

March 17, 2023

1 AND Gate Single layer Perceptron

```
[1]: import numpy as np
def activation(out, threshold):
    act_out = 1/(1 + np.exp(-out))
    if act_out >= threshold:
        return 1
    else:
        return 0

def perceptron(and_input):
    a = [0, 0, 1, 1]
    b = [0, 1, 0, 1]
    y = [0, 0, 0, 1]
    bias = -1
    w = [0.6, 0.8, 1.5]
    threshold = 0.5
    learning_rate = 0.5
    i = 0
    print("Perceptron Training")
    print("#####")
    print("_____")
    while i < 4:
        summation = (a[i]*w[0] + b[i]*w[1]) + bias*w[2]
        target_output = activation(summation, threshold)
        print("Input : " + str(a[i]) + " , "+str(b[i]))
        print("Weights : " + str(w[0]) + " , "+str(w[1]))
        print("Summation : " + str(summation))
        print("Actual output : " + str(y[i]) + " Predicted Output_
↪"+str(target_output))

        if(target_output != y[i]):
            print(".....\nUpdating Weights")
            w[0] = w[0] + learning_rate*(y[i] - target_output)*a[i]
            w[1] = w[1] + learning_rate*(y[i] - target_output)*b[i]
            print("Updated Weights: ", str(w[0]) + ', '+str(w[1]))
            i = -1
```

```

        print("\nWeights Updated Training Again : ")
        print("#####")
        i = i+1
        #print("-----")
        summation = and_input[0]*w[0] + and_input[1]*w[1] + bias*w[2]
        import matplotlib.pyplot as plt
        plt.figure(figsize=(12, 8))
        x_min, x_max = -0.5, 1.5
        y_min, y_max = -0.5, 1.5
        xx, yy = np.meshgrid(np.linspace(x_min, x_max, 100), np.linspace(y_min,
↪y_max, 100))
        Z = np.array([activation((np.dot([w[0],w[1]], [a, b]) + bias*w[2]),
↪threshold) for a, b in np.c_[xx.ravel(), yy.ravel()]])
        Z = Z.reshape(xx.shape)
        plt.contourf(xx, yy, Z, cmap='Oranges')
        for i in range(len(y)):
            if y[i] == 0:
                plt.scatter(a[i], b[i], color='red', marker='x', label='Class 0')
            else:
                plt.scatter(a[i], b[i], color='green', marker='o', label='Class 1')
        #plt.scatter(a,b, c=y, cmap = "Blues_r", label = "a & b values")
        plt.title("AND GATE ")
        plt.xlim(xx.min(), xx.max())
        plt.ylim(yy.min(), yy.max())
        #plt.xticks(())
        #plt.yticks(())
        #plt.grid()
        plt.legend()
        plt.show()
        return activation(summation, threshold)

and_input = [1,1]
output = perceptron(and_input)
print("AND Gate Output for " + str(and_input) + " : " + str(output))

