Some Monetary Doctrines

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The Messages

1. A complete specification of macro policy is necessary for determination of equilibrium
2. Complete specification includes enough information about policy behavior that agents can form expectations of the entire future paths of policy instruments

Which Kind of equilibria are we getting

3. Monetary and fiscal policies *must* interact in certain ways in any equilibrium
4. Every statement about monetary policy effects is conditional on maintained assumptions about fiscal policy behavior
5. And vice versa

The Model

- Draws on "Monetary Doctrines" in Ljungqvist-Sargent
- Shopping time monetary model
  - constant endowment, $y > 0$
  - no uncertainty
  - steady-state analysis
  - lump-sum taxes/transfers
- How money gets valued unimportant to results (Valuing money real)
- Aggregate resource constraint

$$c_t + g_t = y \tag{1}$$

- Preferences

$$\sum_{t=0}^{\infty} \beta^t u(c_t, l_t), 0 < \beta < 1 \tag{2}$$

$$u_c, u_l > 0; u_{cc}, u_{ll} < 0, u_{cl} \geq 0$$

Shopping Technology

- Households must spend time shopping, s_t, to acquire consumption goods, c_t
- Shopping/transactions technology

$$s_t = H\left(c_t, \frac{m_t}{p_t}\right) \tag{3}$$

m_t/p_t real money balances chosen at t

H convex: $H, H_c, H_{cc}, H_{\frac{m}{p}\frac{m}{p}} \geq 0, H_{\frac{m}{p}}, H_{c,\frac{m}{p}} \leq 0$

- Example: Baumol-Tobin

$$H\left(c_t, \frac{m_t}{p_t}\right) = \frac{c_t}{m_t/p_t}\varepsilon$$

$\varepsilon > 0$: time cost per trip to the bank

Other Constraints

- Time constraint
$$l_t + s_t = 1 \tag{4}$$

- Household budget constraint
$$c_t + \frac{b_t}{R_t} + \frac{m_t}{p_t} = y - \tau_t + b_{t-1} + \frac{m_{t-1}}{p_t} \tag{5}$$

  b: 1-period indexed bonds; p: price level; τ: lump-sum tax
- Maximize (2) s.t. (3), (4), (5)
- Note that
  - $m_t \geq 0$ (HH cannot issue currency)
  - $b_t \lesseqgtr 0$ (HH can borrow or lend)
- Multipliers: λ_t for (5), μ_t for (4)
  - write (4) as: $l_t + H(c_t, m_t/p_t) = 1$

Optimality Conditions

- FOC for m_t/p_t is: $\lambda_t = \beta \lambda_{t+1} p_t/p_{t+1} - \mu_t H_{m/p}(t)$
- Let $R_{mt} \equiv p_t/p_{t+1}$, the return on fiat currency
- Arbitrage between m and b

$$1 - \frac{R_{mt}}{R_t} \geq -\frac{\mu_t}{\lambda_t} H_{\frac{m}{p}}(t) \geq 0$$

$$1 - \frac{R_{mt}}{R_t} = \frac{i_t}{1 + i_t} \geq 0 \qquad (6)$$

- (6) leads to the key result that nominal interest rates are non-negative:
  because $R_{mt} \leq R_t$ (currency is dominated in rate of return)

$$i_t \geq 0$$

Optimality Conditions

- Consumption-leisure tradeoff implies

$$\lambda_t = u_c(t) - u_l(t)H_c(t) \tag{7}$$

- From the FOC for b_t, return on bonds can be expressed as

$$R_t = \frac{1}{\beta}\left[\frac{u_c(t) - u_l(t)H_c(t)}{u_c(t+1) - u_l(t+1)H_c(t+1)}\right] \tag{8}$$

- (6) yields

$$\left(\frac{R_t - R_{mt}}{R_t}\right)\lambda_t = -\mu_t H_{\frac{m}{p}}(t) \tag{9}$$

Money Demand

- Combining FOCs [(7),(8),(9)] yields the implicit money demand

$$\left(1 - \frac{R_{mt}}{R_t}\right)\left[\frac{u_c(t)}{u_l(t)} - H_c(t)\right] + H_{\frac{m}{p}}(t) = 0$$

