shore and spray the solution into the water.

The phage density in the solution will have to be relatively high to quickly combat the bloom. These problems provide major logistical problems with creating the phages in a lab or factory, transporting the phages, and finally the administration of the phages to the waterways. Phages can only diffuse through the water, and can't actively swim, so they are dependent on the rate of diffusion and water currents. This will be difficult in marshlands, where the bacteria can "hide" in the grass and crevices created by aquatic life. If the bloom is in a high current area, like in a river or a bay, the water can wash the phages away.

Scientists have not yet fully understood the phage infection mechanism, and research into the artificial engineering of phages is limited, making it challenging to conduct studies in this area [52?].

Algae can produce toxins that threaten wildlife, contaminate drinking water, and disrupt local economies dependent on fishing and tourism. In the state of Florida, between the years 1995 and 2000, the restaurant and hotel industry lost an estimated \$6.5 million to algae blooms. This accounts for about 25% of the average total monthly sales revenue in the region from June through October, the months that are most commonly affected by red tide[53]. During a red bloom event, hospital diagnoses in the county of Sarasota for pneumonia, gastrointestinal, and respiratory illness increased by 19%, 40% and 54% respectively [54, 55], with a respiratory illness visit costing between \$0.5 and \$4 million [56].

Chapter 10

Appendix C: Flowchart of User and System Interactions

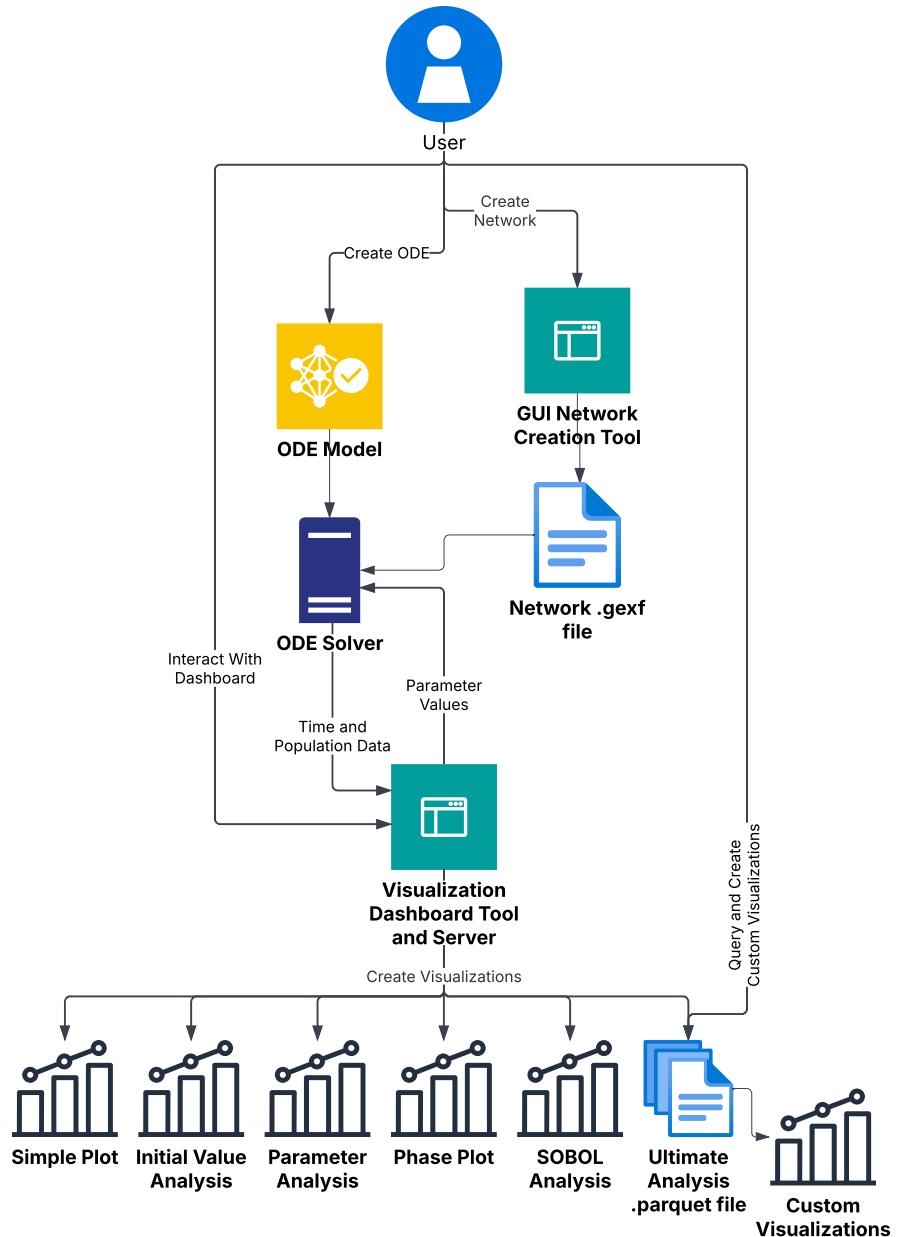


Figure 10.1: The interaction diagram of the user interacting with the system, provided input and output for subsystems, and the systems working with one another. To read the flow chart, start from the top to the bottom. First the user creates a network using the GUI Network Creation Tool. After the graph is finished, the user provides an implementation of the network as an ODE model, using Python. Once finished, the user provides the network file and ODE model to the ODE solver. The solver uses information from the network file to determine the number of agents to create, parameter details (including names, values, and dimensions), and setting values. Then the user interacts with the Visualization Dashboard Tool, for example by clicking on buttons to run simulations, changing parameter values, (un)selecting checkboxes, and zooming in and out of plots, and hovering over plots to show data. Once a user has selected the parameter values, the parameter values are sent to the solver. The solver calculates the time and population values using the provided graph and ODE model and sends the data back to the Visualization Dashboard Tool, which then outputs the visualizations. If the user has run an ultimate analysis, then the user can query the saved data to make their own custom visualizations.

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