```

Perceptron Training

#####

Input : 0 , 0

Weights : 0.6 , 0.8

Summation : -1.5

Actual output : 0 Predicted Output 0

Input : 0 , 1

Weights : 0.6 , 0.8

Summation : -0.7

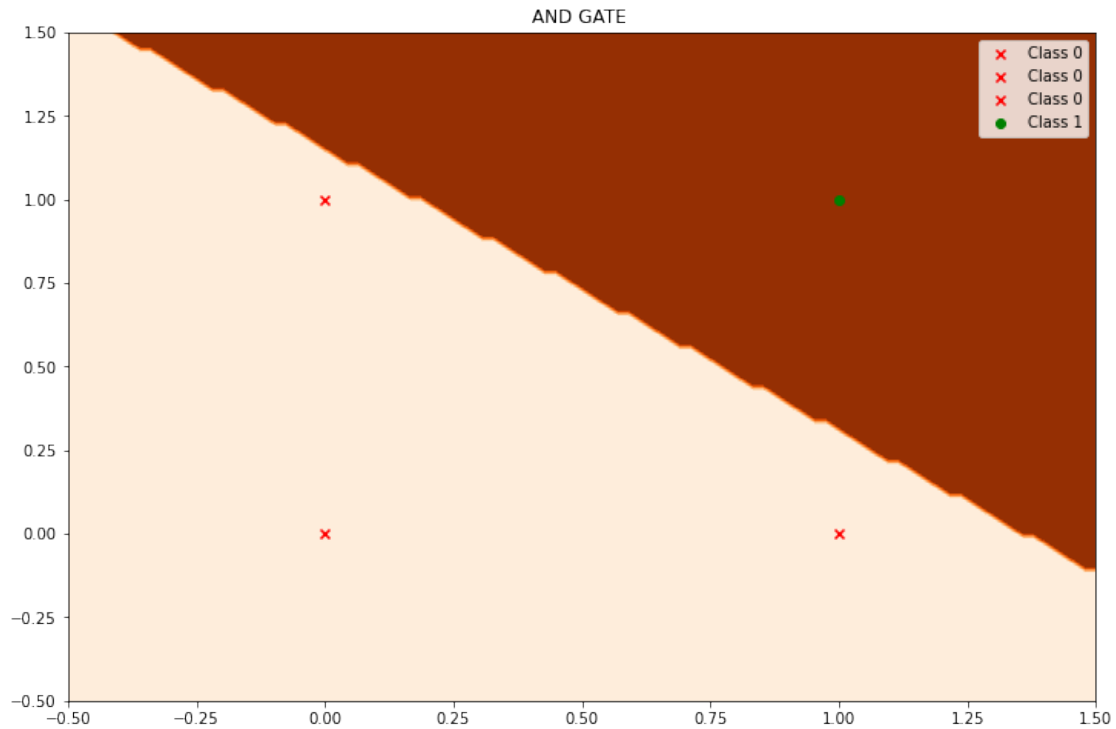
Actual output : 0 Predicted Output 0

Input : 1 , 0

Weights : 0.6 , 0.8
Summation : -0.9
Actual output : 0 Predicted Output 0
Input : 1 , 1
Weights : 0.6 , 0.8
Summation : -0.10000000000000009
Actual output : 1 Predicted Output 0
...
Updating Weights
Updated Weights: 1.1,1.3

Weights Updated Training Again :

Input : 0 , 0
Weights : 1.1 , 1.3
Summation : -1.5
Actual output : 0 Predicted Output 0
Input : 0 , 1
Weights : 1.1 , 1.3
Summation : -0.19999999999999996
Actual output : 0 Predicted Output 0
Input : 1 , 0
Weights : 1.1 , 1.3
Summation : -0.39999999999999999
Actual output : 0 Predicted Output 0
Input : 1 , 1
Weights : 1.1 , 1.3
Summation : 0.90000000000000004
Actual output : 1 Predicted Output 1