- Evaluate $u_c(t), u_l(t)$ at $l_t = 1 - H(c_t, m_t/p_t)$ to get the implicitly defined money demand function

$$\frac{m_t}{p_t} = F\left(c_t, \frac{R_{mt}}{R_t}\right) = F(c_t, i_t) \tag{10}$$

- Straightforward to show in (10) that $F_c > 0, F_i < 0$

Government & Equilibrium

- Government finances $\{g_t\}$ s.t.

$$g_t = \tau_t + \frac{B_t}{R_t} - B_{t-1} + \frac{M_t - M_{t-1}}{p_t} \tag{11}$$

- A **price system** is a pair of positive sequences $\{R_t, p_t\}_{t=0}^{\infty}$

- Take as exogenous $\{g_t, \tau_t\}_{t=0}^{\infty}$ and $B_{-1} = b_{-1}$, $M_{-1} = m_{-1} > 0$.
  An **equilibrium** is a price system, and sequences $\{c_t, B_t, M_t\}_{t=0}^{\infty}$ such that
  - the household's optimum problem is solved with $b_t = B_t, m_t = M_t$
  - the government's budget constraint is satisfied
  - $c_t + g_t = y$

Policy Experiments

- Need a complete specification of policy
- Will give definite meaning to concepts of
  - "short run": initial date
  - "long run": stationary equilibrium
- Assume

$$
\begin{aligned}
g_t &= g \qquad t \geq 0 \\
\tau_t &= \tau \qquad t \geq 1 \\
B_t &= B \qquad t \geq 0
\end{aligned}
$$

  We permit $\tau_0 \neq \tau, B_{-1} \neq B$
- Economy in stationary eqm for $t \geq 1$ but starts from a different position at $t = 0$
- Reduces dynamics to 2 periods: now $(t = 0)$ & future $(t \geq 1)$

Stationary Equilibrium

- Seek an equilibrium with

$$
\left.\begin{array}{rcll}
p_t/p_{t+1} & = & R_m & t \geq 0 \\
R_t & = & R & t \geq 0 \\
c_t & = & c & t \geq 0
\end{array}\right\}
$$

  which imply that

$$
\begin{array}{rcl}
R & = & \beta^{-1} \\
\dfrac{m_t}{p_t} & = & F(c, R_m/R) = f(R_m), \qquad f' > 0
\end{array}
$$

Two Equilibrium Conditions

1. Impose eqm on government budget constraint at $t \geq 1$

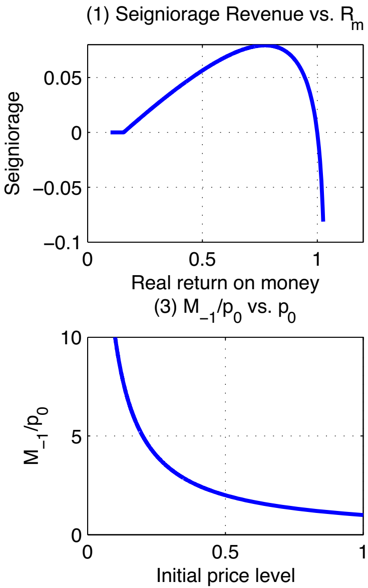
$$g - \tau + \frac{B(R-1)}{R} = f(R_m)(1 - R_m) \qquad \text{(Future)}$$

2. Impose eqm on government budget constraint at $t = 0$

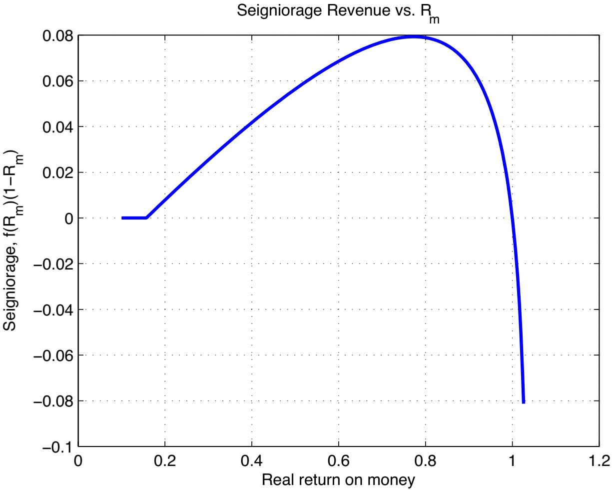
$$\frac{M_{-1}}{p_0} = f(R_m) - (g + B_{-1} - \tau_0) + \frac{B}{R} \qquad \text{(Current)}$$