AND Gate Output for [1, 1] : 1

2 OR Gate Single layer Perceptron

```
[2]: import numpy as np
def activation(out, threshold):
    act_out = 1/(1 + np.exp(-out))
    if act_out >= threshold:
        return 1
    else:
        return 0
def perceptron(and_input):
    a = [0, 0, 1, 1]
    b = [0, 1, 0, 1]
    y = [0, 1, 1, 1]
    bias = -1
    w = [0.6, 0.6, 1]
    threshold = 0.5
    learning_rate = 0.5
    i = 0
    print("Perceptron Training")
    print("#####")
    print("_____")
```

```

while i<4:
    summation = (a[i]*w[0] + b[i]*w[1]) + bias*w[2]
    target_output = activation(summation, threshold)
    print("Input : " + str(a[i]) + " , "+str(b[i]))
    print("Weights : " + str(w[0]) + " , "+str(w[1]))
    print("Summation : " + str(summation))
    print("Actual output : " + str(y[i]) + " Predicted Output_
↪"+str(target_output))
    if(target_output != y[i]):
        print(".....\nUpdating Weights")
        w[0] = w[0] + learning_rate*(y[i] - target_output)*a[i]
        w[1] = w[1] + learning_rate*(y[i] - target_output)*b[i]
        print("Updated Weights: ", str(w[0]) + ', '+str(w[1]))
        i = -1
        print("\nWeights Updated Training Again : ")
        print("#####")
        i = i+1
        print("-----")
    summation = and_input[0]*w[0] + and_input[1]*w[1] + bias*w[2]
    import matplotlib.pyplot as plt
    plt.figure(figsize=(12, 8))
    x_min, x_max = -0.5,1.5
    y_min, y_max = -0.5,1.5
    xx,yy = np.meshgrid(np.linspace(x_min, x_max,100),np.linspace(y_min,
↪y_max,100))

    Z = np.array([activation((np.dot([w[0],w[1]], [a, b]) + bias*w[2]),
↪threshold) for a, b in np.c_[xx.ravel(), yy.ravel()])])
    Z = Z.reshape(xx.shape)
    plt.contourf(xx, yy, Z, cmap='Oranges')
    for i in range(len(y)):
        if y[i] == 0:
            plt.scatter(a[i], b[i], color='red', marker='x', label='Class 0')
        else:
            plt.scatter(a[i], b[i], color='green', marker='o', label='Class 1')

    #plt.scatter(a,b, c=y, cmap = "Blues_r", label = "a & b values")
    plt.title("OR GATE ")
    plt.xlim(xx.min(), xx.max())
    plt.ylim(yy.min(), yy.max())
    #plt.xticks(())
    #plt.yticks(())
    #plt.grid()
    plt.legend()
    plt.show()
    return activation(summation, threshold)

```

```

and_input = [1,1]
print("OR Gate Output for " + str(and_input) + " : " +
↪str(perceptron(and_input)))

```

Perceptron Training

#####

```

-----
Input : 0 , 0
Weights : 0.6 , 0.6
Summation : -1.0
Actual output : 0 Predicted Output 0
-----

```

```

Input : 0 , 1
Weights : 0.6 , 0.6
Summation : -0.4
Actual output : 1 Predicted Output 0
...

```

Updating Weights

Updated Weights: 0.6,1.1

Weights Updated Training Again :

#####

```

-----
Input : 0 , 0
Weights : 0.6 , 1.1
Summation : -1.0
Actual output : 0 Predicted Output 0
-----

```

```

Input : 0 , 1
Weights : 0.6 , 1.1
Summation : 0.10000000000000009
Actual output : 1 Predicted Output 1
-----

```

```

Input : 1 , 0
Weights : 0.6 , 1.1
Summation : -0.4
Actual output : 1 Predicted Output 0
...

```

Updating Weights

Updated Weights: 1.1,1.1

Weights Updated Training Again :

#####

```

-----
Input : 0 , 0
Weights : 1.1 , 1.1
Summation : -1.0

```

Actual output : 0 Predicted Output 0

Input : 0 , 1

Weights : 1.1 , 1.1

Summation : 0.10000000000000009

Actual output : 1 Predicted Output 1

Input : 1 , 0

Weights : 1.1 , 1.1

Summation : 0.10000000000000009

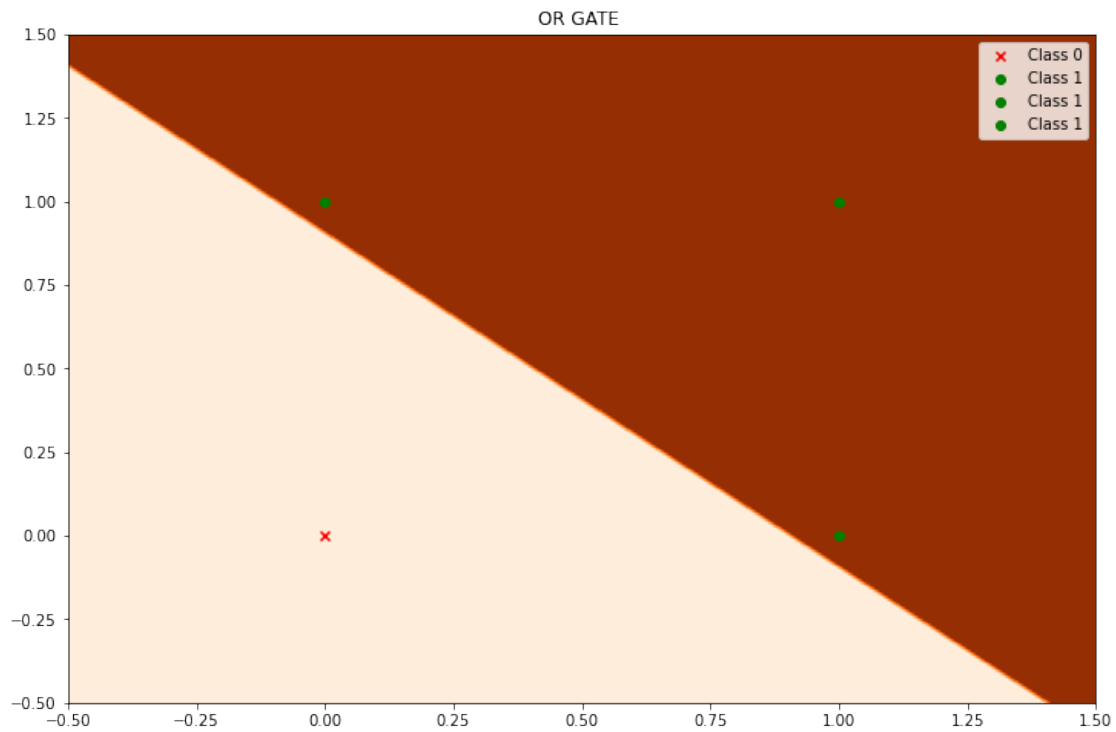
Actual output : 1 Predicted Output 1

Input : 1 , 1

Weights : 1.1 , 1.1

Summation : 1.2000000000000002

Actual output : 1 Predicted Output 1



OR Gate Output for [1, 1] : 1

3 Multi Layer Perceptron for X-OR

```
[3]: import numpy as np
import matplotlib.pyplot as plt

# Define the input data
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])

# Define the target output data
y = np.array([0, 1, 1, 0])

# Define the learning rate
learning_rate = 0.1

# Define the number of neurons in the hidden layer
hidden_layer_size = 2

# Define the initial weights and biases for the hidden layer
hidden_layer_weights = np.random.normal(size=(2, hidden_layer_size))
hidden_layer_bias = np.zeros(hidden_layer_size)

# Define the initial weights and bias for the output layer
output_layer_weights = np.random.normal(size=(hidden_layer_size, 1))
output_layer_bias = 0.0

# Define the activation function (sigmoid function)
def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

# Define the derivative of the activation function (sigmoid function)
def sigmoid_derivative(x):
    return x * (1.0 - x)

# Train the perceptron
for i in range(10000):
    # Forward propagation
    hidden_layer_activation = sigmoid(np.dot(X, hidden_layer_weights) +
    ↪ hidden_layer_bias)
    output_layer_activation = sigmoid(np.dot(hidden_layer_activation,
    ↪ output_layer_weights) + output_layer_bias)

    # Backpropagation
    output_layer_error = y.reshape(-1, 1) - output_layer_activation
    output_layer_delta = output_layer_error *
    ↪ sigmoid_derivative(output_layer_activation)

    hidden_layer_error = output_layer_delta.dot(output_layer_weights.T)
```



```

        hidden_layer_delta = hidden_layer_error * ␣
        ↪sigmoid_derivative(hidden_layer_activation)

        # Update the weights and biases
        output_layer_weights += hidden_layer_activation.T.dot(output_layer_delta) * ␣
        ↪learning_rate
        output_layer_bias += np.sum(output_layer_delta, axis=0, keepdims=True) * ␣
        ↪learning_rate

        hidden_layer_weights += X.T.dot(hidden_layer_delta) * learning_rate
        hidden_layer_bias += np.sum(hidden_layer_delta, axis=0) * learning_rate

# Predictions
t= np.array([[1,1]])
hidden_layer_activation = sigmoid(np.dot(t, hidden_layer_weights) + ␣
        ↪hidden_layer_bias)
output_layer_activation = sigmoid(np.dot(hidden_layer_activation, ␣
        ↪output_layer_weights) + output_layer_bias)
a2 = np.squeeze(output_layer_activation)
if a2>=0.5:
    print("For input", t[0], "output is 1")
else:
    print("For input", t[0], "output is 0")
#print(output_layer_activation)