- Given (g, τ, B), (Future) $\Rightarrow R_m$—inflation rate
- Given (g, τ_0, B) & initial conditions (M_{-1}, B_{-1}), (Current) $\Rightarrow p_0$—initial price level
- Have completely determined eqm $\{p_t\}_{t=0}^{\infty}$
- Now consider alternative policies and how they affect price-level determination

Deriving Equilibria Graphically

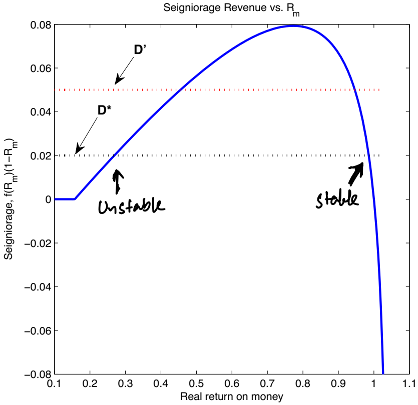


1. Sustained Deficits Cause Inflation



Let $D = g - \tau + \frac{B(R-1)}{R}$ and consider $D' > D^*$

1. Sustained Deficits Cause Inflation



"normal" side: $D' > D^* \Rightarrow R'_m < R^*_m$ (classical doctrine)

2. Zero Inflation Policy

- $\pi = 0 \Rightarrow R_m = 1 \Rightarrow$ seigniorage $= 0$
- (Future) $\Rightarrow$

$$g - \tau + \frac{B(R-1)}{R} = 0$$

or

$$\frac{B}{R} = \frac{\tau - g}{R-1} = \sum_{t=1}^{\infty} R^{-t}(\tau - g)$$

- Real value of interest bearing government debt $=$ present value of net-of-interest primary surpluses
- Of course, this generalizes to any fixed inflation rate policy (e.g., inflation targeting)
- It is strange—and troubling—that *no* country that adopted inflation targeting simultaneously adopted fiscal policies that are consistent with it

3. Unpleasant Monetarist Arithmetic

- A little history—US FP in early 1980s
- Consider an open-market sale of bonds at $t = 0$, $-d(M_0/p_0) = dB_0 > 0$
- *Hold fiscal policy*—(g, τ_0, τ)—*fixed*
- OM sale raises B in eqm conditions (Current) & (Future)
- Higher debt service in the future, but FP fixed
- Future seigniorage must rise: $f(R_m)(1 - R_m)$ rises by $\frac{R-1}{R} dB$
- Stationary π rises (R_m falls) unambiguously

3. Unpleasant Monetarist Arithmetic

$$\frac{M_{-1}}{p_0} = f(R_m) - (g + B_{-1} - \tau_0) + \frac{B}{R} \qquad \text{(Current)}$$

- By (Current), effect on p_0 can be *anything*
  - if $f'(R_m)$ small, p_0 falls (usual result)
  - if $f'(R_m)$ large, p_0 *rises* (extreme unpleasantness)
- Tighter money via OMO—at best—temporarily lowers p but at the cost of permanently raising π

4. Quantity Theory of Money

- Classic quantity theory of money experiment is a helicopter drop of money
  - change M_{-1} to $\lambda M_{-1}, \lambda > 0$
  - *holding fiscal policy*—(g, τ_0, τ, B)—*fixed*
- By (Current), if $p_0 \to \lambda p_0$, then M_{-1}/p_0 unchanged

$$\frac{\lambda M_{-1}}{\lambda p_0} = f(R_m) - (g + B_{-1} - \tau_0) + \frac{B}{R} \qquad \text{(Current)}$$

- Nothing happens to growth rate of money, R_m, or π
- Produces "neutrality of money" (not "superneutrality")
- Tobin's gremlins: required to leave portfolios unperturbed by M drop