```

For input [1 1] output is 0

```

[4]: # Plot the decision boundary
plt.figure(figsize=(12, 8))
x1 = np.linspace(-0.5, 1.5, 10)
x2 = np.linspace(-0.5, 1.5, 10)
X1, X2 = np.meshgrid(x1, x2)
Z = np.zeros_like(X1)

for i in range(X1.shape[0]):
    for j in range(X1.shape[1]):
        hidden_layer_activation = sigmoid(np.dot(np.array([X1[i,j], X2[i,j]]), ␣
        ↪hidden_layer_weights)+ hidden_layer_bias)
        output_layer_activation = sigmoid(np.dot(hidden_layer_activation, ␣
        ↪output_layer_weights)+ output_layer_bias)
        Z[i,j] = output_layer_activation[0]
plt.contourf(X1, X2, Z, cmap='coolwarm', alpha=0.5)
#plt.colorbar()
# Plot the input data
for i in range(len(X)):
    if y[i] == 0:

```

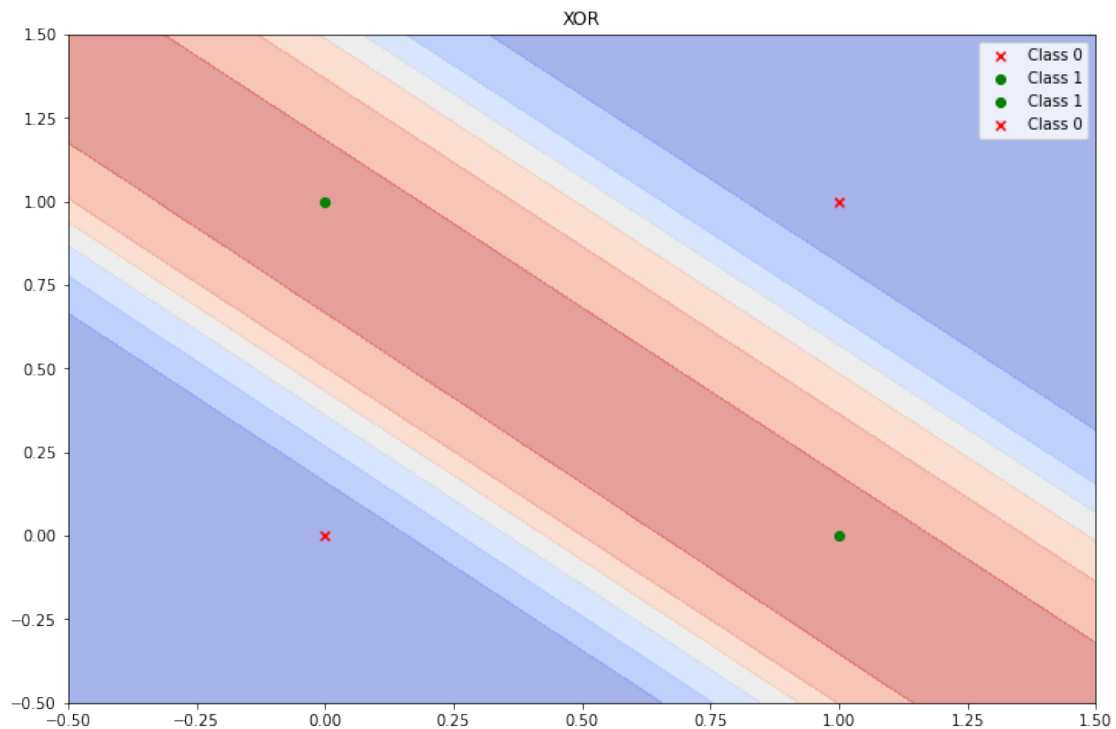
```

plt.scatter(X[i][0], X[i][1], color='red', marker='x', label='Class 0')
else:
plt.scatter(X[i][0], X[i][1], color='green', marker='o', label='Class_
↪1')

# Add labels and legend

plt.title('XOR')
plt.legend()
plt.show()

```



4 Information Gain with Decision Tree

```

[5]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt

```

```

[16]: data = pd.read_excel("/content/DataSet.xlsx")
data.head()

```

```

[16]:   A  B  C Output
0  1  1  5      S

```

1	0	1	1	L
2	1	2	5	S
3	0	2	1	L
4	0	1	1	M

```
[17]: count_1 = 0
count_2 = 0
count_3 = 0
for i in range(len(data)):
    if(data["Output"][i]=="S"):
        count_1 = count_1+1
    elif(data["Output"][i]=="M"):
        count_2 = count_2 +1
    else:
        count_3 = count_3 +1
```

```
[18]: print("Total S : ", count_1, "\nTotal M : ", count_2, "\nTotal L : ", count_3)
```

```
Total S : 10
Total M : 12
Total L : 8
```

```
[19]: def cal_Entropy(x,y,w):
    t = x+y+w
    if(x == 0):
        entropy = -((y/t)*np.log2(y/t)+(w/t)*np.log2(w/t))
    elif(y == 0):
        entropy = -((x/t)*np.log2(x/t)+(w/t)*np.log2(w/t))
    elif(w == 0):
        entropy = -((x/t)*np.log2(x/t)+(y/t)*np.log2(y/t))
    else:
        entropy = -((x/t)*np.log2(x/t)+(y/t)*np.log2(y/t)+(w/t)*np.log2(w/t))
    #entropy = "{:.2f}".format(entropy)
    #t = "{:.2f}".format(t)
    return t, entropy
```

```
[20]: total_data, parent_Entropy = cal_Entropy(count_1,count_2,count_3)

print(f"Total Data : {total_data} \nParent Entropy : {parent_Entropy}")
```

```
Total Data : 30
Parent Entropy : 1.5655962303576019
```

```
[21]: def child_data(c_data, x):
    child1= []
    child2= []
    #print(c_data)
```

```

for i in range(len(c_data)):
    if(c_data[x][i]==1):
        child1.append(c_data["Output"][i])
    else:
        child2.append(c_data["Output"][i])
#print(len(child1), len(child2))
#child = pd.DataFrame(list(zip(child1, child2)),columns=['child1',
↳ 'child2'])
return child1, child2

def count_data(data):
    count_1 = 0
    count_2 = 0
    count_3 = 0
    for i in range(len(data)):
        if(data[i]=="S"):
            count_1 = count_1+1
        elif(data[i]=="M"):
            count_2 = count_2 +1
        else:
            count_3 = count_3 +1
    return count_1, count_2, count_3

def wgh_avg_entropy(total_data, child_total_data1, child_entropy1,
↳ child_total_data2, child_entropy2):
    avg_entropy = (((child_total_data1 / total_data)*child_entropy1) +
↳ ((child_total_data2 / total_data)*child_entropy2))
    return avg_entropy

def information_gain(child1, child2):
    count_1, count_2, count_3 = count_data(child1)
    child_total_data1, child_entropy1 = cal_Entropy(count_1,count_2,count_3)
    count_1, count_2, count_3 = count_data(child2)
    child_total_data2, child_entropy2 = cal_Entropy(count_1,count_2,count_3)
    avg_entropy = wgh_avg_entropy(total_data, child_total_data1,
↳ child_entropy1, child_total_data2, child_entropy2)
    I_Gain= "{:.2f}".format(parent_Entropy-avg_entropy)
    return I_Gain