5. A Neutral Open-Market Operation

- Redefine OMO from that used in unpleasant arithmetic to give MA fiscal powers so OMO have QT effects
- Denote initial eqm by $\bar{x}$; new eqm by $\hat{x}$
- Consider OMO that decreases M_0 and increases B and τ (with $\bar{\tau}_0 = \hat{\tau}_0$) such that

$$\left(1 - \frac{1}{R}\right)(\hat{B} - \bar{B}) = \hat{\tau} - \bar{\tau}$$

- If future taxes obey this for $t \geq 1$, then (Future) satisfied at initial R_m (that is, $-d\tau + dB(1 - 1/R) = 0$)
- Highlights a key aspect of conventional MP analysis
  - lump-sum taxes in future adjust by just enough to service any additional interest payments arising from the OMO's effects on B
  - FP "held constant" via unchanged gross-of-interest deficit

6. The Optimum Quantity of Money

- Given stationary (g, B), Friedman argued that agents are better off with higher stationary real money balances (ones associated with higher rates of return on money)
- By running sufficiently large gross surpluses $(g - \tau + B(R-1)/R < 0)$, government can attain any $R_m \in (1, 1/\beta)$
- So given (g, B), choose τ to get required surplus to hit the target R_m
- Use proceeds of tax to retire currency (achieve negative growth of M)

Use goods to take out money

- Pursues Friedman's optimal policy of saturating economy with real balances

6. The Optimum Quantity of Money

- Social value of real balances in model comes from reducing shopping time
- Optimum quantity of M minimizes time spent shopping
- Suppose there is a satiation point in real balances $\psi(c)$ for any c

$$H_{m/p}(c, m_t/p_t) = 0 \text{ for } m_t/p_t \geq \psi(c)$$

- Can achieve this only by setting $R = R_m$ (since $\mu_t, \lambda_t > 0$)
- If $H(c, m/p) = \frac{c}{m/p}\varepsilon$, can only approximate Friedman's rule since money demand insatiable

7. One Big Open-Market Operation

- Consider a large OM purchase of *private* indebtedness at $t = 0$
  - gives government a portfolio of interest-earning claims on private sector
  - permits the government to run a gross-of-interest surplus
  - government uses surplus to reduce money supply and create deflation
  - this raises return on money > 1
  - idea underlies some optimal fiscal policy results
- Impose $g - \tau \geq 0$ so cannot achieve deflation through direct taxation
- Proposal: $M_0 \uparrow, B \downarrow$ with $B < 0$

7. One Big Open-Market Operation

- Given (g, τ), use (Future) to pick B consistent with desired R_m $(1 \leq R_m \leq 1/\beta)$

$$\frac{M_{-1}}{p_0} = \underbrace{\left(\frac{R - R_m}{1 - R_m}\right)\frac{B}{R}}_{>0} + \underbrace{\left(\frac{1}{1 - R_m}\right)(g - \tau) - (g + B_{-1} - \tau_0)}_{\lesseqgtr 0}$$

- The candidate policy is an equilibrium policy if $(g, \tau, \tau_0, B_{-1})$ are such that $RHS > 0$ so that there exists a $p_0 > 0$ that solves this
- Example: $g - \tau = 0$ & $g + B_{-1} - \tau_0 = 0$ (balance budget $t \geq 1$
  - then $RHS > 0$ and it's feasible to get $1 < R_m < 1/\beta$
- Note: Cannot get $R_m = 1/\beta$ since then $R = R_m$ and government earns no arbitrage income and cannot finance deflation

8. A Ricardian Experiment

- Consider a debt-financed tax cut at $t = 0$, with future taxes adjusting
  - MP held fixed: no change in $\{M_t\}_{t=0}^{\infty}$
- $-d\tau_0 = \frac{1}{R} dB$ & $d\tau = \frac{R-1}{R} dB$
- Both (Current) & (Future) satisfied at initial R_m, p_0
- Lump-sum taxes in future adjust by just enough to service any additional interest payments arising from the tax cut's effects on B
- Of course, lump-sum essential
- A central neutrality result in fiscal policy

Wrap Up

- These doctrines, though simple, highlight the centrality of monetary-fiscal policy interactions for the nature of eqm
- Although this general point has been known, we often ignore it
  - introduces inconvenient considerations
  - makes policy analysis *much* harder
  - prescribing both MP & FP is many times harder than prescribing MP, assuming FP—i.e., lump-sum taxes—will adjust to ensure fiscal sustainability
- The doctrines should have made clear that once you deviate from this kind of FP, lots of interesting things can happen