```

```

[22]: child1, child2 = child_data(data[["A", "Output"]], "A")
print("Information Gain for attribute A : ", information_gain(child1, child2))

```

Information Gain for attribute A : 0.04

```

[23]: child1, child2 = child_data(data[["B", "Output"]], "B")
print("Information Gain for attribute B : ", information_gain(child1, child2))

```

Information Gain for attribute B : 0.06

```
[24]: child1, child2 = child_data(data[["C", "Output"]], "C")
      print("Information Gain for attribute C : ", information_gain(child1, child2))
```

Information Gain for attribute C : 0.54

```
[25]: import sys
      import matplotlib
      matplotlib.use('Agg')
      %matplotlib inline
      import pandas
      from sklearn import tree
      from sklearn.tree import DecisionTreeClassifier
      import matplotlib.pyplot as plt

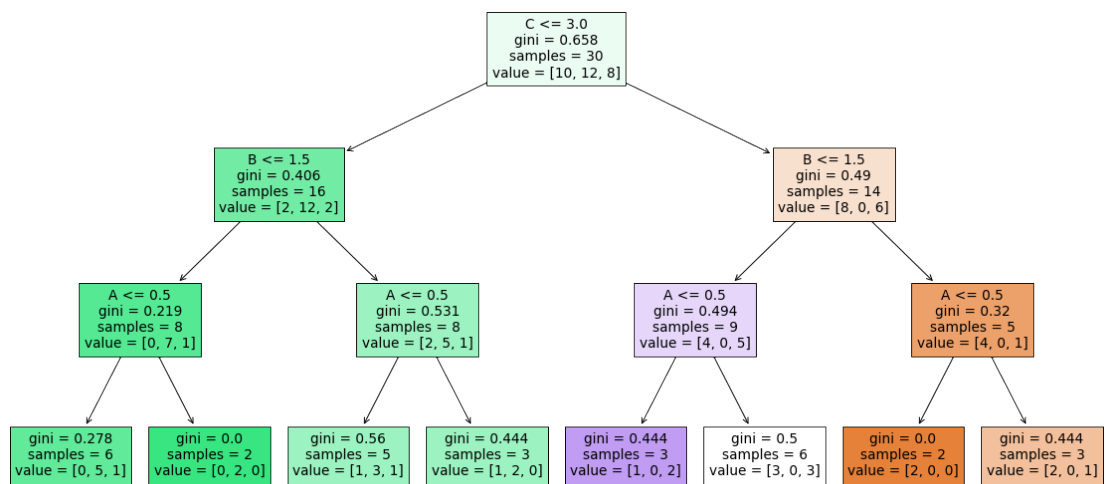
      df = pandas.read_excel("DataSet.xlsx")

      d = {'S': 0, 'M': 1, 'L': 2}
      df["Output"] = df['Output'].map(d)

      features = ['A', 'B', 'C']

      X = df[features]
      y = df['Output']

      dtree = DecisionTreeClassifier(max_depth = 3)
      dtree = dtree.fit(X, y)
      plt.figure(figsize=(20, 10))
      tree.plot_tree(dtree, feature_names=features, filled = True)
      #plt.savefig(sys.stdout.buffer)
      sys.stdout.flush()
```



[]: